

# Air Shower Simulations

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Johannes Knapp,  
Physics & Astronomy  
U of Leeds, UK

3<sup>rd</sup> School on  
Cosmic Rays and Astrophysics  
Arequipa, Peru  
2008

- Part 1: Astroparticle Physics, Air Showers and Simulations
- Part 2, 3: Hadronic & Nuclear Models, CORSIKA, Performance and Limitations
- Part 4: Selected Aspects of EAS simulations, Simulation Techniques

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# Shower development (qualitatively)

crucial:

- inelastic cross-sections ( $S_{inel}$ )
- hadronic particle production  
(inelasticity  $\kappa_{inel}$  i.e. fraction of energy converted into secondaries)

correlated!

large cross-sections,  
high inelasticity

} make short showers

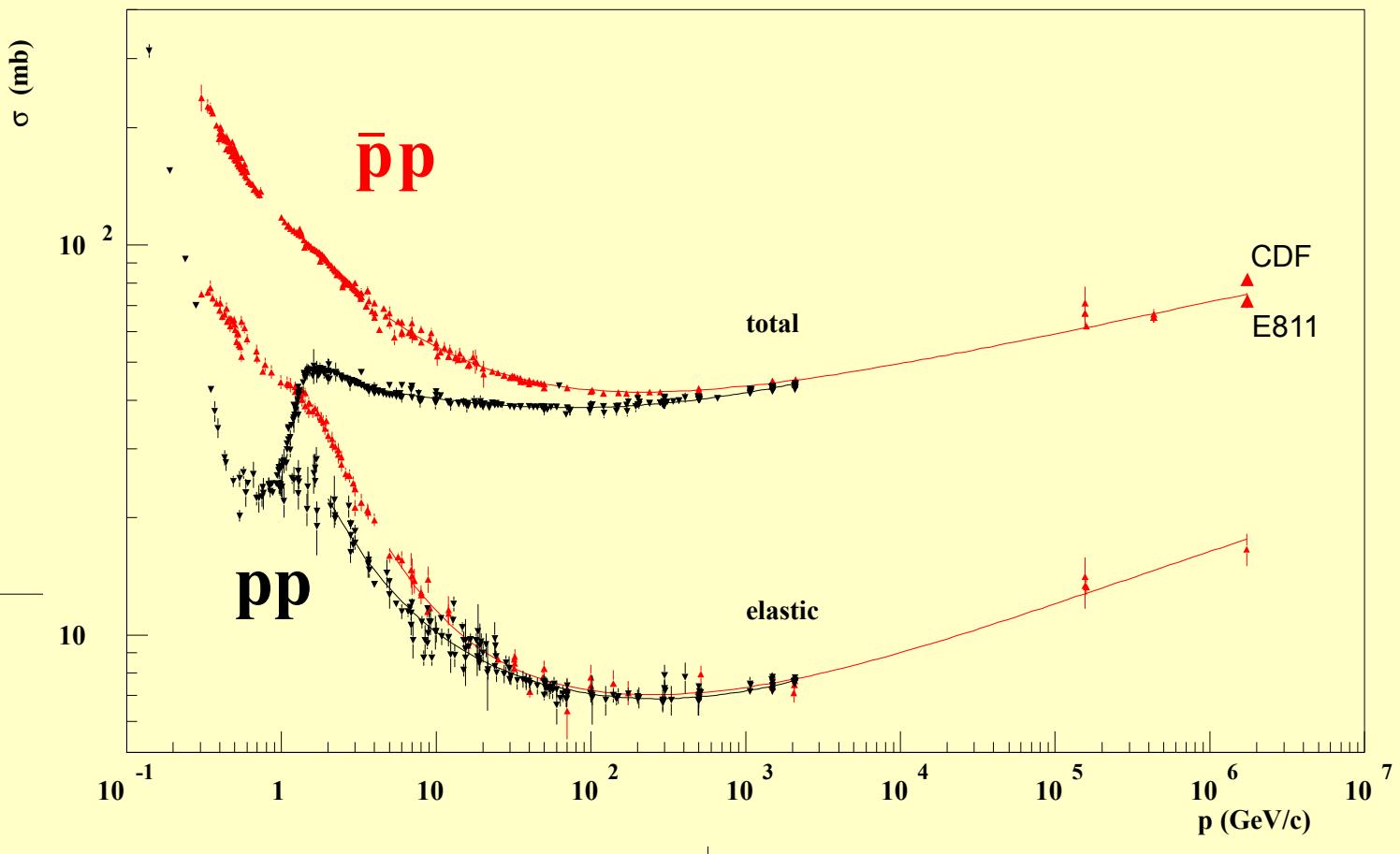
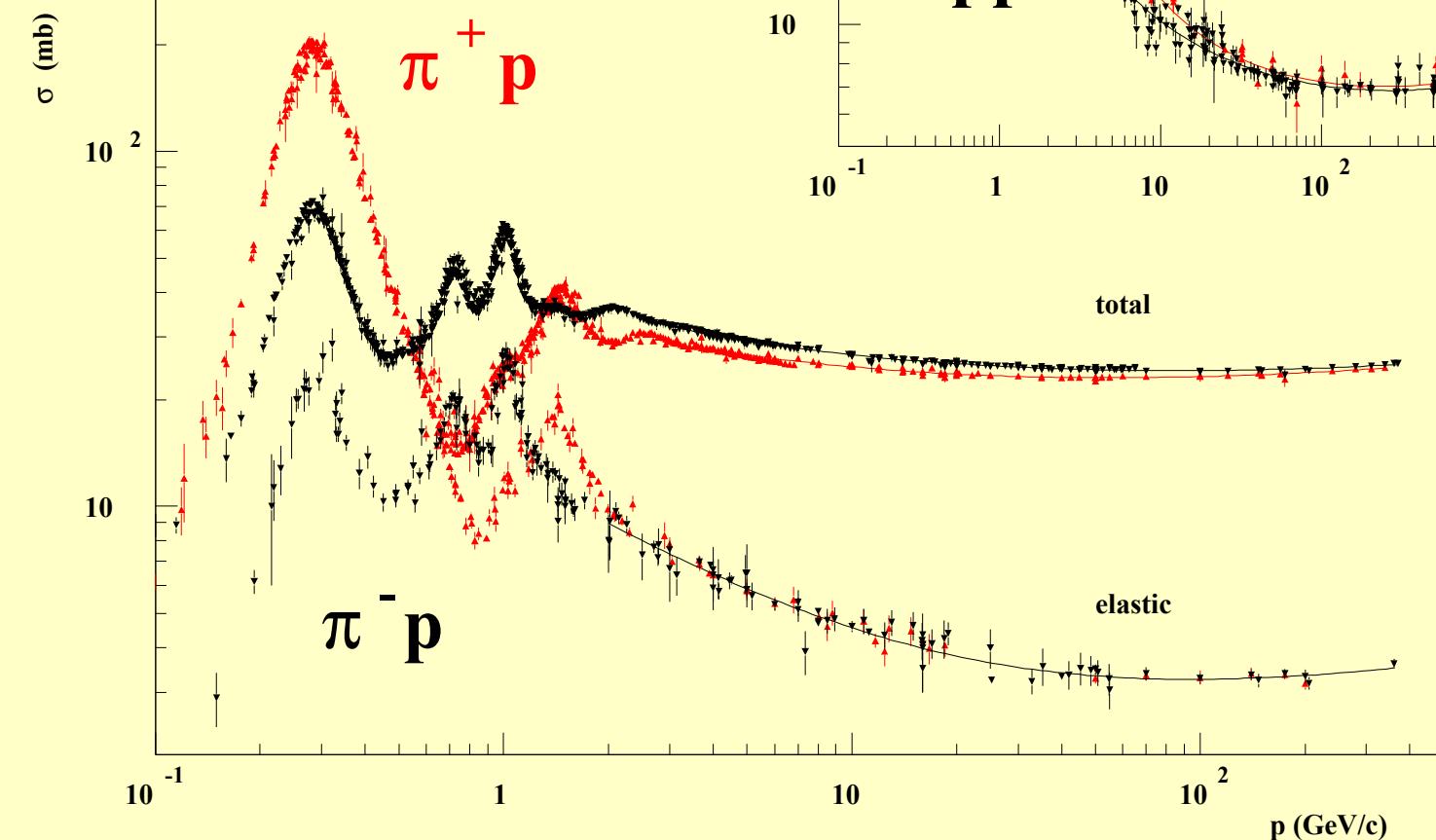
small cross-sections,  
low inelasticity

} make long showers

less crucial:

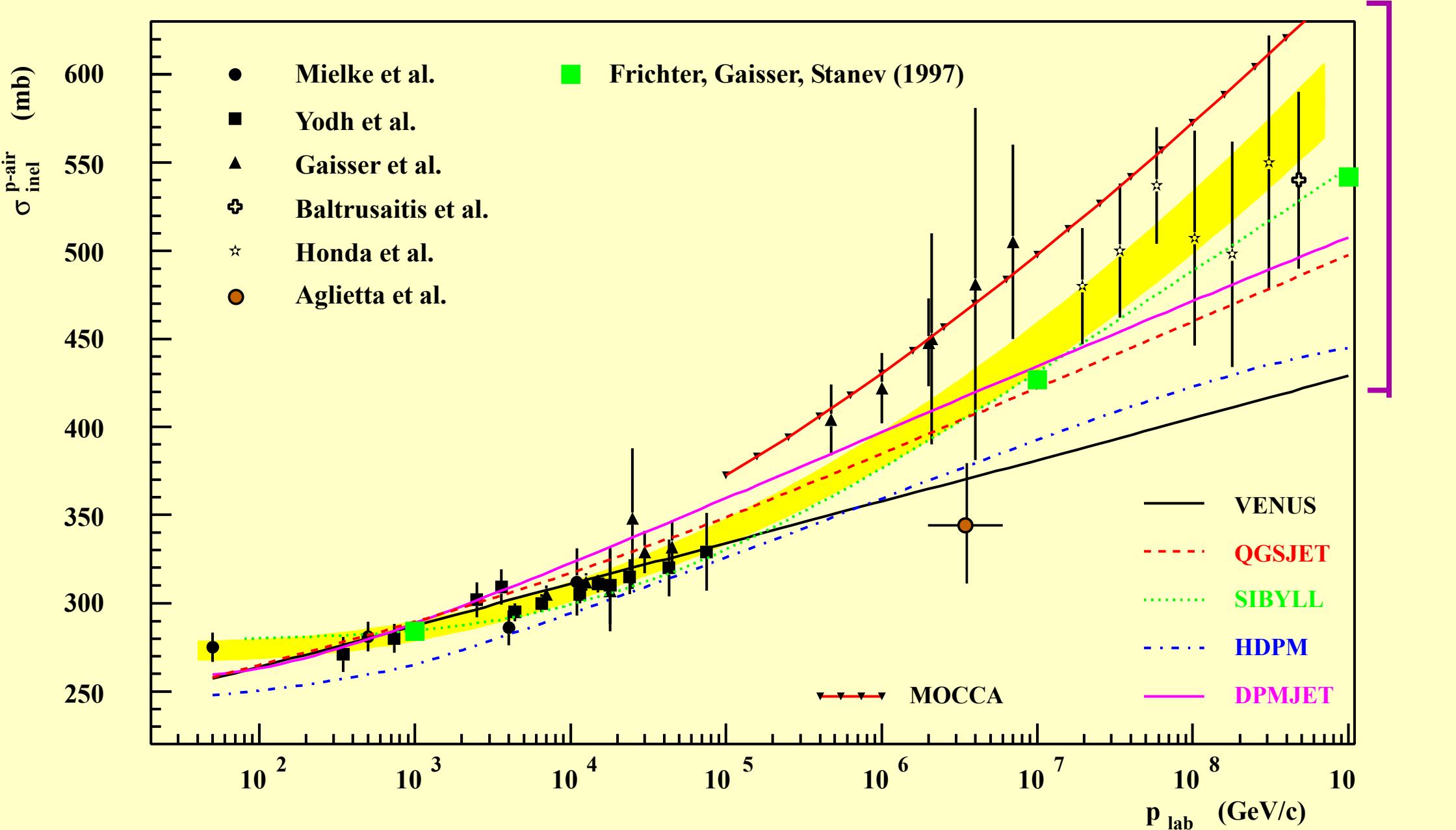
nuclear fragmentation,  $dE/dx$ , decays, tracking,  
electromagnetic reactions, ....

# Measured Cross-Sections



# p-Air Inelastic Cross-Sections 1997

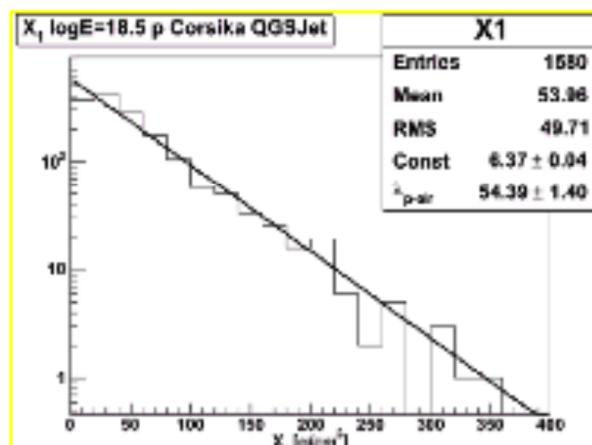
~50%



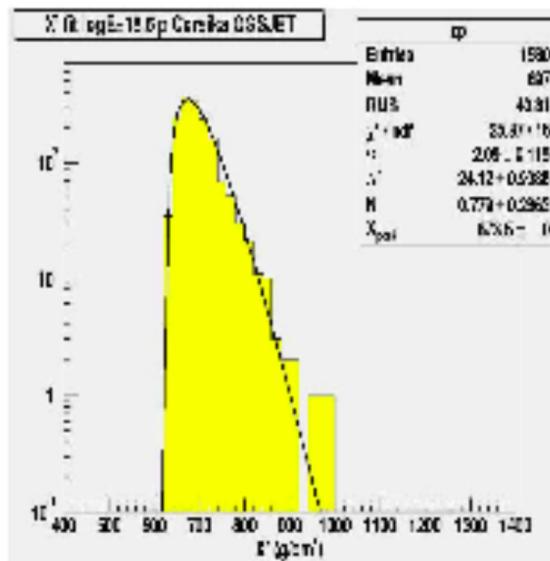
# Measuring $\sigma_{p\text{-air}}$ : De-convolution Method by HiRes

Pierre Sokolsky

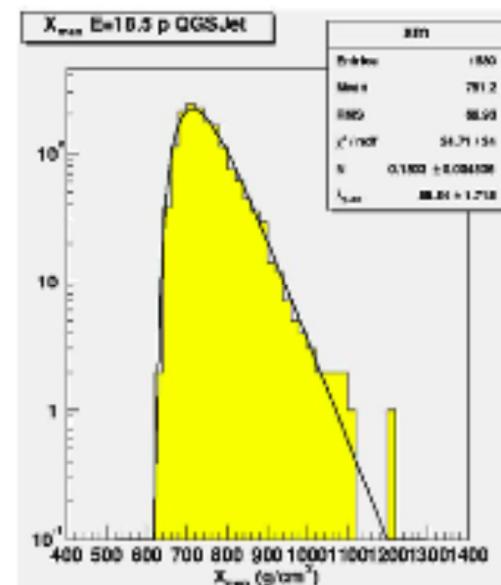
Point of first interaction distribution. Exponential index reflects inelastic Cross-section



Atmospheric part of air shower fluctuations



$X_{\text{max}}$  distribution



$$f_{\text{int}} = e^{-\frac{x_1}{\lambda_{p\text{-Air}}}};$$

$$\lambda_{p\text{-Air}} = \frac{1}{\tilde{n} \sigma_{p\text{-air}}^{\text{inel}}};$$

$$X' = X_{\text{max}} - X_1$$

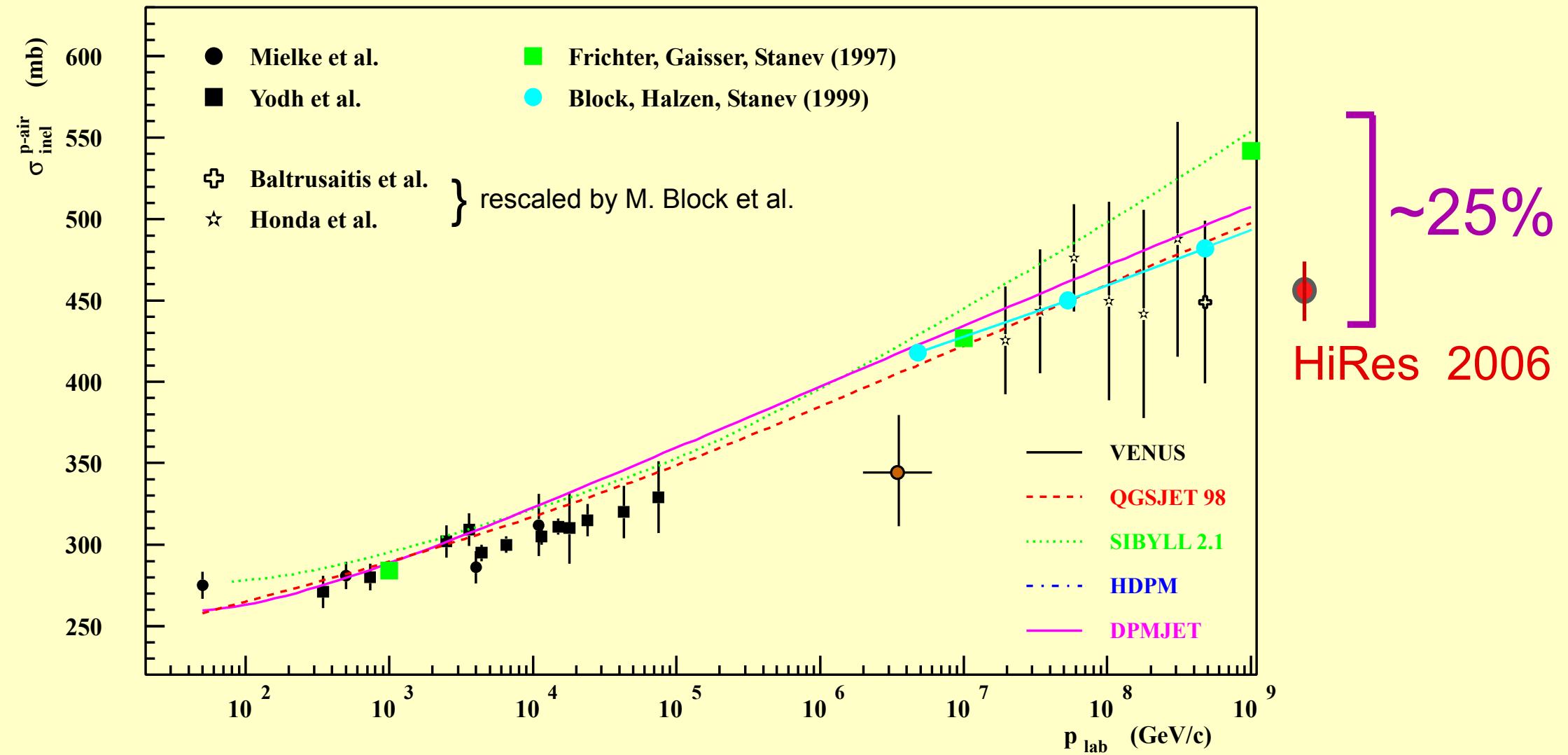
$$f_{\text{fluct}} = \left[ \frac{x_{\text{max}} - x_{\text{peak}} - x_1 + \Lambda' \alpha}{e} \right]^{\alpha} e^{-\frac{x_{\text{max}} - x_1 - x_{\text{peak}}}{\Lambda'}}$$

$$f_{\text{fluct}}(x_{\text{peak}}(E), \Lambda'(E), \alpha(E)) \Rightarrow f_{\text{fluct}}(E)$$

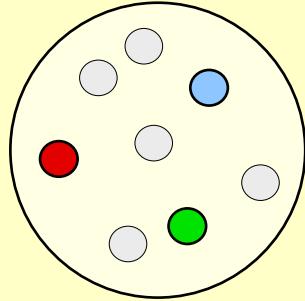
$$P_m(x_m) = N \int_0^{x_m - x_{\text{peak}} + \Lambda' \alpha} e^{\frac{-x_1}{\lambda_{p\text{-Air}}}} \left[ \frac{x_{\text{max}} - x_{\text{peak}} - x_1 + \Lambda' \alpha}{e} \right]^{\alpha} e^{-\frac{x_{\text{max}} - x_1 - x_{\text{peak}}}{\Lambda'}} dx_1;$$



# $p$ -Air Inelastic cross-sections 2001



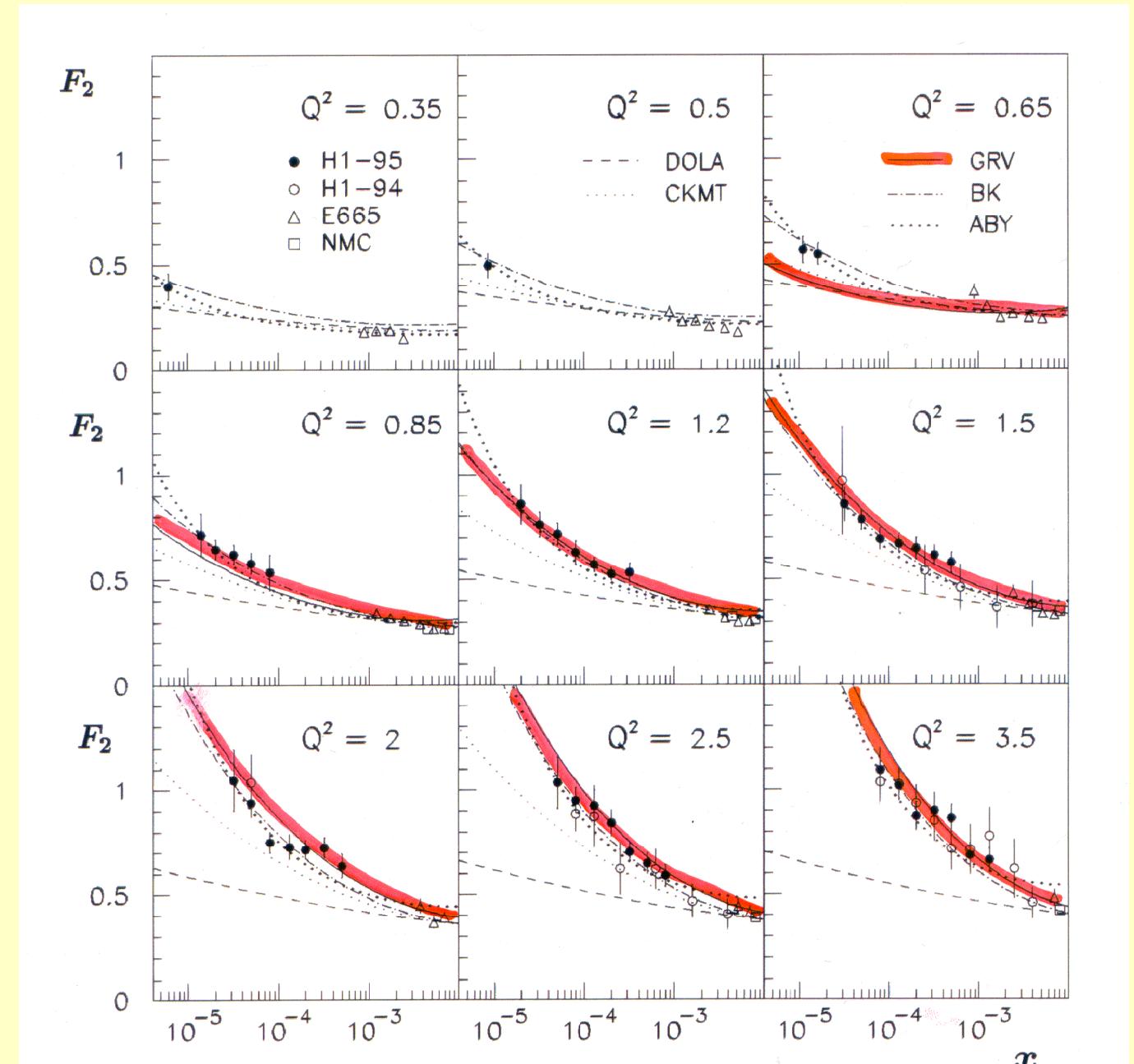
# HERA measured structure functions at small $x$



The more partons (quarks & gluons) there are in a nucleon at small  $x$ ,

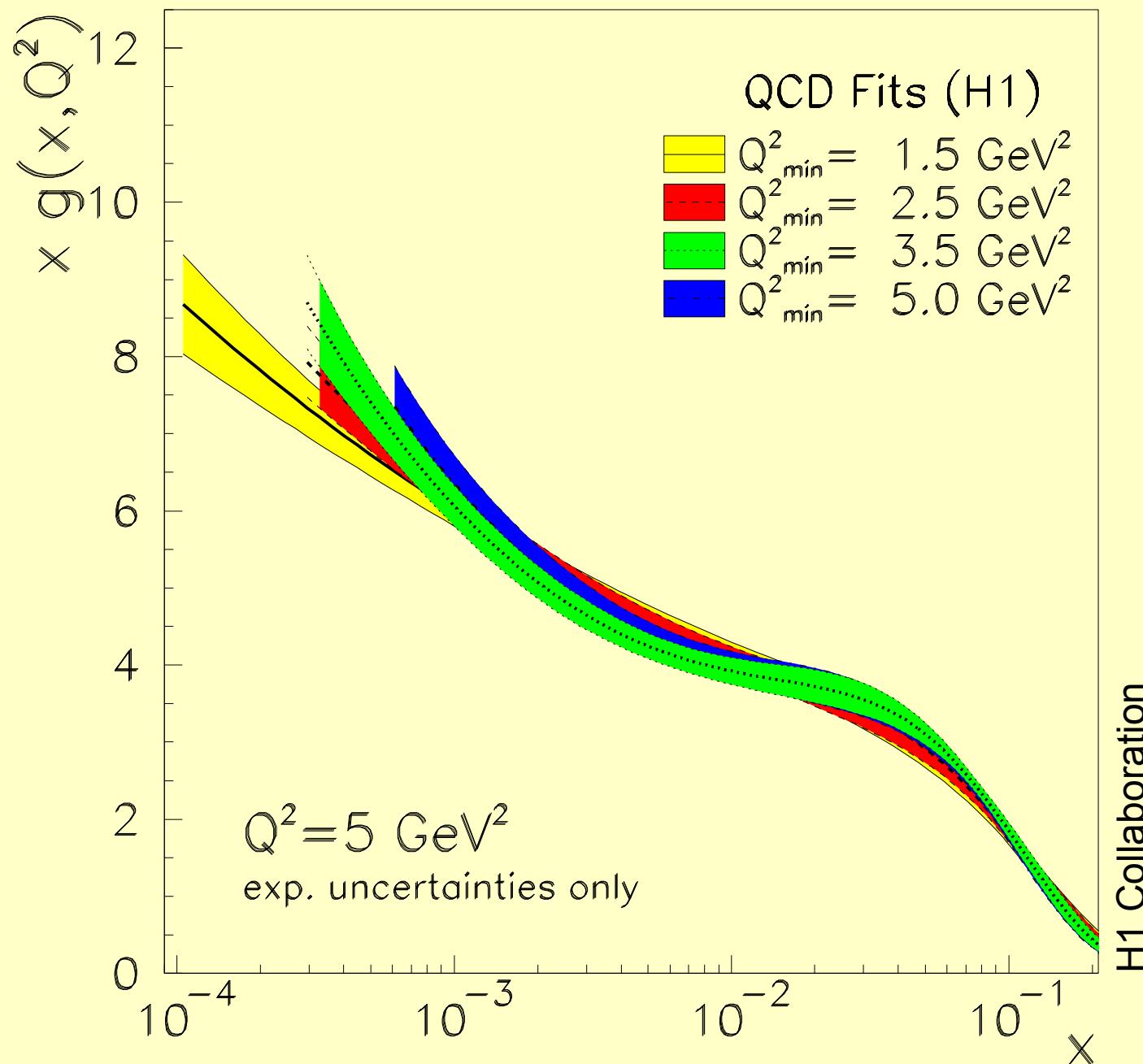
the more likely a collision is to happen with a high-energy projectile, and the higher is the interaction cross-section.

HERA data help with extrapolation of cross-sections to high energies.

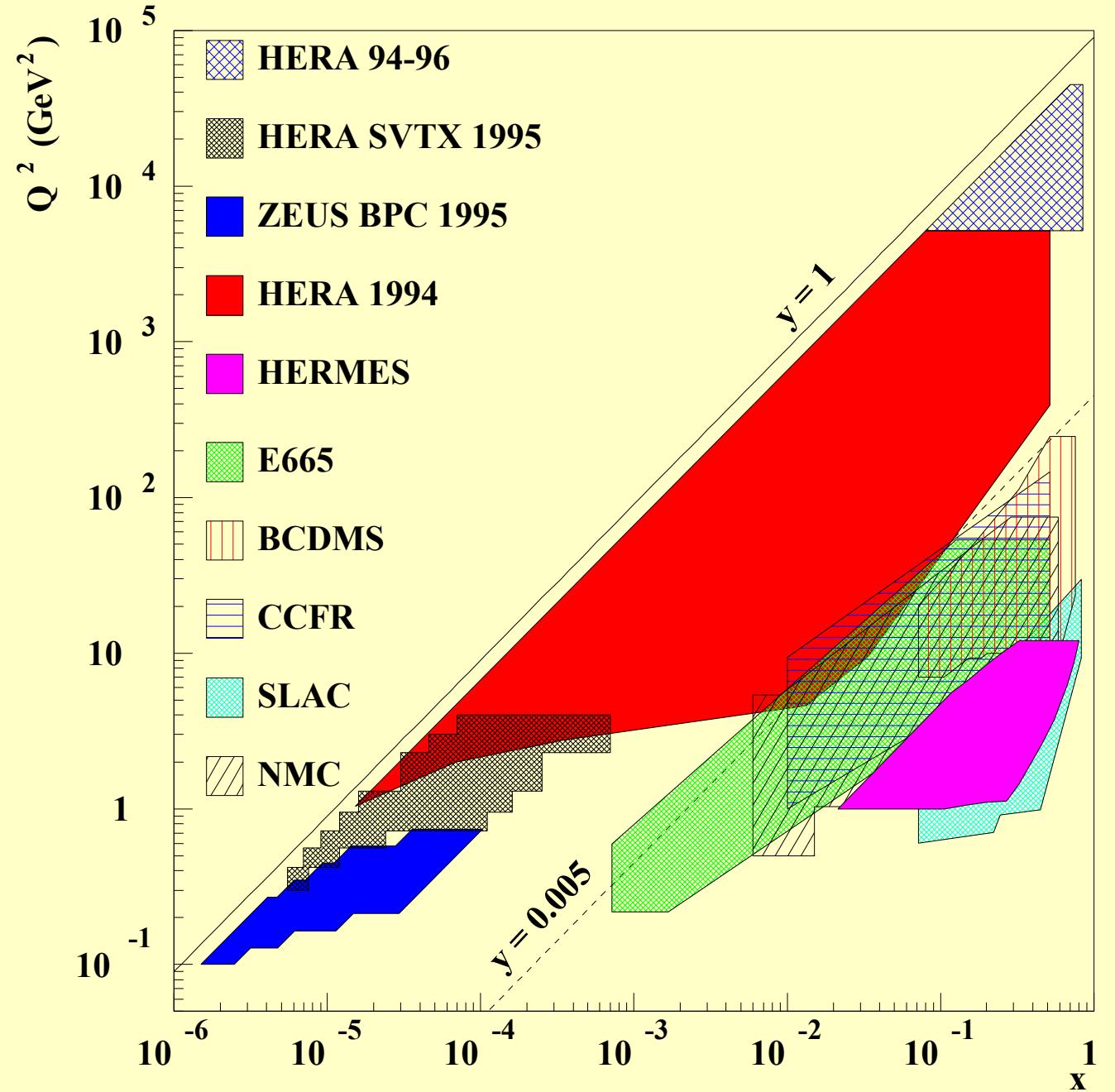


$x$  = momentum fraction of a parton

# Gluon density at low x



# Coverage in $x$ - $Q^2$ plane

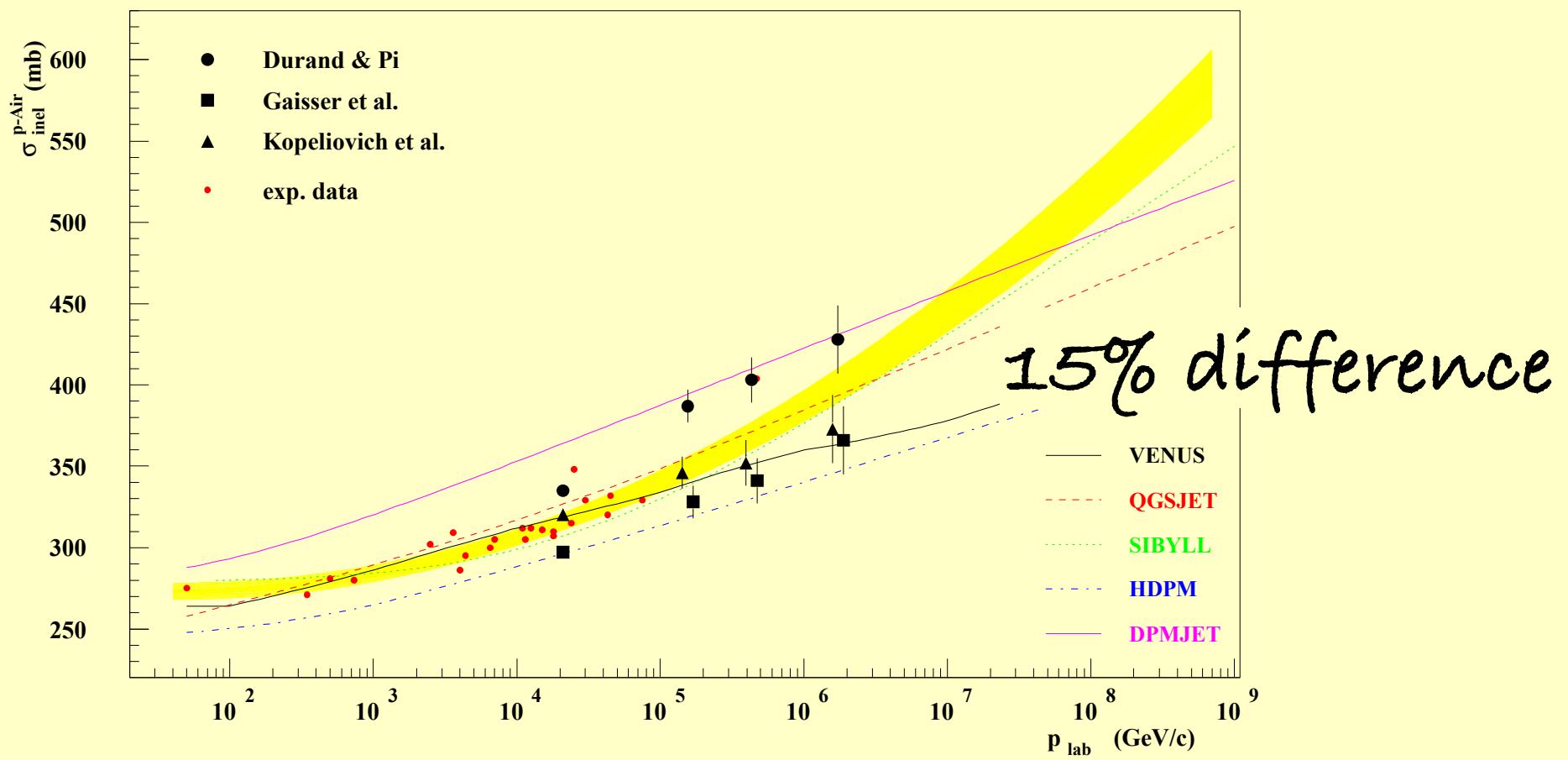


cosmic ray regime:

$$Q^2 \approx 0$$

$$x \approx 0$$

# Conversion from p-p to p-Air cross sections (Glauber Theory)



3 groups applied Glauber theory to deduce  
the proton-Air inelastic cross-section from  
the measured p-p cross-sections (SppS, Tevatron)

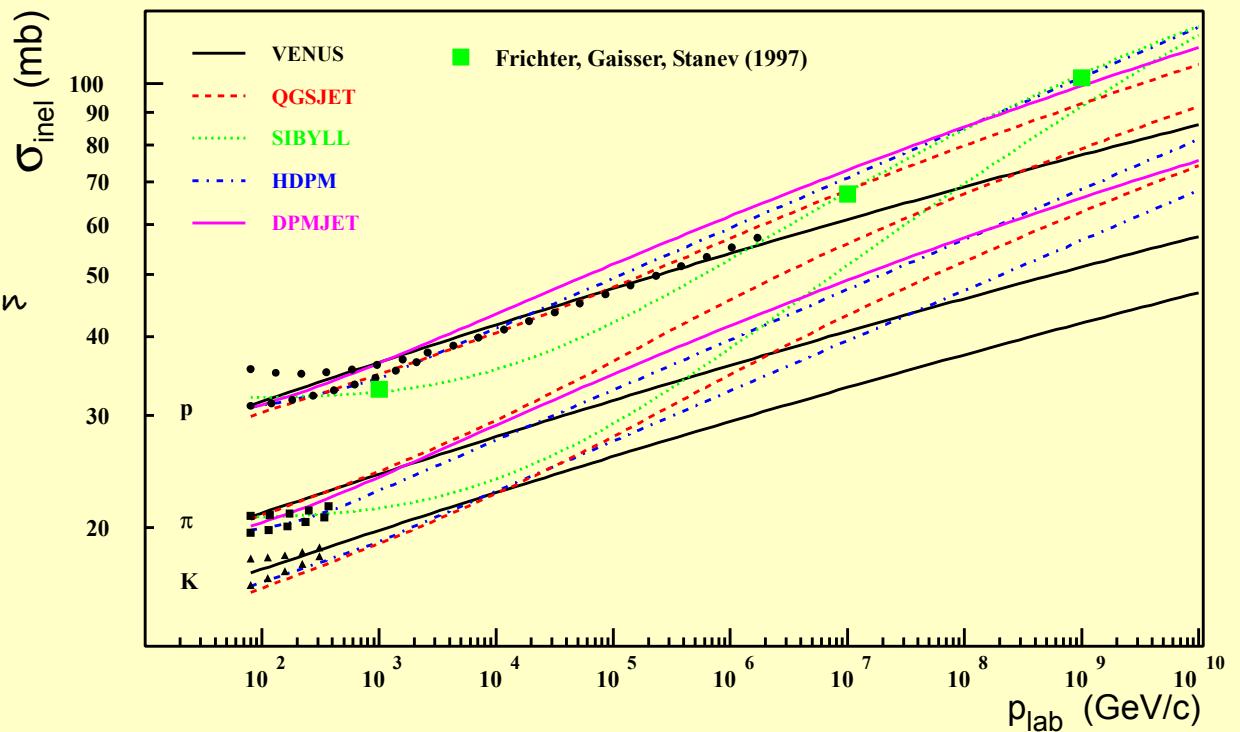
origin of difference?

what exactly is the nucleon distribution of a nucleus?

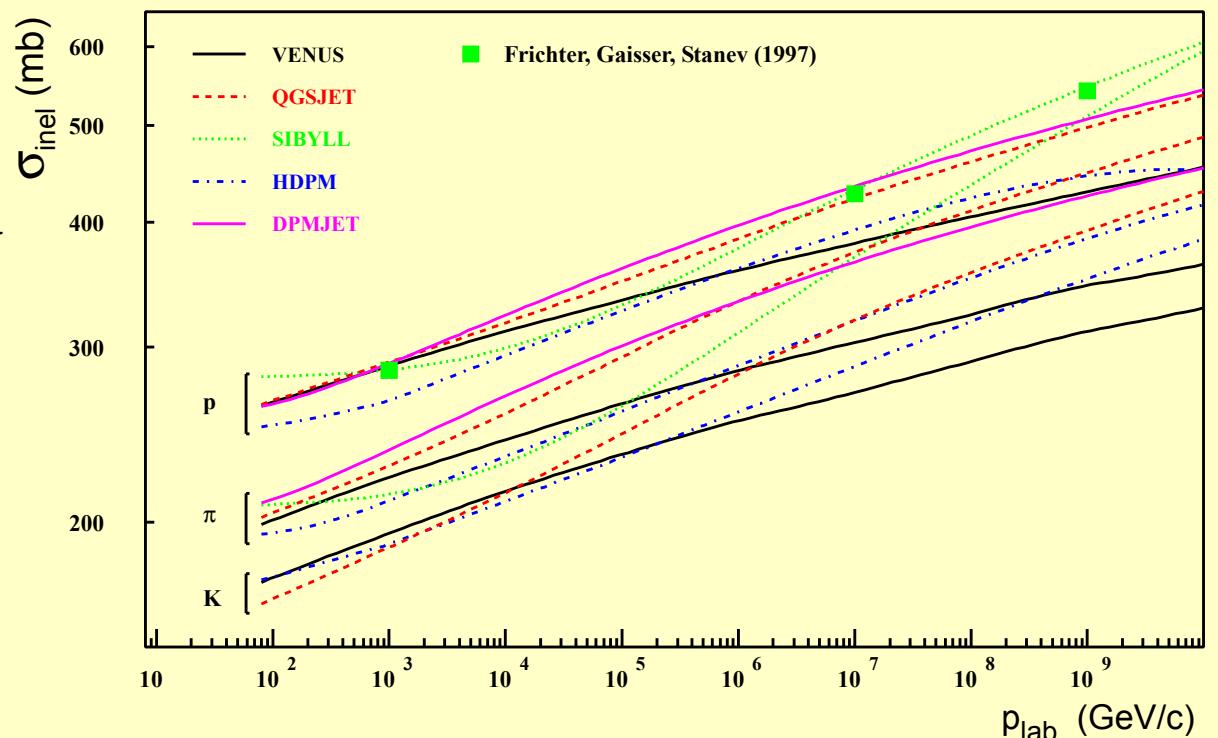
# Cross-sections on Proton and Air

Where data exist  
models agree,  
where no data exist,  
models diverge.

Hadron-Proton



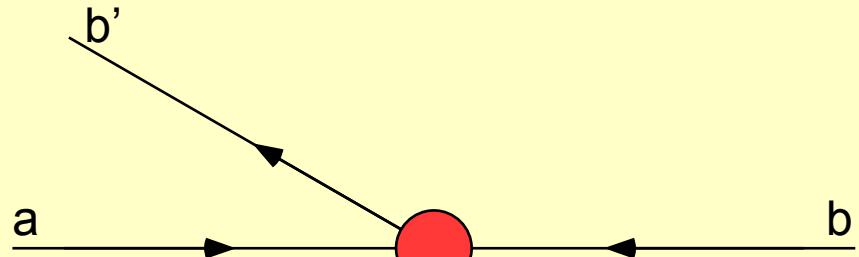
Hadron-Air



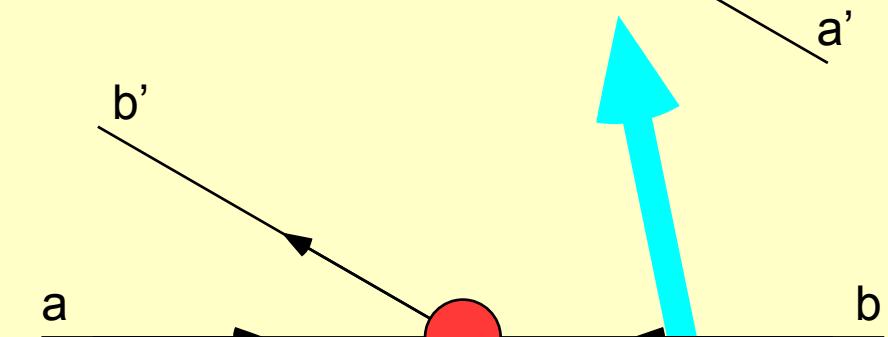
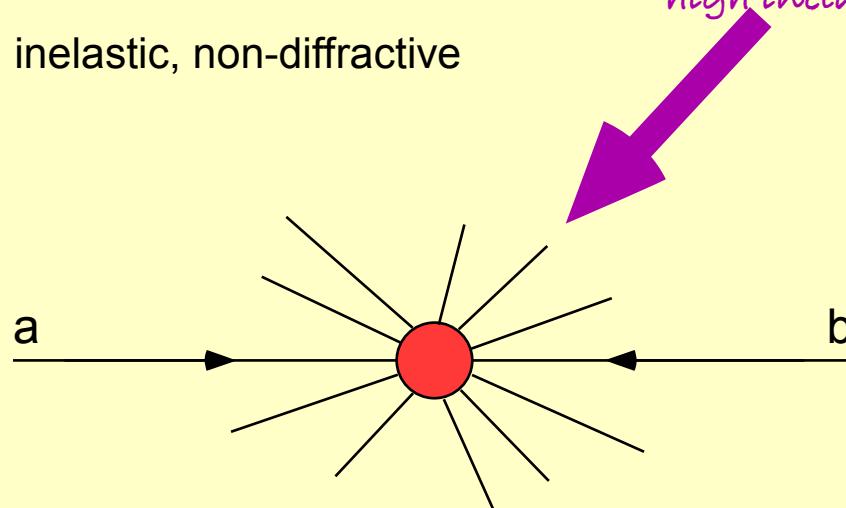
# Soft Hadronic Interaction Types

particle production,  
colour exchange,  
high center-of-mass energy,  
high inelasticity

elastic scattering

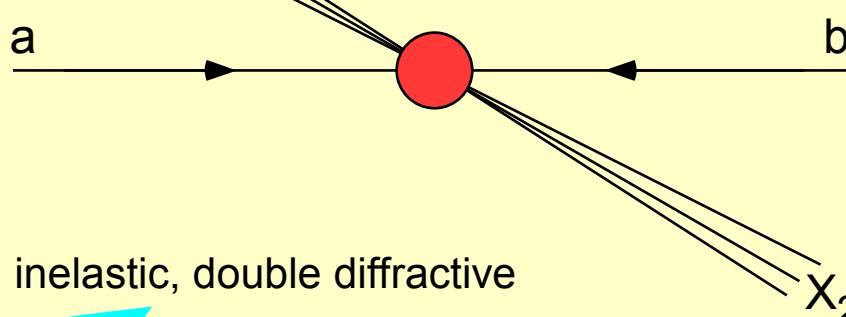


inelastic, non-diffractive



inelastic, single diffractive

no colour exchange,  
low center-of-mass energy,  
low inelasticity

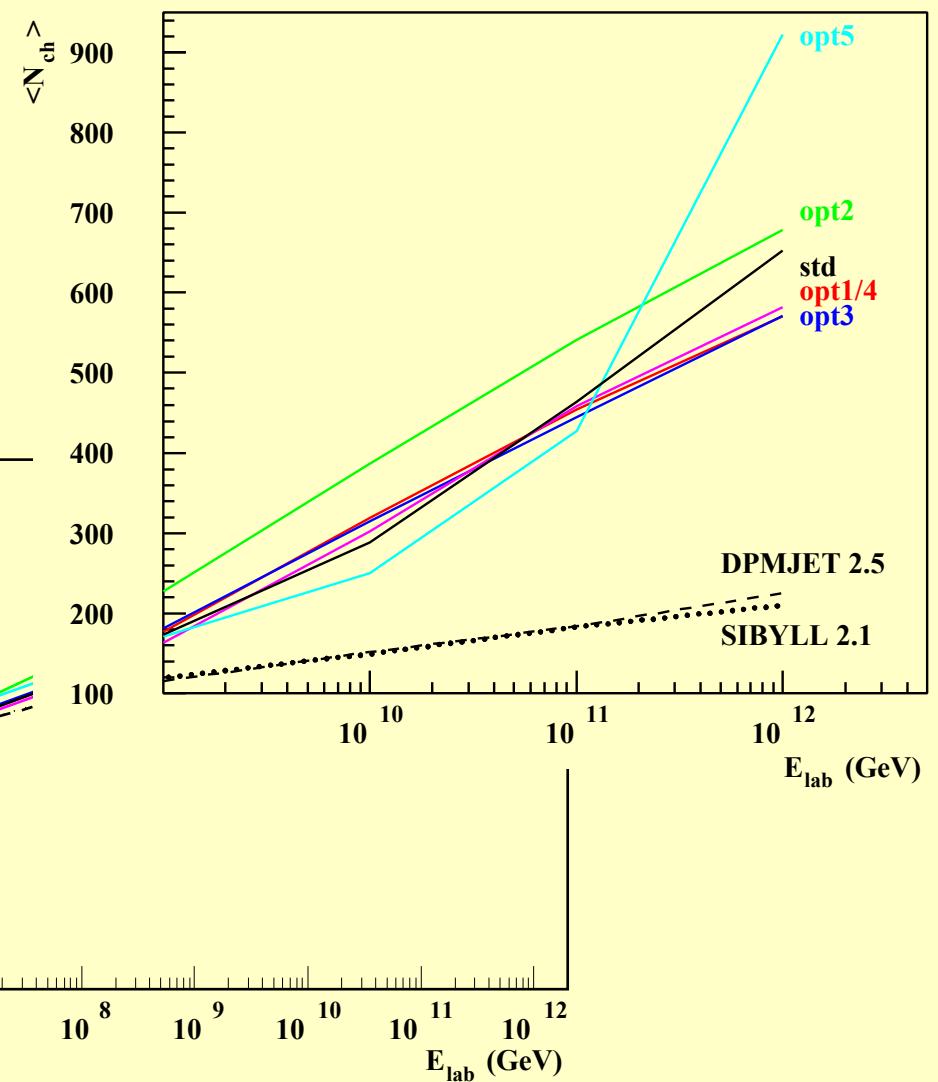
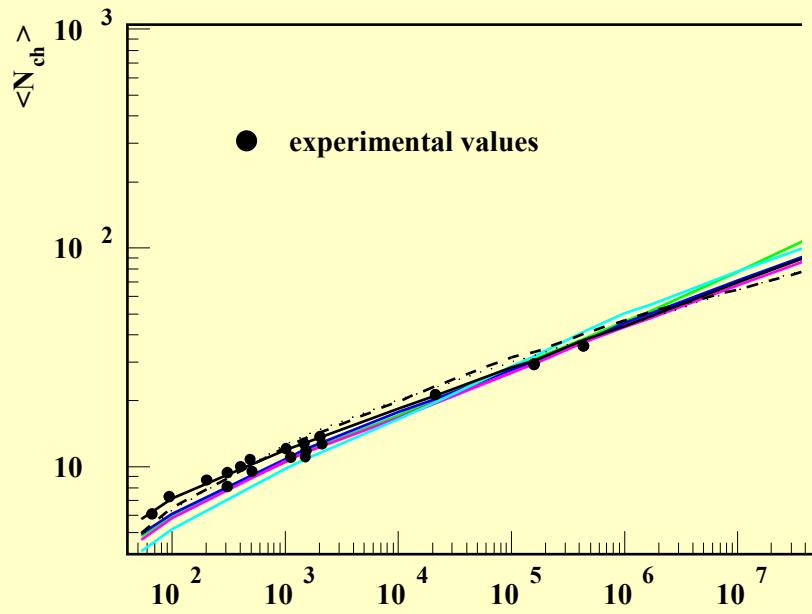


inelastic, double diffractive

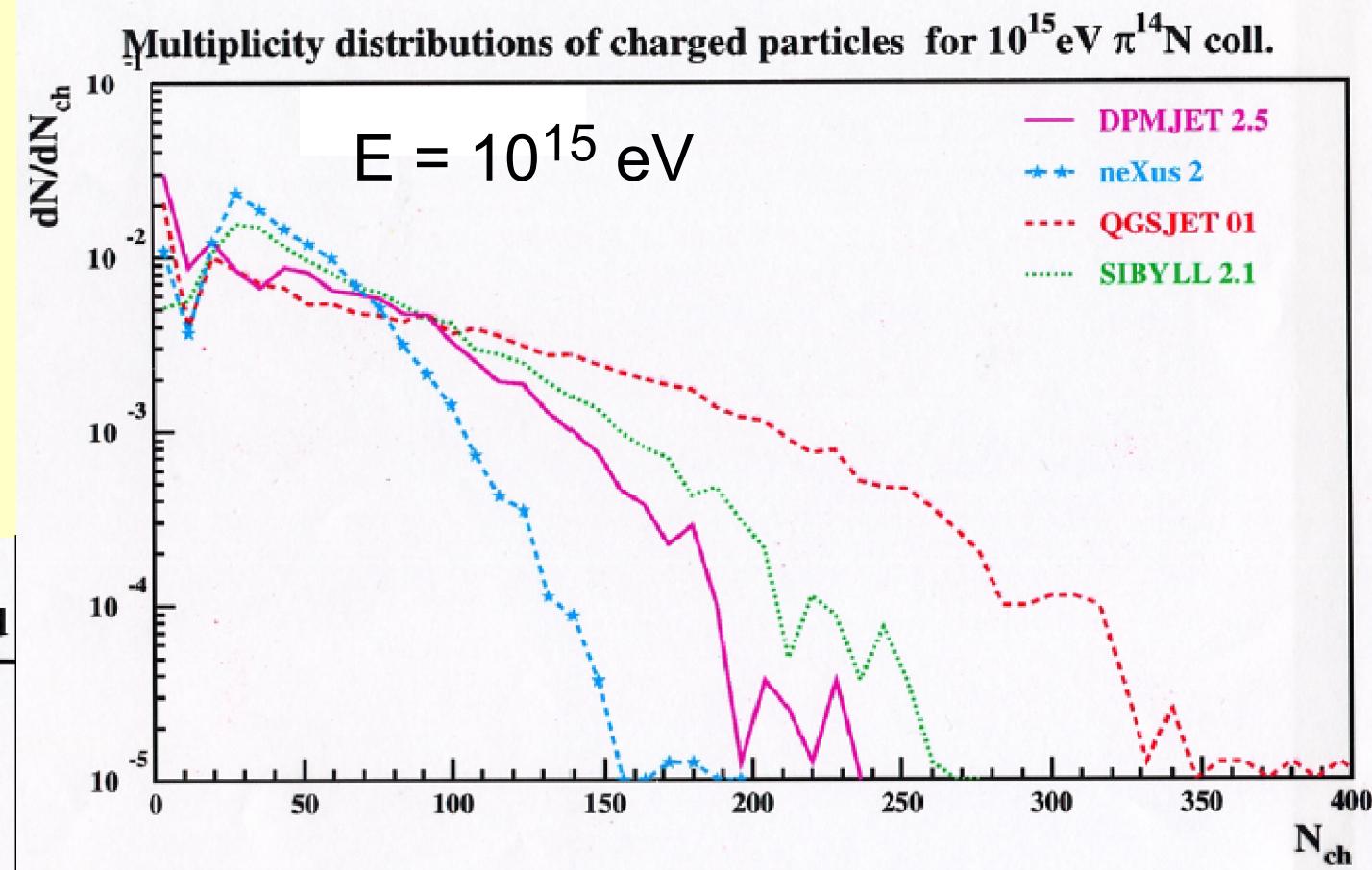
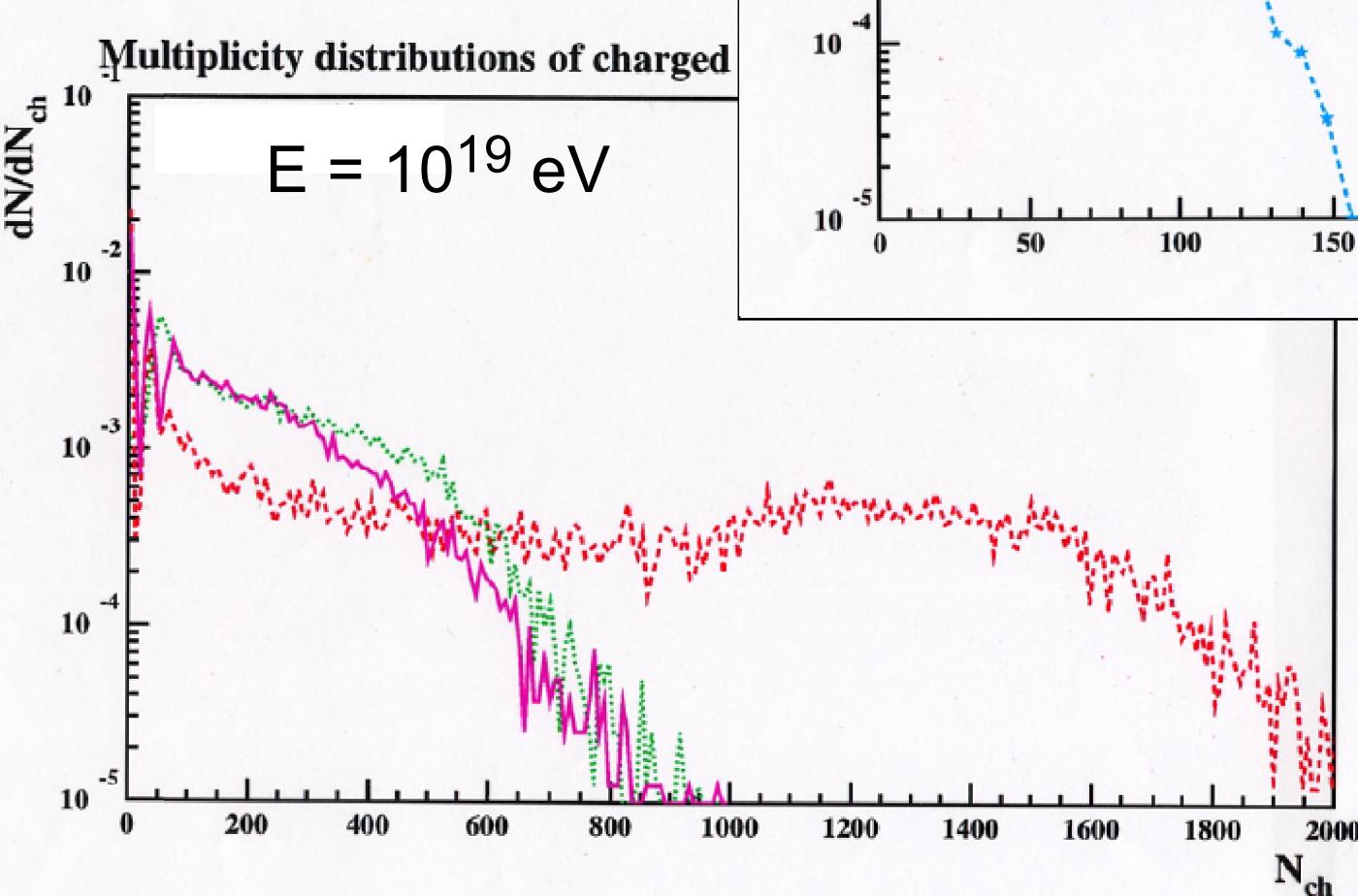
diffractive - non-diffractive  
ratio is very important

# Results on particle production

particle multiplicity  
in  $p\bar{p}$  collisions



*QGSJet produces  
much more secondaries  
than other models.*



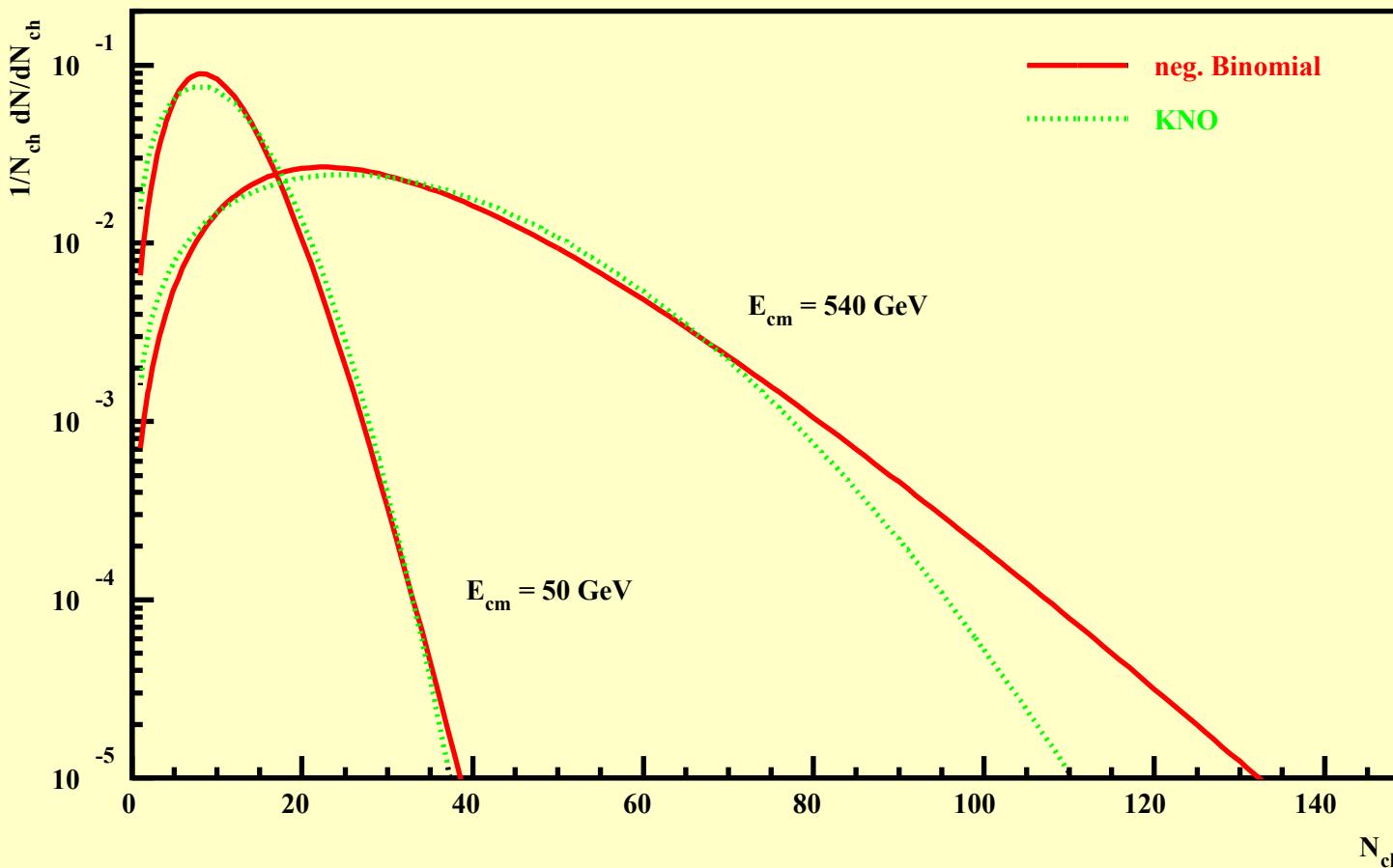
Huge difference,  
but does it matter ?

# Multiplicity Distribution

at high energies: **Negative Binomial Distribution**

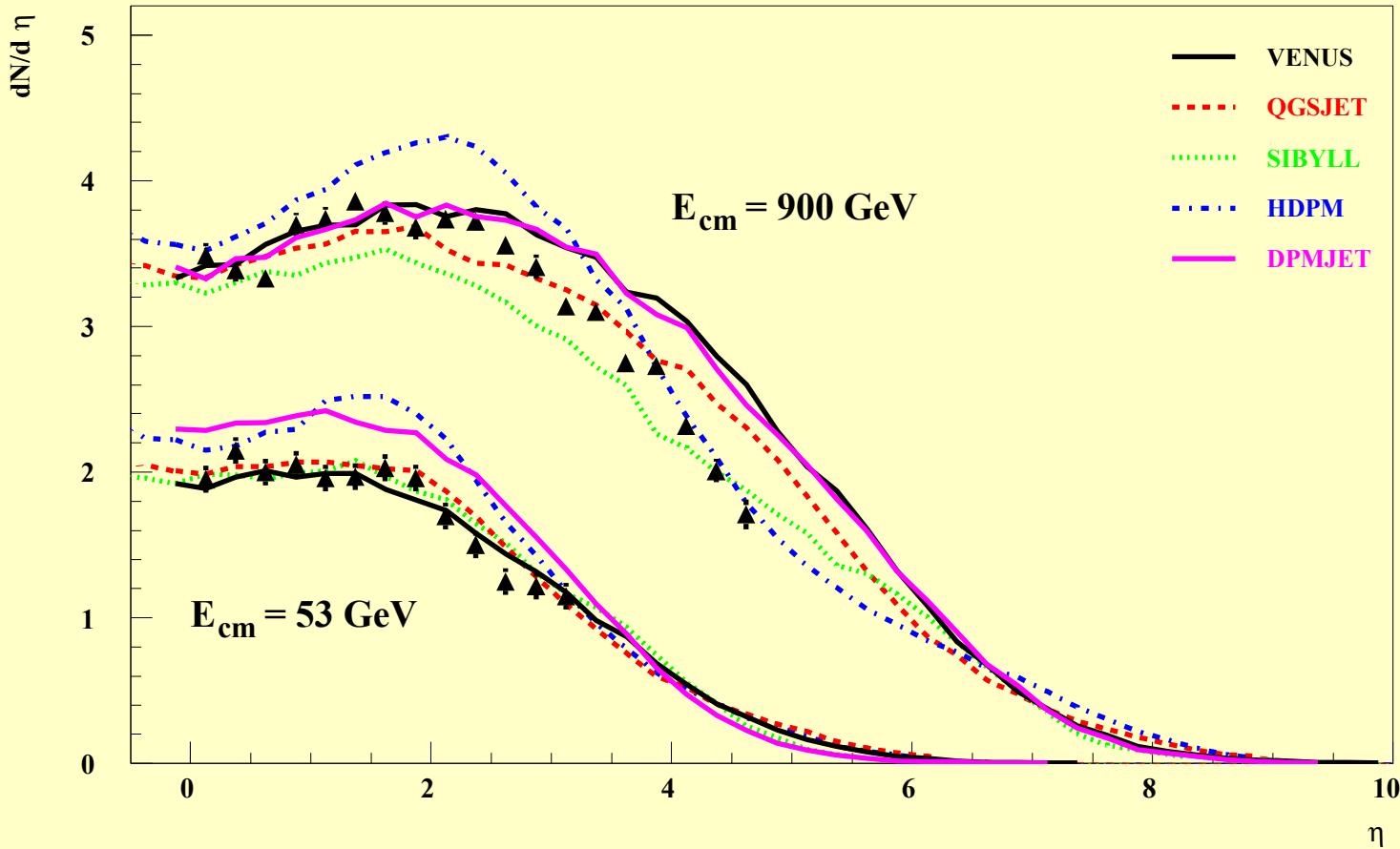
describes the wider range of values for  $n$  observed in collider data

$$P(n, \langle n \rangle, k) = \binom{n+k-1}{n} \left( \frac{\langle n \rangle/k}{1+\langle n \rangle/k} \right)^n \left( \frac{1}{1+\langle n \rangle/k} \right)^k$$



At  $\sim 10^{15} \text{ eV}$   
negative binomial  
distribution  
is needed to describe  
the experimental data.

# WA5 results at the SPPS



Rapidity:

$$y = \frac{1}{2} \ln \frac{E+p_L}{E-p_L}$$

Pseudorapidity:

$$\eta = \frac{1}{2} \ln \frac{p+p_L}{p-p_L}$$

$$\eta = -\ln(\tan(\theta/2))$$

$\eta \sim y$   
for high energies  
(or zero mass)

(Pseudo)rapidity  
is additive in Lorentz  
transformation.

Pseudorapidity ( $\eta$ ) distributions initially not very well described:  
models can fit either  $dN/d\eta (\eta=0)$  or  
the tail to large  $\eta$ -values,  
but not both.

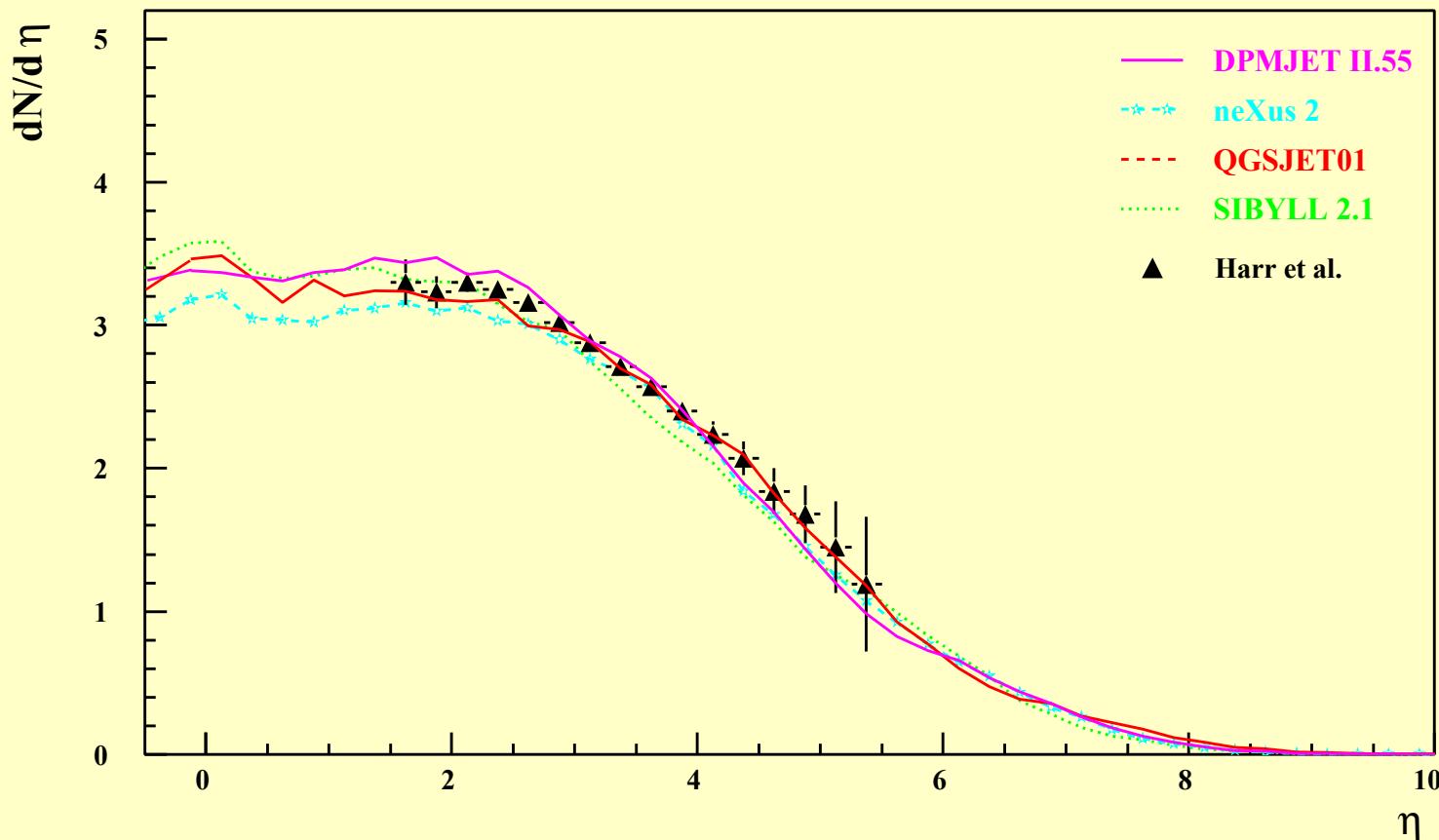
are models wrong or badly tuned?

## Another experiment at the same collider ....

$E_{cm} = 630 \text{ GeV}$

P238 (Harr et al.)

Simulations including experimental trigger

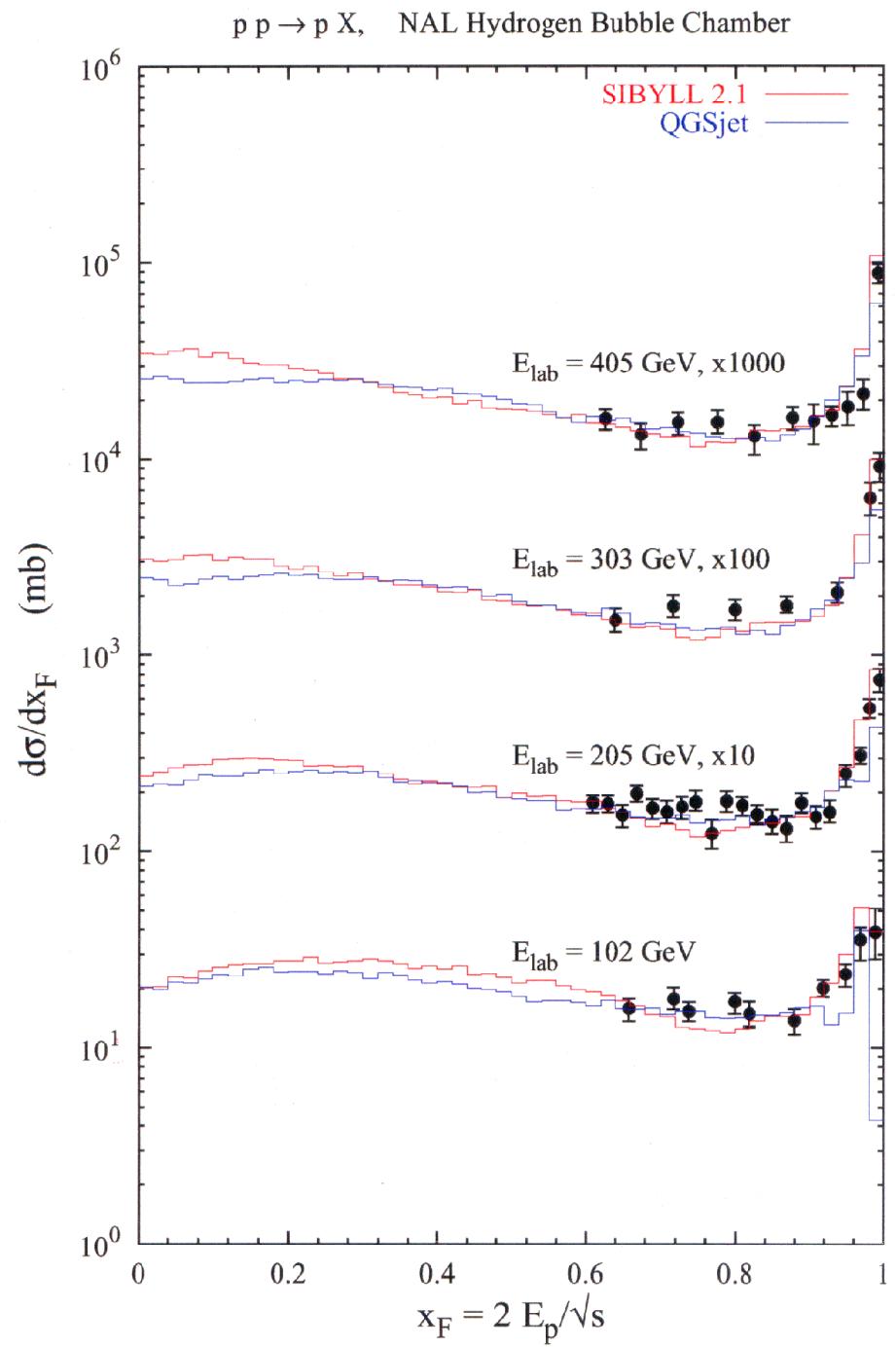
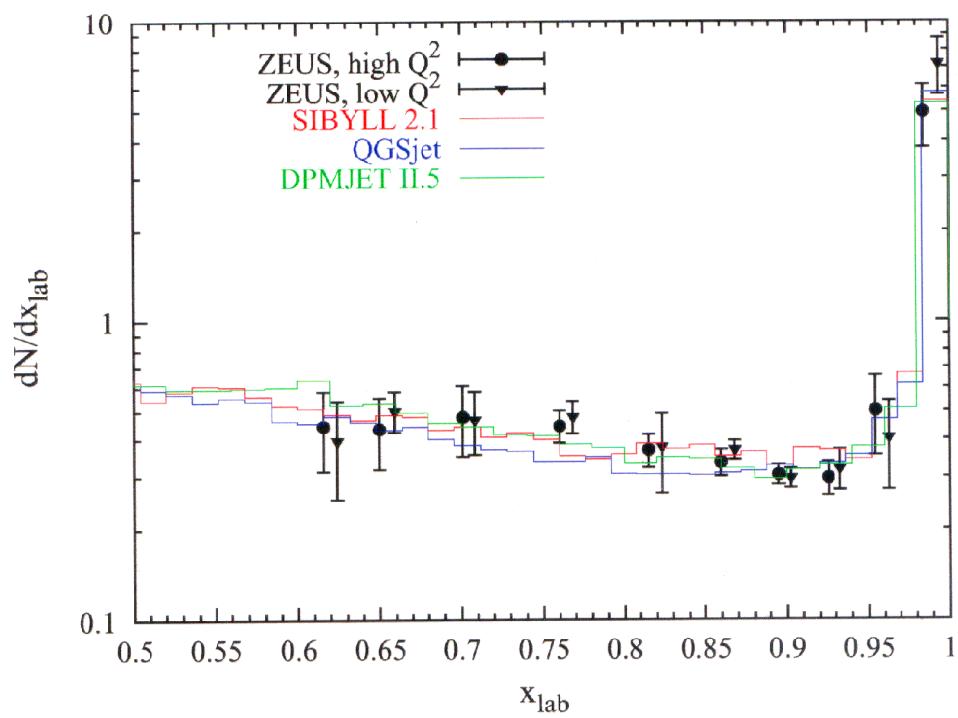


New experimental results in contradiction to older UA5 distributions,  
but very good agreement with simulations.

Experimental results are not always to be taken at face value.

# Particle production in forward direction

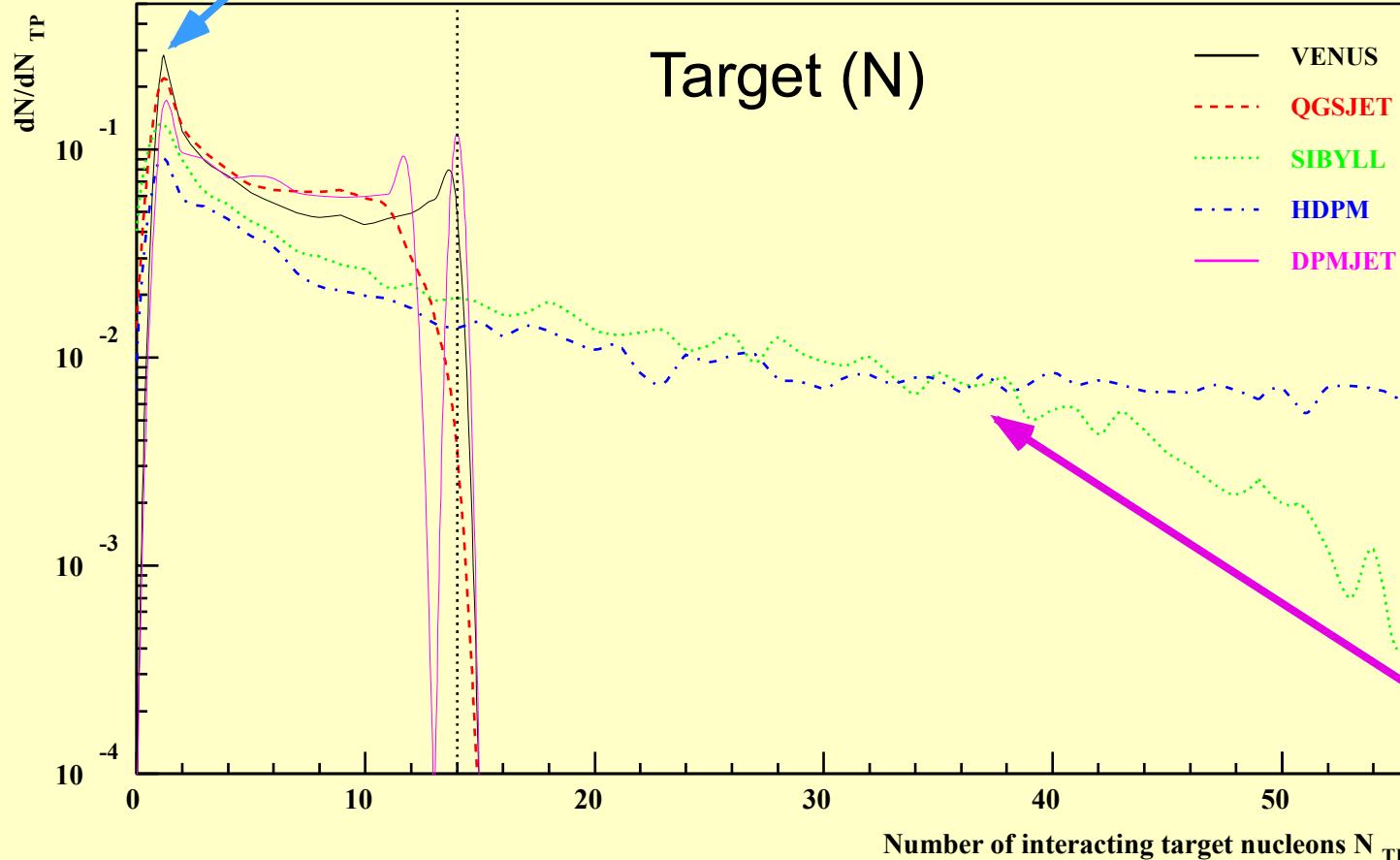
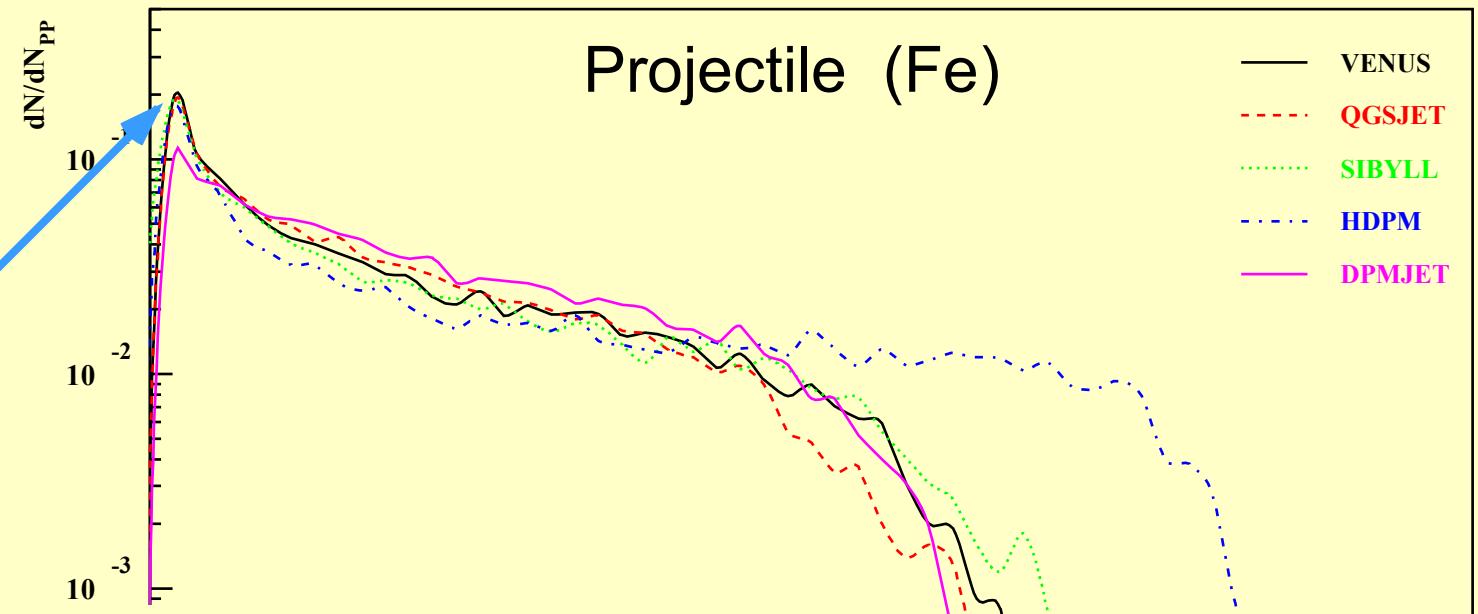
... important since forward particles carry energy efficiently down the atmosphere



# Projectile & Target Participants

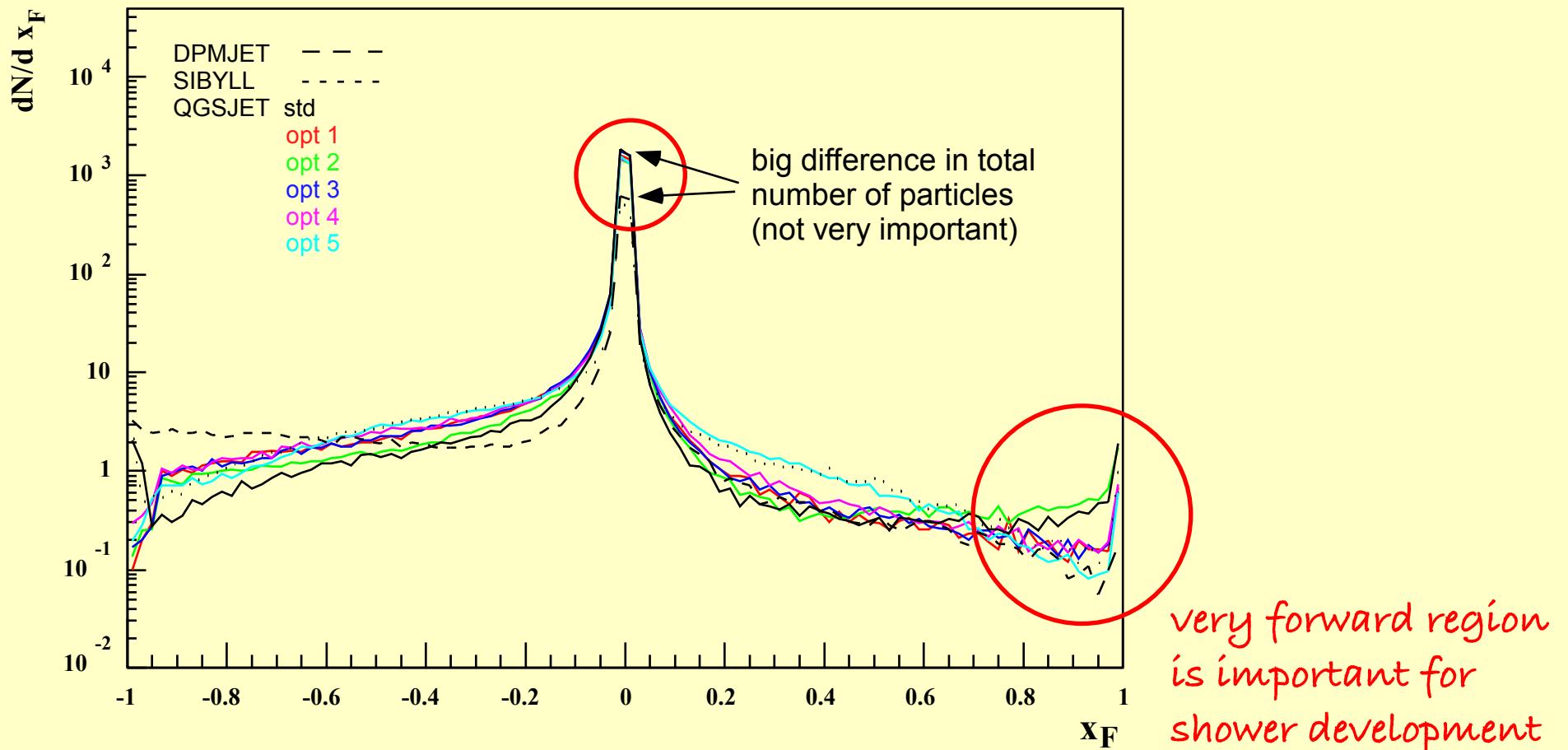
Fe - N collisions

most probable:  
one projectile nucleon  
hits one target nucleon

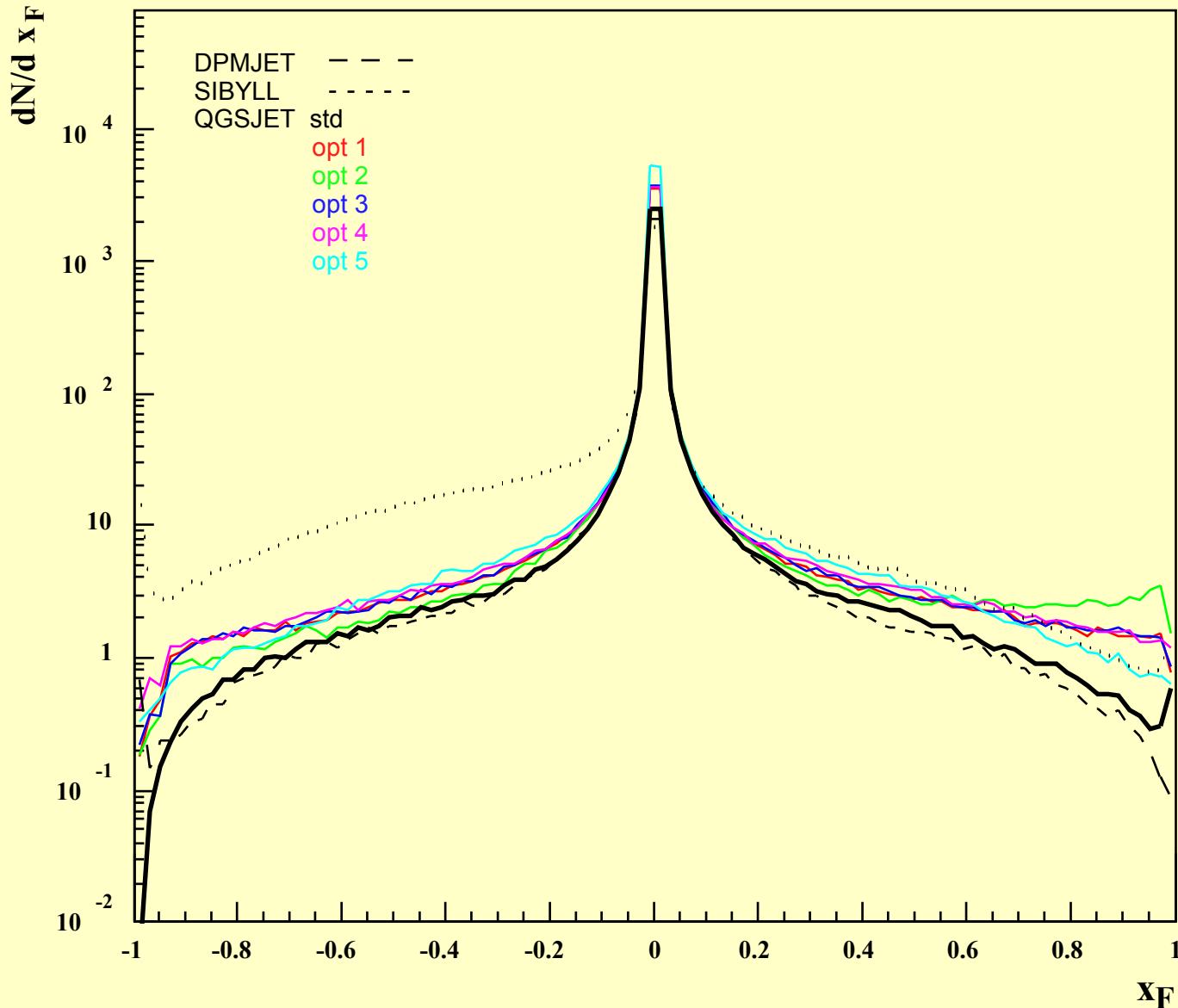


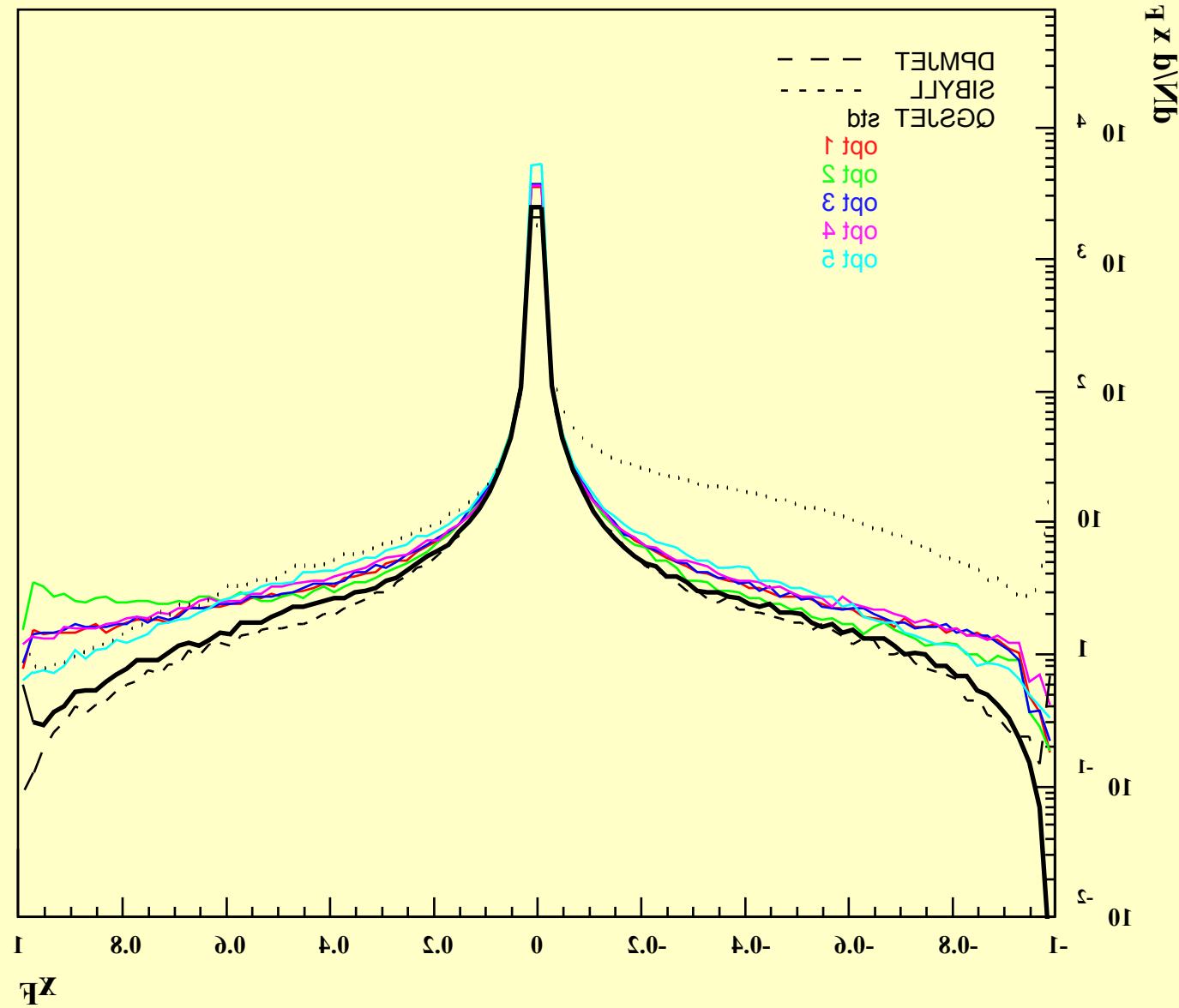
unphysical  
since too simple  
nucleus-nucleus  
model

# Feynman x distribution in p-N collisions



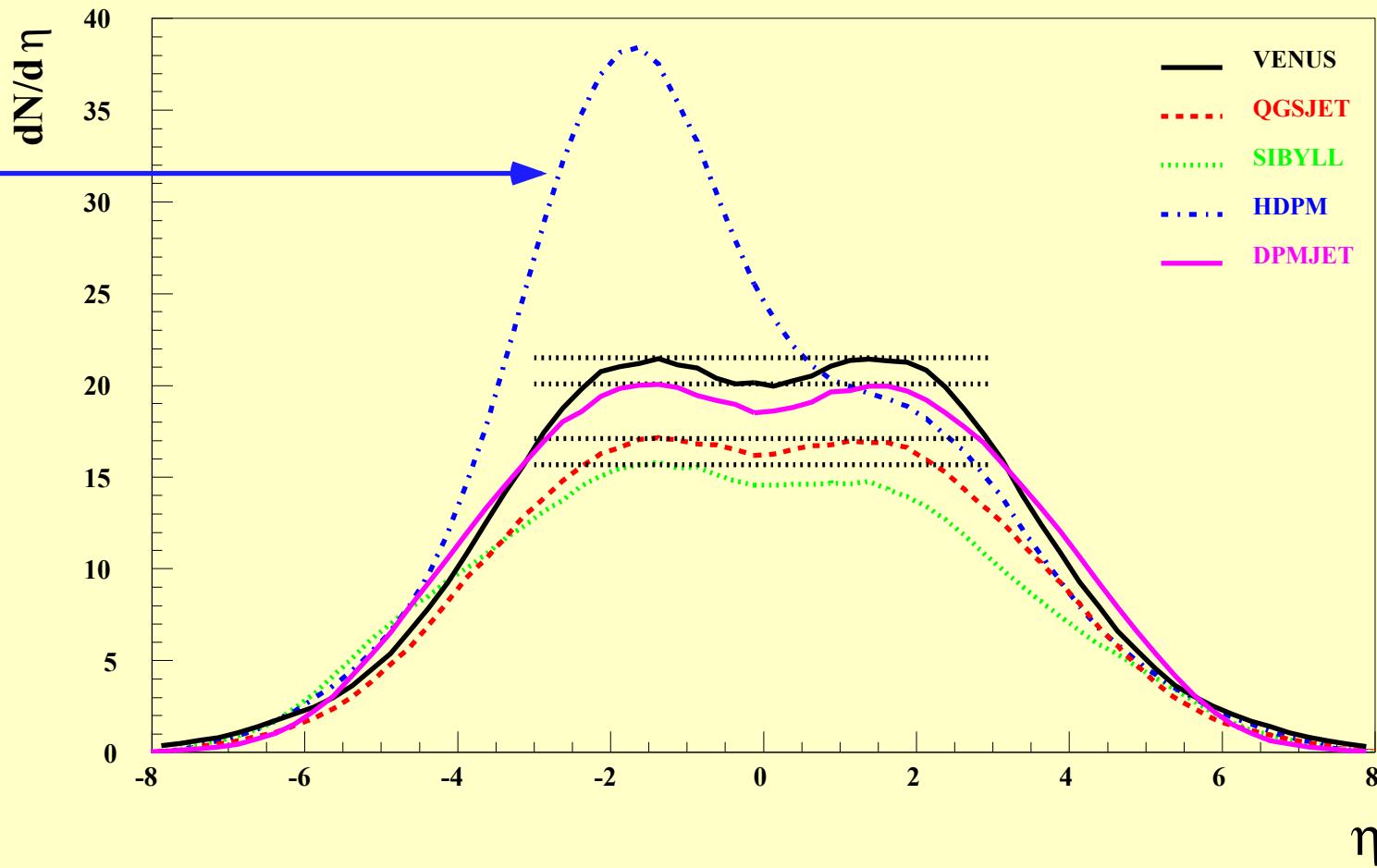
# Feynman $x$ distribution in N-N collisions ... ... should be symmetric as well





# Nitrogen-Nitrogen Collisions

very bad !



... should be perfectly symmetric,  
if nuclear interactions are treated well.

# Longitudinal Shower Profiles

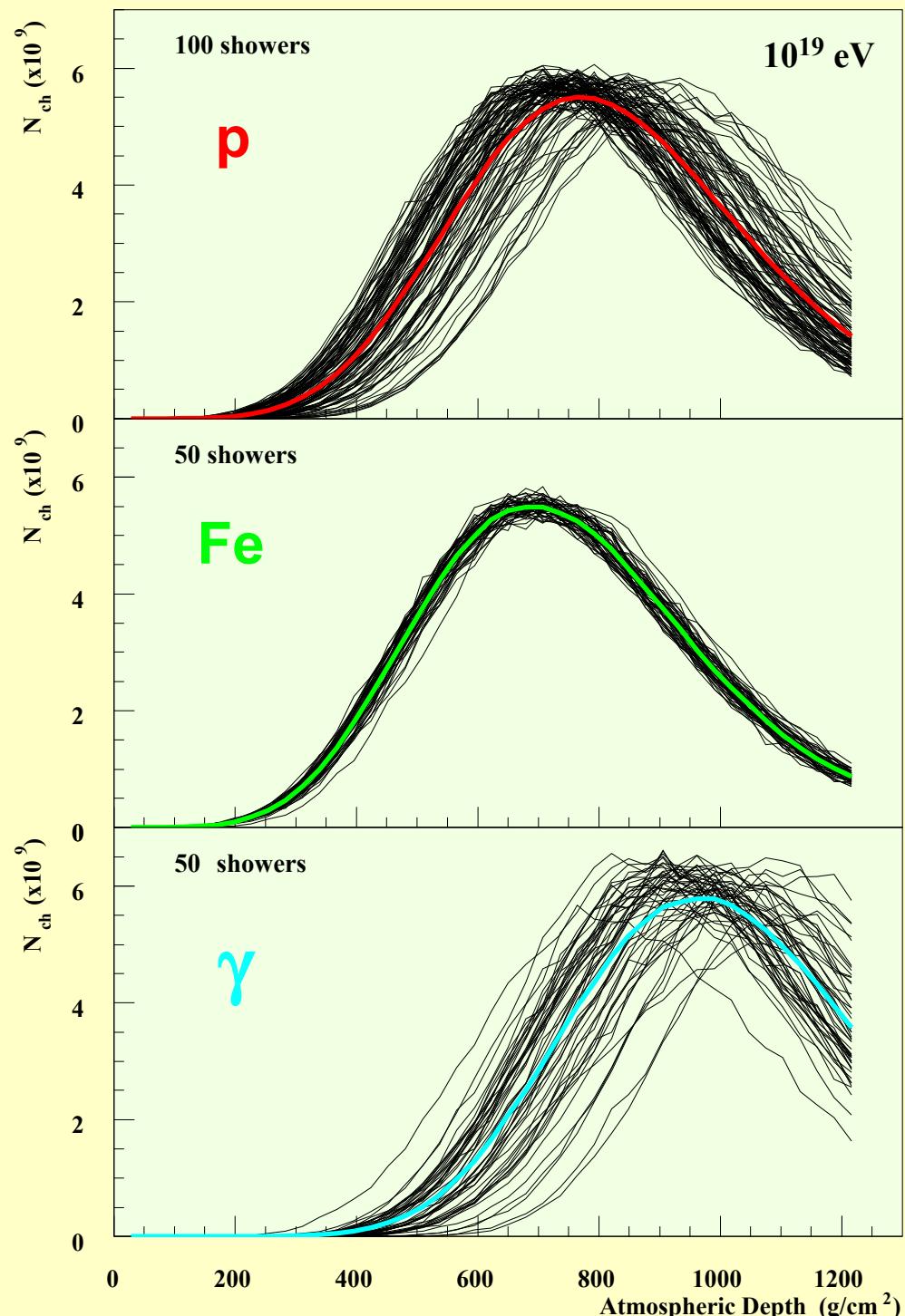
difference in  $x_{\max}$   
but large fluctuations

differences between  
hadrons and photons are large

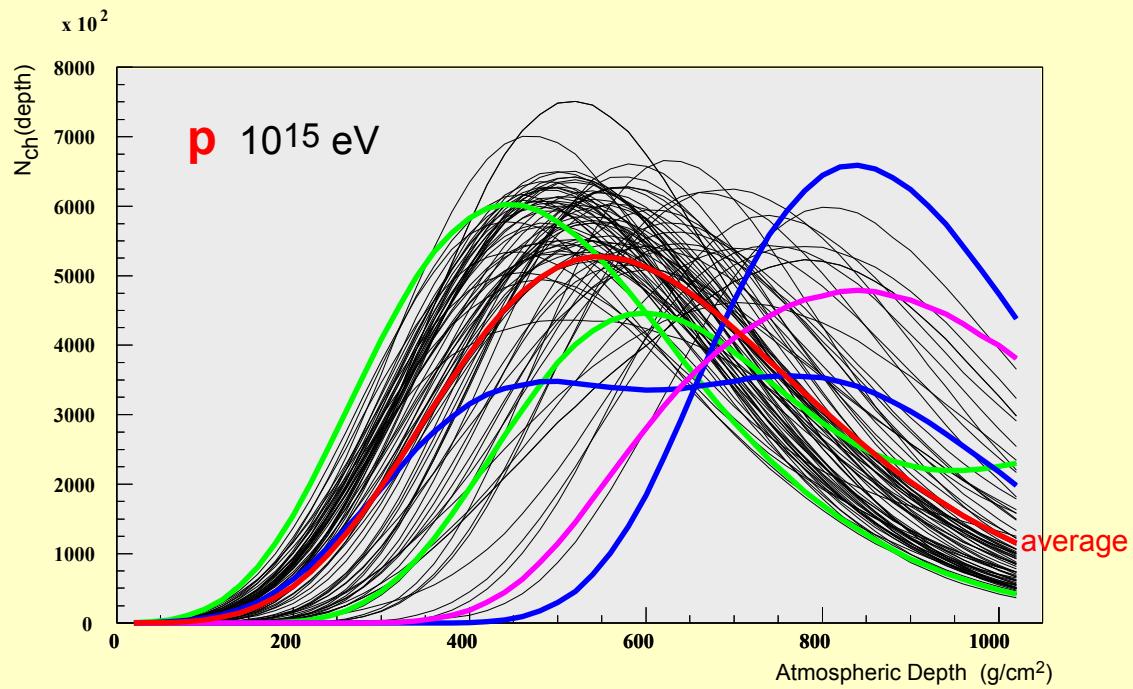
differences between  
proton and iron (or nuclei)  
are subtle

On average Fe have:

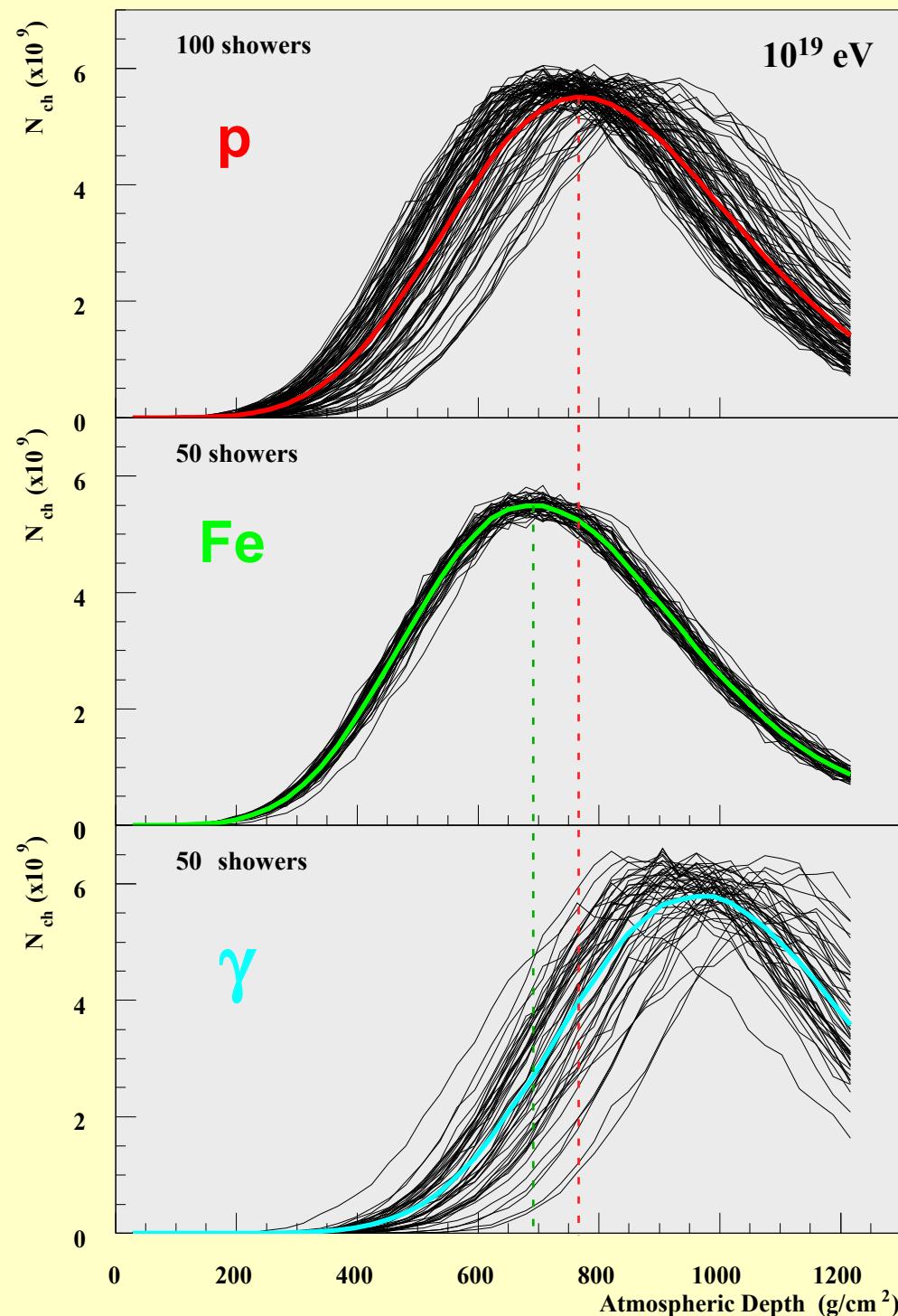
- higher 1st interaction, since  $\sigma_{\text{int}}$  larger,
- more secondaries, since  $N_{\text{sec}} \sim \ln(E)$ ,
- more  $\mu$ , less  $e, \gamma$  at ground,
- smaller fluctuations,  
since superposition of 56 subshowers
- faster signal rise, since  $\mu$ s faster  
than p showers.



# Longitudinal Shower Development

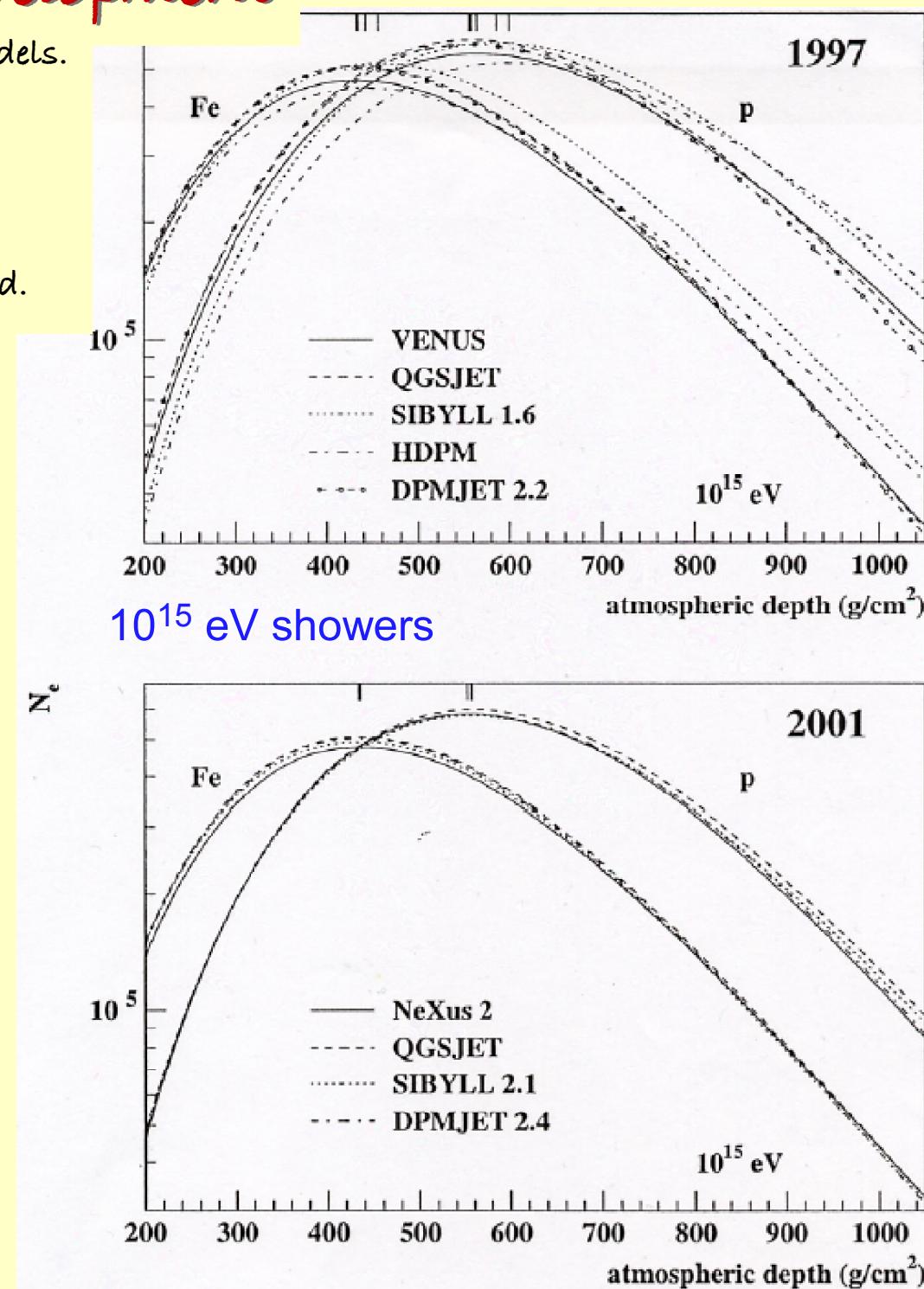
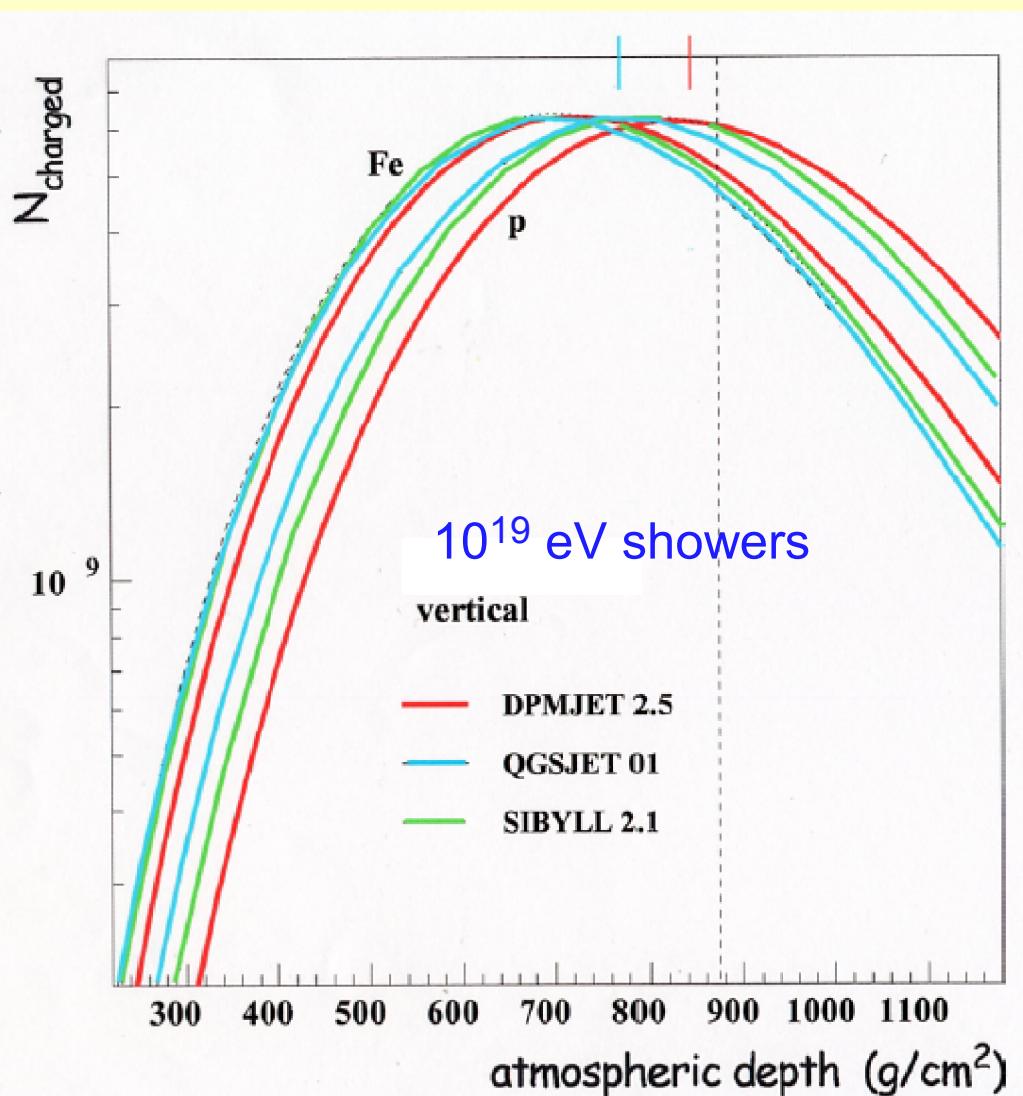


at lower energies:  
 large fluctuations  
 "strange" shower curves because of  
 fluctuations in height and type of  
 first few interactions.

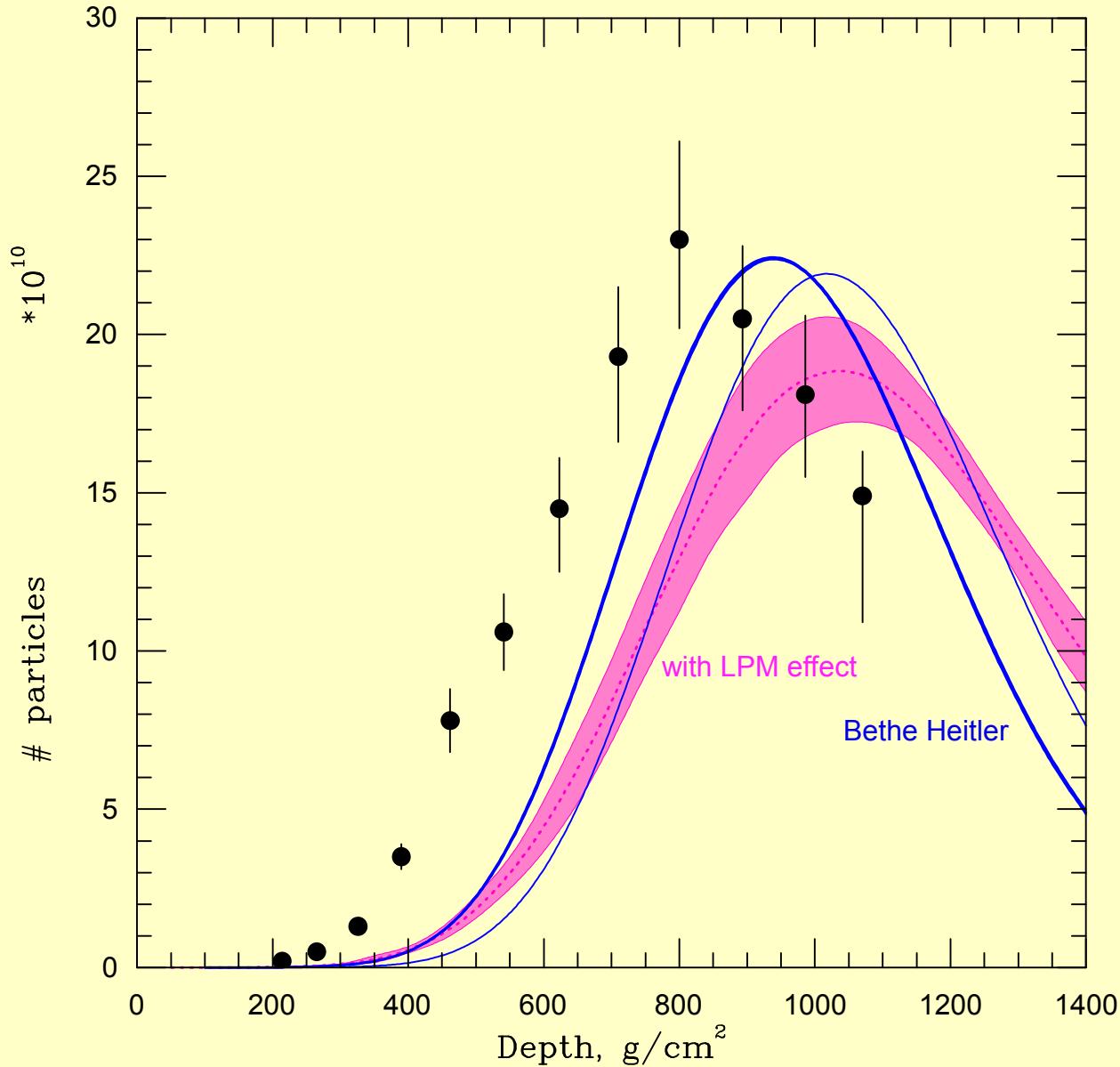


# Average Longitudinal Shower Development

QGSJET well in line with other models.  
High multiplicity  
partly compensated by  
lower cross-section and  
partly irrelevant since mostly  
low-energy particles produced.

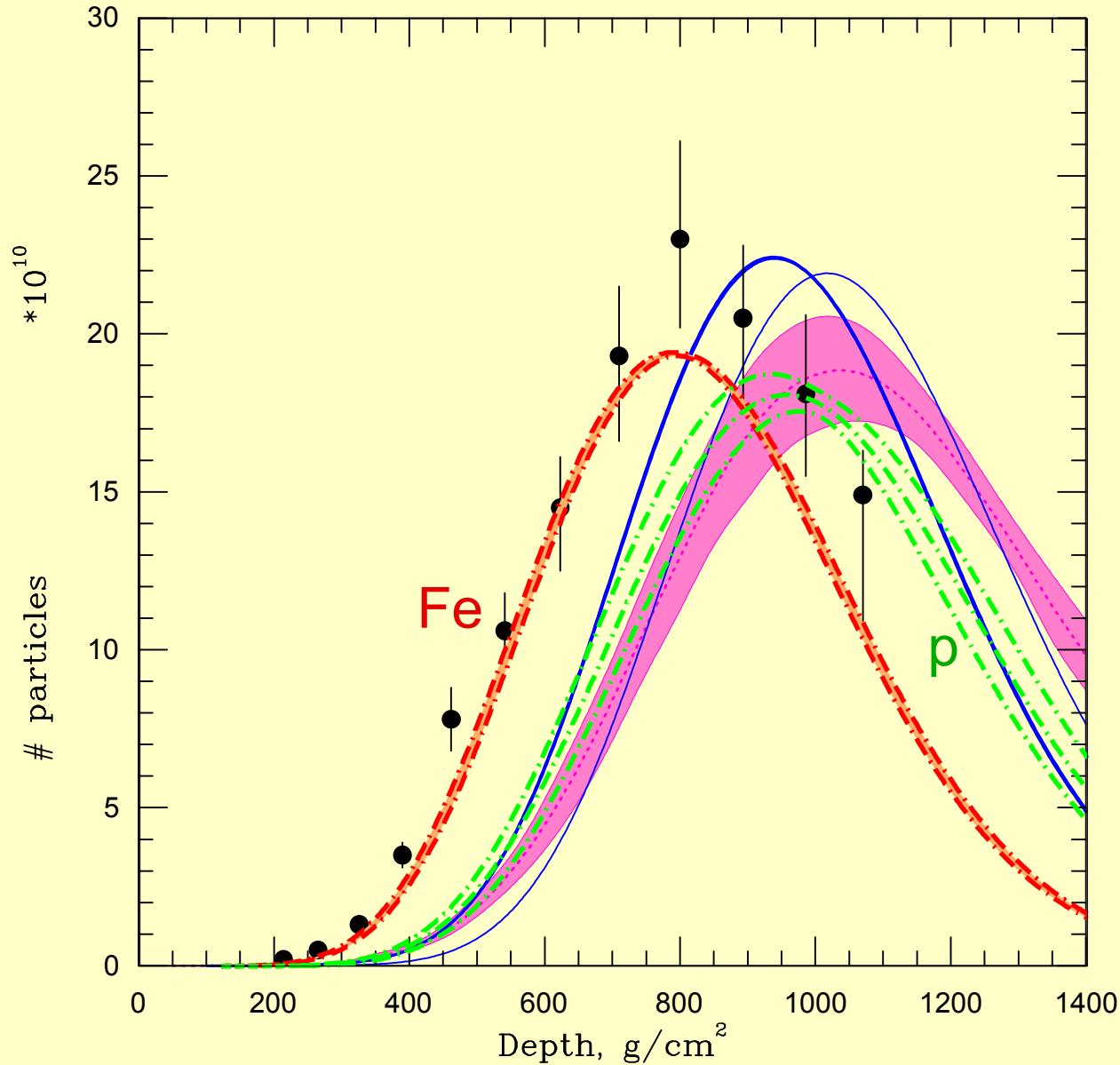


# The $3 \times 10^{20}$ eV Fly's Eye Event ... is it a photon shower?



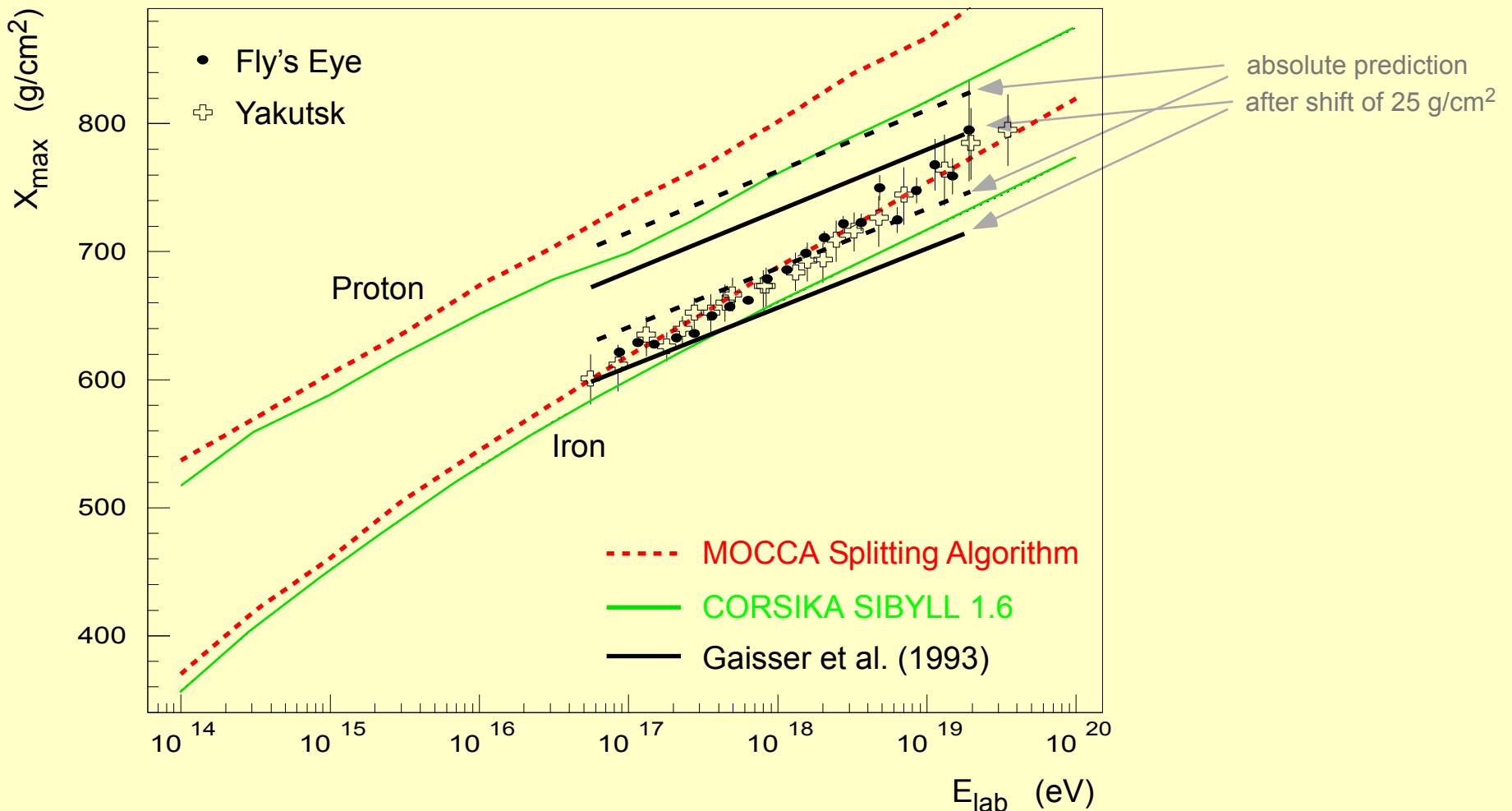
# The $3 \times 10^{20}$ eV Fly's Eye Event

... is it a photon shower?



# Data versus Simulations

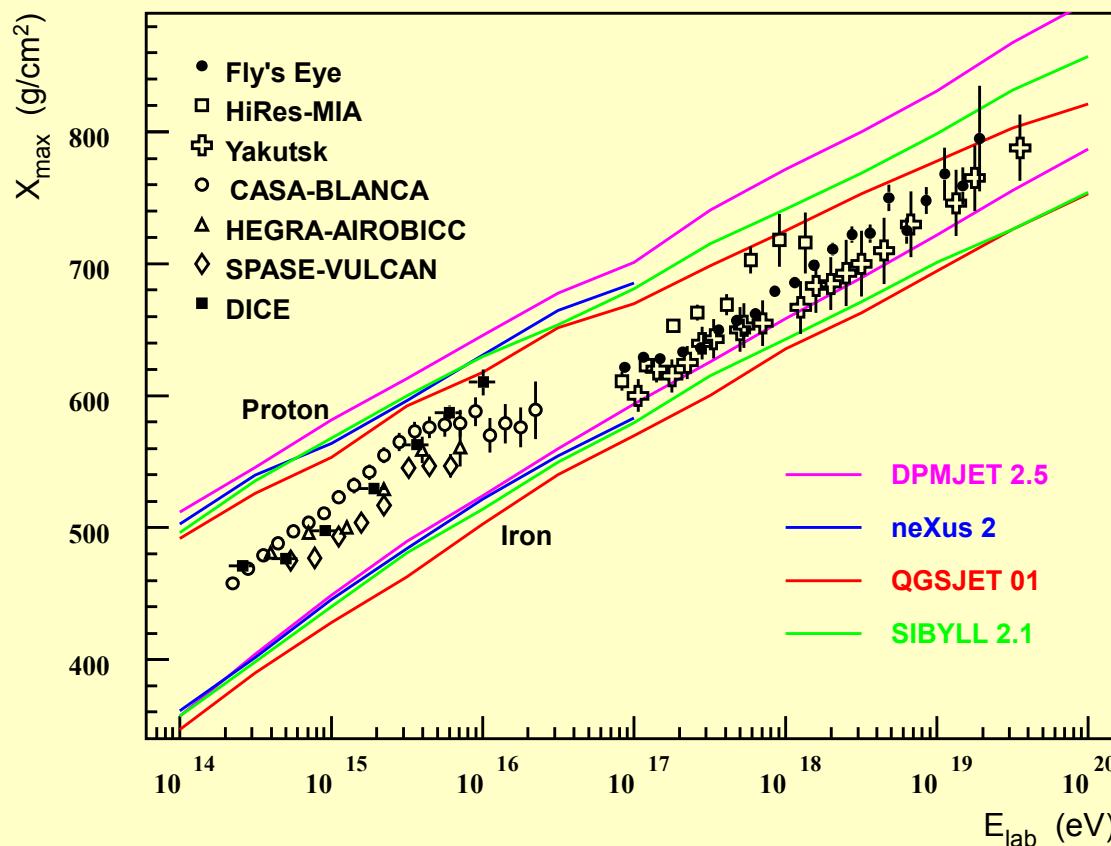
$X_{\max}$  versus energy : comparison with model suggested  
composition change from Fe to p



# Data versus Simulations

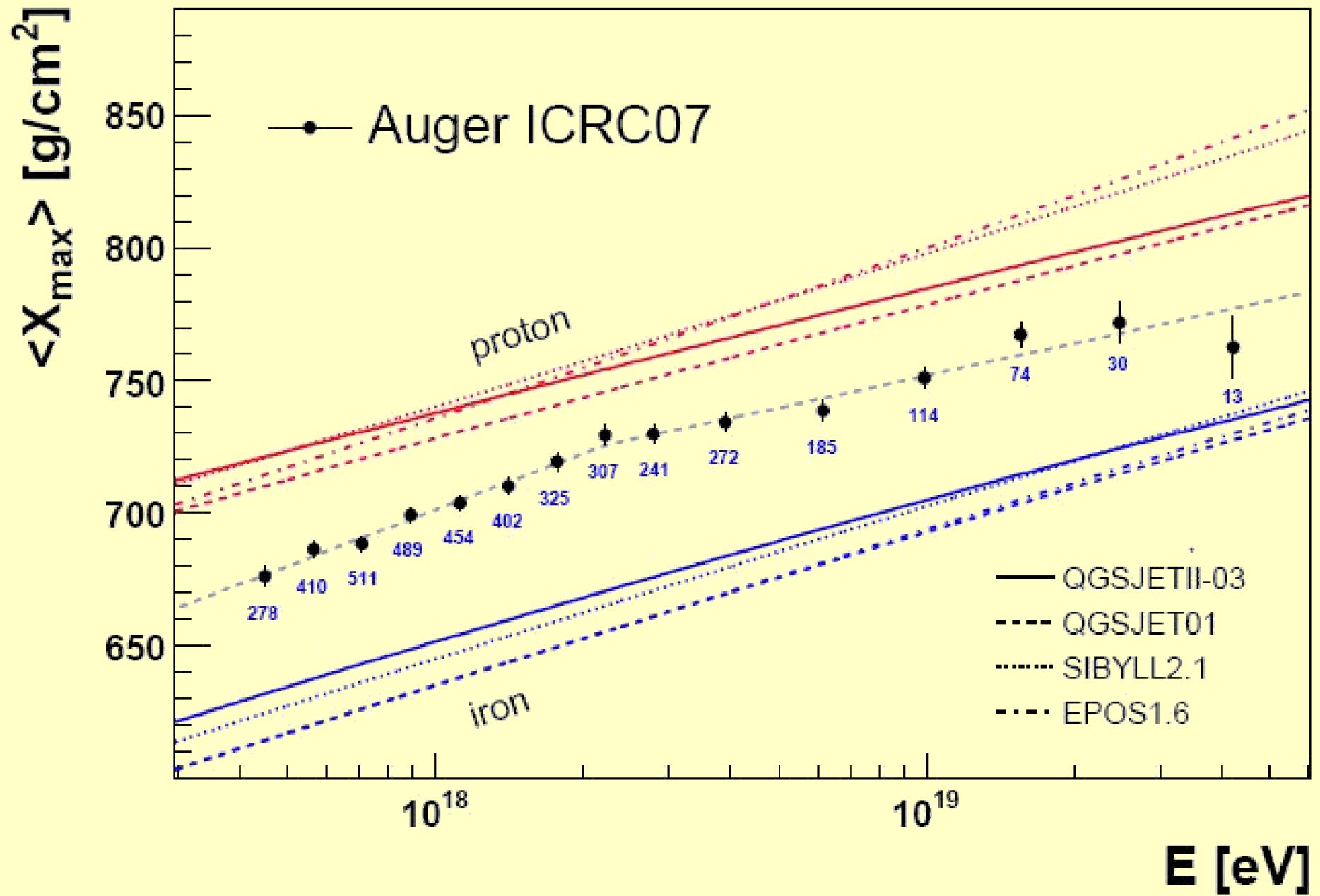
$X_{\max}$  versus energy

Now: in general good agreement (absolute prediction) over 6 orders of mag.



Model dependence of composition persists, though at much lower level.

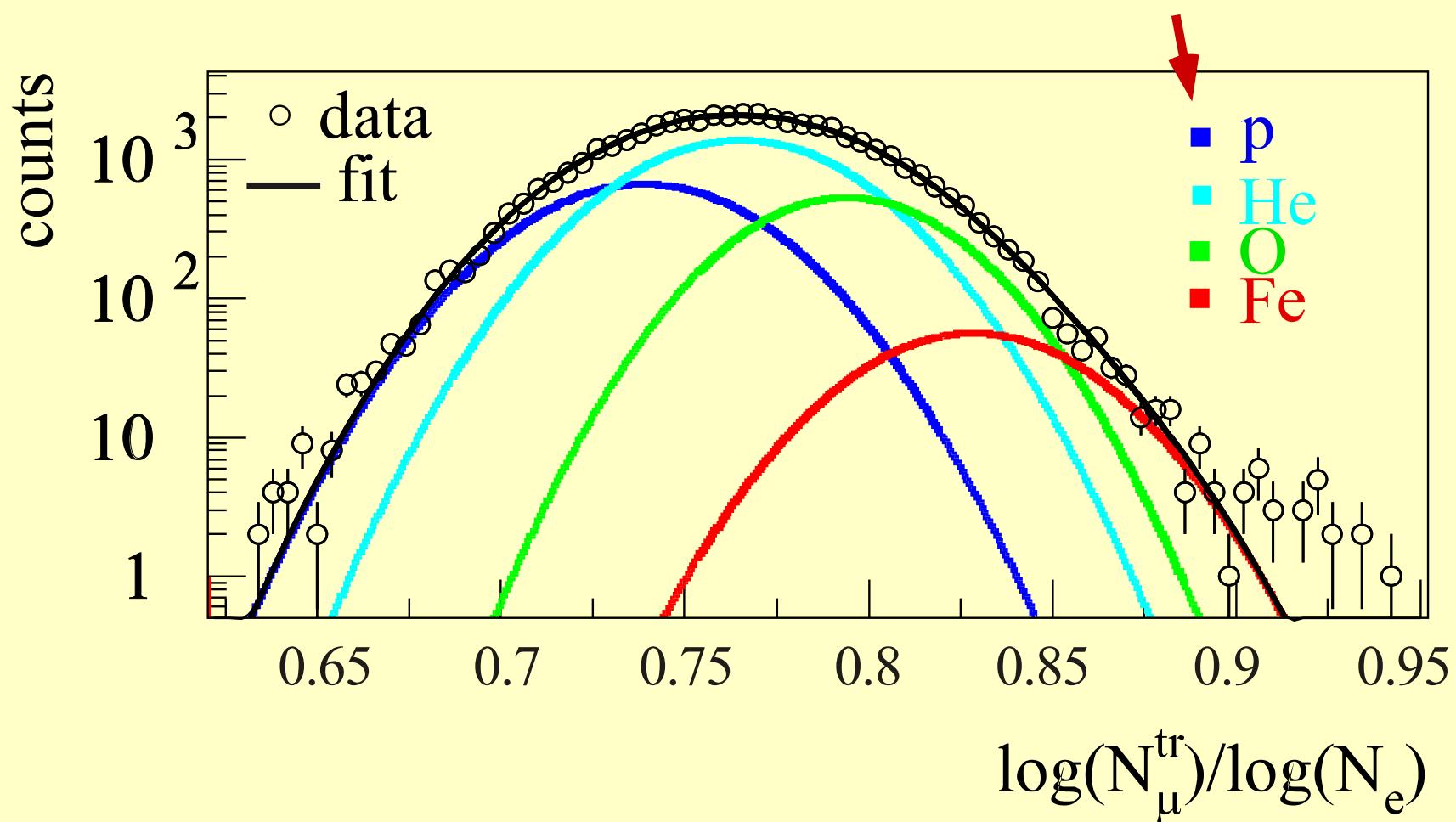
# Data versus Simulations



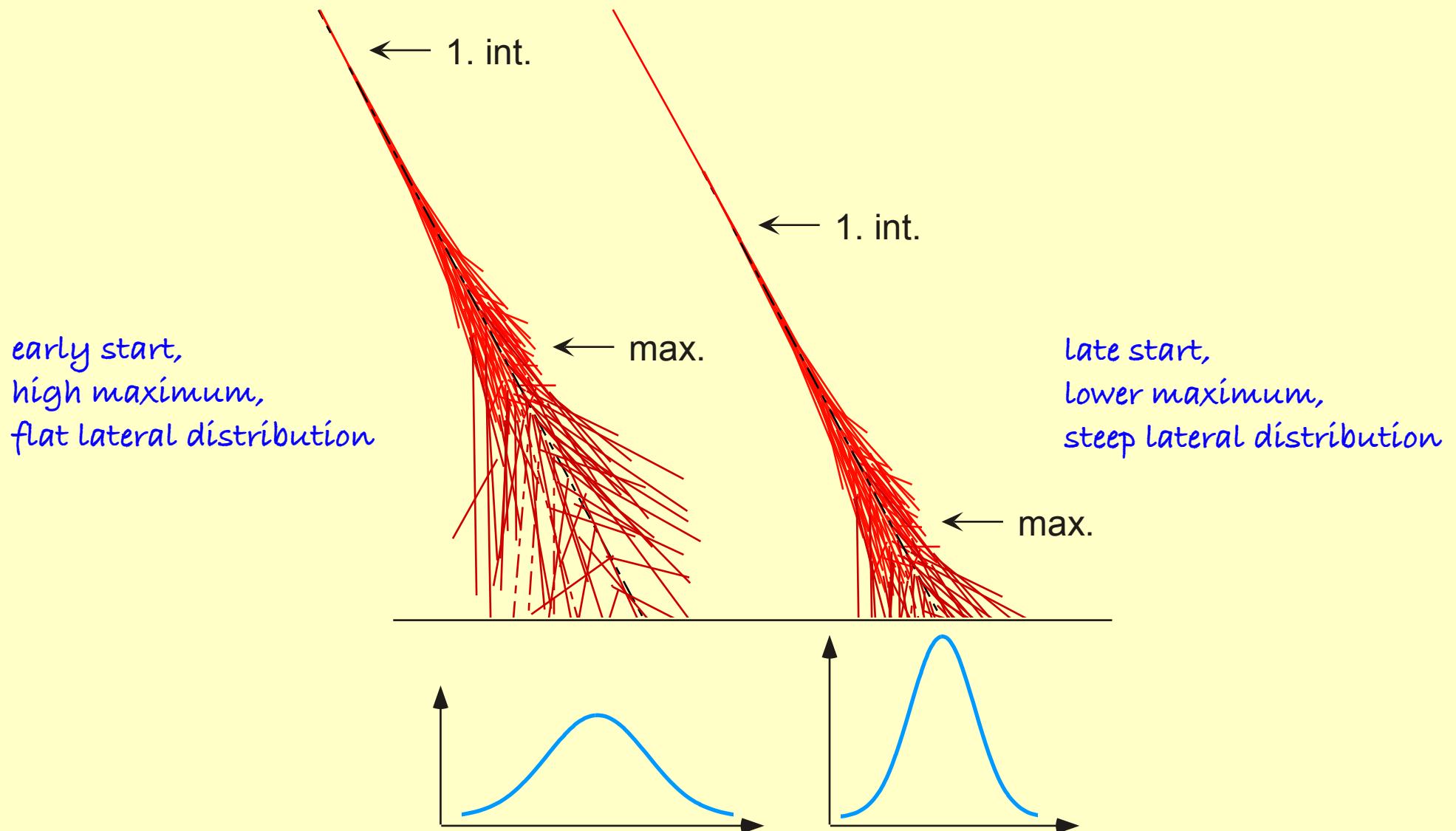
# Data versus Simulations ... another example

KASCADE:  $10^{15} - 10^{16}$  eV  
muon-electron ratio

CORSIKA Simulations

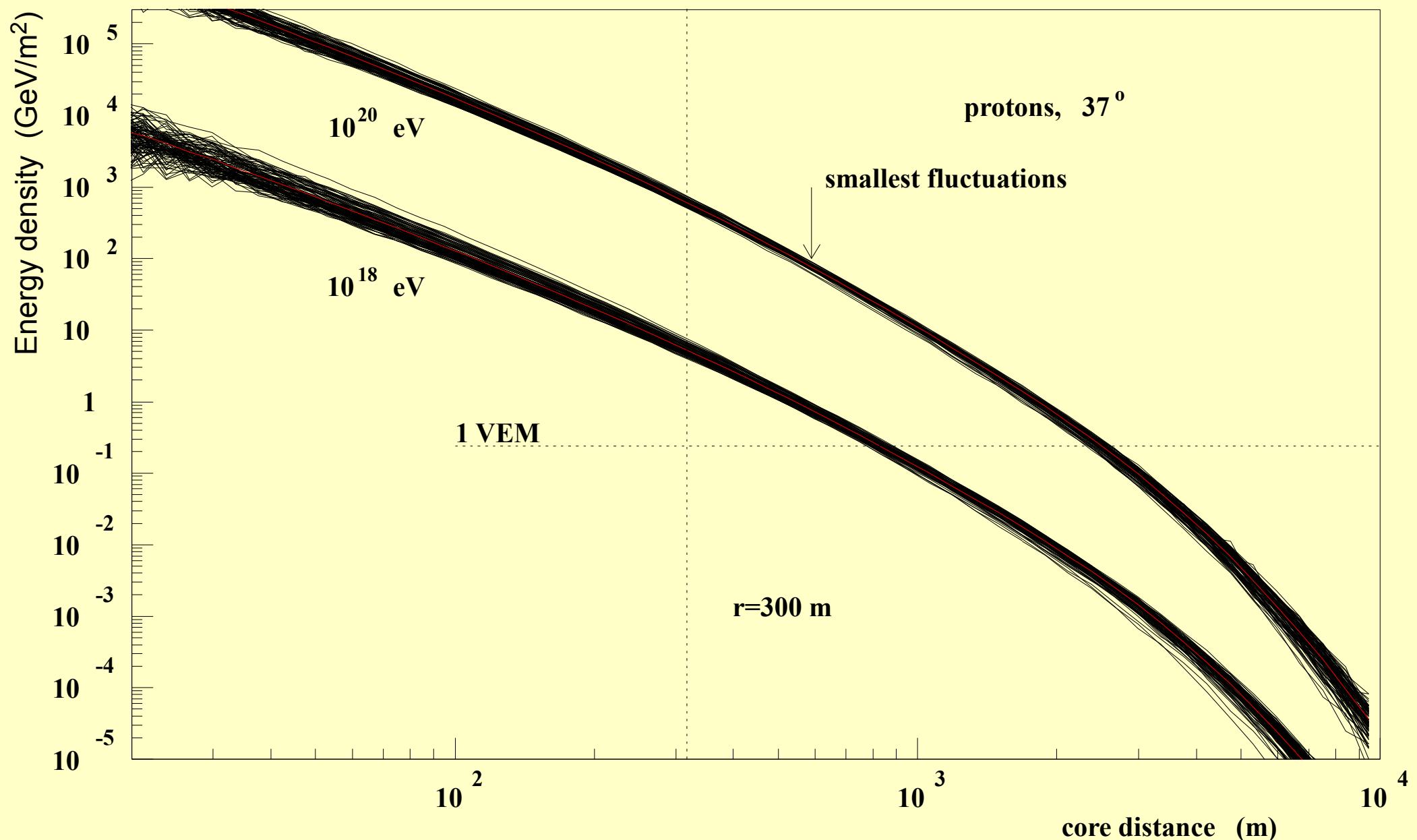


# Lateral Distribution

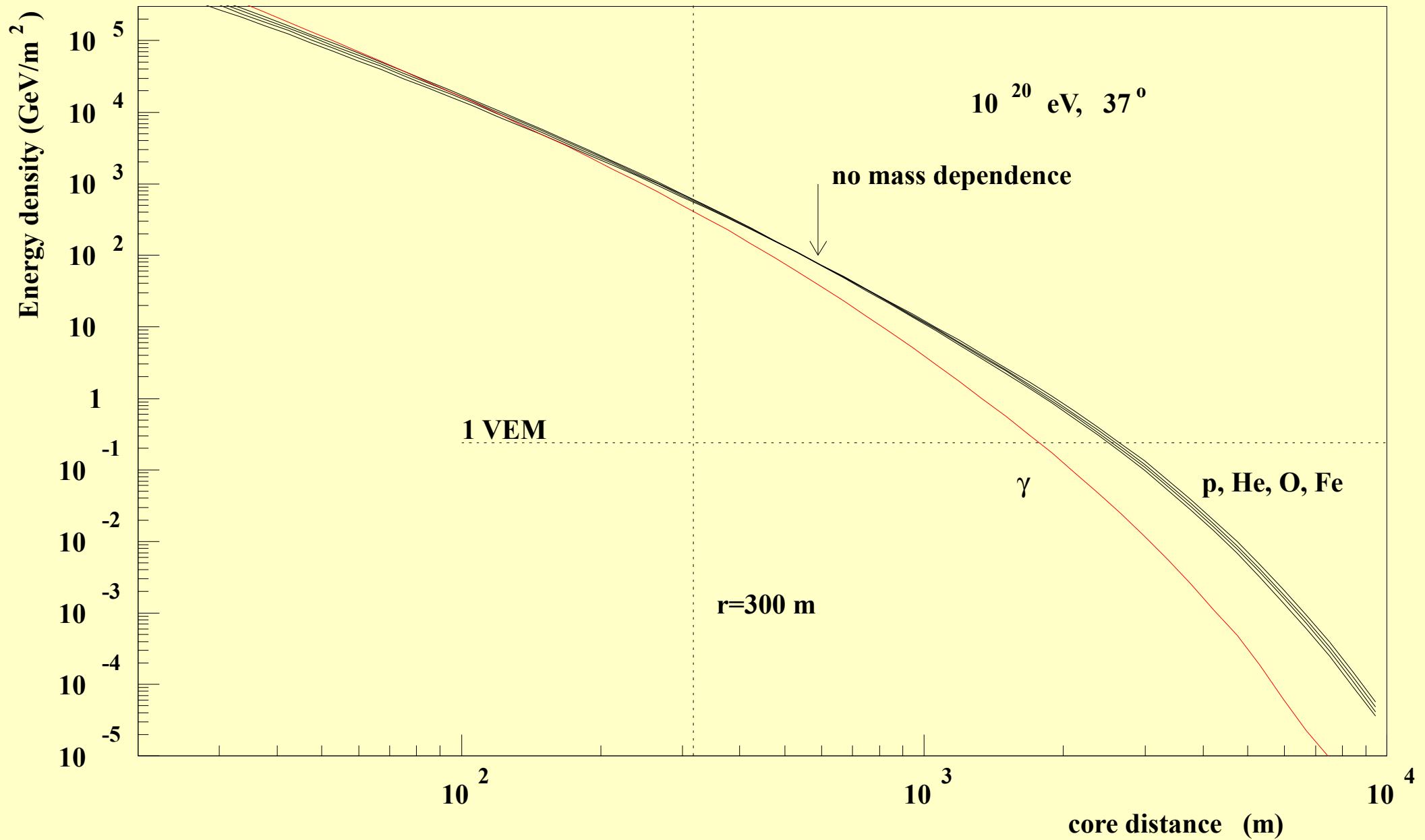


lateral distribution is sensitive to  $x_{\max}$  (i.e. to particle type)

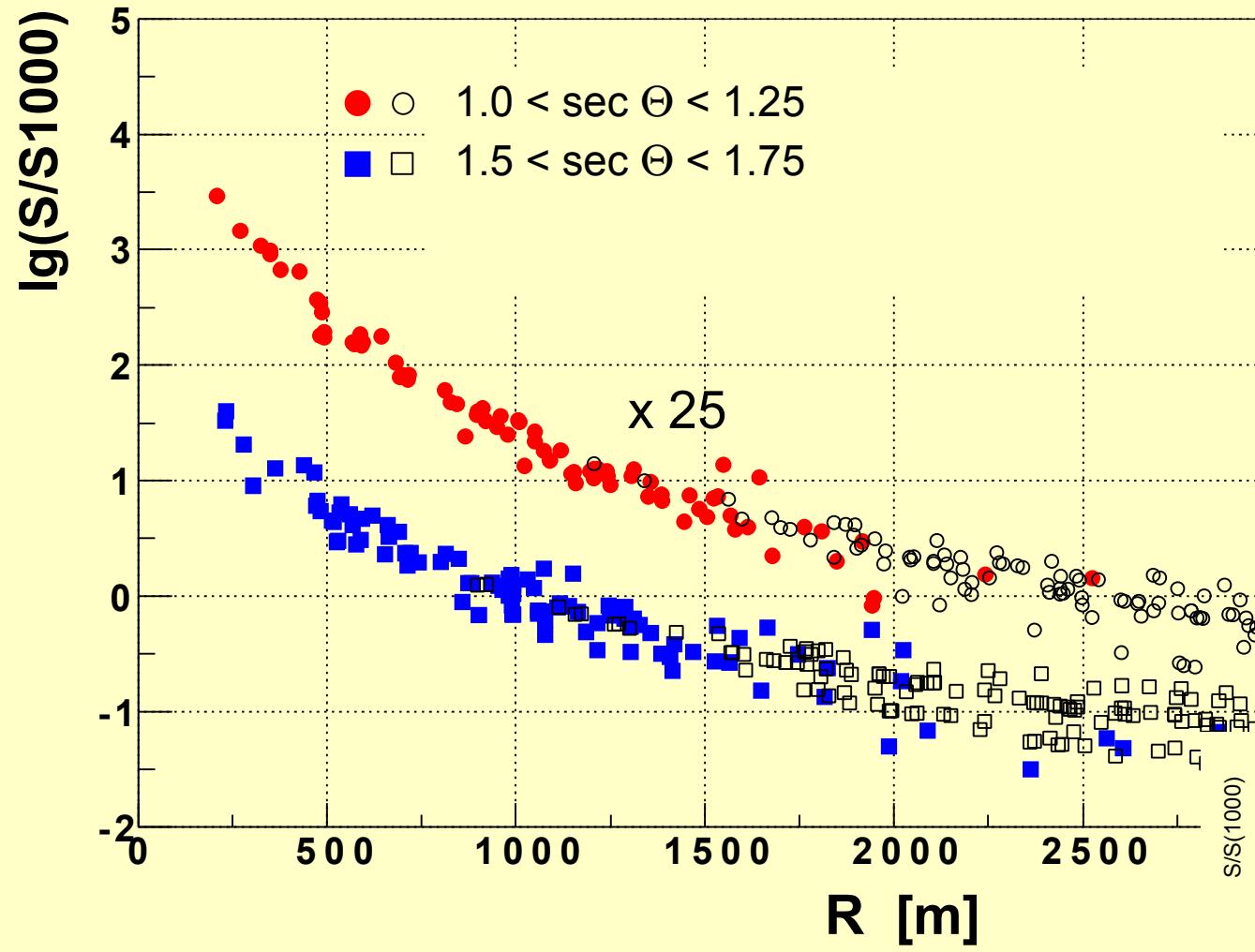
# Lateral distribution of energy deposit: protons 37°



# Lateral distribution of energy deposit: different masses



# Lateral distribution (measured by Auger)



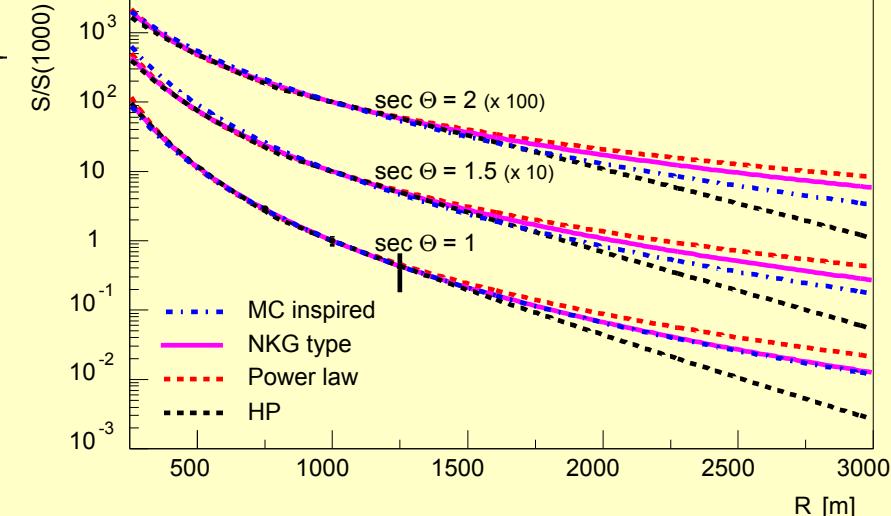
scale  
parameters

shape  
parameters

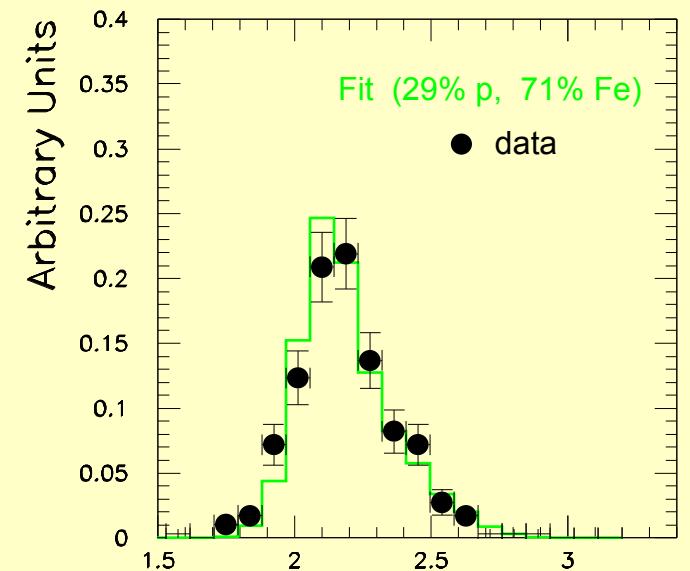
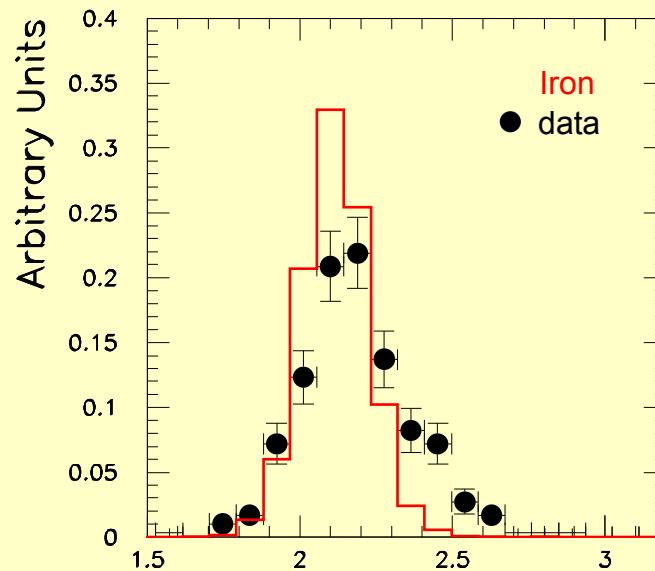
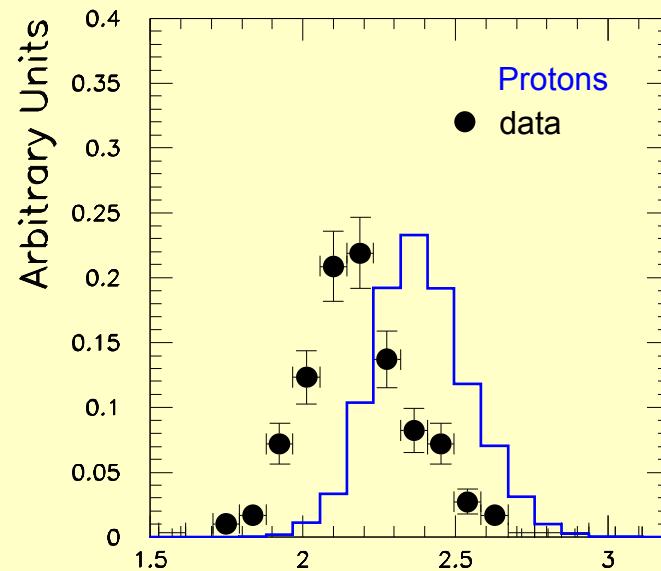
$$\text{power law: } S(r) = S(1000) (r/1000)^{-\nu}$$

$$\text{NKG type: } S(r) = \text{const.} (r/r_s)^{-\beta-\delta} (1+r/r_s)^{-\beta} \quad \text{with } r_s = 700 \text{ m}, \delta = 0.2$$

$$\text{MC inspired: } S(r) = 10^{A+Bx+Cx^2} \quad \text{with } x = \lg(r/1000 \text{ m}), B, C \text{ from MC}$$



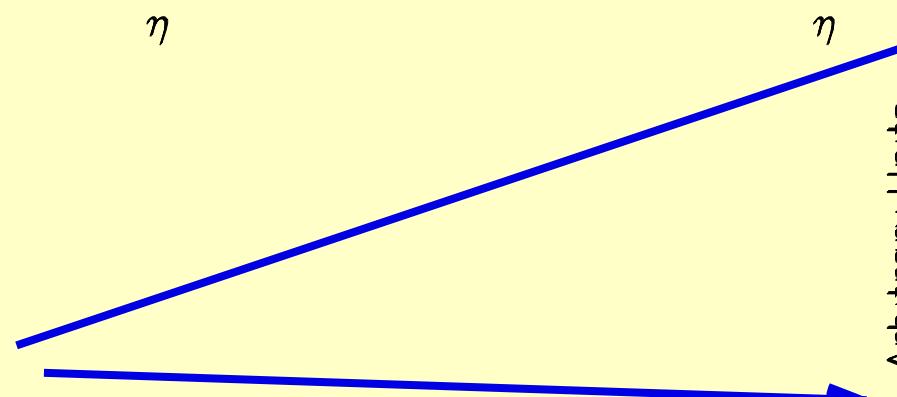
# Haverah Park data (re-analysed 2003)



$0.2 \text{ EeV} < E < 0.6 \text{ EeV}$

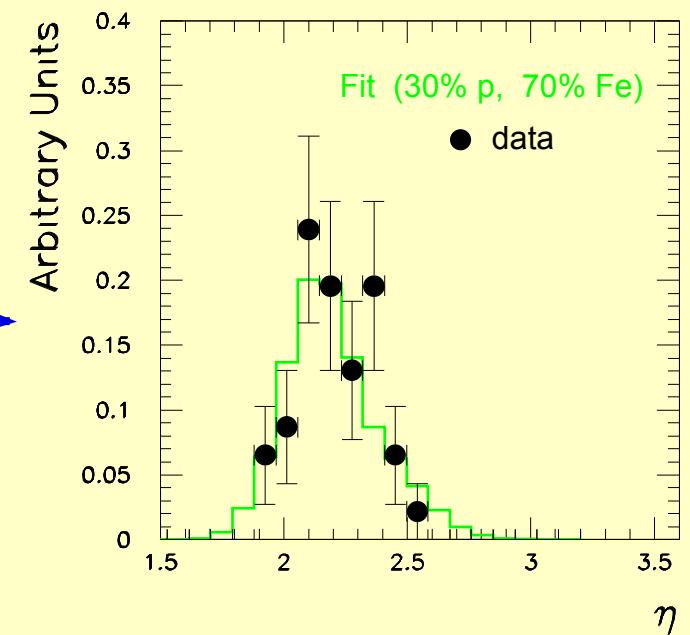
292 events

Models can  
describe data

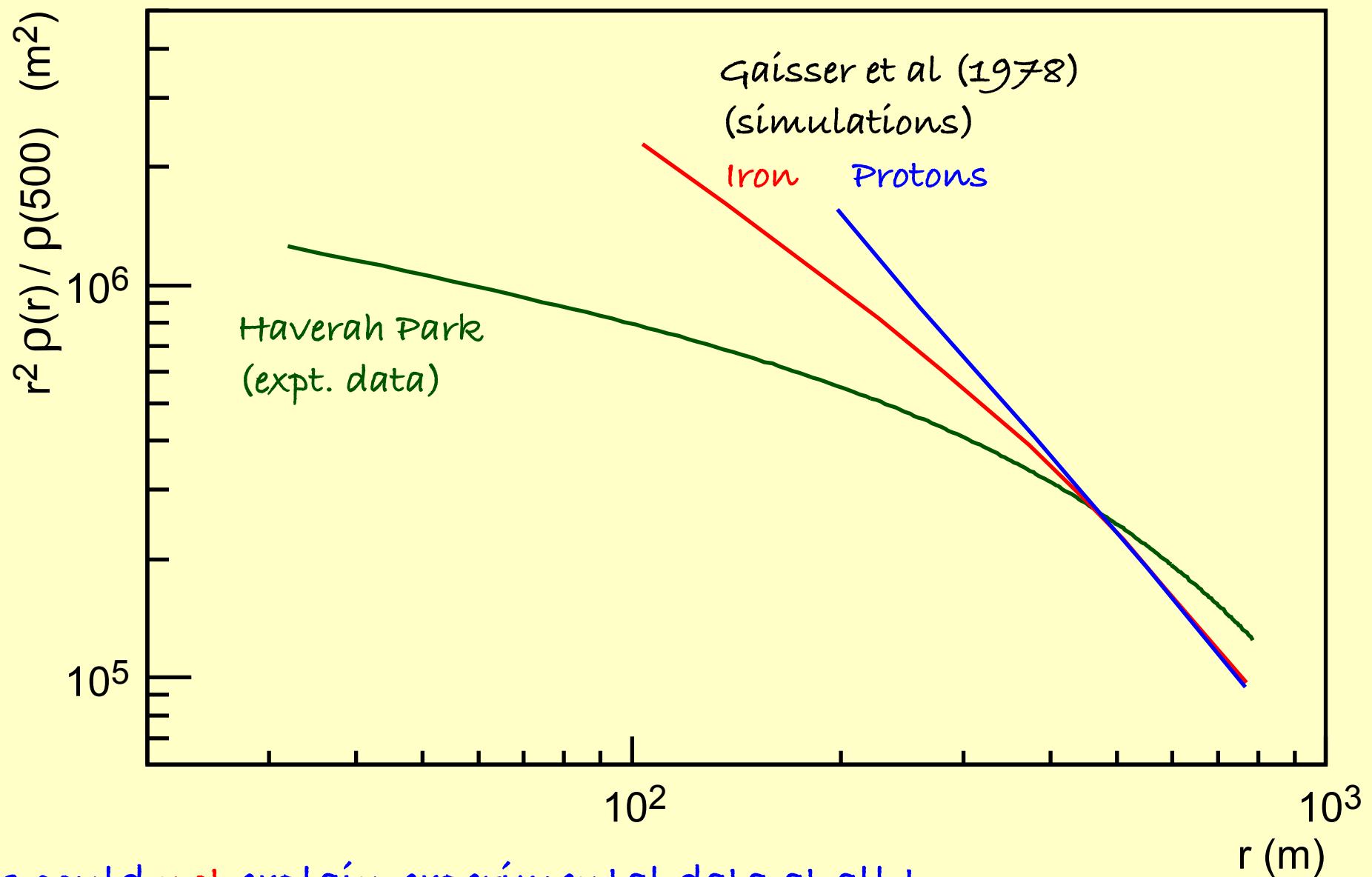


$0.6 \text{ EeV} < E < 1 \text{ EeV}$

46 events



## State-of-the-art model 1978



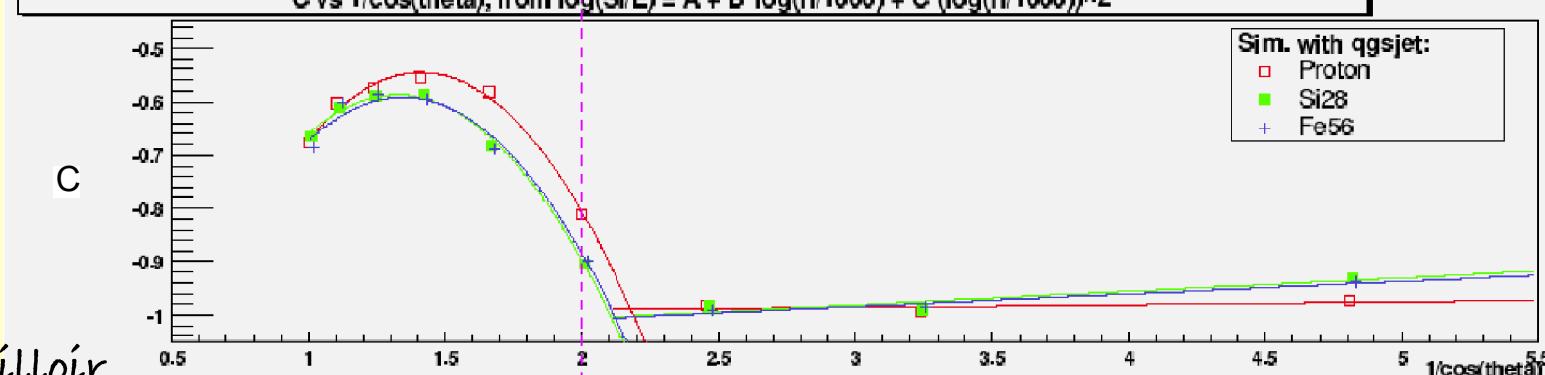
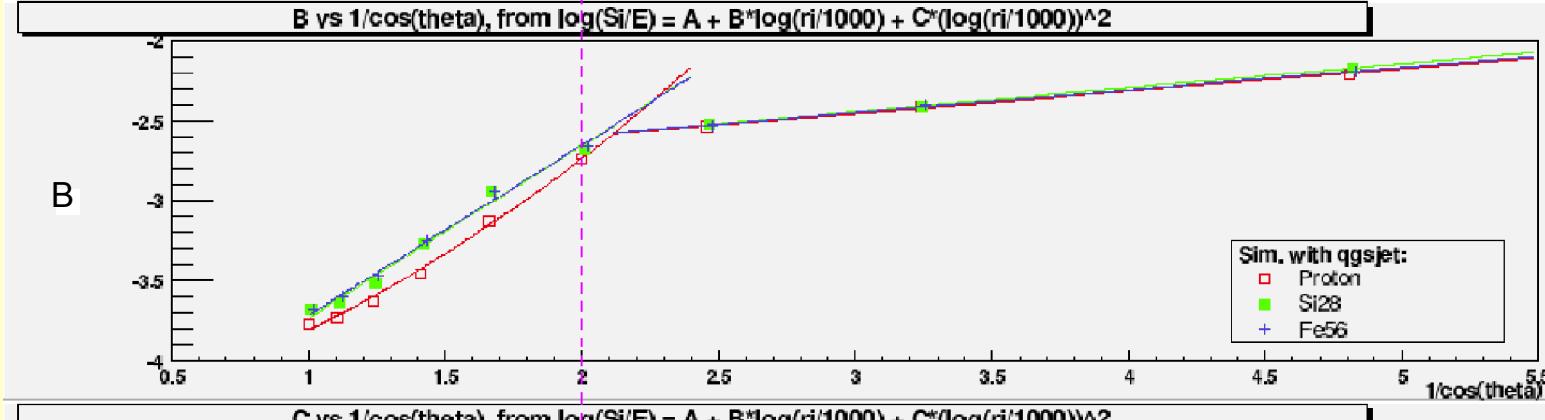
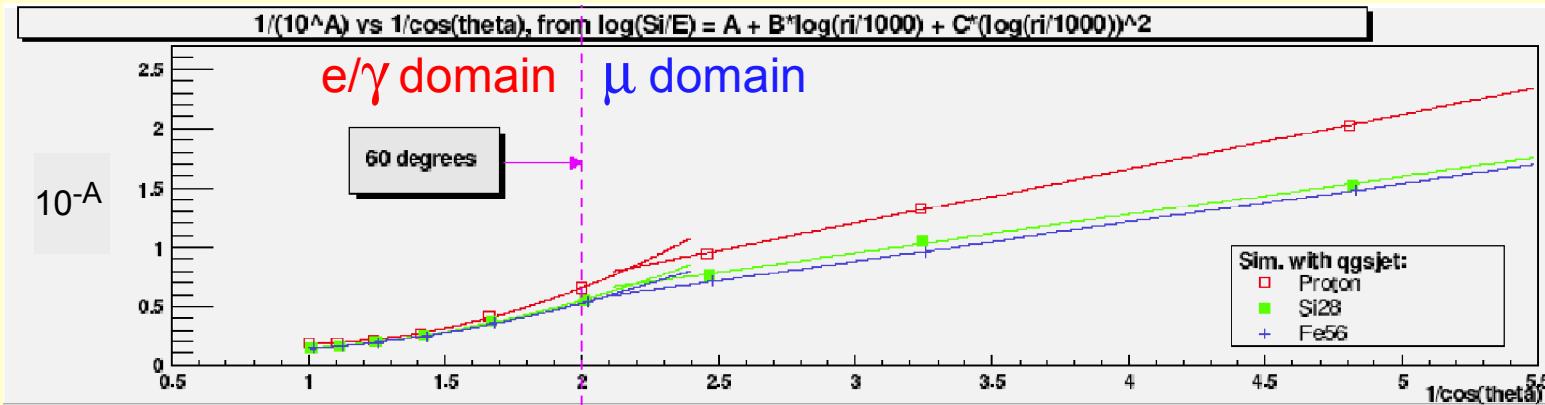
Models could not explain experimental data at all !  
How to interpret the data? (mass >> Fe ???)

# Inclined showers ( $\theta > 60^\circ$ ) are different

$$S(r) = E \cdot 10^{(A+Bx+Cx^2)}$$

$$x = \lg(r/1000 \text{ m})$$

$$E = 1 \dots 100 \text{ EeV}$$



<  $60^\circ$ :  
el.mag. dominate  
>  $60^\circ$ :  
muons dominate

Models tell  
us how to  
reconstruct  
air showers.

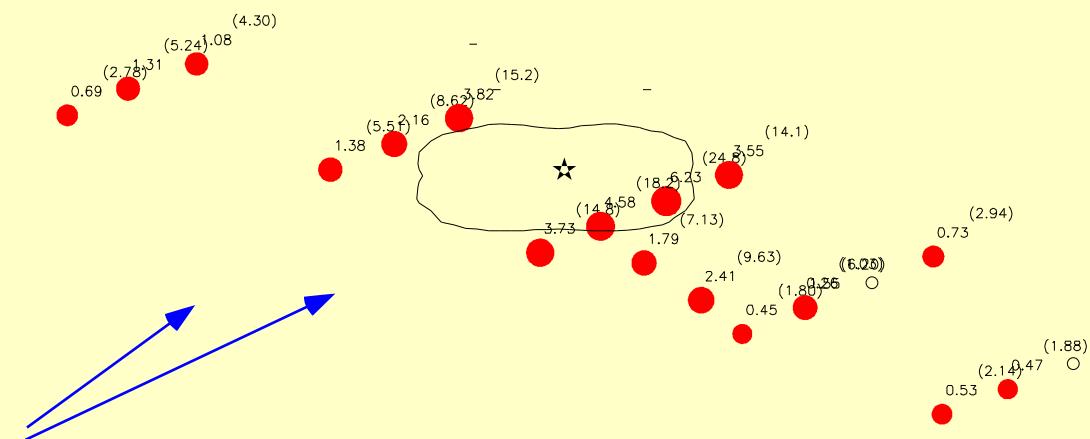
# Near-Horizontal Events

muonic component dominant  
(very short pulses)

deflection in Earth magnetic field  
(dependent on azimuth)

expected density contours  
for specific angle of incidence

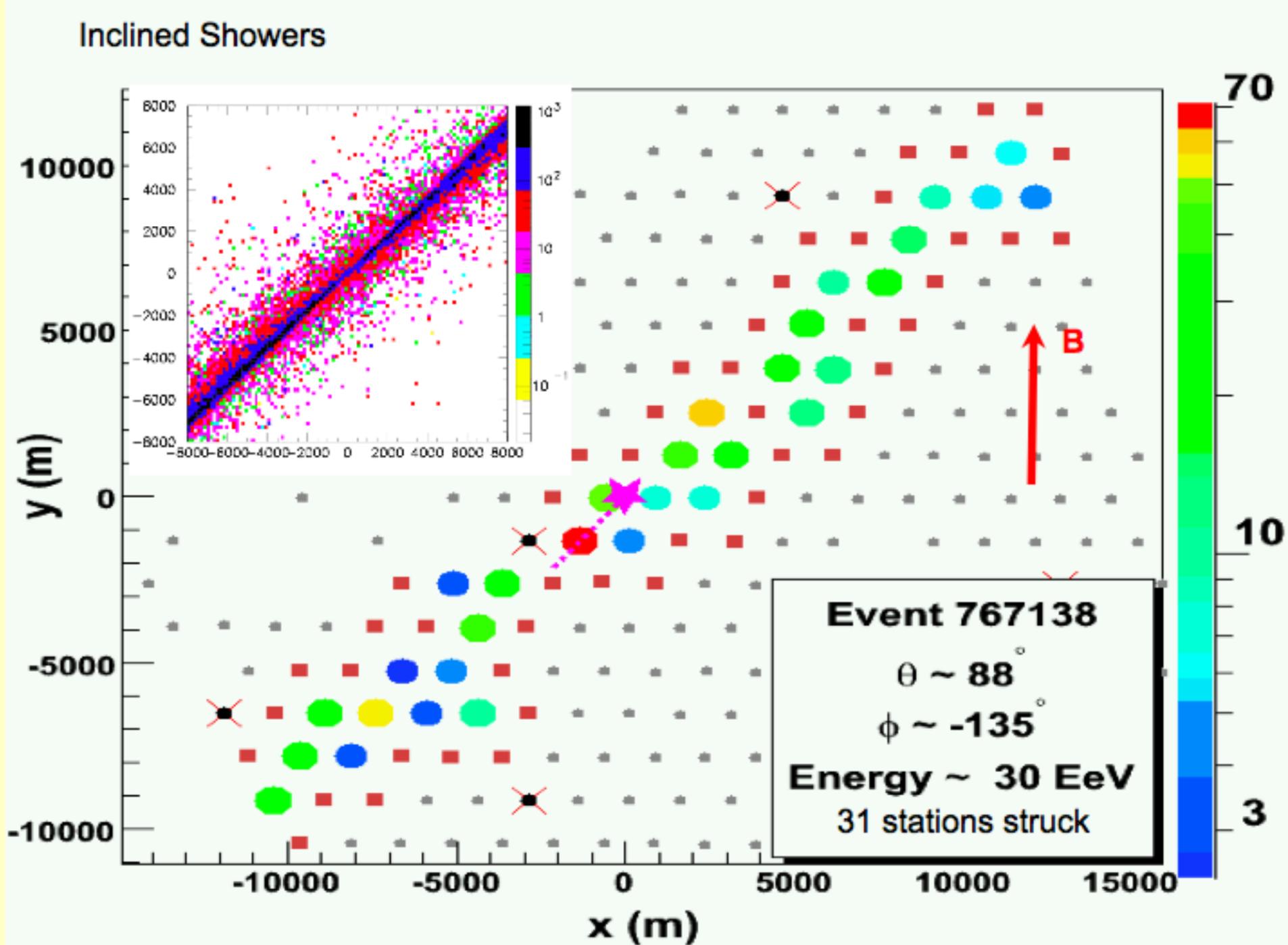
Auger



500 m

Density map.EVENT: 204272

# Pierre Auger Observatory



# Primary $\gamma$ 's, e.g. from decays of topological defects ??

Haverah Park,  
Ave et al., PRL 85 (2000) 2244

49 Events  $> 10^{19}$  eV

$60^\circ < \theta < 80^\circ$

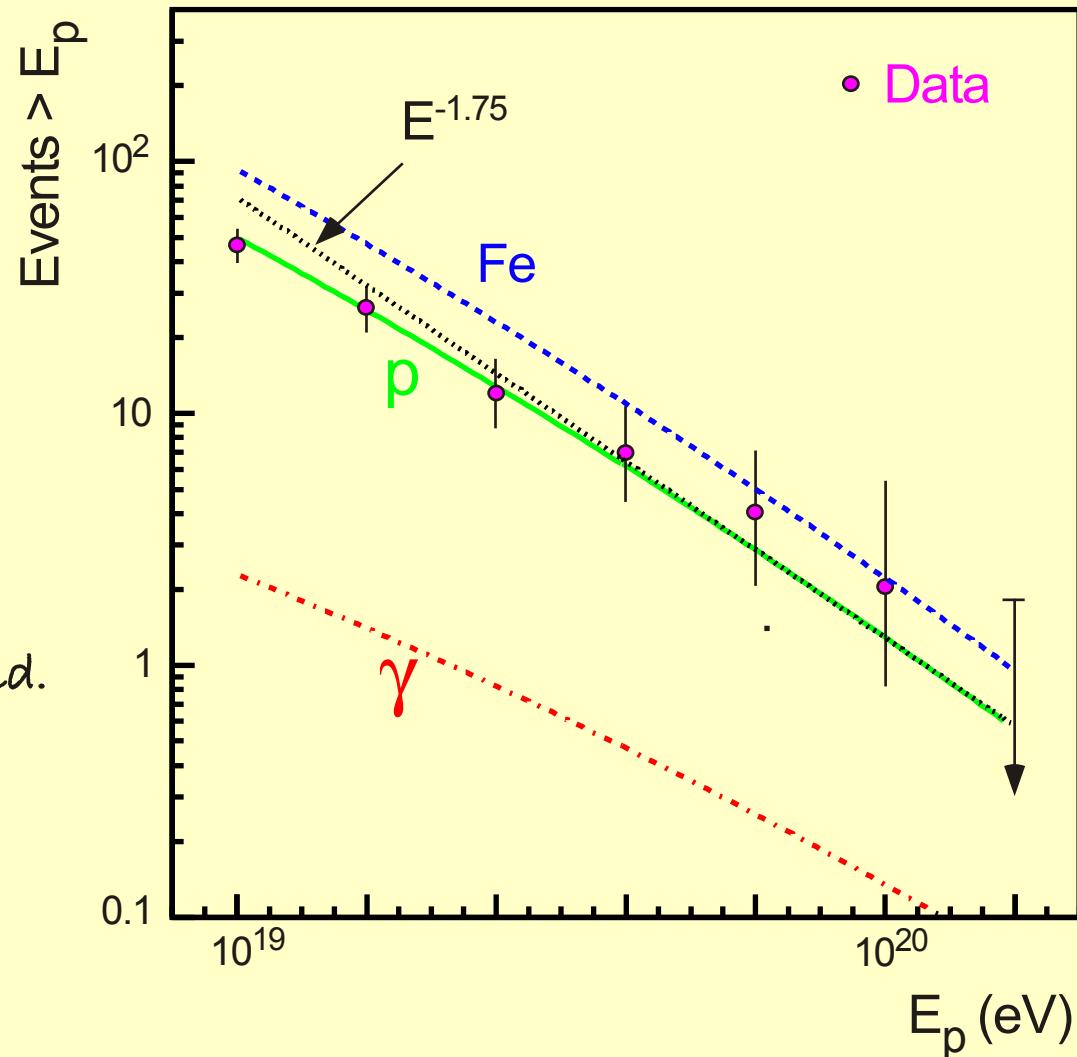
thick atmosphere:

only muons arrive at ground  
long path through atmosphere  
with influence of mag. field.

$$\gamma/p < 40\%$$

$$Fe/p < 54\%$$

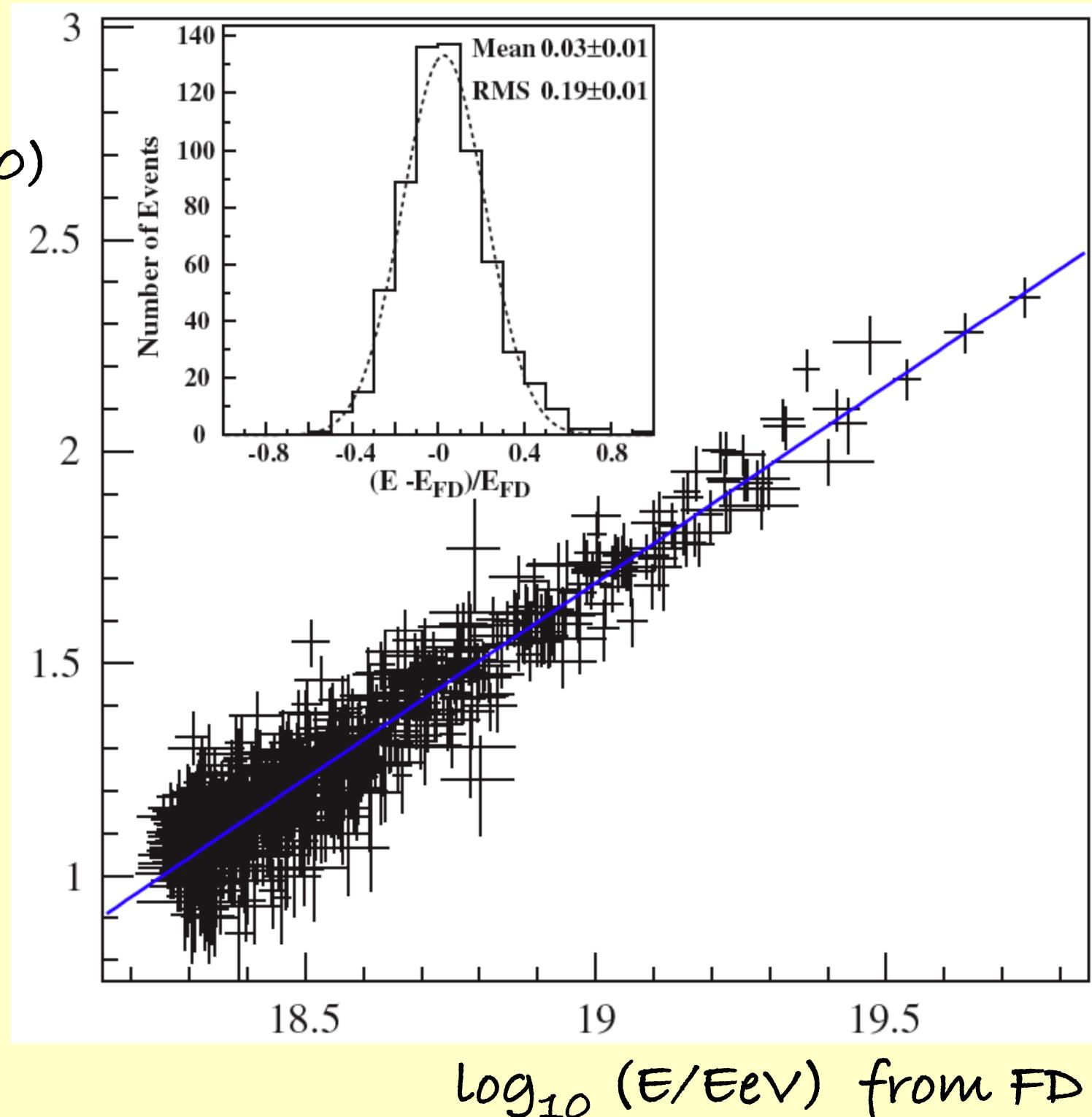
(95% confidence level)



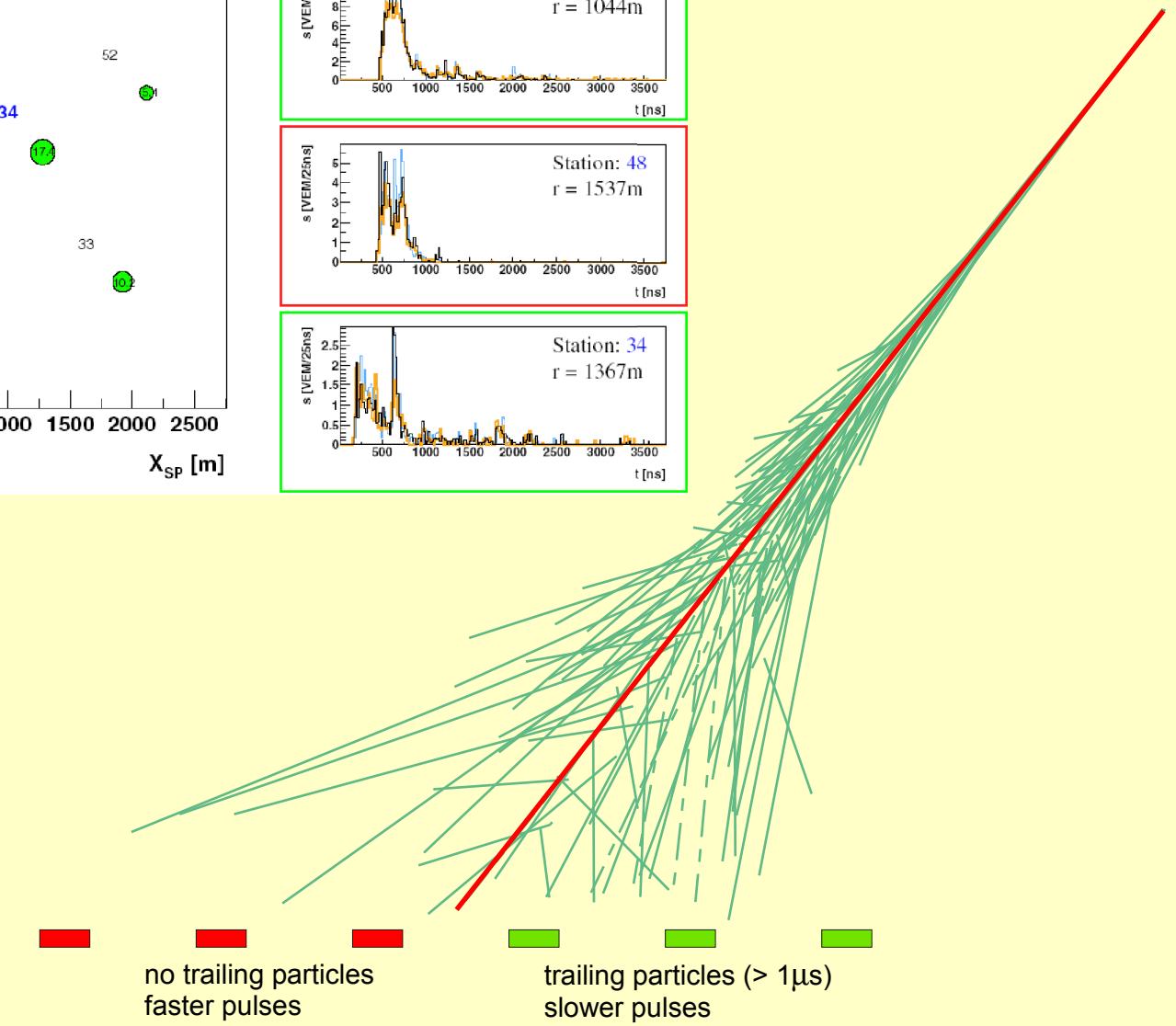
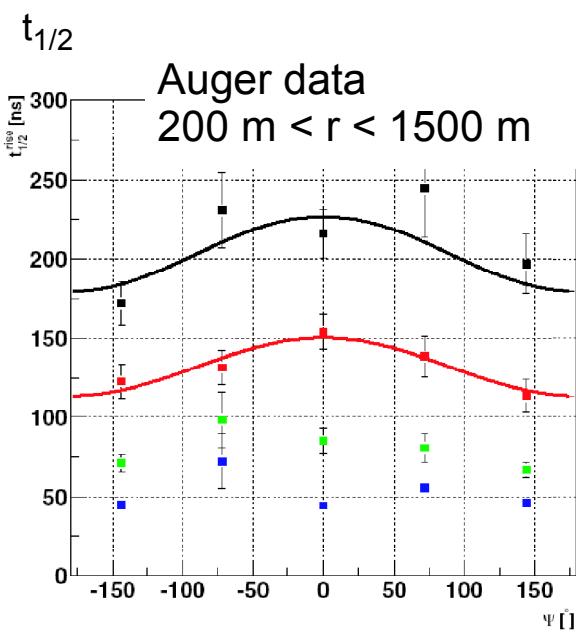
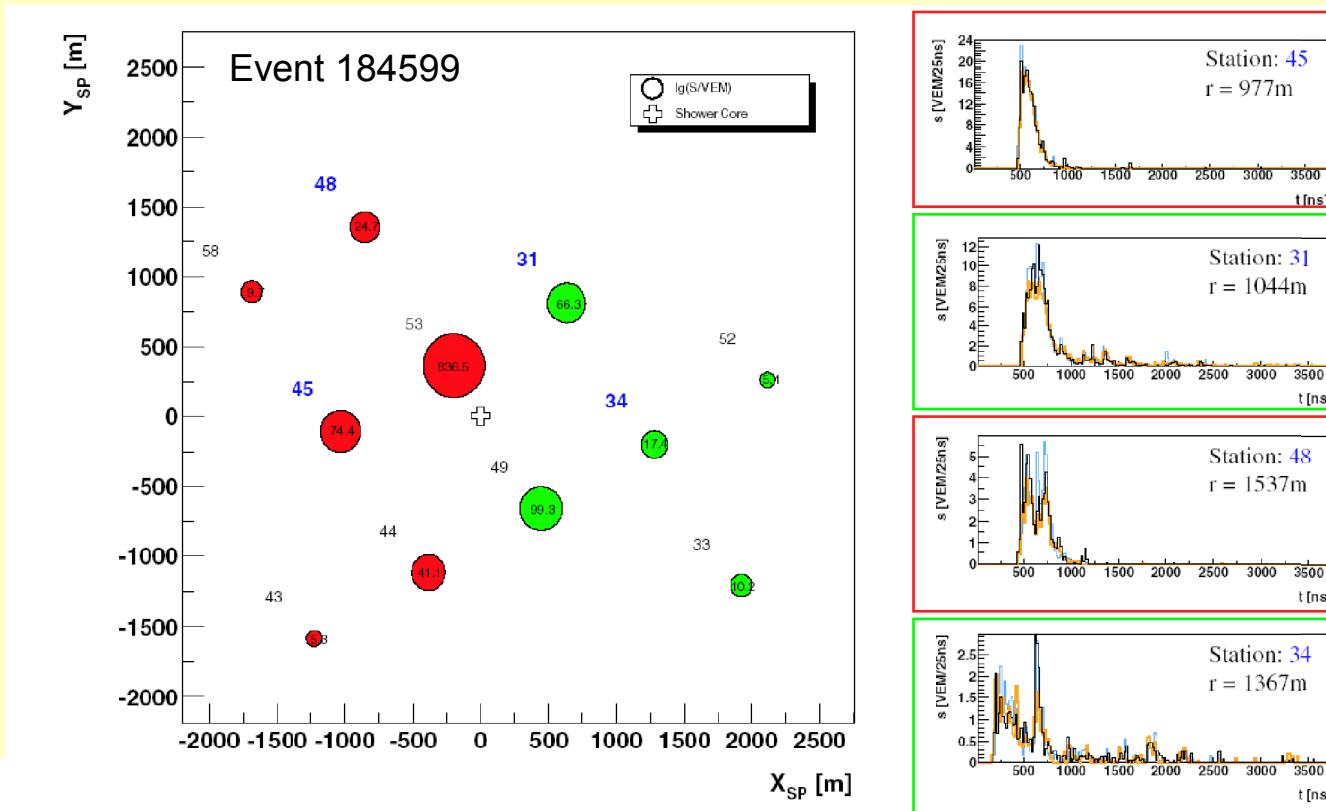
This analysis could only be made since models do describe (roughly) the experimental data.

# Auger Data

$\log_{10} (S1000)$   
from SD



# Azimuthal Asymmetry in Signal and Rise Time



# MUONS in MACRO detector

$N_{\text{CLUSTERS}} \geq 3$

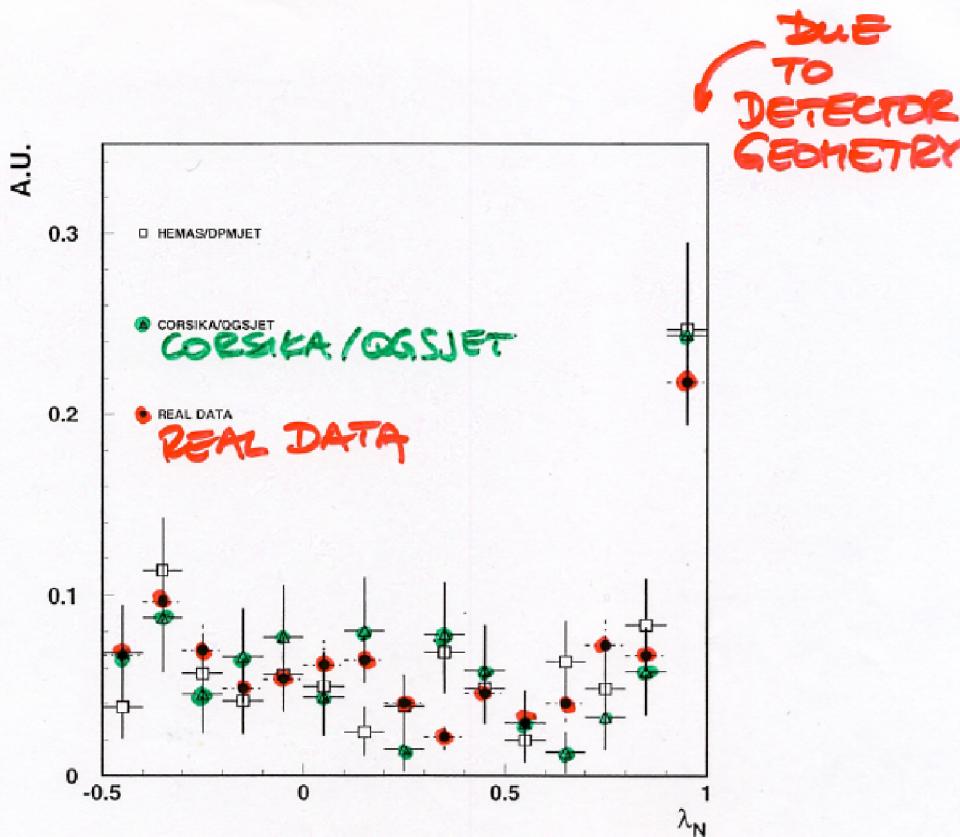


Figure 5.25: Search for aligned clusters in the MACRO detector. We plot the normalized distributions of events as a function of the parameter  $\lambda_N$  (see text), both for experimental (full circles) and simulated data (open markers).

↑  
NOT  
ALIGNED

↑  
COMPLETELY  
ALIGNED

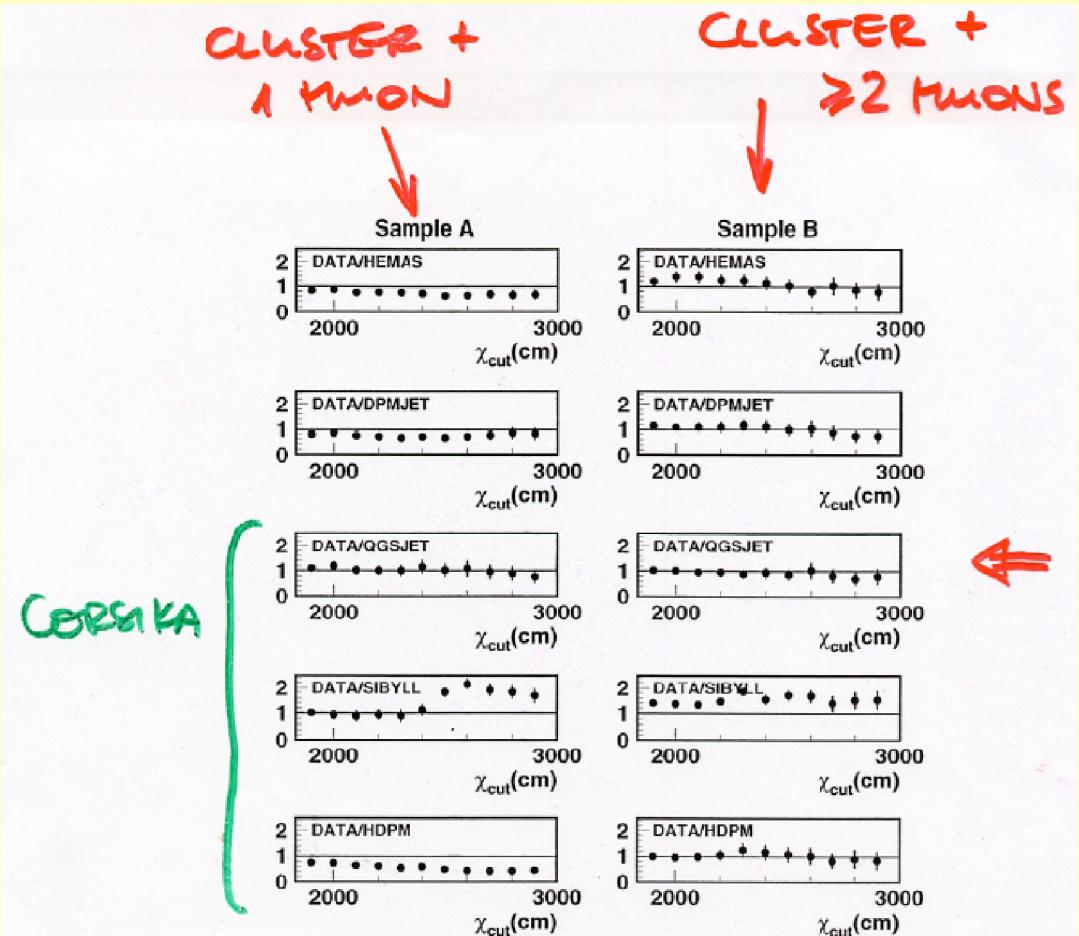


Figure 5.20: 2-cluster events ratio of experimental data over simulated data. The plots on the right refer to events reconstructed with a central cluster plus an isolated muon; on the right side: events reconstructed with a central cluster plus a cluster with at least two muons.

CLUSTER + 1 MUON:  
SENSITIVE TO EARLY INTERACTIONS

# Muon bundles in MACRO detector

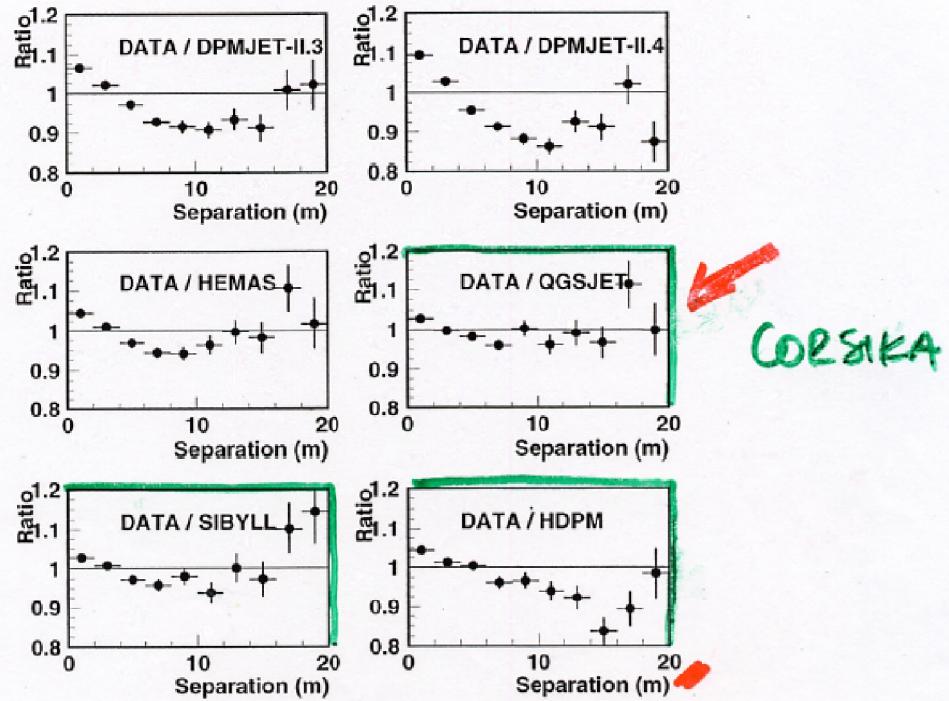


Figure 5.9: Ratio between the experimental and simulated decoherence functions for the sample of  $N_{\text{wire}} \geq 8$ . The ratio was computed between distributions normalized to the same number of events.

DISTRIBUTION OF DISTANCES  
BETWEEN TWO MUONS

CORSIKA / QGSjet describes experimental data rather well.

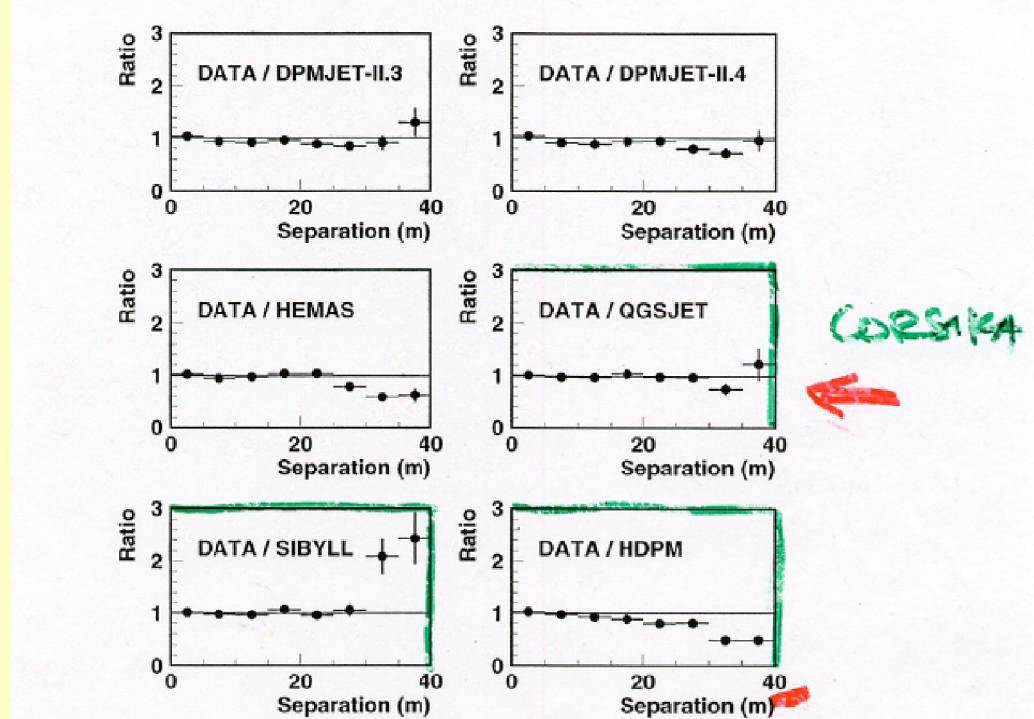
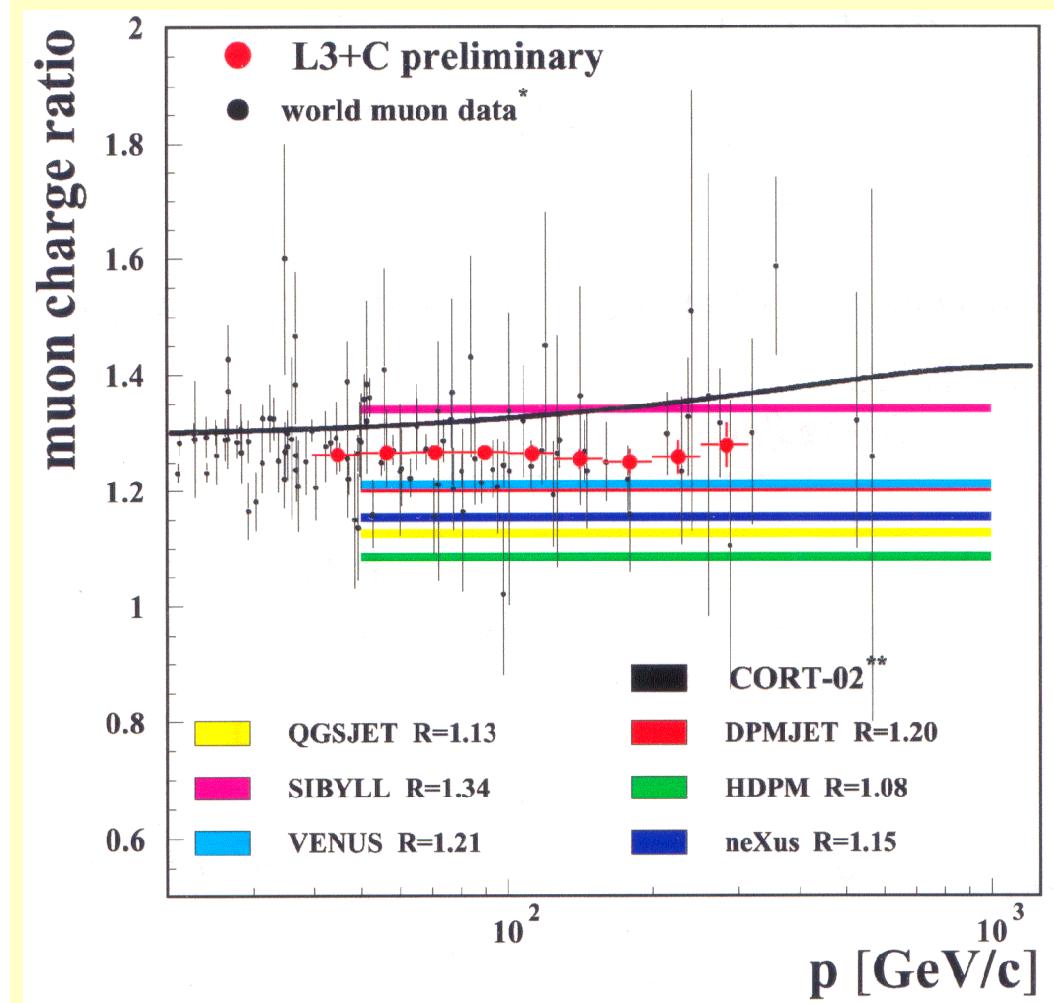
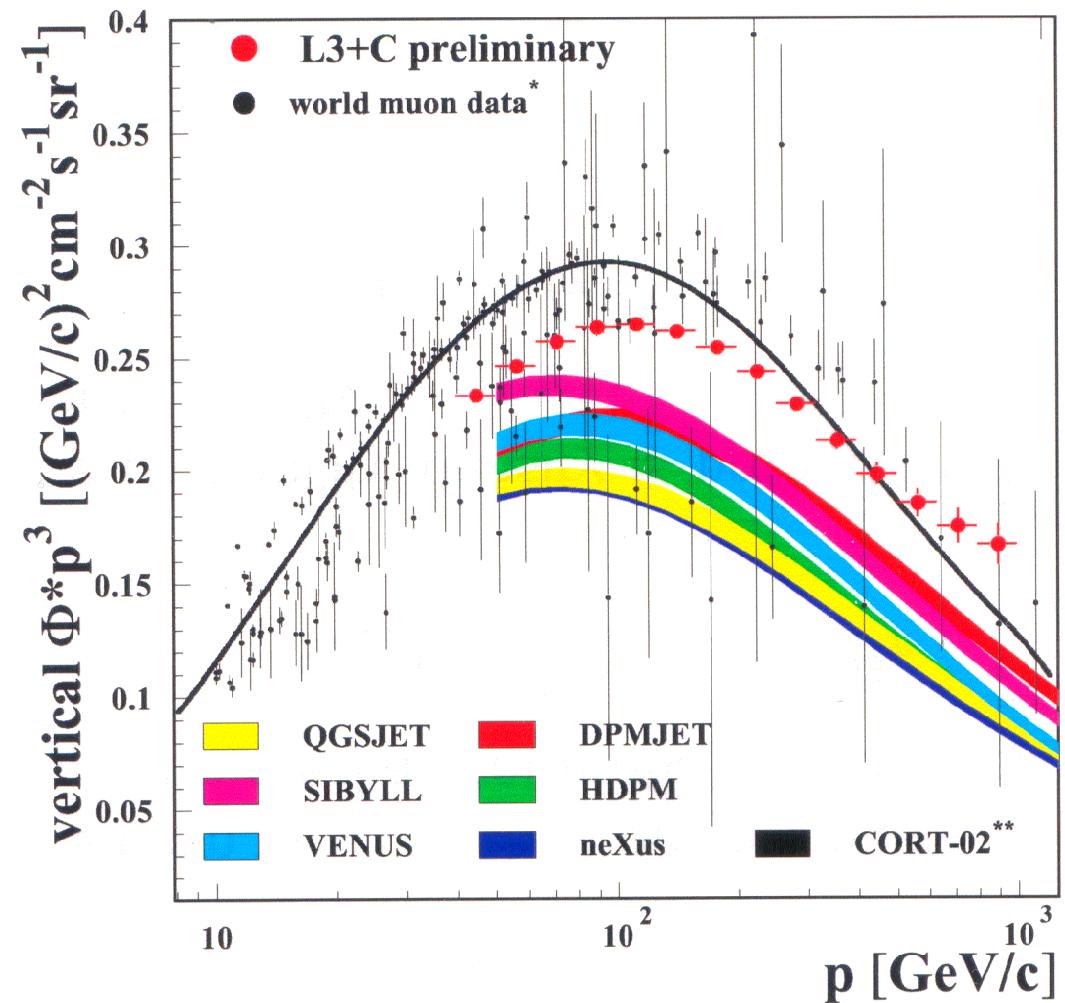


Figure 5.10: Ratio between the experimental and simulated decoherence functions for the sample  $N_{\text{wire}} \geq 8$ . The ratio has been computed between distributions normalized to the same number of events.

LARGER  
DISTANCES

PhD thesis Marco Sioli, Bologna 1999

# L3+C vertical Muon Spectrum & charge Ratio ( $\cos\theta > 0.98$ )

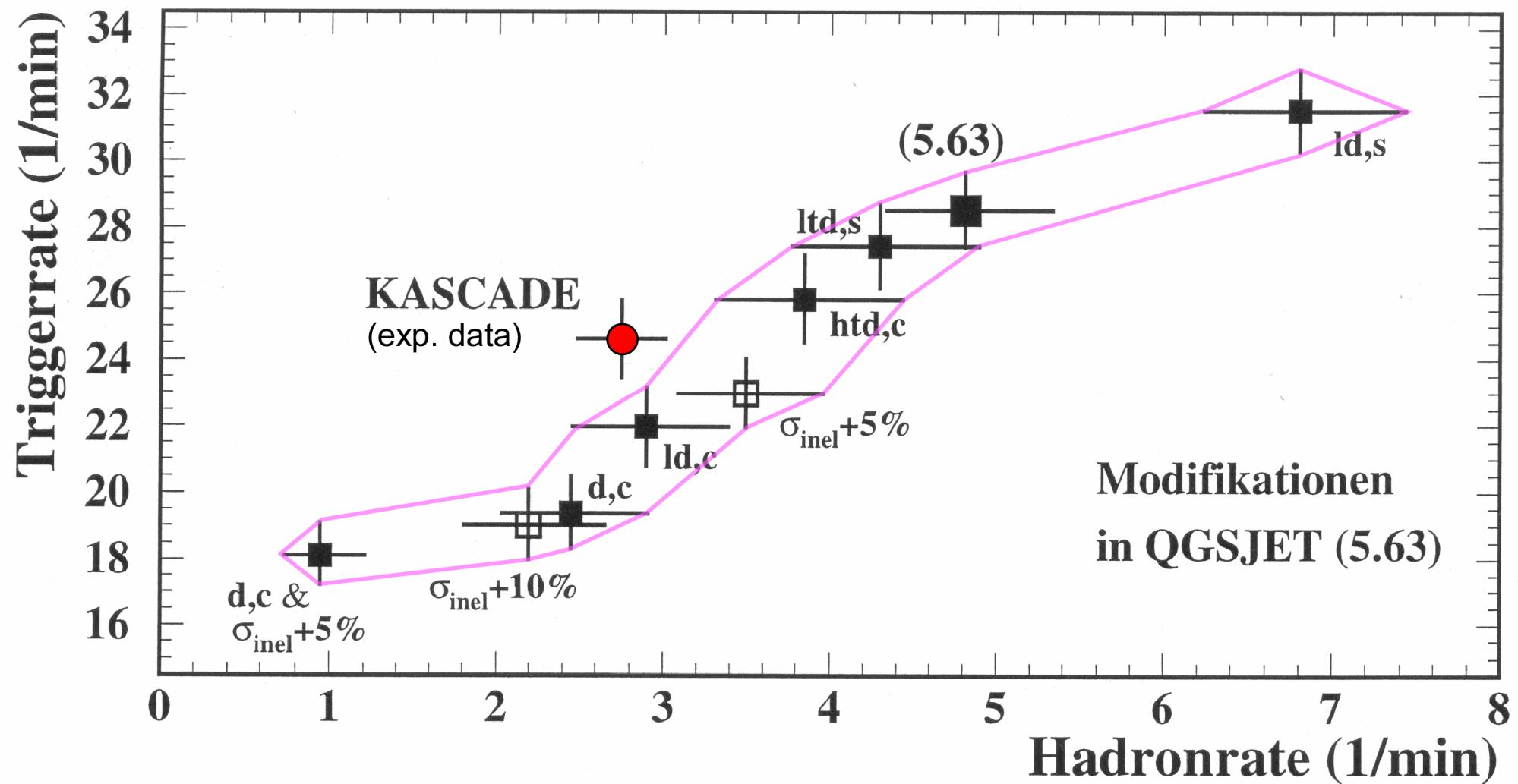


statistical errors only

\* hep-ph/0102042

\*\* hep-ph/0201310

# KASCADE hadron and trigger rates



- ltd: low-mass target diffraction switched off
- htd: high-mass target diffraction switched off
- c: constant inelastic cross-section
- s: reduced inelastic cross-section

# Summary & Outlook

- Great improvements in EAS simulations in past few years.  
Soft hadronic and nuclear interactions modeled on basis of  
Gribov-Regge & Glauber Theory.  
New models allow a safer extrapolation to highest energies.
- Assumption of a mixed CR composition (p, He, .... Fe)  
and extrapolation of models from 100 GeV range (e.g. QGSJET)  
yields amazingly good agreement with CR data from  $\sim 10^{12} \dots 10^{19}$  ev.
- Many new accelerator experiments will provide new experimental input to  
cross-sections, diffraction and hadronic particle production under small angles.
- New astroparticle experiments will provide new constraints at higher energies  
and data with improved quality (e.g. KASCADE-Grande, Auger, ICE Cube .....  
AMS, direct C, ....)

Only HEP and Astroparticle physicists together can solve the problem of  
origin of the high energy cosmic rays (the highest-energy particles in the universe)  
and its hadronic interaction with the atmosphere.