

# Structure of Exotic Nuclei --- a theoretical review ---

Shan-Gui Zhou (周善贵)

Institute of Theoretical Physics, Chinese Academy of Sciences, Beijing

School of Physics, University of Chinese Academy of Sciences, Beijing

Center of Theoretical Nuclear Physics, National Laboratory of Heavy Ion Accelerator, Lanzhou

Synergetic Innovation Center for Quantum Effects and Application, Hunan Normal University, Changsha

*Supported by:*

NSFC & MOST

HPC Cluster of SKLTP/ITP-CAS

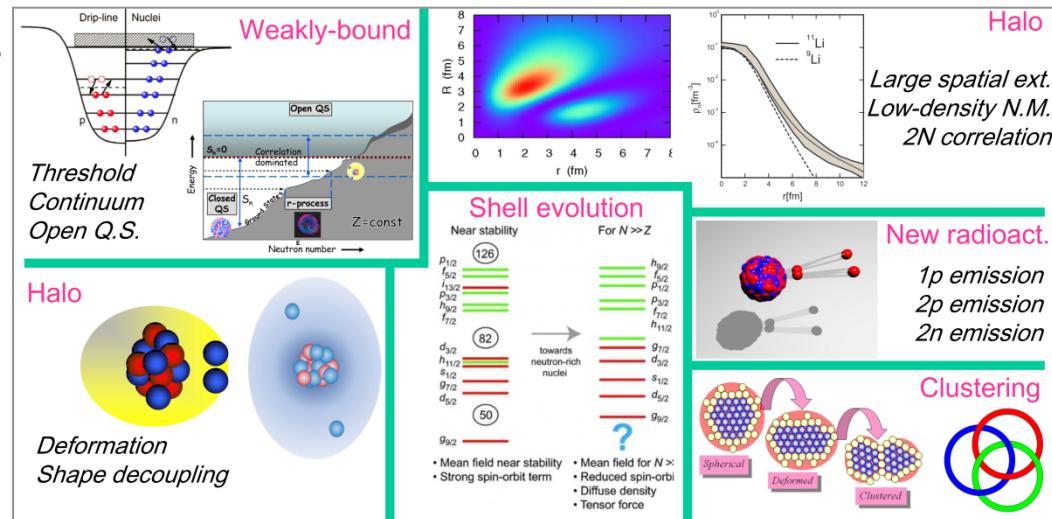
ScGrid of CNIC-CAS

# Outline

## □ Introduction

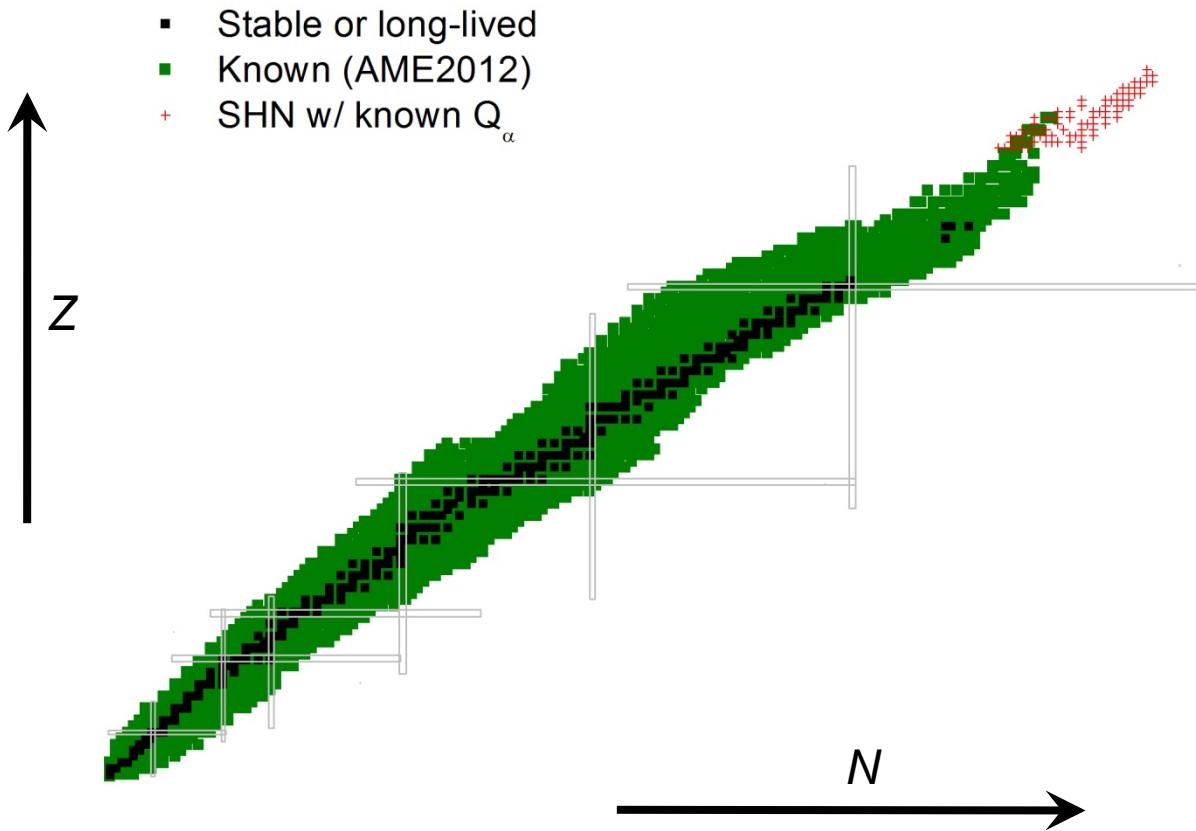
## □ Physics of exotic nuclei

- Weakly-bound features
- Large spatial extension
- Deformation effects
- Shell evolution
- New radioactivities
- Clustering



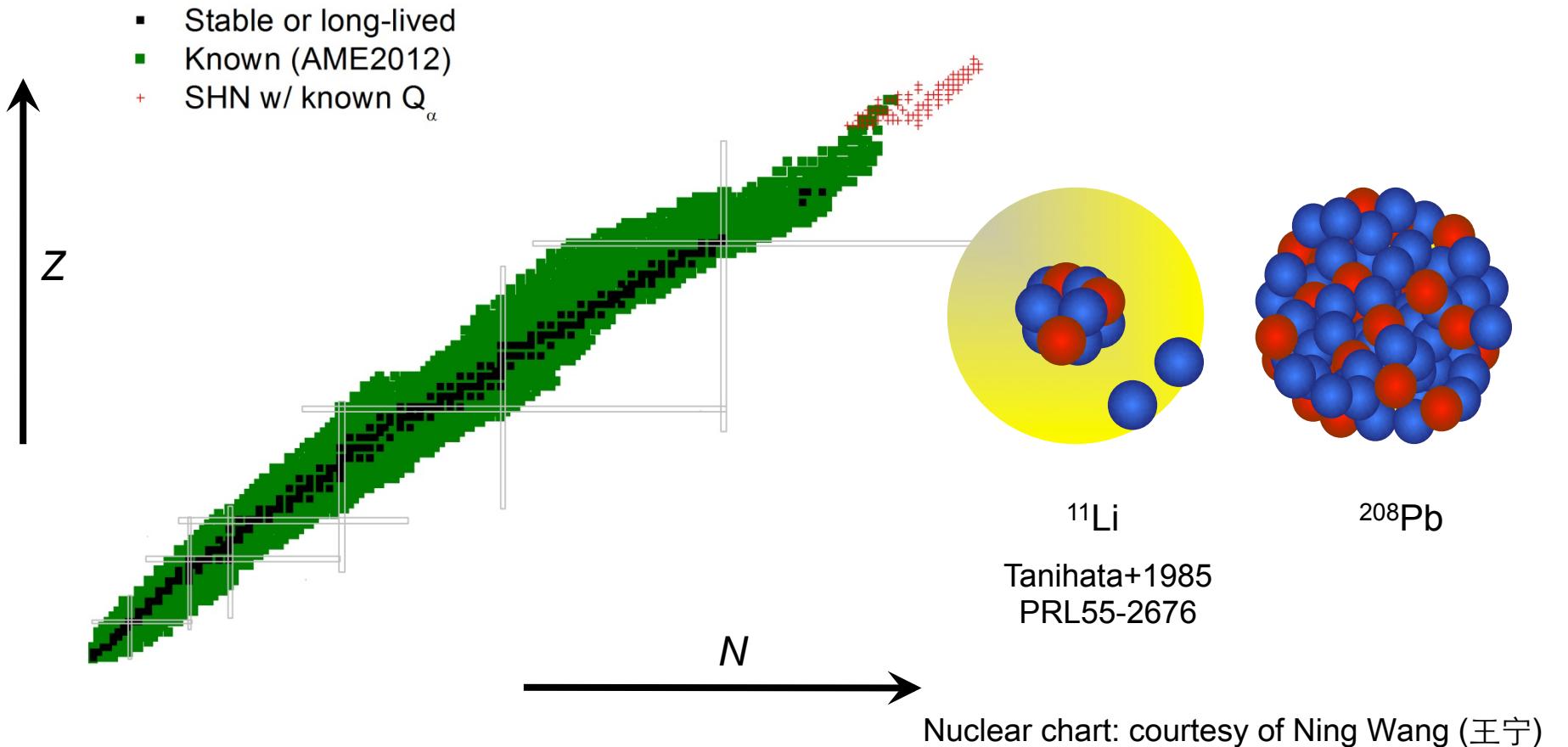
## □ Perspectives

# Extension of Nuclear Chart: Exotic Nuclei

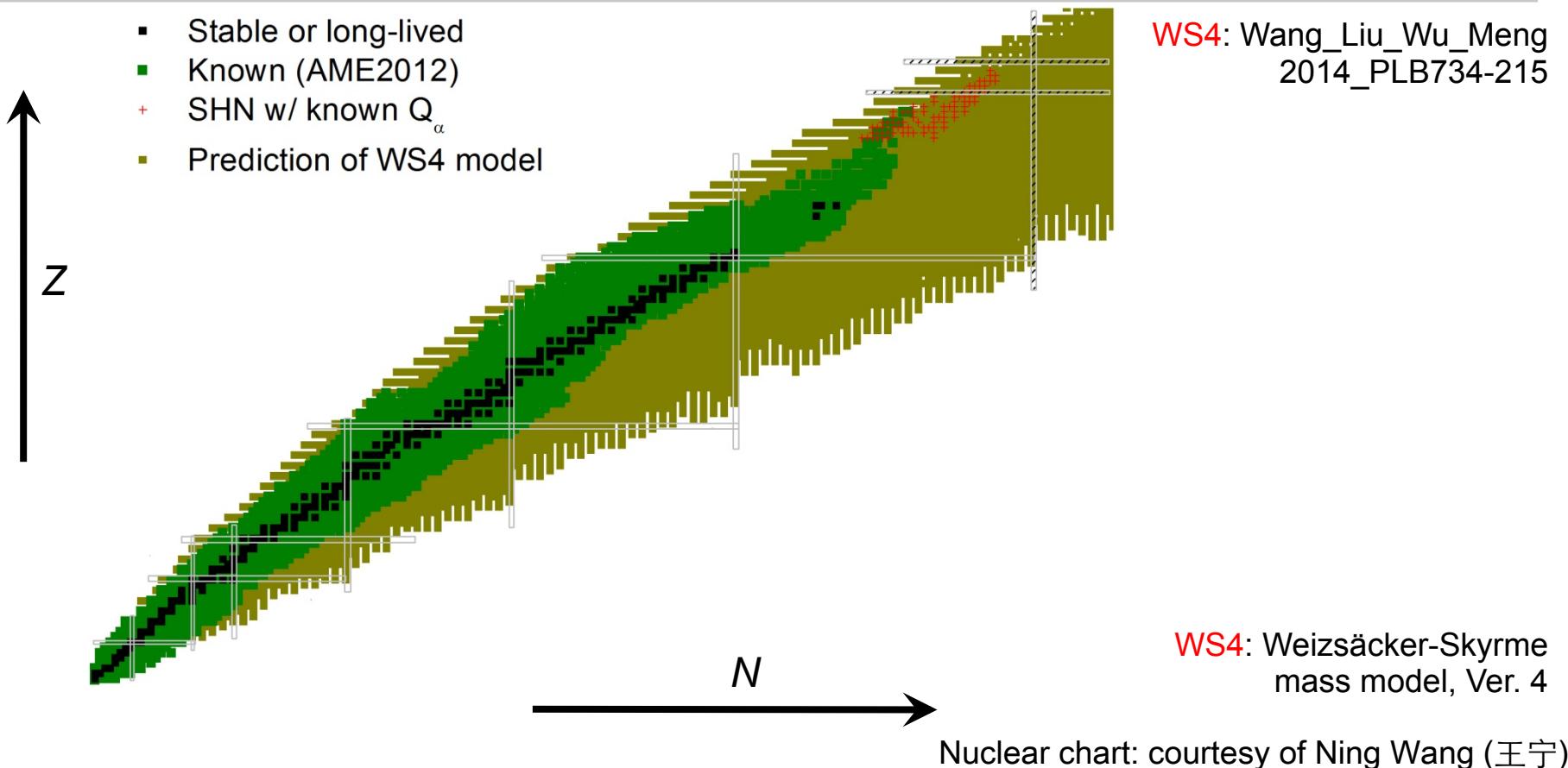


Nuclear chart: courtesy of Ning Wang (王宁)

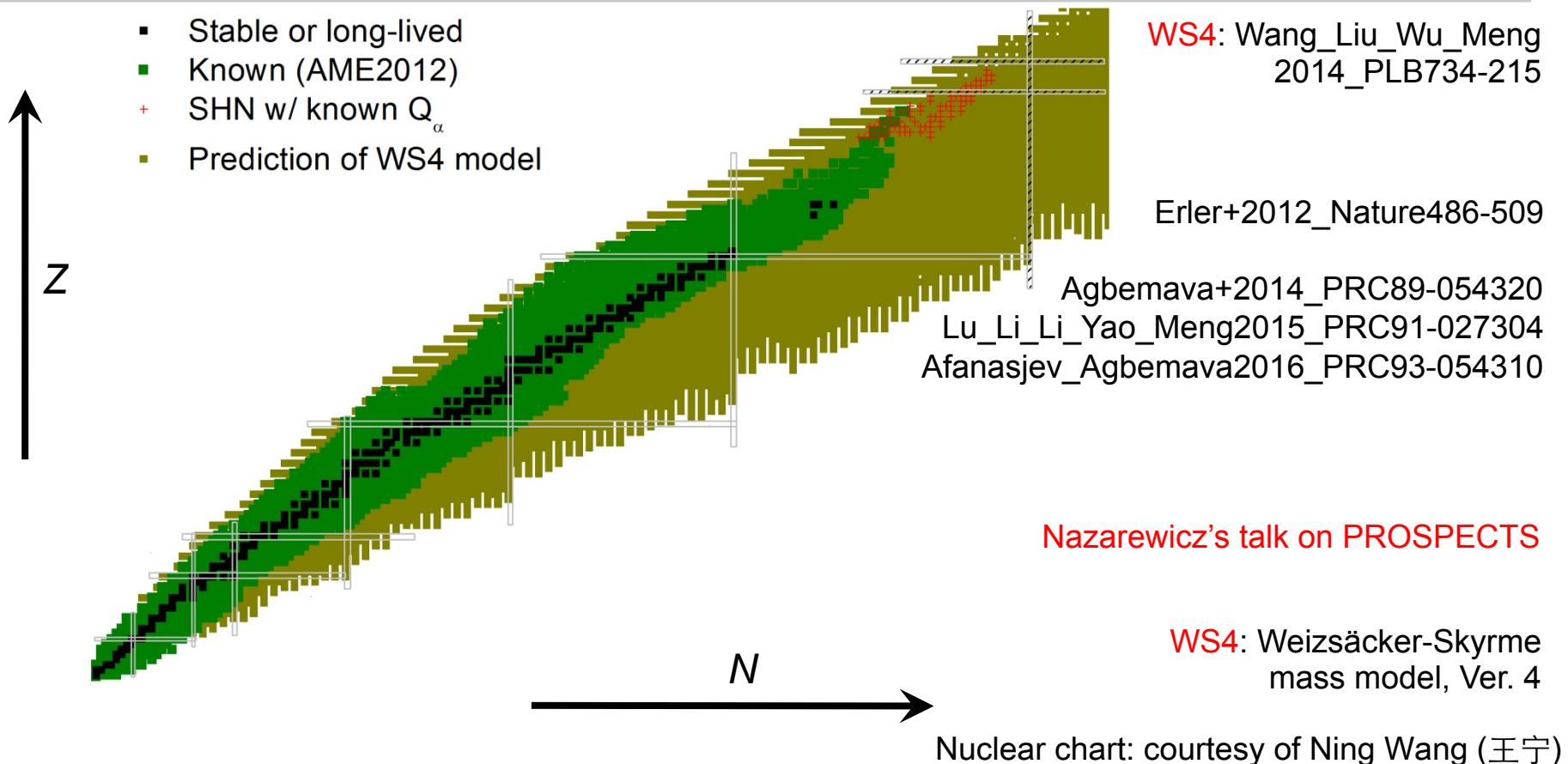
# Extension of Nuclear Chart: Exotic Nuclei



# Extension of Nuclear Chart: Exotic Nuclei

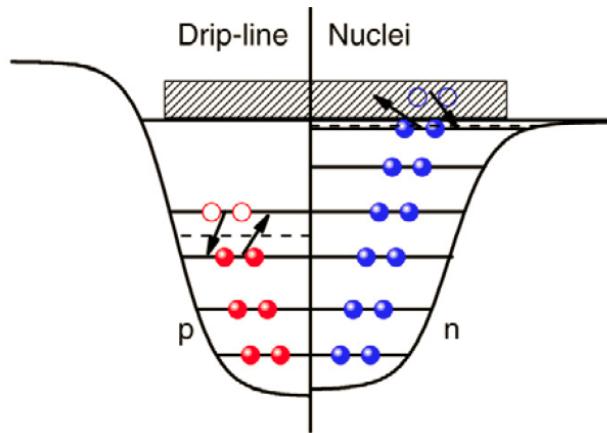


# Extension of Nuclear Chart: Exotic Nuclei



# Exotic nuclei: Weakly bound

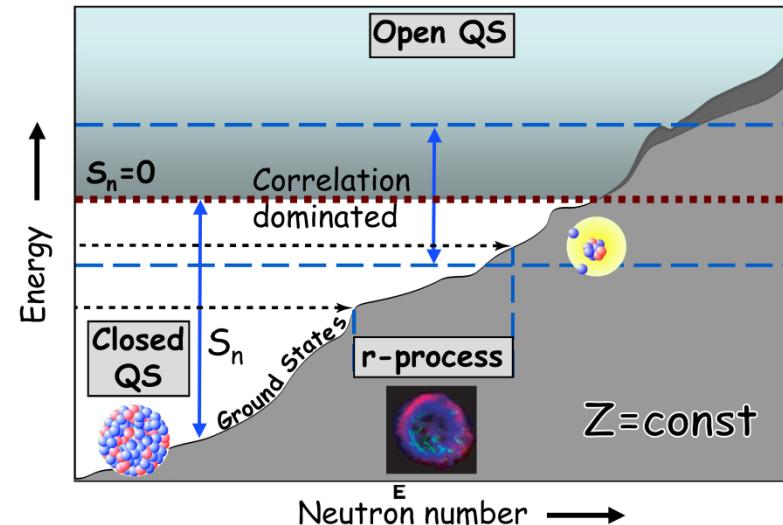
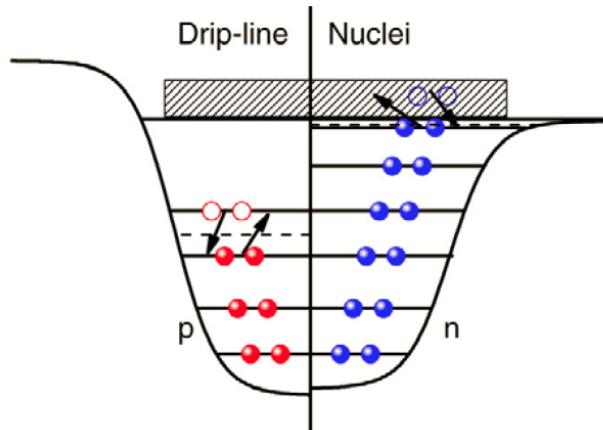
Threshold; Continuum & resonance; Open quantum systems



Meng+2006\_PPNP57-470  
Meng\_SGZ2015\_JPG42-093101

# Exotic nuclei: Weakly bound

Threshold; Continuum & resonance; Open quantum systems

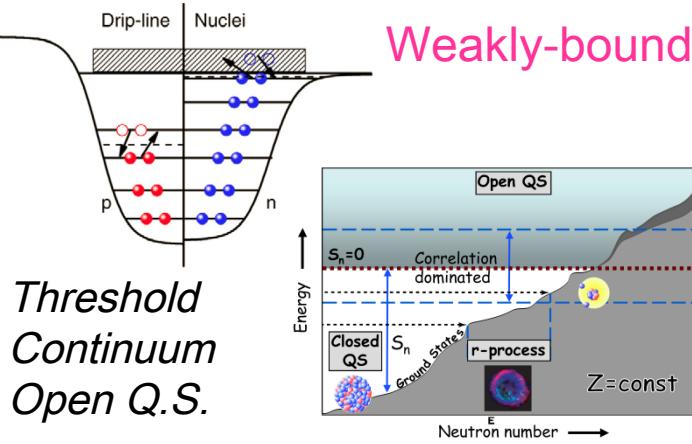


Meng+2006\_PPNP57-470  
Meng\_SGZ2015\_JPG42-093101

Dobaczewski+2007\_PPNP59-432  
Michel+2009\_JPG36-013101

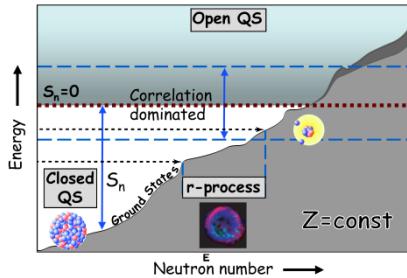
Bonaccorso & Larsen's talks  
Lugaro & Surman's talks

# Physics of exotic nuclei



Weakly-bound

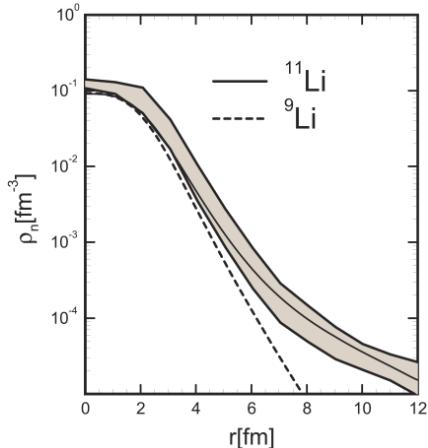
Threshold  
Continuum  
Open Q.S.



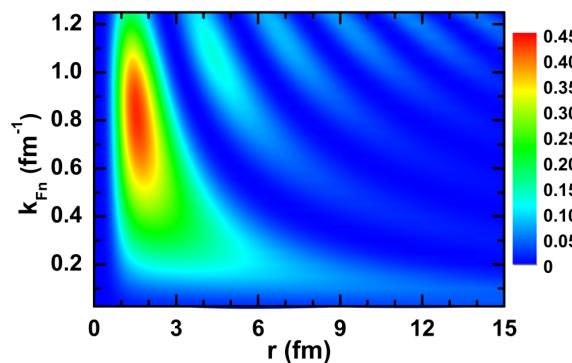
# Halo: Large spatial extension

Low-density neutron matter; Di-neutron correlation; Soft dipole mode

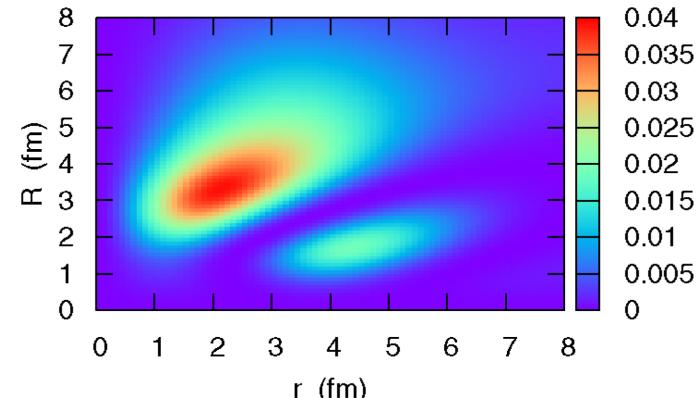
Meng\_Ring1996\_PRL77-3963



Sun\_Toki\_Meng2010\_PLB683-134



Hagino+2007\_PRL99-022506



Vretenar2005\_PRL94-101

Meng+2006\_PPNP57-470

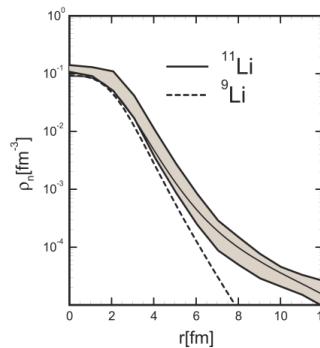
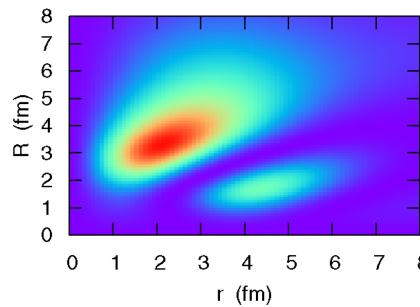
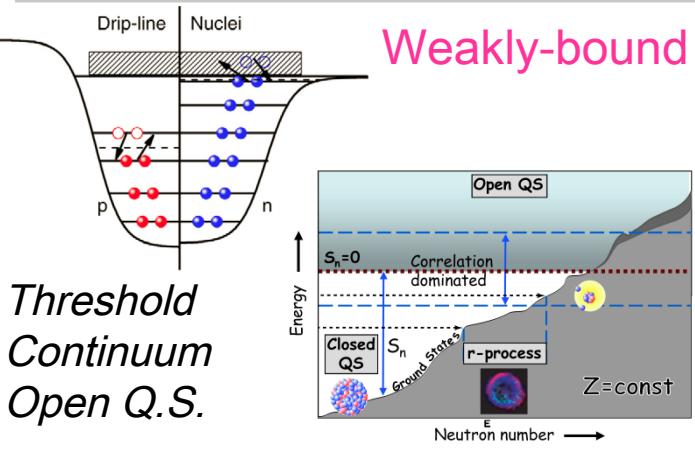
Matsuo2006\_PRC73-044309

Sun\_Sun\_Meng2012\_PRC86-014305

Sagawa\_Hagino2015\_EPJA51-102

$^{11}\text{Li}$ : Nakamura+2006\_PRL96-252502; ...; Kanungo+2015\_PRL114-192502

# Physics of exotic nuclei



Halo

*Large spatial ext.  
Low-density N.M.  
2N correlation*

# Halo: Deformation effects

$$R(\theta, \varphi) = R_0 \left[ 1 + \beta_{00} + \sum_{\lambda=1}^{\infty} \sum_{\mu=-\lambda}^{\lambda} \beta_{\lambda\mu}^* Y_{\lambda\mu}(\theta, \varphi) \right]$$

SGZ 2016\_PhysScr 91- 063008

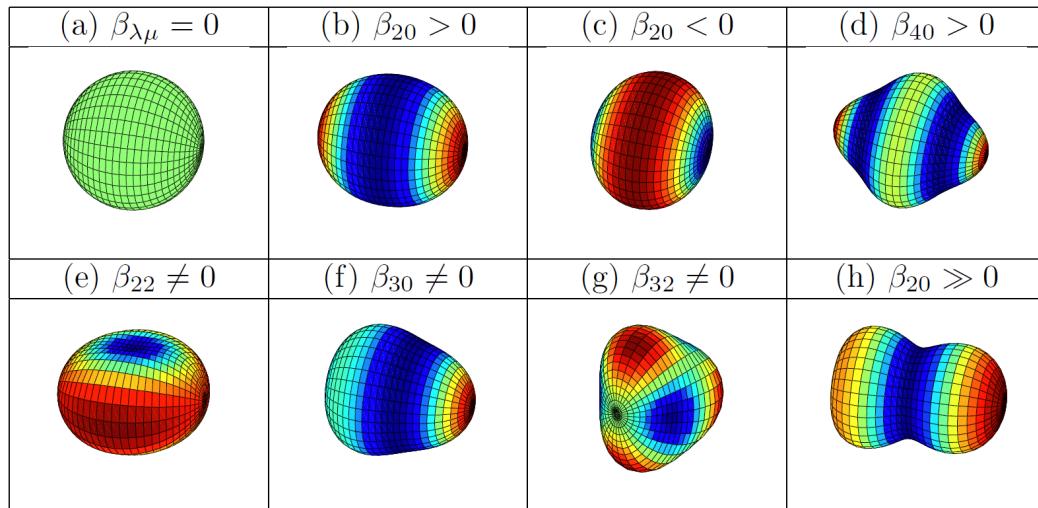


Figure courtesy of Bing-Nan Lu (吕炳楠)

# Halo: Deformation effects

$$R(\theta, \varphi) = R_0 \left[ 1 + \beta_{00} + \sum_{\lambda=1}^{\infty} \sum_{\mu=-\lambda}^{\lambda} \beta_{\lambda\mu}^* Y_{\lambda\mu}(\theta, \varphi) \right]$$

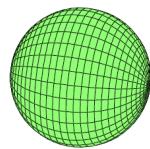
PRL 112, 142501 (2014)

PHYSICAL REVIEW LETTERS

Nakamura+2014\_PRL112-142501

week ending  
11 APRIL 2014

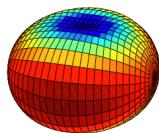
(a)  $\beta_{\lambda\mu} = 0$



## Deformation-Driven *p*-Wave Halos at the Drip Line: $^{31}\text{Ne}$

T. Nakamura,<sup>1</sup> N. Kobayashi,<sup>1</sup> Y. Kondo,<sup>1</sup> Y. Satou,<sup>1,2</sup> J. A. Tostevin,<sup>3</sup> Y. Utsuno,<sup>4</sup> N. Aoi,<sup>5</sup> H. Baba,<sup>5</sup> N. Fukuda,<sup>5</sup> J. Gobel,<sup>6</sup> N. Inabe,<sup>5</sup> M. Ishihara,<sup>5</sup> D. Kameda,<sup>5</sup> T. Kubo,<sup>5</sup> T. Motobayashi,<sup>5</sup> T. Ohnishi,<sup>5</sup> N. A. Orr,<sup>6</sup> H. Otsu,<sup>5</sup> T. Otsuka,<sup>7</sup> H. Sakurai,<sup>5</sup> T. Sumikama,<sup>8</sup> H. Takeda,<sup>5</sup> E. Takeshita,<sup>5</sup> M. Takechi,<sup>5</sup> S. Takeuchi,<sup>5</sup> Y. Togano,<sup>1,5</sup> and K. Yoneda<sup>5</sup>

(e)  $\beta_{22} \neq 0$



PRL 112, 242501 (2014)

PHYSICAL REVIEW LETTERS

Kobayashi+2014\_PRL112-242501

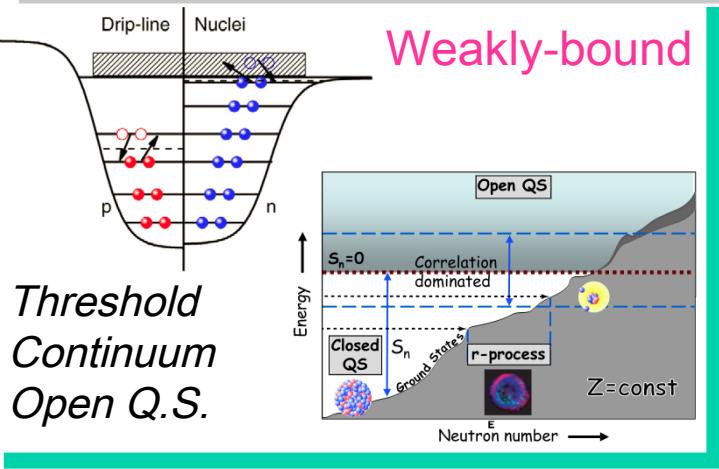
week ending  
20 JUNE 2014

## Observation of a *p*-Wave One-Neutron Halo Configuration in $^{37}\text{Mg}$

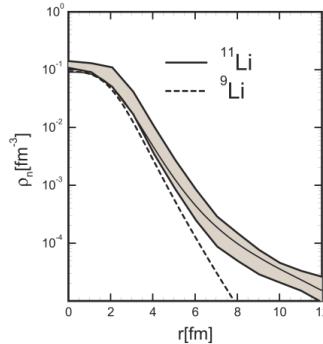
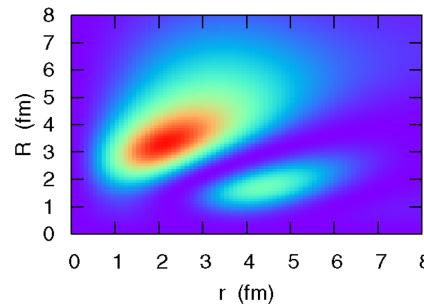
N. Kobayashi,<sup>1,\*</sup> T. Nakamura,<sup>1</sup> Y. Kondo,<sup>1</sup> J. A. Tostevin,<sup>2,1</sup> Y. Utsuno,<sup>3</sup> N. Aoi,<sup>4,†</sup> H. Baba,<sup>4</sup> R. Barthelemy,<sup>5</sup> M. A. Famiano,<sup>5</sup> N. Fukuda,<sup>4</sup> N. Inabe,<sup>4</sup> M. Ishihara,<sup>4</sup> R. Kanungo,<sup>6</sup> S. Kim,<sup>7</sup> T. Kubo,<sup>4</sup> G. S. Lee,<sup>1</sup> H. S. Lee,<sup>7</sup> M. Matsushita,<sup>4,‡</sup> T. Motobayashi,<sup>4</sup> T. Ohnishi,<sup>4</sup> N. A. Orr,<sup>8</sup> H. Otsu,<sup>4</sup> T. Otsuka,<sup>9</sup> T. Sako,<sup>1</sup> H. Sakurai,<sup>4</sup> Y. Satou,<sup>7</sup> T. Sumikama,<sup>10,§</sup> H. Takeda,<sup>4</sup> S. Takeuchi,<sup>4</sup> R. Tanaka,<sup>1</sup> Y. Togano,<sup>4,¶</sup> and K. Yoneda<sup>4</sup>

Figure courtesy of

# Physics of exotic nuclei



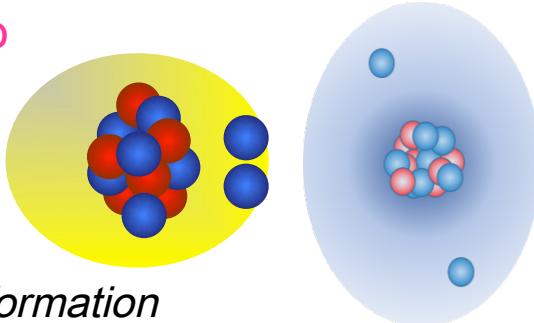
Threshold  
Continuum  
Open Q.S.



Halo

Large spatial ext.  
Low-density N.M.  
2N correlation

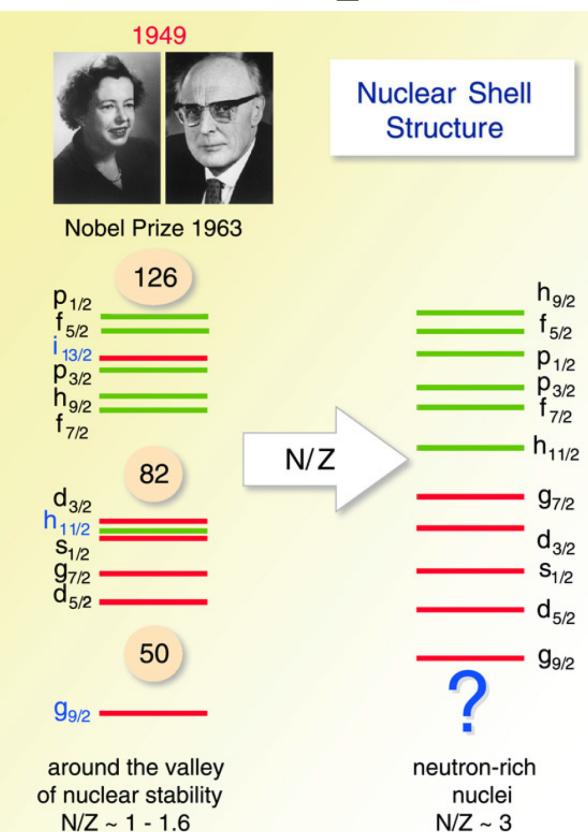
Halo



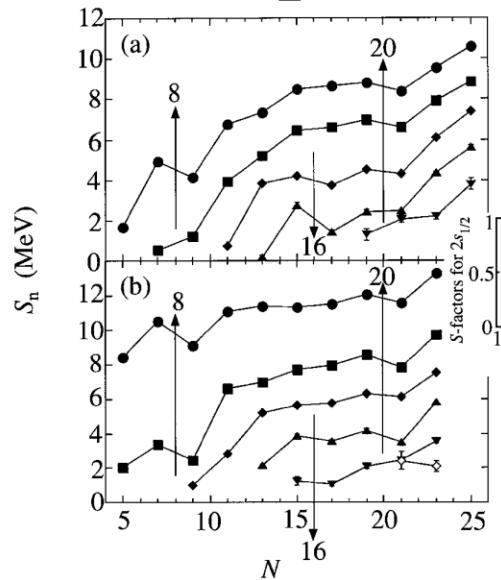
Deformation  
Shape decoupling

# Exotic Nuclei: Shell Evolution

Dobaczewski+2007\_PPNP59-432

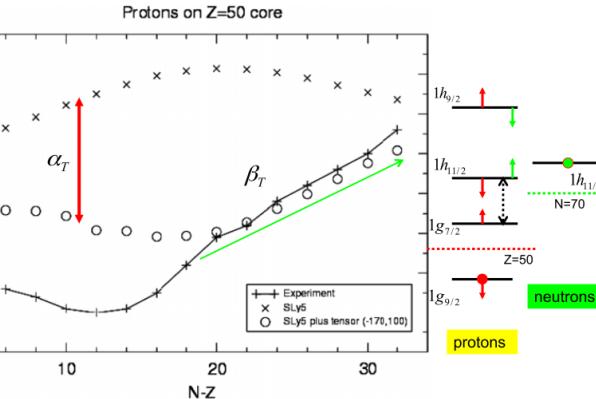


Ozawa+2000\_PRL84-5493



Shape evolution  
Shape coexistence

Colo+2007\_PLB646-227  
Sagawa\_Colo2014\_PPNP76-76



Peru\_Girod\_Berger2000\_EPJA9-35

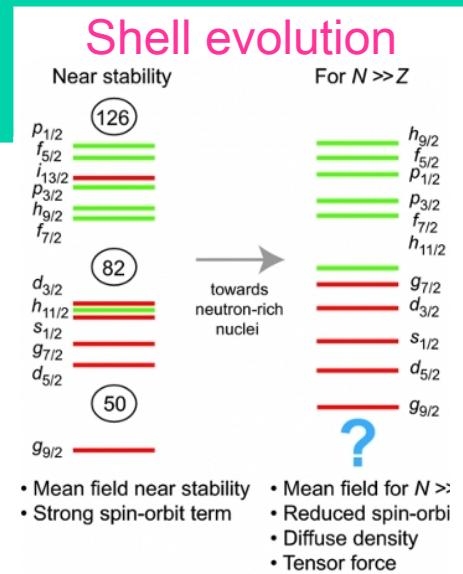
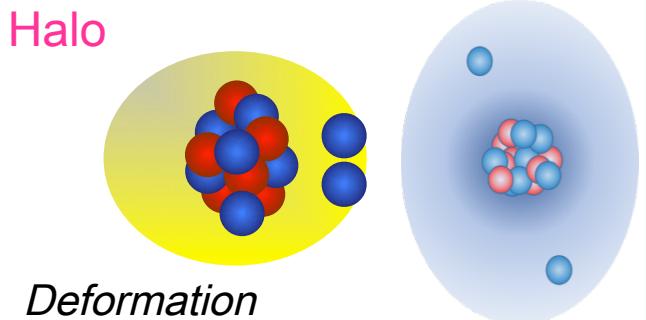
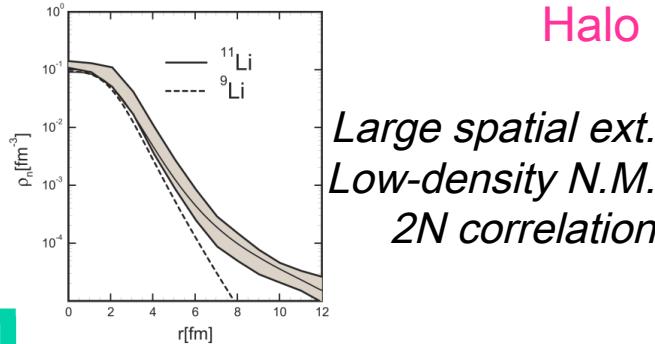
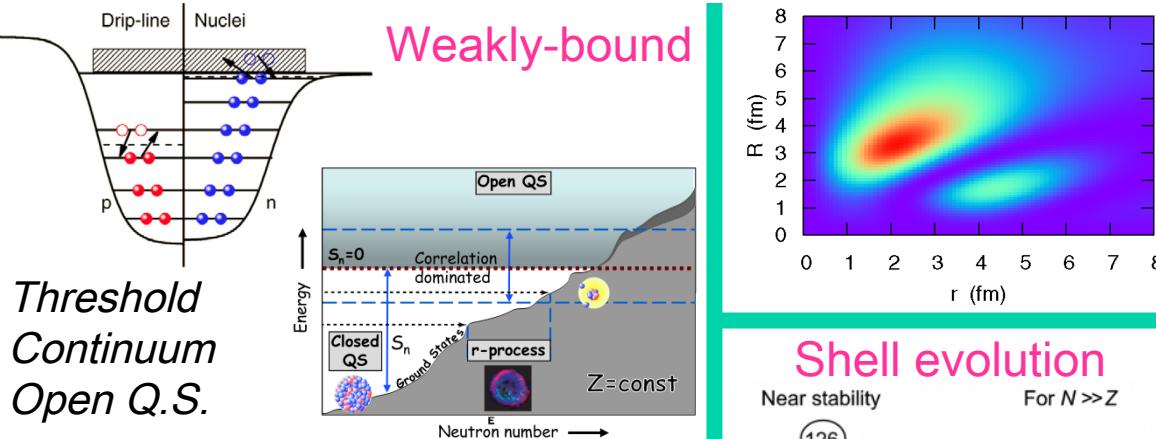
Otsuka+2005\_PRL95-232502

Otsuka+2010\_PRL104-012501

Otsuka+2010\_PRL105-032501

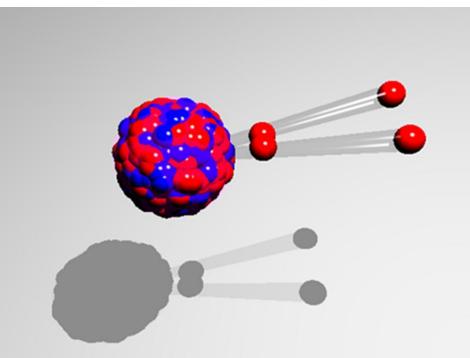
Sorlin\_Porquet2008\_PPNP61-602

# Physics of exotic nuclei



# Exotic Nuclei: New Radioactivities

Woods\_Davids1997\_ARNPS47-541  
Thoennesen2004\_RPP67-1187  
Pfutzner+2012\_RMP84-567



Lin+2011\_SciChinaPMA54S1-73  
**SCIENCE CHINA**  
Physics, Mechanics & Astronomy

• Research Paper •  
Radioactive Nuclear Beam Physics and Nuclear Astrophysics

August 2011 Vol.54 Suppl. 1: s73–s80  
doi: 10.1007/s11433-011-4431-9

## Experimental research into the two-proton emissions from $^{17,18}\text{Ne}$ , $^{28}\text{P}$ and $^{28,29}\text{S}$

Physics Letters B 743 (2015) 306–309

Ma+2015\_PLB743-306



Contents lists available at ScienceDirect

Physics Letters B

[www.elsevier.com/locate/physletb](http://www.elsevier.com/locate/physletb)



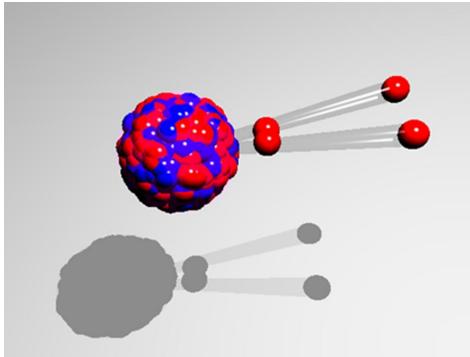
Different mechanism of two-proton emission from proton-rich nuclei  
 $^{23}\text{Al}$  and  $^{22}\text{Mg}$



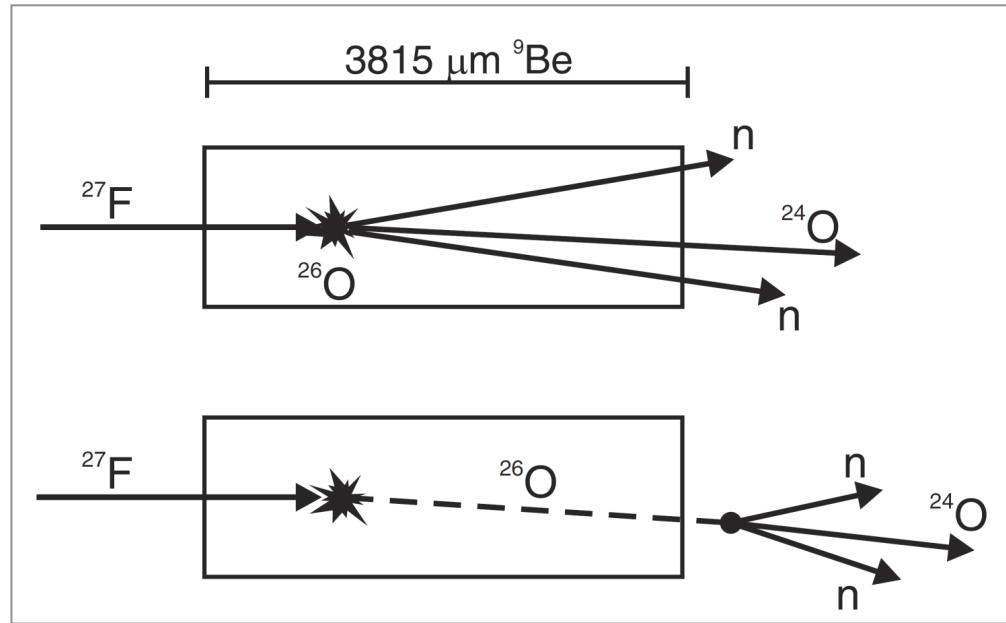
# Exotic Nuclei: New Radioactivities

Woods\_Davids1997\_ARNPS47-541  
Thoennesen2004\_RPP67-1187

Pfutzner+2012\_RMP84-567



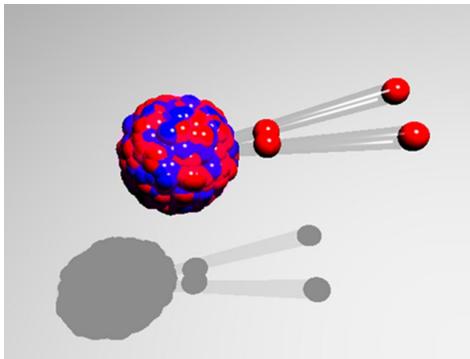
Lunderberg+2012\_PRL108-142503:  $E=150^{+50}_{-150}$  keV  
Kohley+2013\_PRL110-152501:  $T_{1/2} (^{26}\text{O}) \sim 4.5$  ps



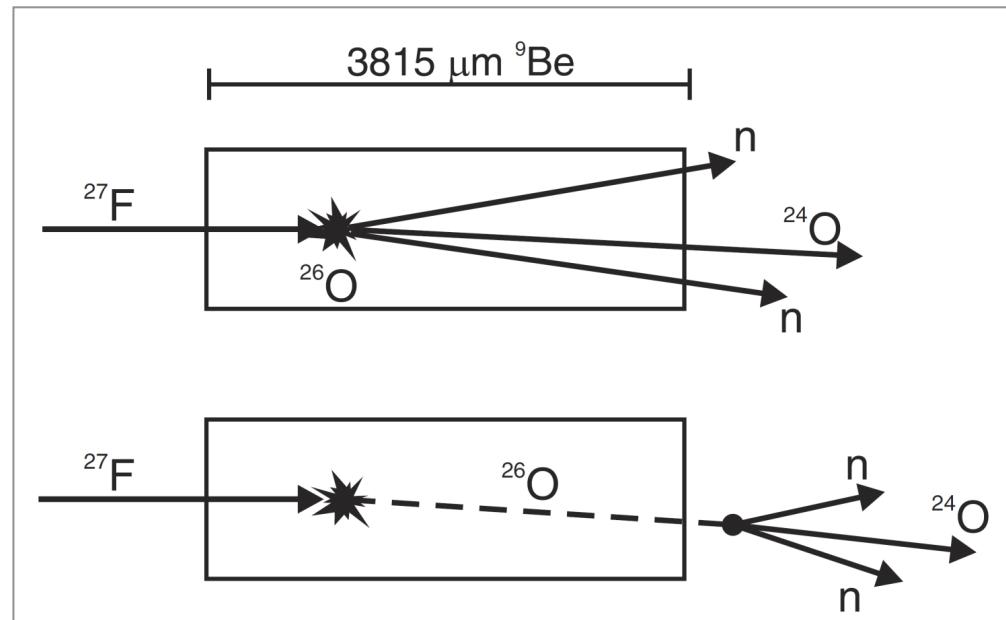
# Exotic Nuclei: New Radioactivities

Woods\_Davids1997\_ARNPS47-541  
Thoennesen2004\_RPP67-1187

Pfutzner+2012\_RMP84-567

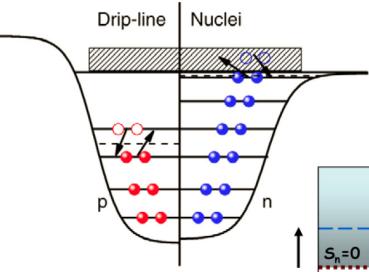


Lunderberg+2012\_PRL108-142503:  $E=150^{+50}_{-150}$  keV  
Kohley+2013\_PRL110-152501:  $T_{1/2}$  ( $^{26}\text{O}$ )  $\sim 4.5$  ps

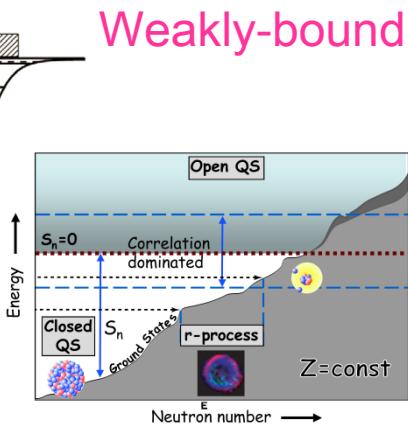


Kondo+2016\_PRL116-102503:  $T_{1/2}$  ( $^{26}\text{O}$ )  $\sim 10^{-17}$ - $10^{-15}$  s

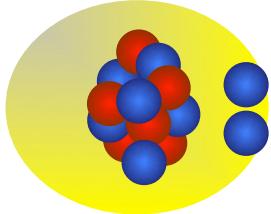
# Physics of exotic nuclei



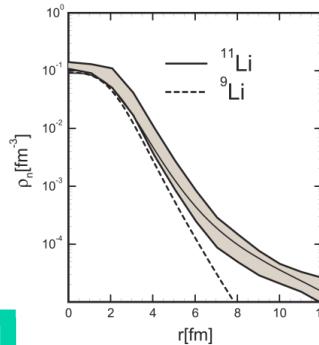
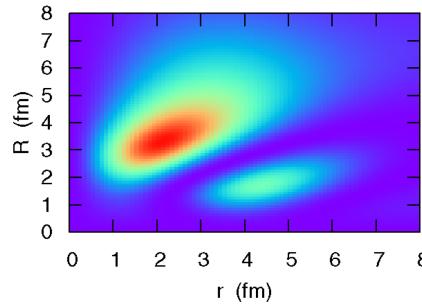
Threshold  
Continuum  
Open Q.S.



Halo



Deformation  
Shape decoupling



Halo

Large spatial ext.  
Low-density N.M.  
2N correlation

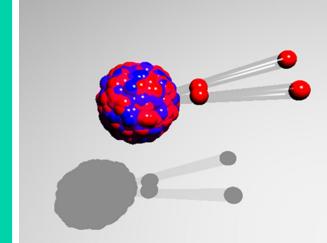
Shell evolution

Near stability

For  $N \gg Z$

(126)	$p_{1/2}$	$h_{9/2}$
	$f_{5/2}$	$f_{5/2}$
	$f_{1/2}$	$p_{1/2}$
	$p_{3/2}$	$p_{3/2}$
	$h_{9/2}$	$f_{7/2}$
	$f_{7/2}$	$h_{11/2}$
(82)	$d_{3/2}$	$g_{7/2}$
	$h_{11/2}$	$d_{3/2}$
	$s_{1/2}$	$s_{1/2}$
	$g_{7/2}$	$d_{5/2}$
(50)	$d_{5/2}$	$g_{9/2}$
	$g_{9/2}$	?

towards neutron-rich nuclei



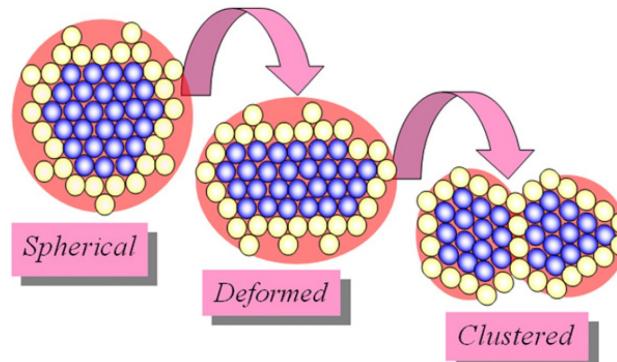
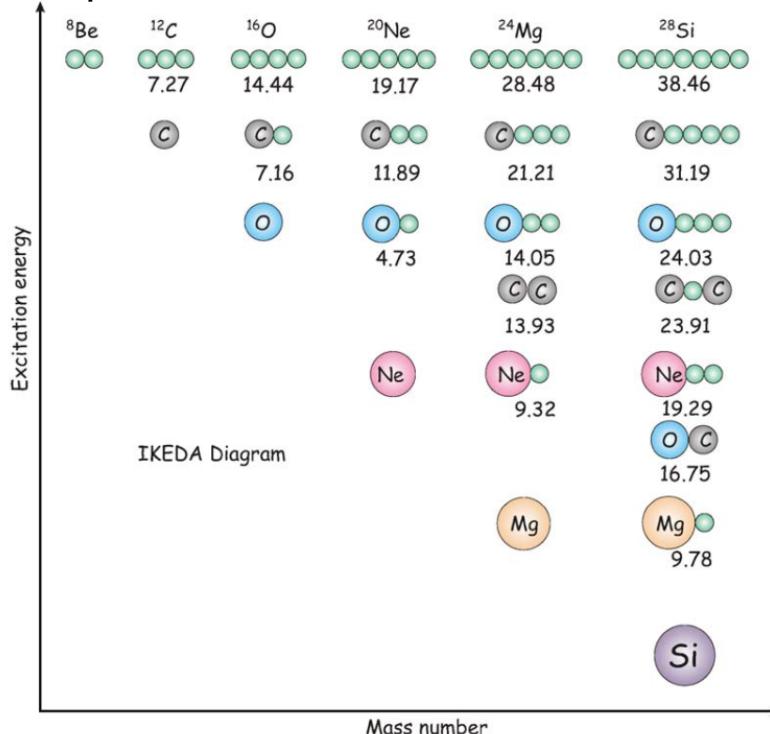
New radioact.

1p emission  
2p emission  
2n emission

- Mean field near stability
- Strong spin-orbit term
- Mean field for  $N \gg Z$
- Reduced spin-orbit
- Diffuse density
- Tensor force

# Exotic Nuclei: Clustering

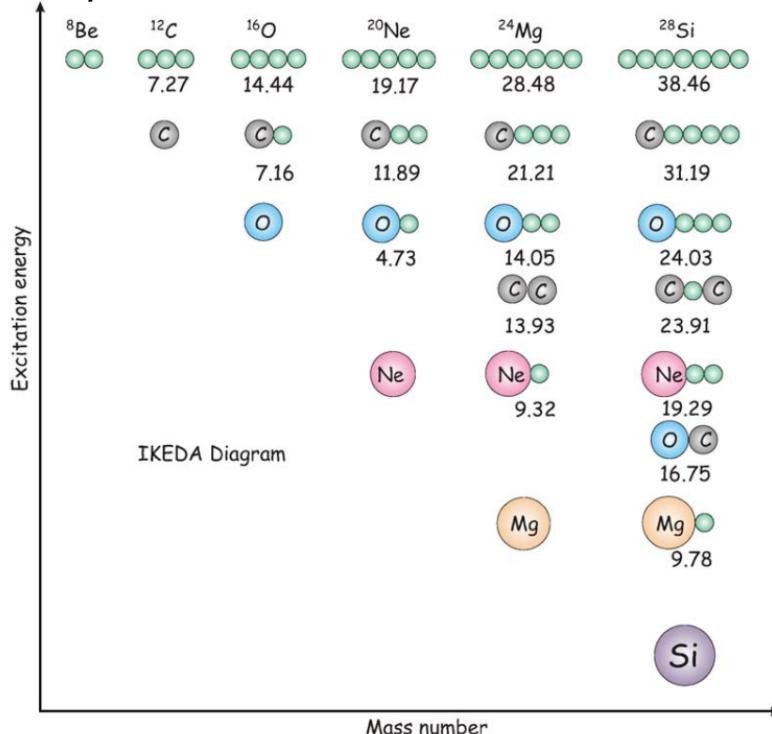
Alpha-nuclei:  $N=Z=\text{even number}$



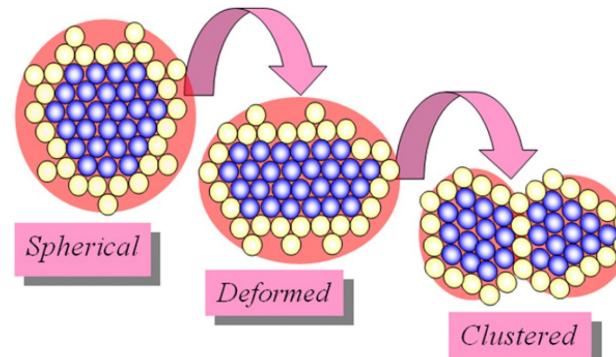
Freer2007\_RPP70-2149

# Exotic Nuclei: Clustering

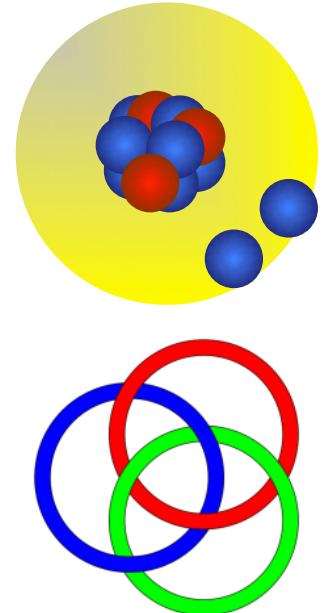
Alpha-nuclei:  $N=Z=\text{even number}$



vonOertzen\_Freer\_Kanada-En'yo  
2006\_PR432-43



Freer2007\_RPP70-2149



Borromean Ring

# Exotic Nuclei: Clustering

Alpha-nuclei:  $N=Z=\text{even number}$



PRL 112, 162501 (2014)

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25 APRIL 2014

## Observation of Enhanced Monopole Strength and Clustering in $^{12}\text{Be}$

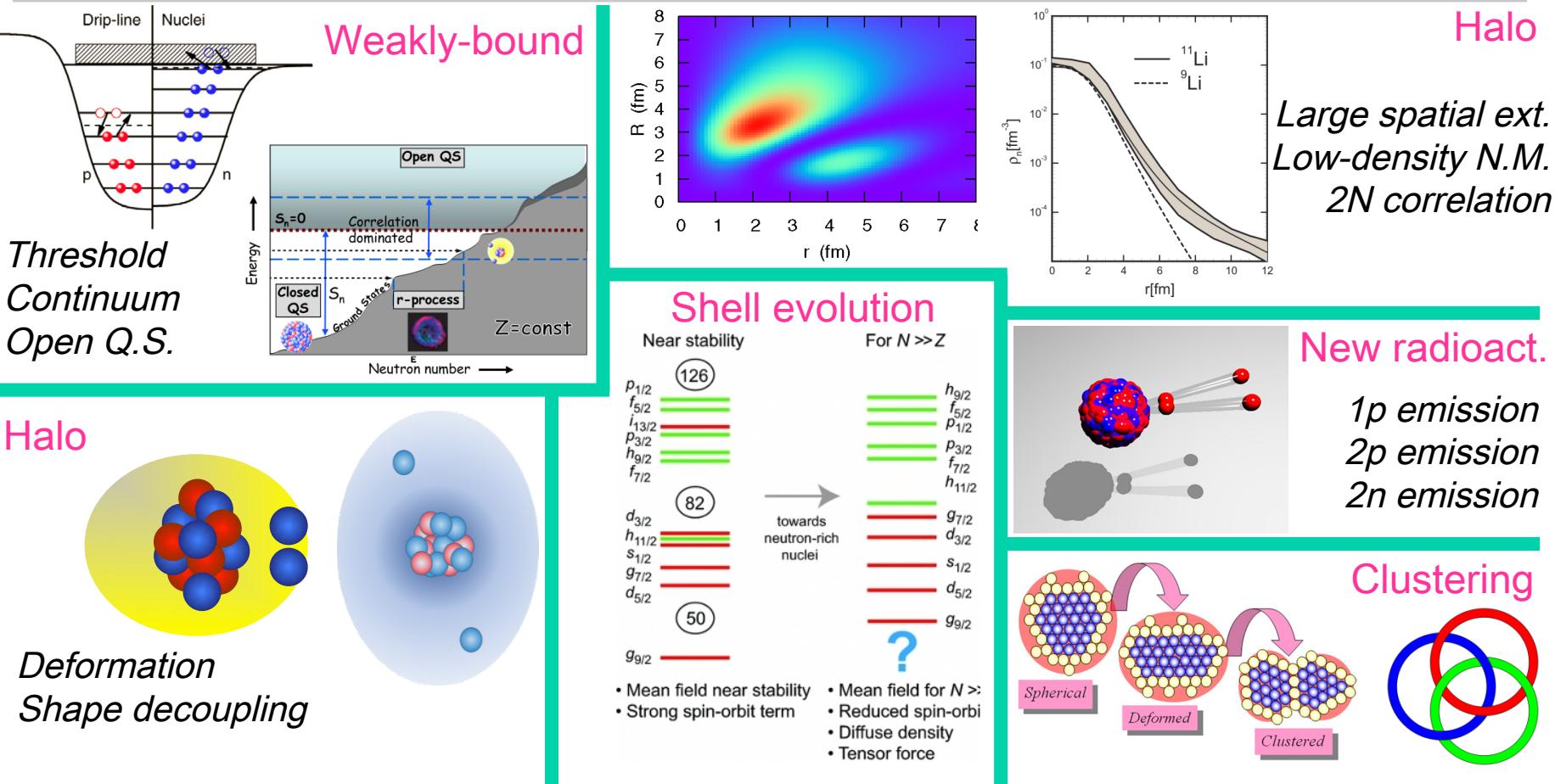
Z. H. Yang (杨再宏),<sup>1</sup> Y. L. Ye (叶沿林),<sup>1,\*</sup> Z. H. Li (李智焕),<sup>1</sup> J. L. Lou (楼建玲),<sup>1</sup> J. S. Wang (王建松),<sup>2</sup> D. X. Jiang (江栋兴),<sup>1</sup> Y. C. Ge (葛渝成),<sup>1</sup> Q. T. Li (李奇特),<sup>1</sup> H. Hua (华辉),<sup>1</sup> X. Q. Li (李湘庆),<sup>1</sup> F. R. Xu (许甫荣),<sup>1</sup> J. C. Pei (裴俊琛),<sup>1</sup> R. Qiao (乔锐),<sup>1</sup> H. B. You (游海波),<sup>1</sup> H. Wang (王赫),<sup>1,3</sup> Z. Y. Tian (田正阳),<sup>1</sup> K. A. Li (李阔昂),<sup>1</sup> Y. L. Sun (孙叶磊),<sup>1</sup> H. N. Liu (刘红娜),<sup>1,3</sup> J. Chen (陈洁),<sup>1</sup> J. Wu (吴锦),<sup>1,3</sup> J. Li (李晶),<sup>1</sup> W. Jiang (蒋伟),<sup>1</sup> C. Wen (文超),<sup>1,3</sup> B. Yang (杨彪),<sup>1</sup> Y. Y. Yang (杨彦云),<sup>2</sup> P. Ma (马朋),<sup>2</sup> J. B. Ma (马军兵),<sup>2</sup> S. L. Jin (金仕纶),<sup>2</sup> J. L. Han (韩建龙),<sup>2</sup> and J. Lee (李晓菁)<sup>3</sup>

Mass number

Si



# Physics of exotic nuclei



# Weakly bound: Models dealing w/ Continuum

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- Few-body approach
  - Two-particle Green's function or complex scaling methods
- Shell model
  - Berggren basis
- (Relativistic) Hartree(-Fock) + resonance BCS approach
- (Relativistic) Hartree(-Fock)  
Bogoliubov model
  - *R*-space or equivalent basis

Frederico+2012\_PPNP67-939

[Meng\\_SGZ2015\\_JPG42-093101](#)

Sagawa\_Hagino2015\_EPJA51-102

Ji2016\_IJMPE25-1641003

# Weakly bound: Models dealing w/ Continuum

- Few-body approach
  - Two-particle Green's function or complex scaling methods
- Shell model
  - Berggren basis
- (Relativistic) Hartree(-Fock) + resonance BCS approach
- (Relativistic) Hartree(-Fock) Bogoliubov model
  - *R*-space or equivalent basis

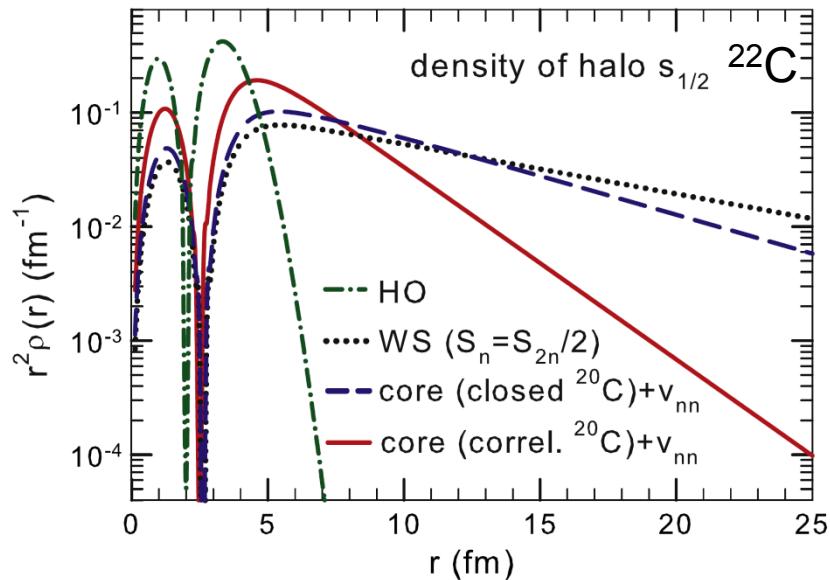
Frederico+2012\_PPNP67-939

Meng\_SGZ2015\_JPG42-093101

Sagawa\_Hagino2015\_EPJA51-102

Ji2016\_IJMPE25-1641003

Suzuki\_Otsuka\_Yuan\_Navin2016\_PLB753-199



Togano+2016\_PLB761-412:  $r_m = 3.44 \pm 0.08$  fm

Tanaka+2010\_PRL104-062701:  $r_m = 5.4 \pm 0.9$  fm

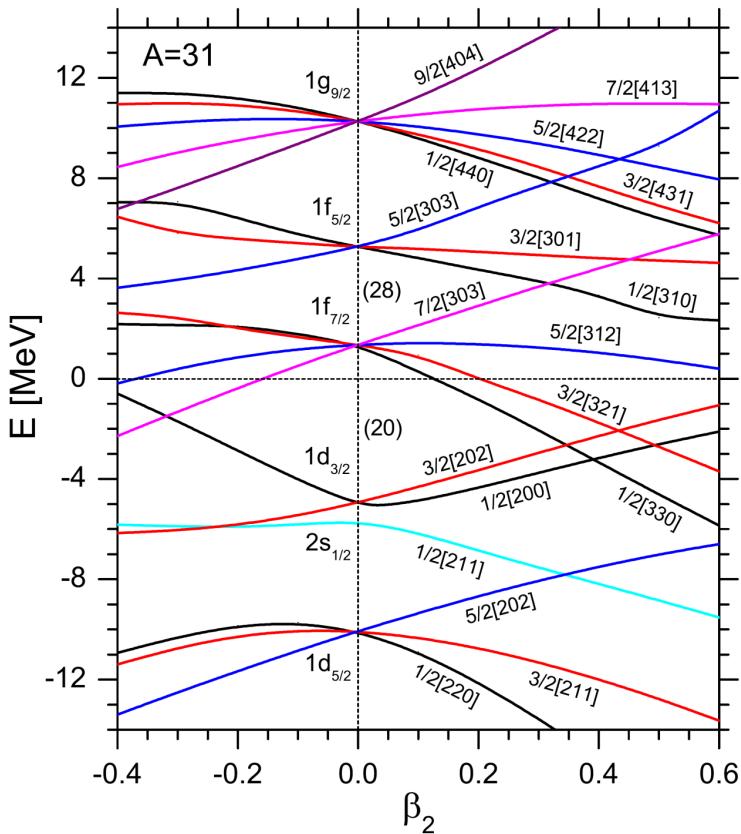
# Single Particle Resonances

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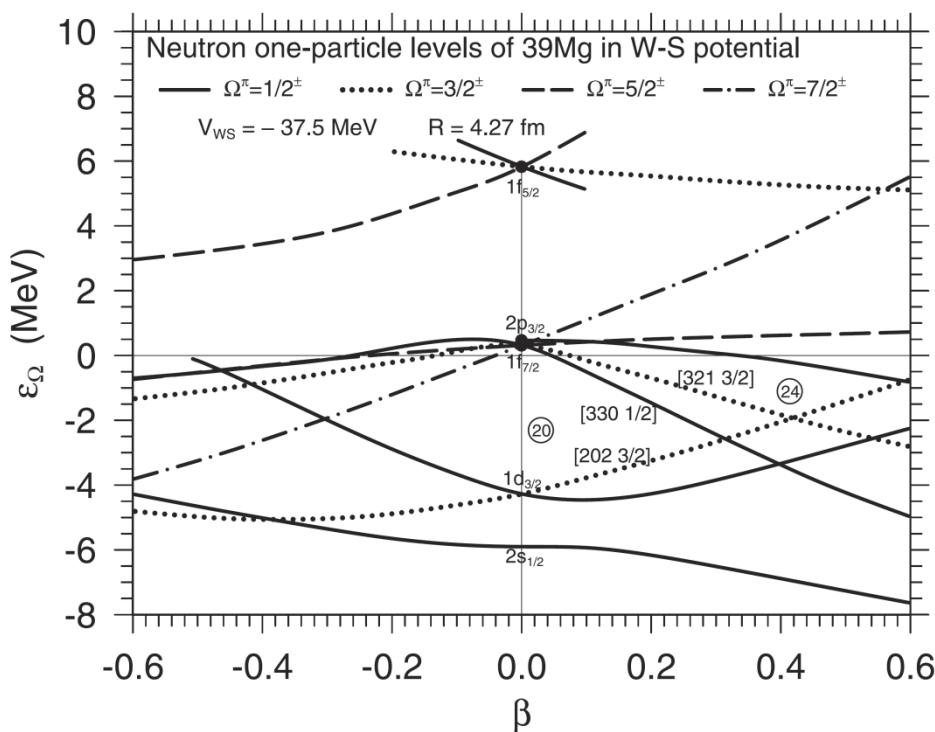
- Scattering phase shift method
- Bound-state-like approaches Efros+2007\_JPG34-R459; Carbonell+2014\_PPNP74-55
  - Analytical continuation of coupling constant (ACCC)  
Tanaka+1997\_PRC56-562; Yang\_Meng\_SGZ2001\_CPL8-196; Zhang+2004\_PRC70-034308  
Guo\_Fang2006\_PRC74-024320; Zhang+2012\_PRC86-032802; Xu+2015\_PRC92-024324
  - Real stabilization method (RSM)  
Zhang+2008\_PRC77-014312; Pei\_Kruppa\_Nazarewicz2011\_PRC84-024311
  - Complex scaling method (CSM)  
.....; Myo+2014\_PPNP79-1; Papadimitriou\_Vary2015\_PRC91-021001R  
Shi2015\_PRC92-054313
- Jost function method Lu\_Zhao\_SGZ2012\_PRL109-072501; 2013\_PRC88-024323
- Green's function method Matsuo2001\_NPA696-371; .....; Sun+2014\_PRC90-054321
- Green's function + CSM Shi+2015\_PRC92-054313; Shi+2016\_PRC94-024302
- Complex momentum representation Li+2016\_PRL117-062502; Liang's talk

# Nilsson Diagram w/ Resonances

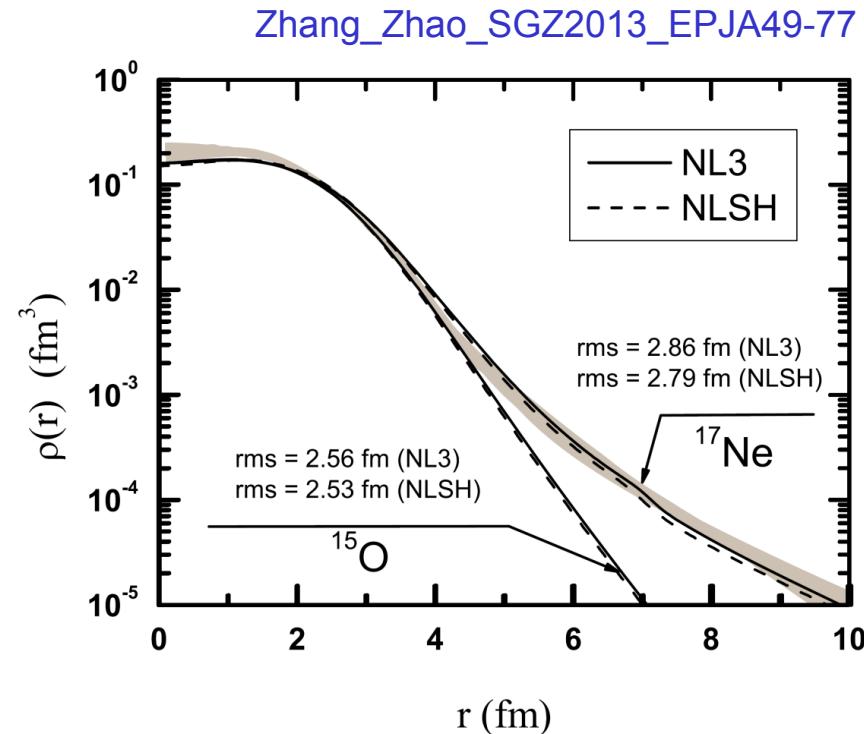
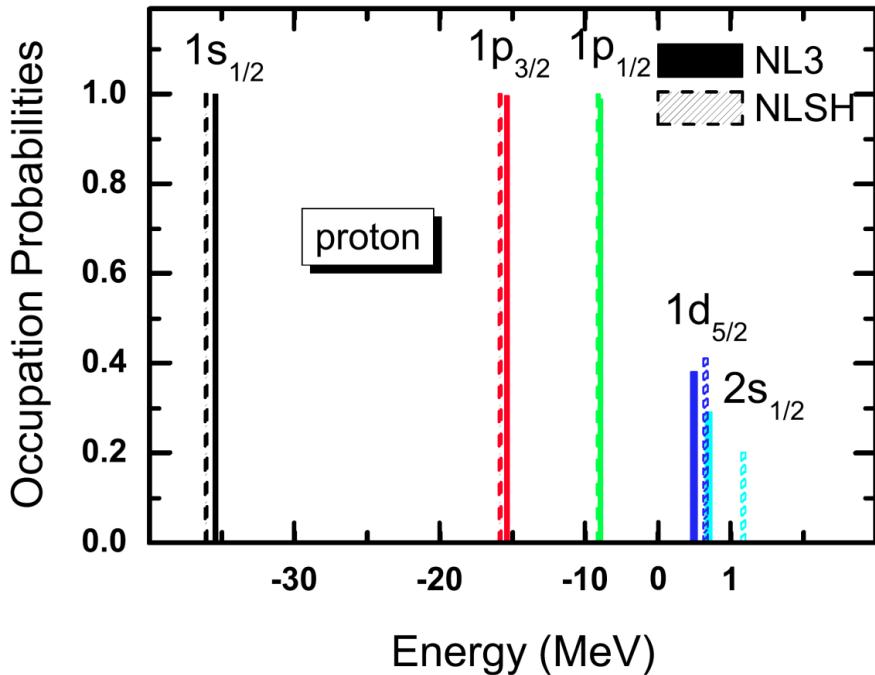
Shi\_Liu\_Niu\_Guo2014\_PRC90-034319



Hamamoto2016\_PRC93-054328



# $^{17}\text{Ne}$ : RMF+ACCC+BCS



rBCS: Sandulescu\_Giai\_Liotta2000\_PRC61-061301R; Sandulescu+2003\_PRC68-054323

# Weakly bound: Continuum (R)HFB model

---

Contribution of continuum can be taken into account  
by solving HFB equations in *r*-space

Bulgac1980 (nucl-th/9907088) ; Dobaczewski\_Flocard\_Treiner1984\_NPA422-103

# Weakly bound: Continuum (R)HFB model

Contribution of continuum can be taken into account  
by solving HFB equations in *r*-space

Bulgac1980 (nucl-th/9907088) ; Dobaczewski\_Flocard\_Treiner1984\_NPA422-103

Skyrme or Gogny Hartree-Fock-Bogoliubov models

	Spherical Nuclei	Deformed Nuclei
Box Boundary	Dobaczewski_Flocard_Treiner1984_NPA422 Dobaczewski+1996_PRC53-2809  Schunck_Egido2008_PRC78-064305	Nakada2008_NPA808-47  Pei_Zhang_Xu2013_PRC87-051302R Pei+2014_PRC90-024317
Scattering Boundary	Zhang_Matsuo_Meng2011_PRC83-054301 Zhang_Matsuo_Meng2012_PRC86-054318	N/A

# Weakly bound: Continuum (R)HFB model

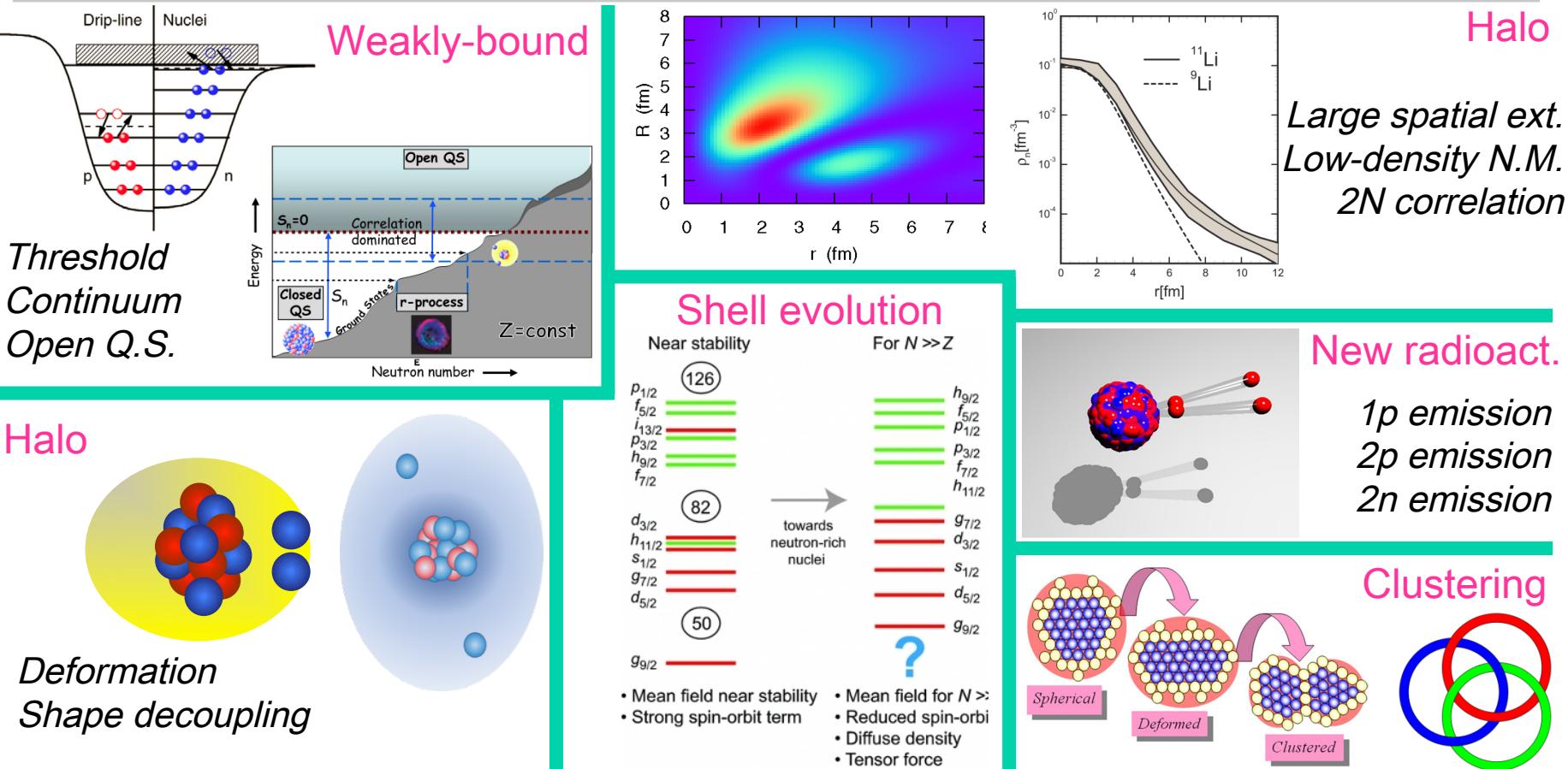
Contribution of continuum can be taken into account  
by solving HFB equations in *r*-space

Bulgac1980 (nucl-th/9907088) ; Dobaczewski\_Flocard\_Treiner1984\_NPA422-103

## Relativistic Hartree(-Fock)-Bogoliubov models

	Spherical Nuclei	Deformed Nuclei
Box Boundary	Meng_Ring1996_PRL77-3963 Meng1998_NPA635-3 Poschl+1997_PRL79-3841  Long+2010_PRC81-024308	SGZ+2010_PRC82-011301R Li+2012_PRC85-024312 Li+2012_ChinPhysLett29-042101  Chen+2012_PRC85-067301
Scattering Boundary	N/A	N/A

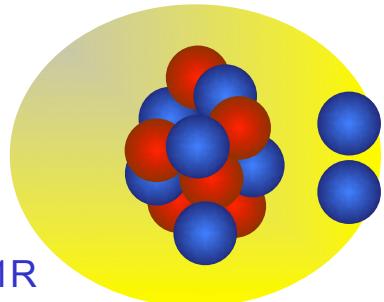
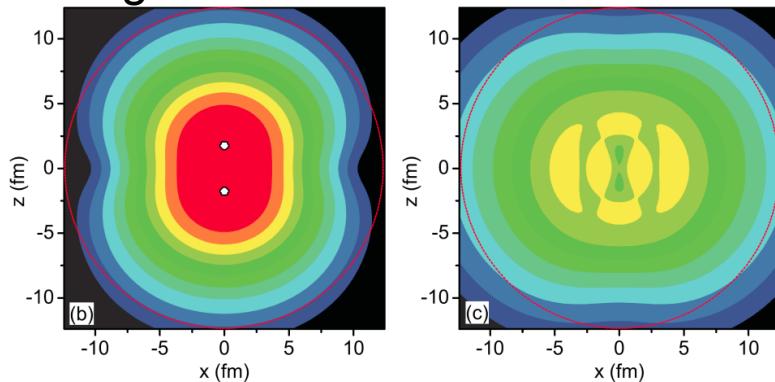
# Physics of exotic nuclei



# Shape Decoupling in Deformed Halo Nuclei

Relativistic HB model

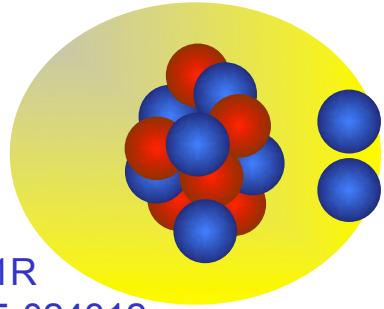
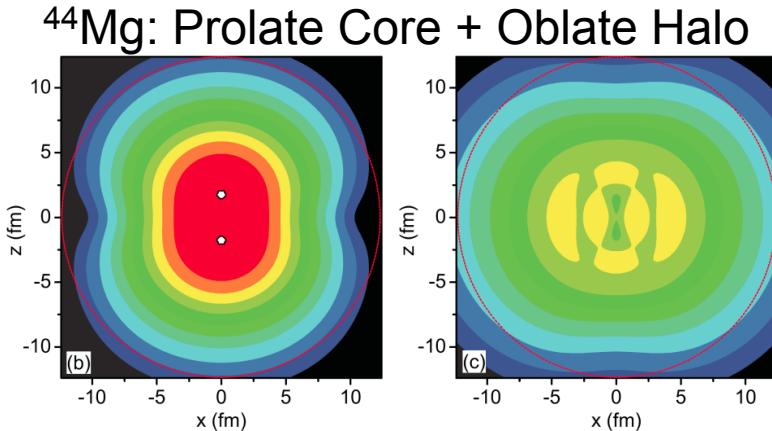
$^{44}\text{Mg}$ : Prolate Core + Oblate Halo



SGZ+2010  
PRC82-011301R  
Li+2012\_PRC85-024312

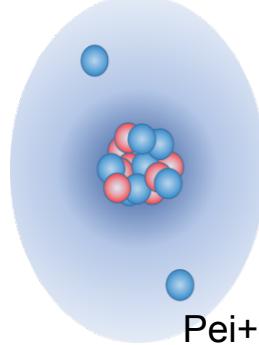
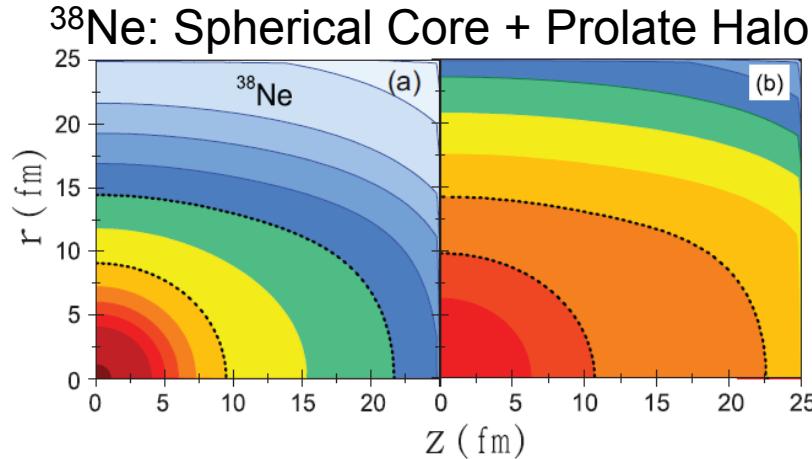
# Shape Decoupling in Deformed Halo Nuclei

Relativistic HB model



SGZ+2010  
PRC82-011301R  
Li+2012\_PRC85-024312

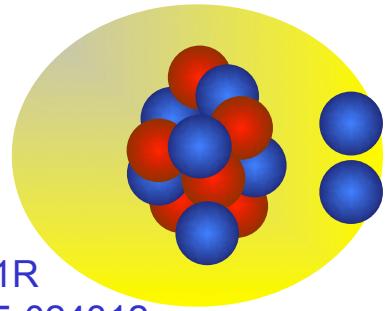
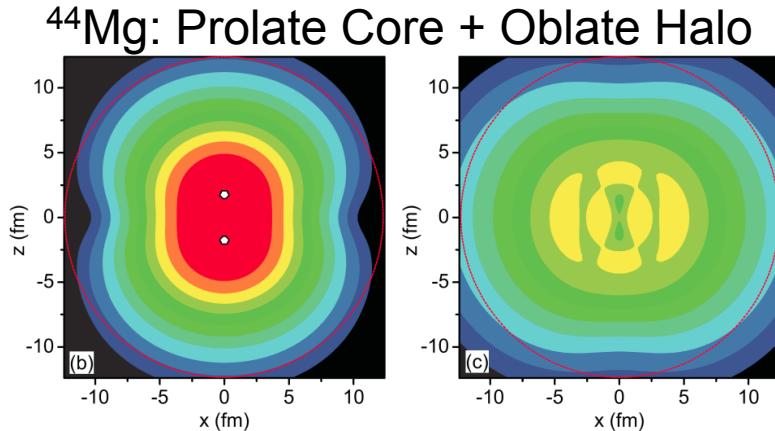
Skyrme HFB model



Pei\_Zhang\_Xu2013  
PRC87-051302R  
Pei+2014\_PRC90-024317

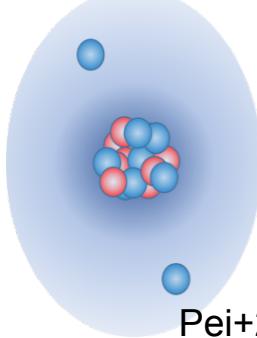
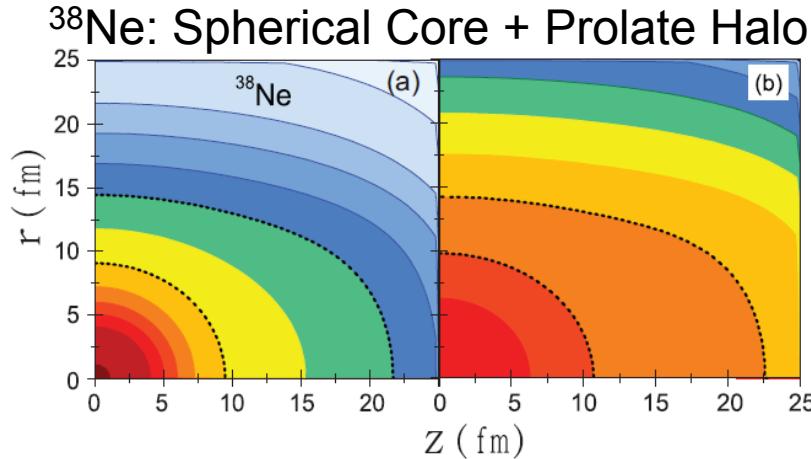
# Shape Decoupling in Deformed Halo Nuclei

Relativistic HB model



SGZ+2010  
PRC82-011301R  
Li+2012\_PRC85-024312

Skyrme HFB model

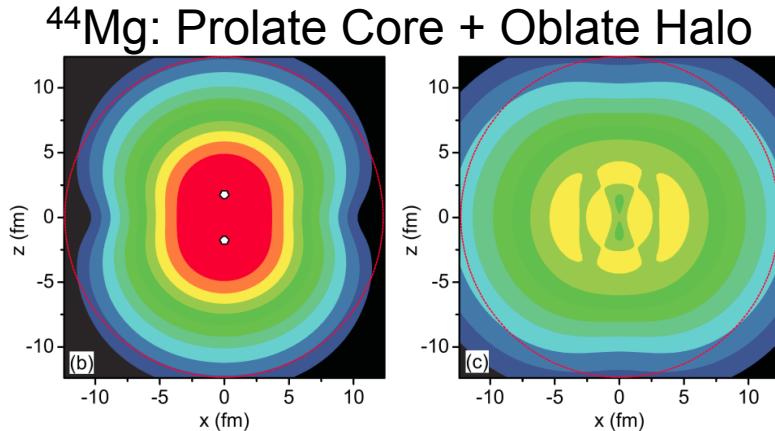


Square well w/o ls  
Misu\_Nazarewicz\_Aberg  
1997\_NPA614-44

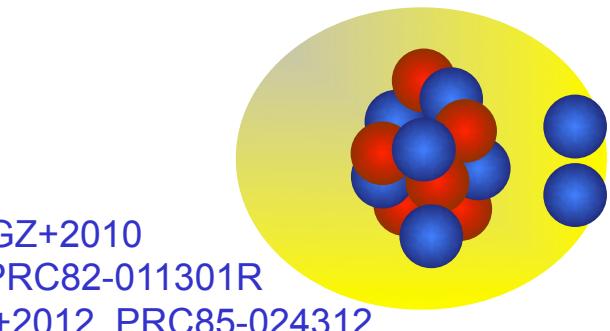
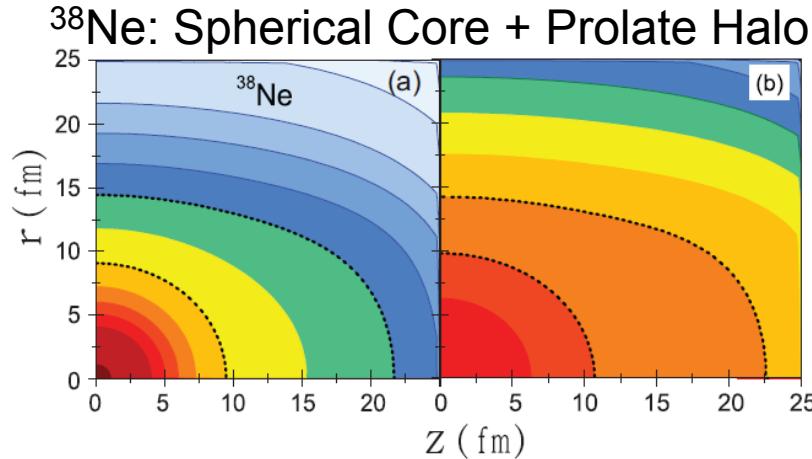
Pei\_Zhang\_Xu2013  
PRC87-051302R  
Pei+2014\_PRC90-024317

# Shape Decoupling in Deformed Halo Nuclei

Relativistic HB model

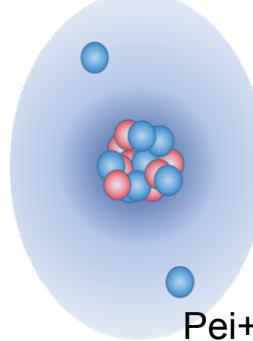


Skyrme HFB model



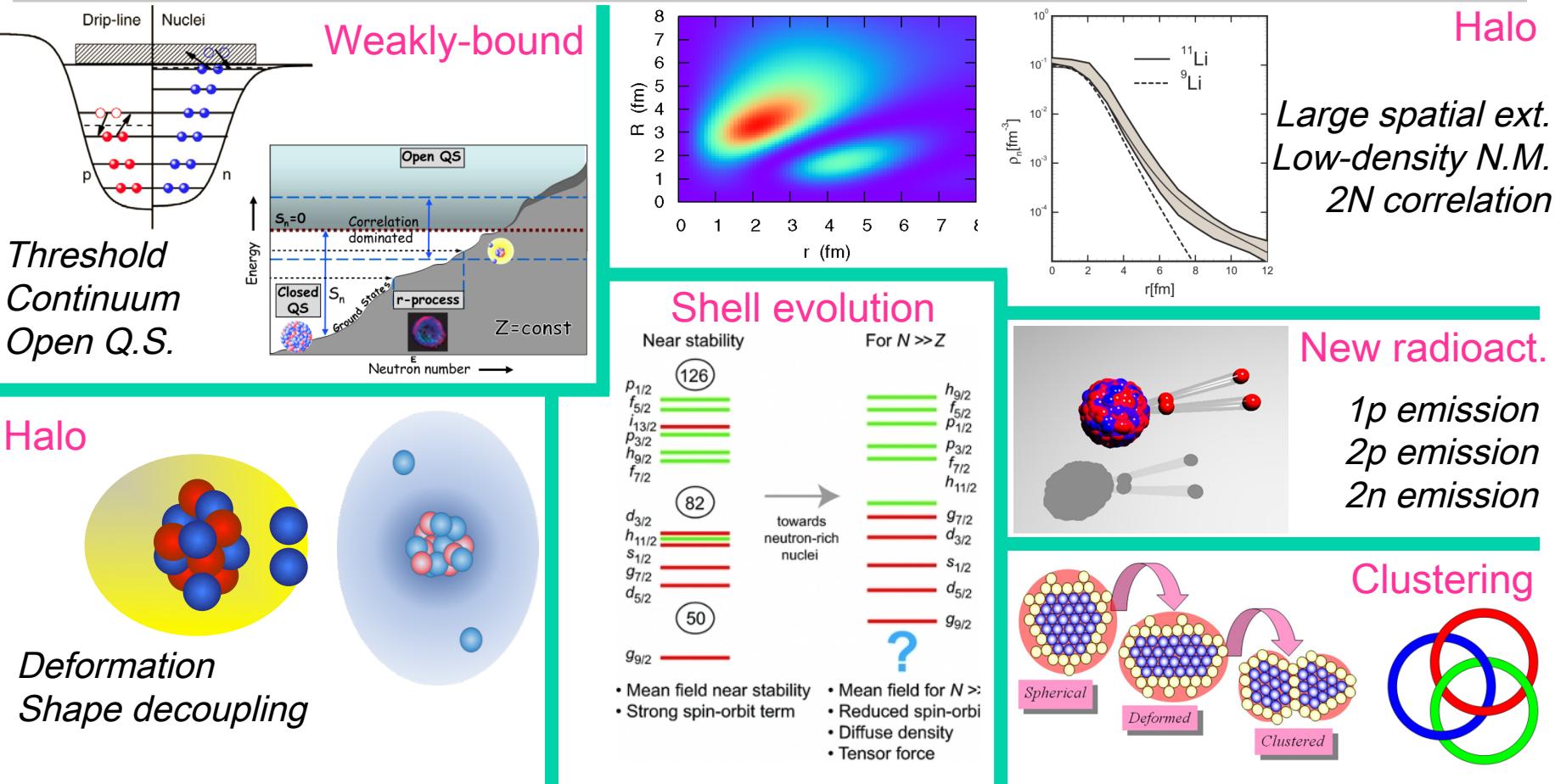
SGZ+2010  
PRC82-011301R  
Li+2012\_PRC85-024312

How about rotation?  
Fossez+2016\_PRC93-011305R



Pei\_Zhang\_Xu2013  
PRC87-051302R  
Pei+2014\_PRC90-024317

# Physics of exotic nuclei



# Di-nucleon correlations

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- Asymptotic form of neutron Cooper pairs

Zhang\_Matsuo\_Meng2014\_PRC90-034313R

- Di-neutron corr.:  $^{10}\text{Be} = ^8\text{Be} + 2\text{n}$

Kobayashi\_Kanada-En'yo2016\_PRC93-024310

- Di-proton corr.:  $^6\text{Be} = ^4\text{He} + 2\text{p}$

Oishi\_Hagino\_Sagawa2014\_PRC90-034303

- Neutron-proton corr.:  $^{18}\text{F} = ^{16}\text{O} + ^2\text{H}$

Masui\_Kimura2016\_PTEP2016-053D01

# Di-nucleon correlations

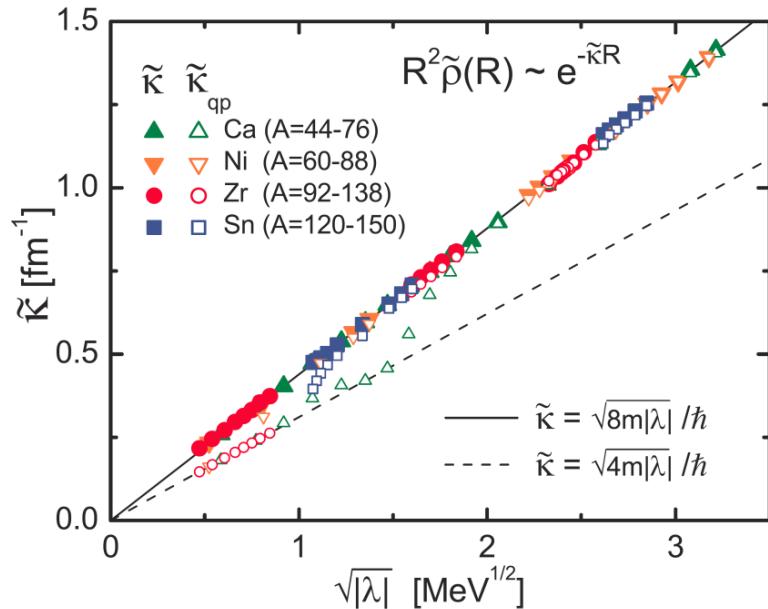
## □ Asymptotic form of neutron Cooper pairs

Zhang\_Matsuo\_Meng2014\_PRC90-034313R

Cooper pairs are spatially correlated in the asymptotic large distance limit, and the penetration length of the pair condensate is universally governed by the two-neutron separation energy

■ Neutron-proton con...

Masui\_Kimura2016\_PTEP2016-053D01



# Soft dipole modes

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Theo. Review: Paar\_Vretenar\_Colo2007\_RPP70-691

Nakatsukasa\_Matsuyanagi\_Matsuo\_Yabana2016\_arXiv1606.04717 (RMP, in press)

Expt. Review: Savran\_Aumann\_Zilges2013\_PPNP70-210

Ebata\_Nakatsukasa\_Inakura2014\_PRC90-024303

Roca-Maza+2012\_PRC85-024601

Vretenar+2012\_PRC85-044317

Inakura+2014\_PRC89-064316

Papakonstantinou\_Hergert\_Roth2015\_PRC92-034311

Ma+2016\_PRC93-014317

DeGregorio2016\_PRC93-044314

Zheng2016\_PRC94-014313

# Soft dipole modes

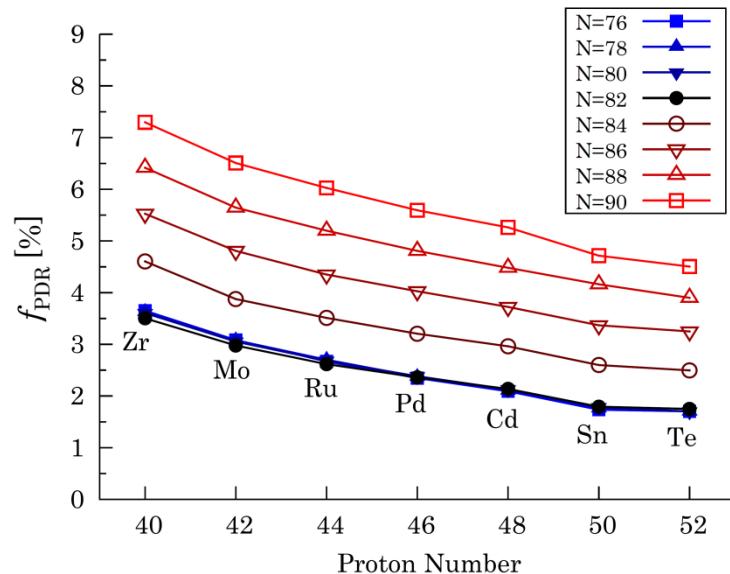
Theo. Review: Paar\_Vretenar\_Colo2007\_RPP70-691

Nakatsukasa\_Matsuyanagi\_Matsuo\_Yabana2016\_arXiv1606.04717 (RMP, in press)

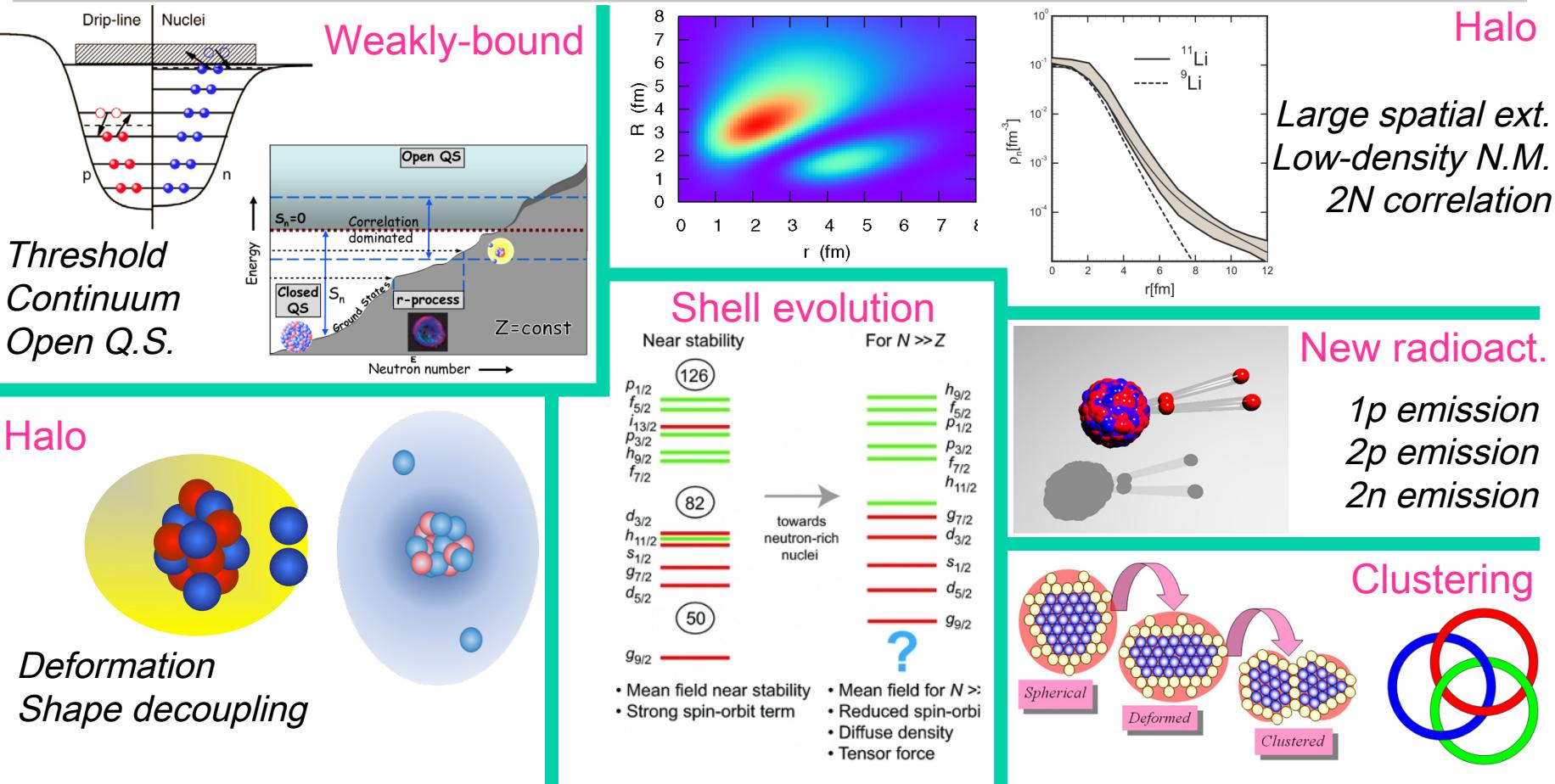
Expt. Review: Savran\_Aumann\_Zilges2013\_PPNP70-210

Ebata\_Nakatsukasa\_Inakura2014\_PRC90-024303

A systematic study with Cb-TDHFB reveals a number of characteristic features of the low-energy E1 modes, e.g., a universal behavior in the low-energy E1 modes for heavy neutron-rich isotopes, which suggests the emergence of decoupled E1 peaks beyond  $N = 82$ .



# Physics of exotic nuclei



# New doubly magic Ca isotopes?

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Wienholtz+2013\_Nature498-346

## LETTER

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doi:10.1038/nature12226

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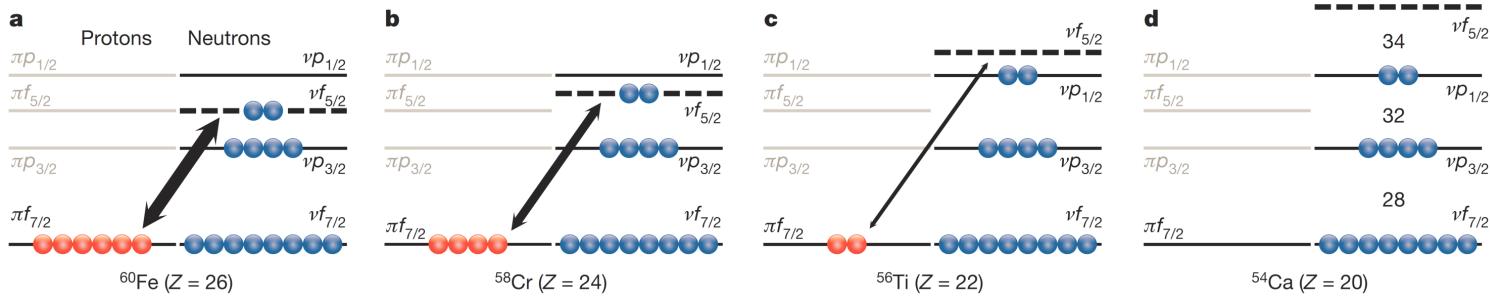
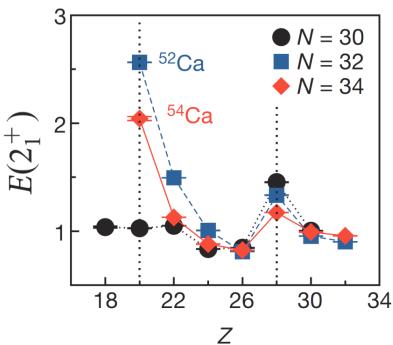
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## Masses of exotic calcium isotopes pin down nuclear forces

F. Wienholtz<sup>1</sup>, D. Beck<sup>2</sup>, K. Blaum<sup>3</sup>, Ch. Borgmann<sup>3</sup>, M. Breitenfeldt<sup>4</sup>, R. B. Cakirli<sup>3,5</sup>, S. George<sup>1</sup>, F. Herfurth<sup>2</sup>, J. D. Holt<sup>6,7</sup>, M. Kowalska<sup>8</sup>, S. Kreim<sup>3,8</sup>, D. Lunney<sup>9</sup>, V. Manea<sup>9</sup>, J. Menéndez<sup>6,7</sup>, D. Neidherr<sup>2</sup>, M. Rosenbusch<sup>1</sup>, L. Schweikhard<sup>1</sup>, A. Schwenk<sup>7,6</sup>, J. Simonis<sup>6,7</sup>, J. Stanja<sup>10</sup>, R. N. Wolf<sup>1</sup> & K. Zuber<sup>10</sup>

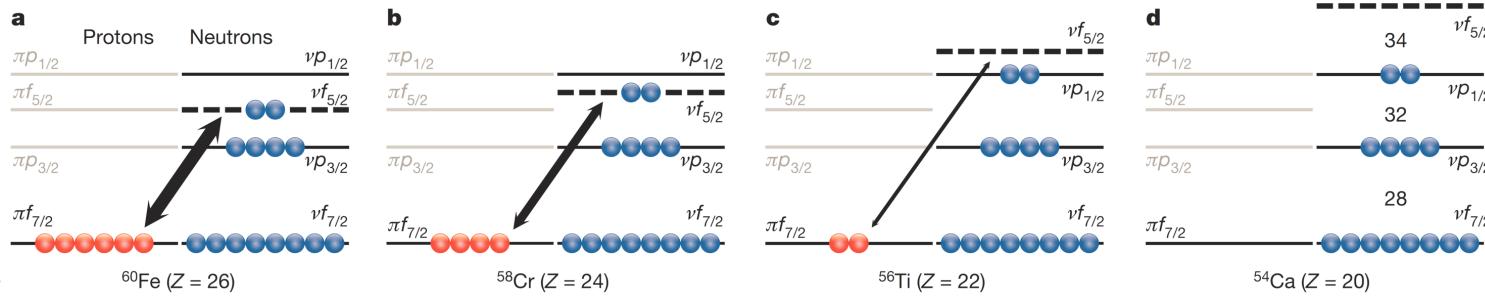
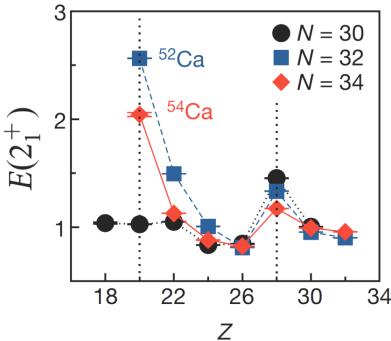
# New doubly magic Ca isotopes?

Steffenbeck+2013  
Nature 502-207



# New doubly magic Ca isotopes?

Steffenbeck+2013  
Nature 502-207



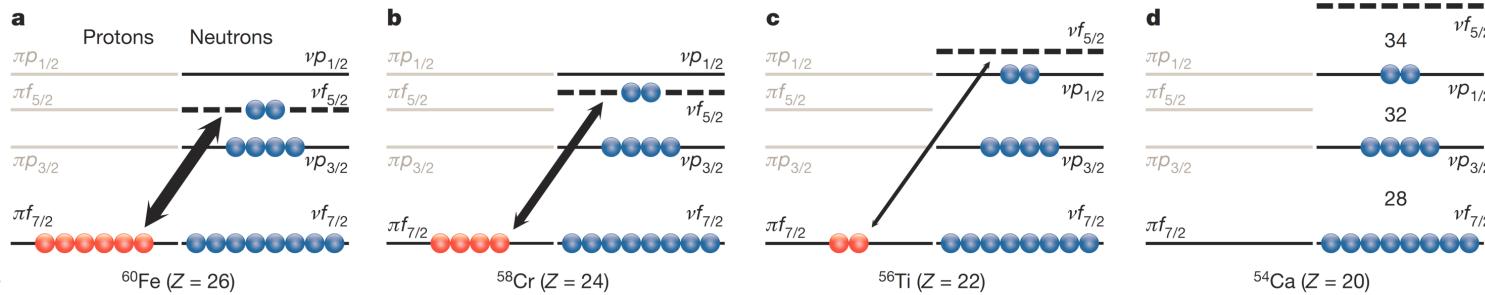
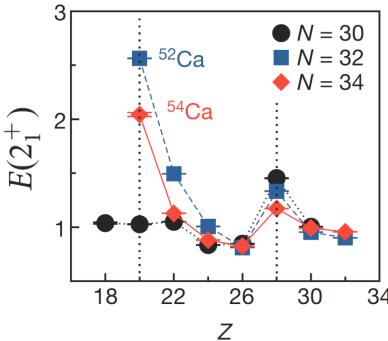
Grasso2014\_PRC89-034316

Yueksel+2014\_PRC89-064322

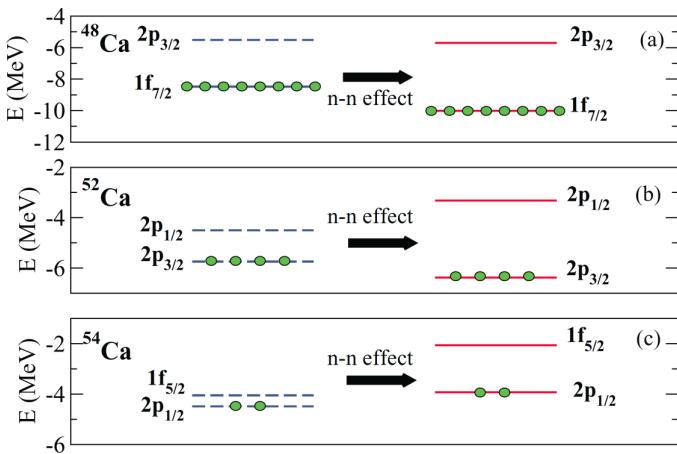
Wang\_Dong2015\_JPG42-125101

# New doubly magic Ca isotopes?

Steffenbeck+2013  
Nature 502-207

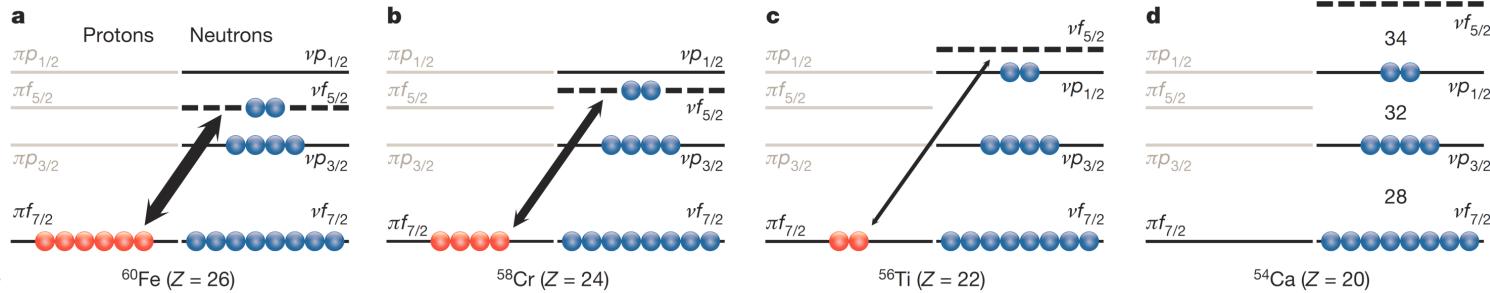
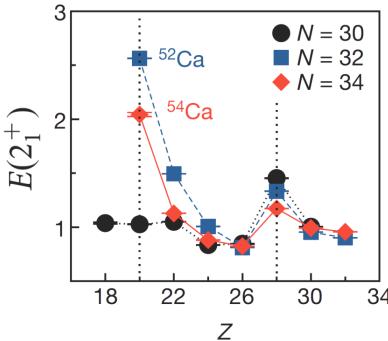


Grasso2014\_PRC89-034316

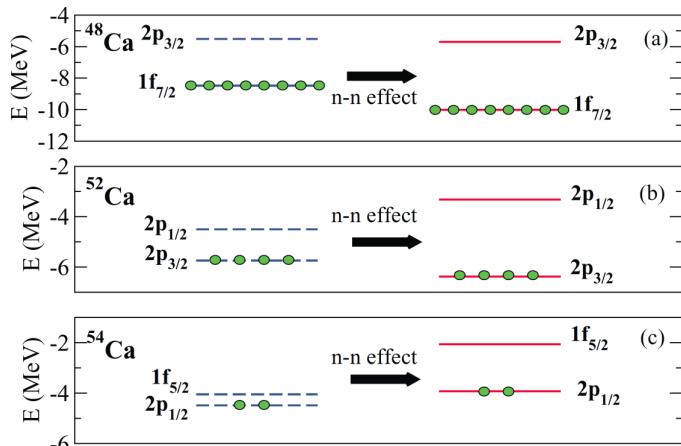


# New doubly magic Ca isotopes?

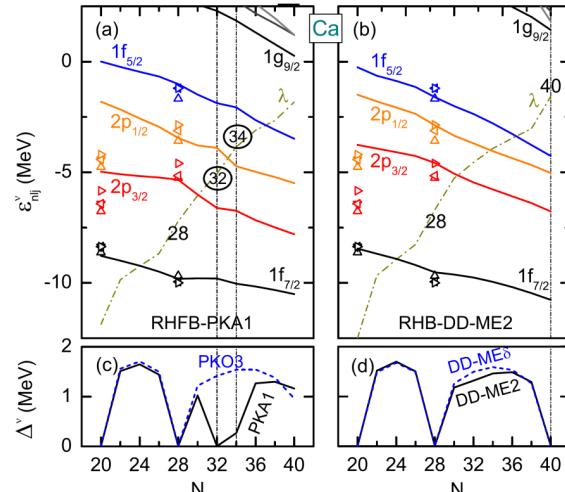
Steffenbeck+2013  
Nature 502-207



Grasso2014\_PRC89-034316

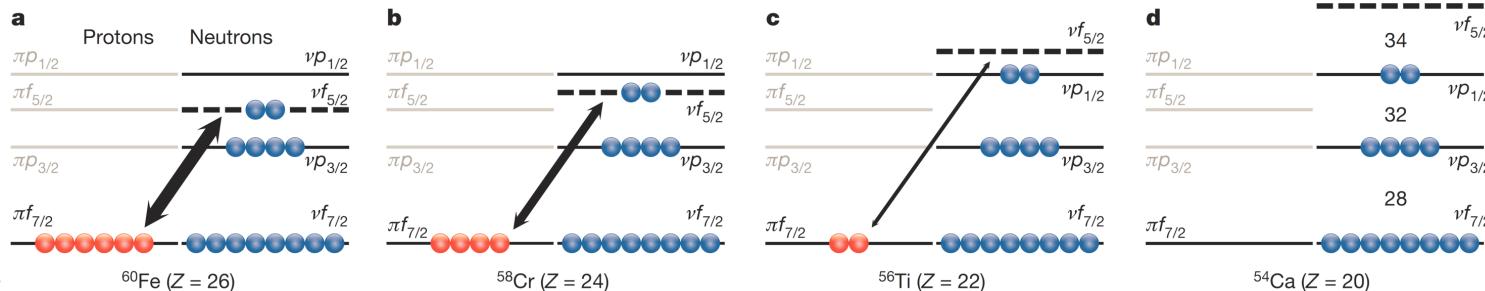
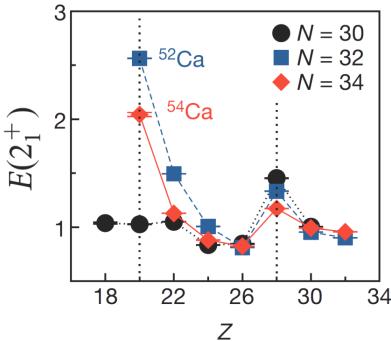


Li+2016 PLB753-97

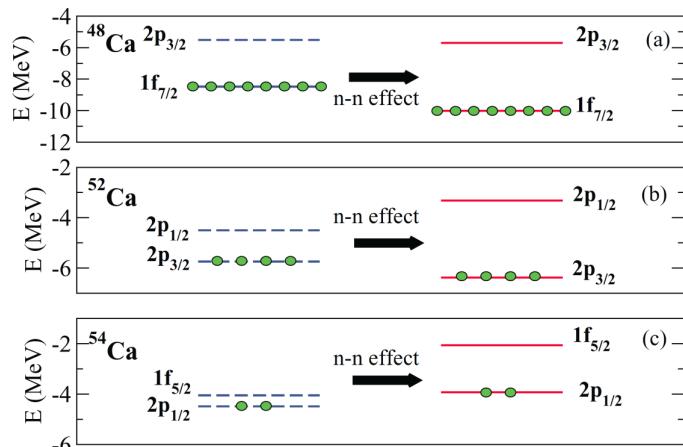


# New doubly magic Ca isotopes?

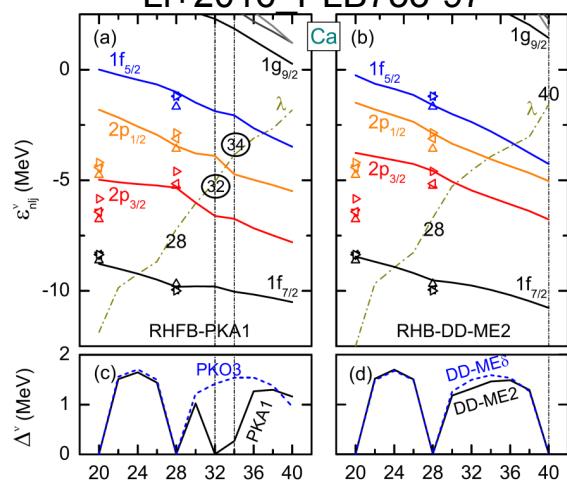
Steppenbeck+2013  
Nature 502-207



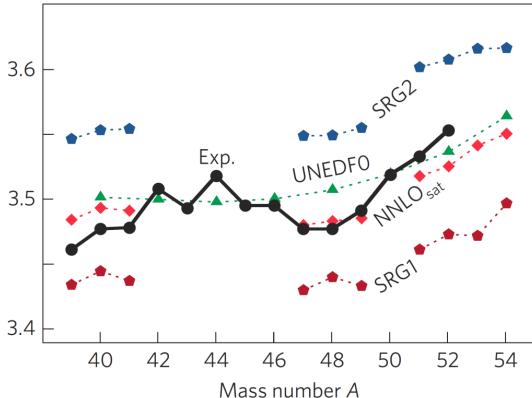
Grasso2014\_PRC89-034316



Li+2016 PLB753-97

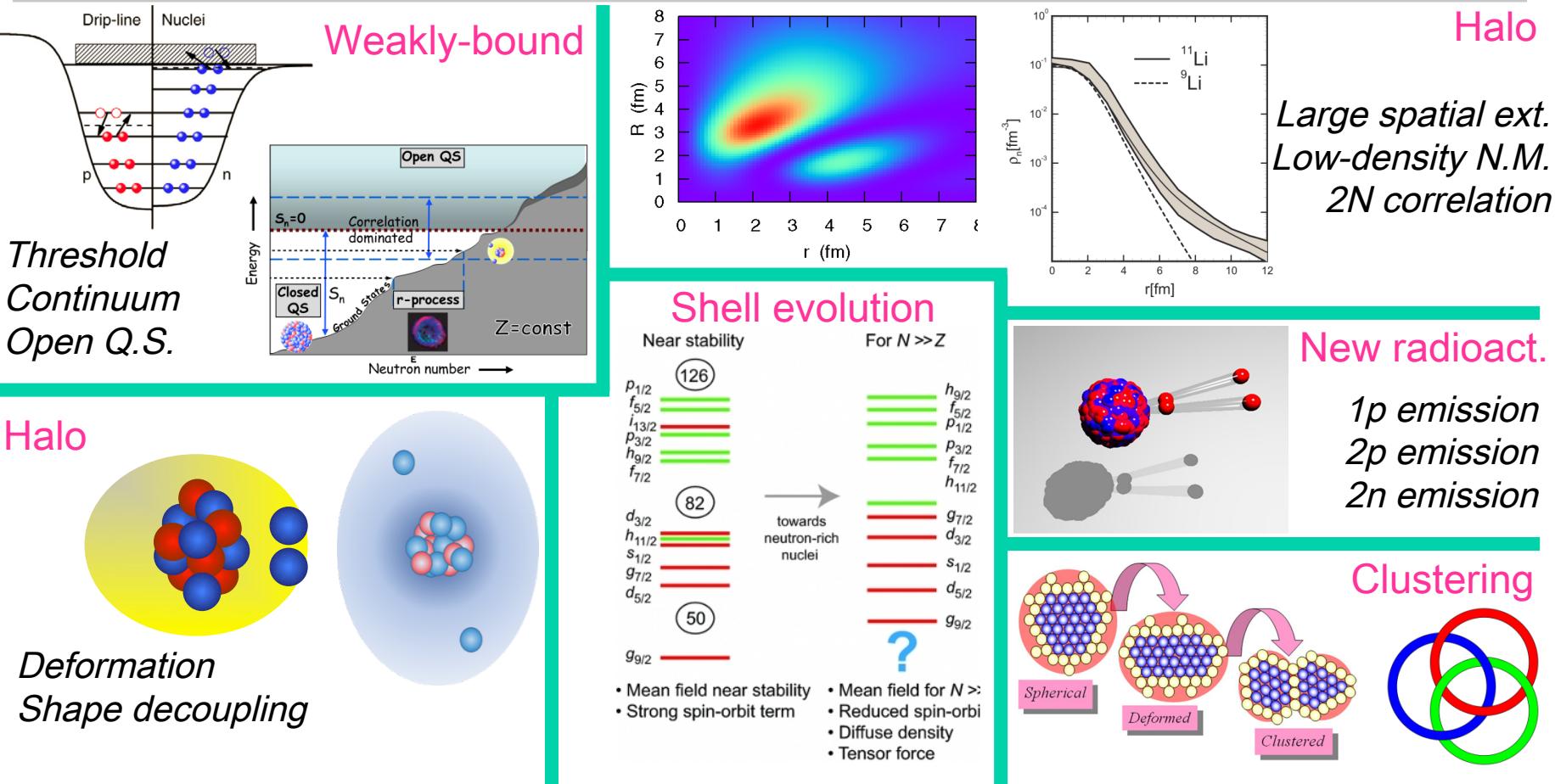


GarciaRuiz+2016NatPhys12-594



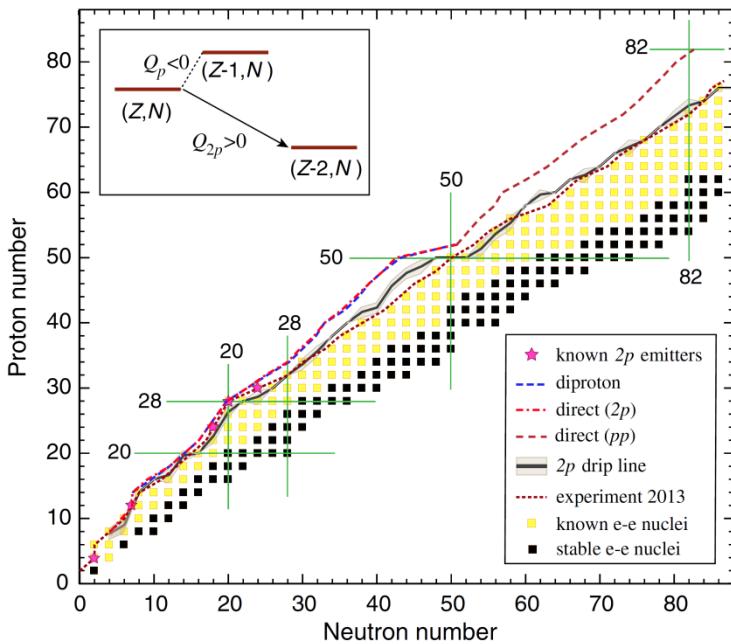
Nazarewicz & Eksröm's talks

# Physics of exotic nuclei



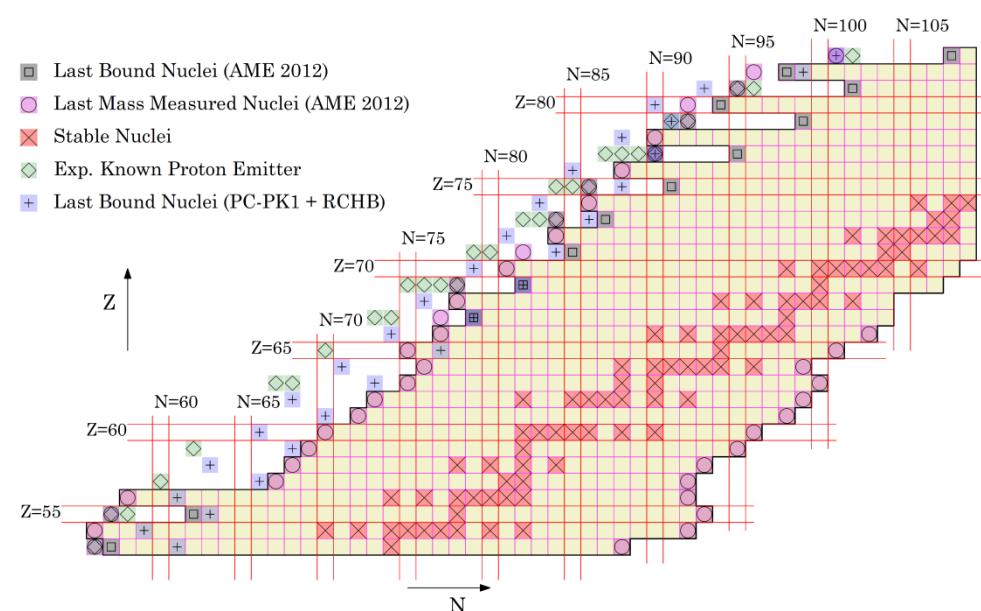
# Study of 2p emitters with DFT

## Hartree-Fock-Bogoliubov model



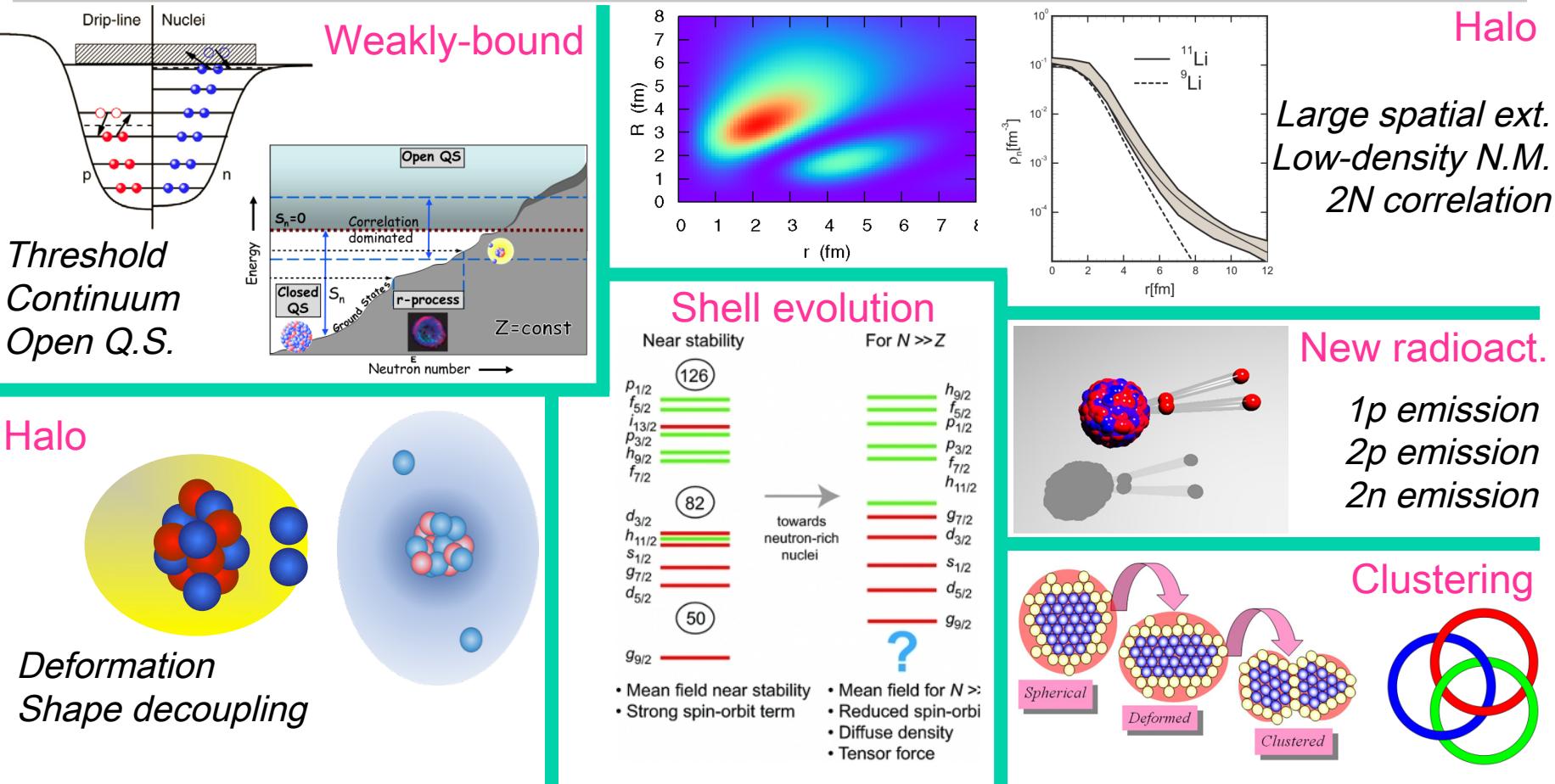
Olsen+2013\_PRL110-222501  
PRL111-139903E

## Relativistic cont. Hartree Bogoliubov model



Lim\_Xia\_Kim2016\_PRC93-014314

# Physics of exotic nuclei



# Clustering phenomena in nuclei

PRL 110, 262501 (2013)

PHYSICAL REVIEW LETTERS

week ending  
28 JUNE 2013

Zhou+2013\_PRL111-103604

## Nonlocalized Clustering: A New Concept in Nuclear Cluster Structure Physics

Bo Zhou,<sup>1,2,3,\*</sup> Y. Funaki,<sup>3,†</sup> H. Horiuchi,<sup>2,4</sup> Zhongzhou Ren,<sup>1,5,‡</sup> G. Röpke,<sup>6</sup> P. Schuck,<sup>7,8</sup> A. Tohsaki,<sup>2</sup> Chang Xu,<sup>1</sup> and T. Yamada<sup>9</sup>

PRL 113, 032506 (2014)

PHYSICAL REVIEW LETTERS

week ending  
18 JULY 2014

Cluster model  
Container picture

## Giant Dipole Resonance as a Fingerprint of $\alpha$ Clustering Configurations in $^{12}\text{C}$ and $^{16}\text{O}$

W. B. He (何万兵),<sup>1,2</sup> Y. G. Ma (马余刚),<sup>1,3,\*</sup> X. G. Cao (曹喜光),<sup>1,†</sup> X. Z. Cai (蔡翔舟),<sup>1</sup> and G. Q. Zhang (张国强)<sup>1</sup>

PRL 115, 022501 (2015)

PHYSICAL REVIEW LETTERS

week ending  
10 JULY 2015

QMD model  
GDR connected  
to clustering

## Rod-shaped Nuclei at Extreme Spin and Isospin

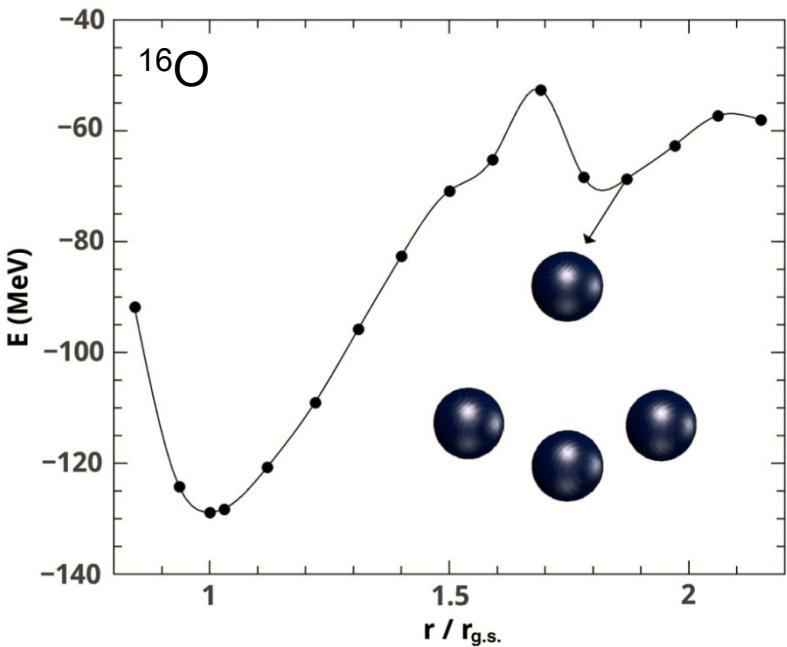
P. W. Zhao (赵鹏巍),<sup>1,2,3</sup> N. Itagaki (板垣直之),<sup>1</sup> and J. Meng (孟杰)<sup>3,4,5,\*</sup>

Zhao\_Itagaki\_Meng2015  
PRL115-022501

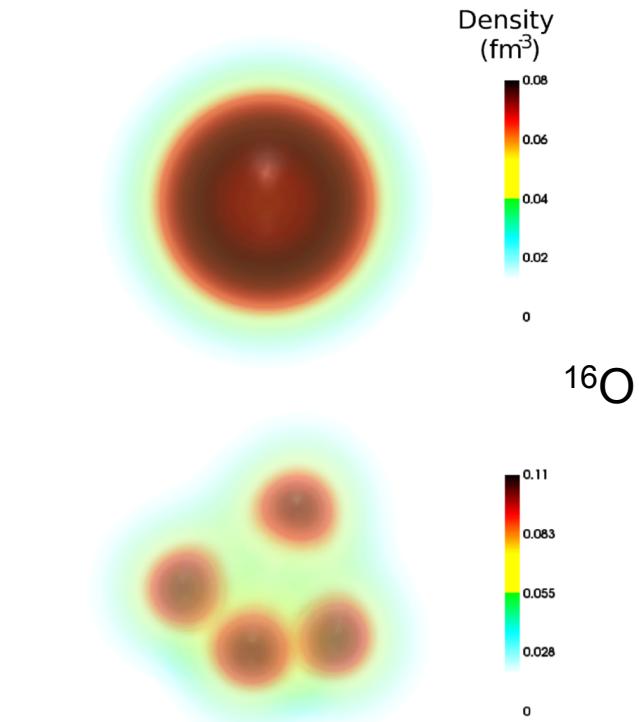
Cranking RMF model  
Clustering at extreme  
spin & isospin

# Constrained Cluster Structure

Hartree-Fock model



Relativistic mean field model

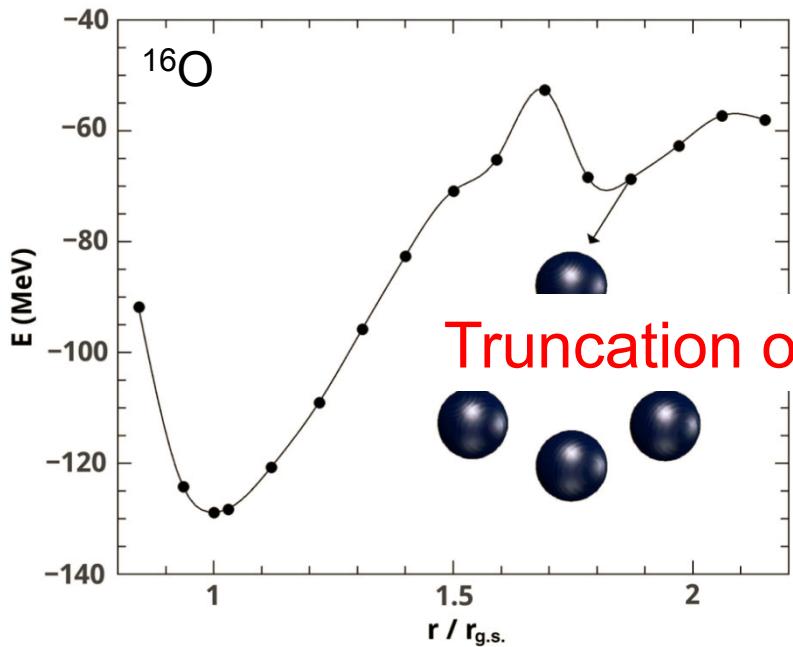


Girod\_Schuck2013\_PRL111-132503

Ebran\_Khan\_Niksic\_Vretenar2012\_Nature487-341  
2014\_PRC89-031303R

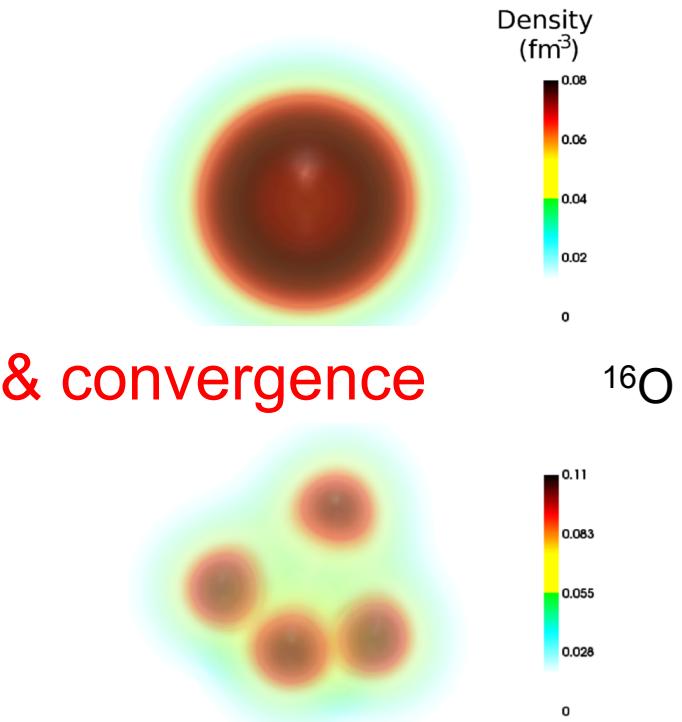
# Constrained Cluster Structure

Hartree-Fock model



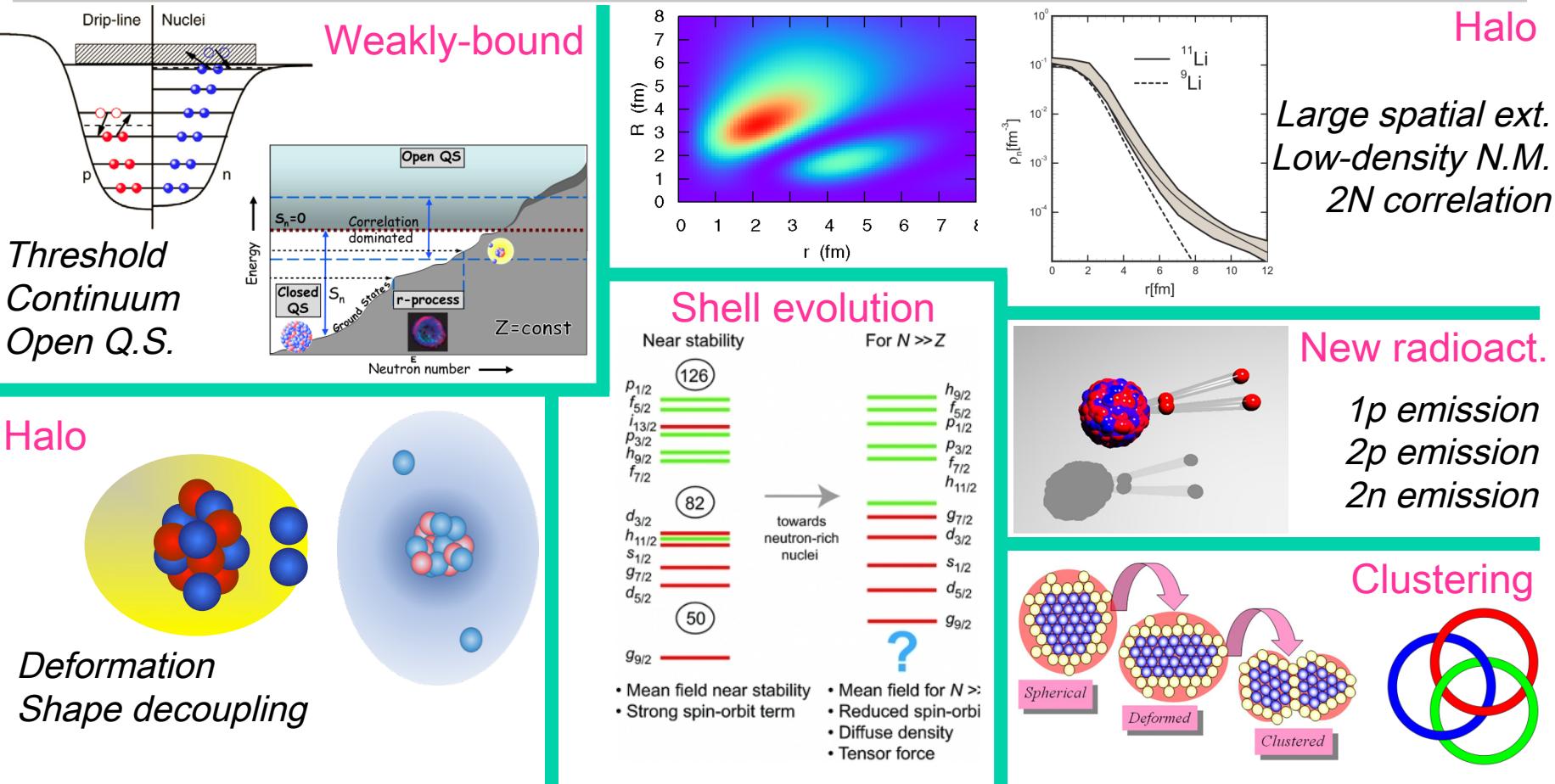
Girod\_Schuck2013\_PRL111-132503

Relativistic mean field model



Ebran\_Khan\_Niksic\_Vretenar2012\_Nature487-341  
2014\_PRC89-031303R

# Physics of exotic nuclei



# Model, models, models's, ...

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(INPC1995, Beijing)

Krishna Kumar:

We

not only

use different models to  
describe different nuclei,

but also

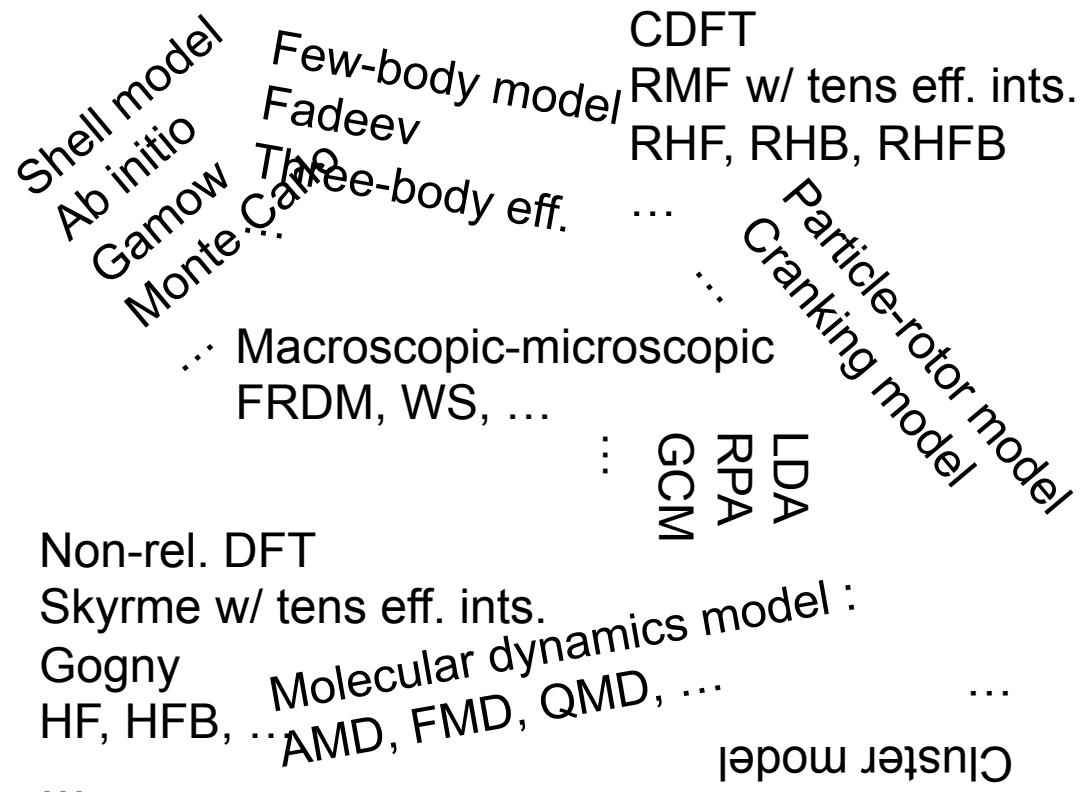
use different models to  
describe the same nucleus !

# Model, models, models's, ...

(INPC1995, Beijing)

Krishna Kumar:

We  
not only  
**use different models to  
describe different nuclei,**  
but also  
**use different models to  
describe the same nucleus !**



# Efforts to unify models & work more together

---

- Ab initio Ekström & Bacca's talks
- Density functional theories
  - Skyrme(-like): Ab initio derivation of model energy density functionals  
Dobaczewski et al., see, e.g., Dobaczewski2016\_JPG43-04LT01
  - Covariant: Toward an ab initio covariant investigations of heavy nuclei  
Meng et al., see, e.g., Shen+2016\_arXiv1609.01866; Liang's talk
- ...

# Efforts to unify models & work more together

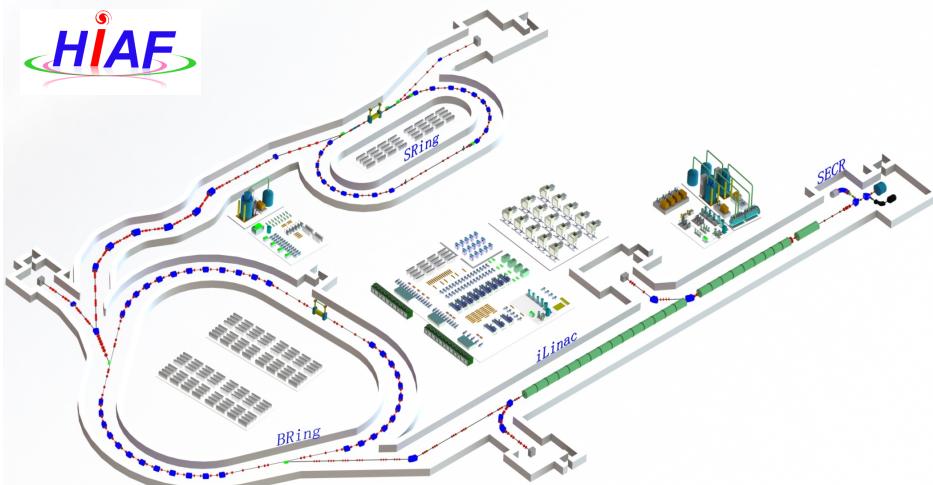
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- ...
- China-US Theory Inst. Phys. Exotic Nuclei (CUSTIPEN)
- DFG-NSFC Collaborative Research Centre (CRC110)
- ...

# Two future RIB facilities in China

HIAF, Lanzhou-Huizhou

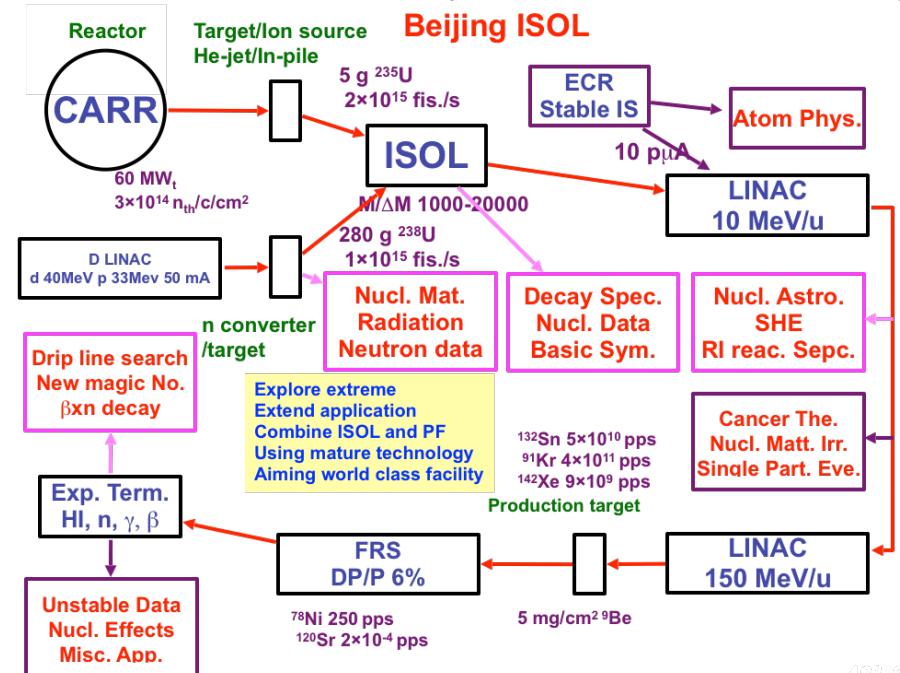
(High Intensity heavy-ion Accelerator Facility)



Phase 1: 2016-2023?

Courtesy of Xiao-Hong Zhou (周小红)

Beijing ISOL, CIAE-PKU  
Proposed & successfully evaluated future facility



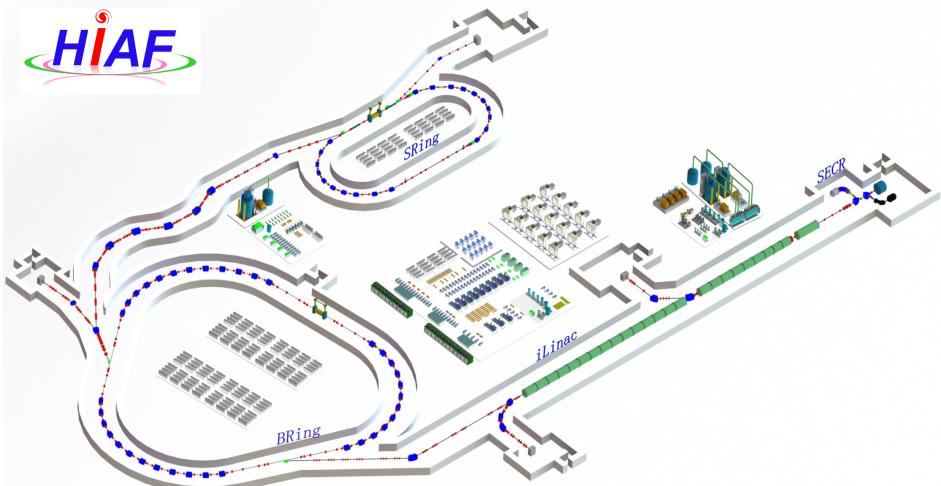
Courtesy of Wei-Ping Liu (柳卫平) & Yanlin Ye (叶沿林)

# Two future RIB facilities in China

THANK YOU !

HIAF, Lanzhou-Huizhou

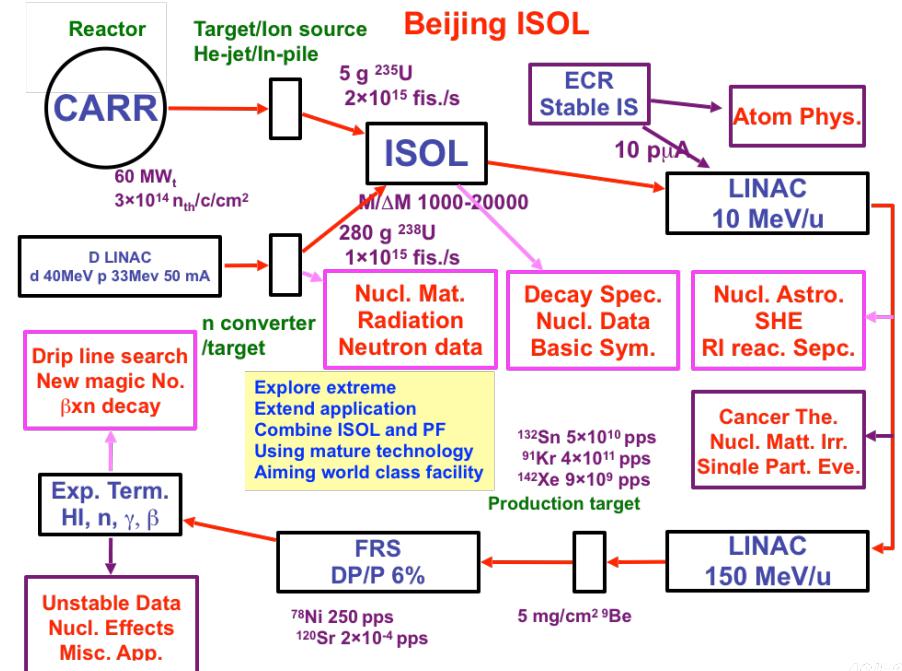
(High Intensity heavy-ion Accelerator Facility)



Phase 1: 2016-2023?

Courtesy of Xiao-Hong Zhou (周小红)

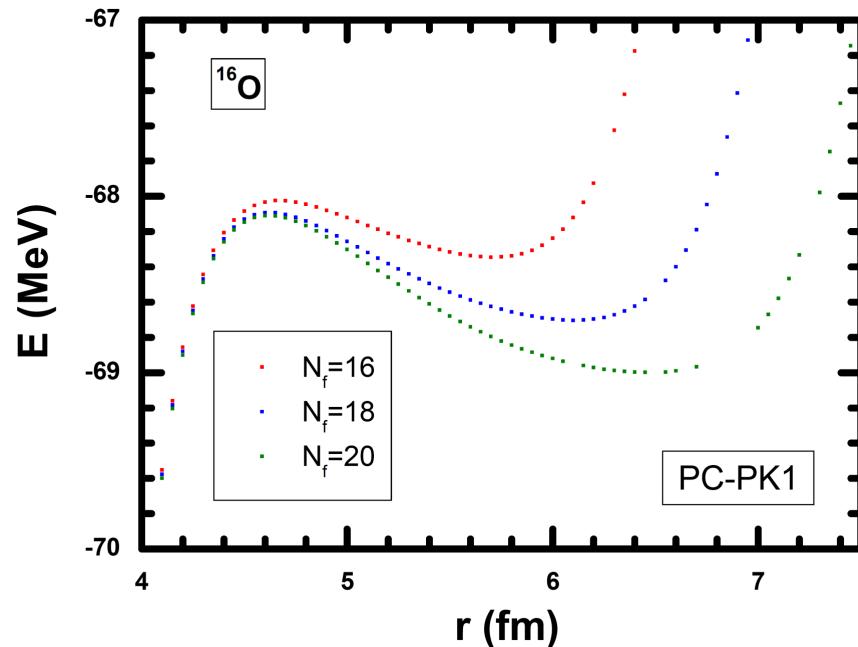
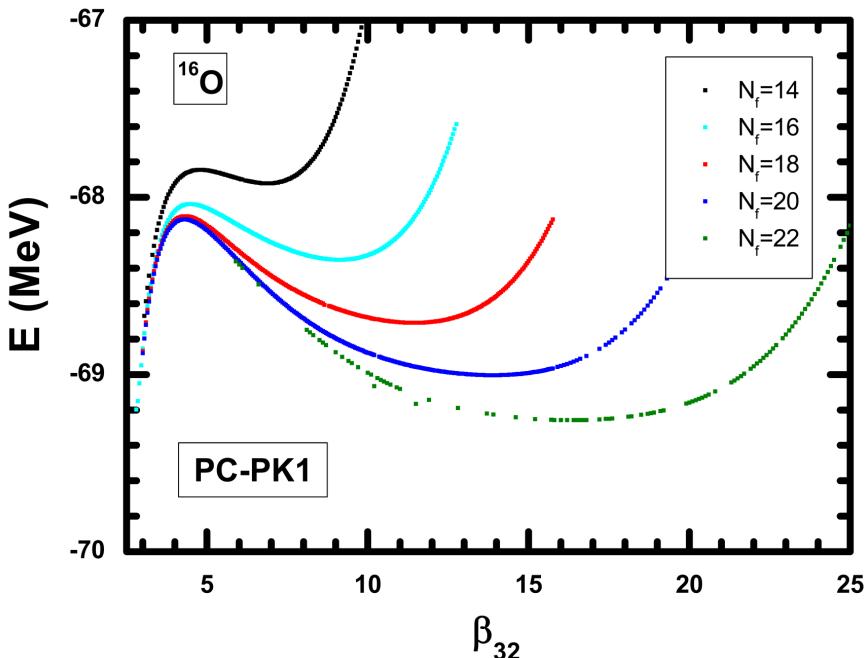
Beijing ISOL, CIAE-PKU  
Proposed & successfully evaluated future facility



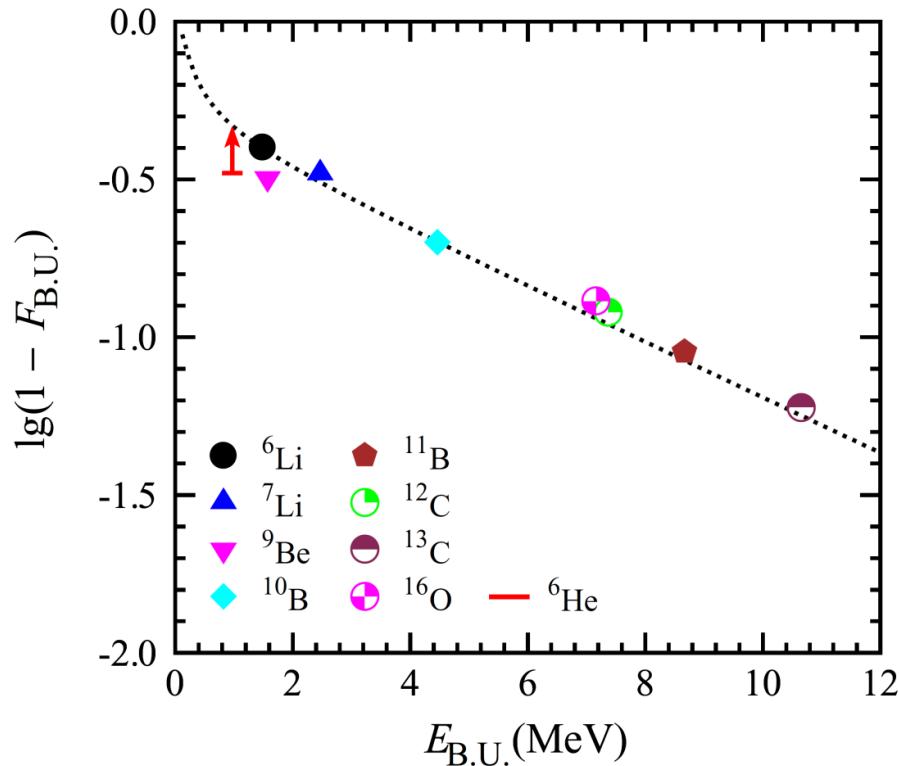
Courtesy of Wei-Ping Liu (柳卫平) & Yanlin Ye (叶沿林)

# Constraint Cluster Structure: Convergence?

Calc. w/ multidimensionally-constrained covariant density functional (MDC-CDFT) theory

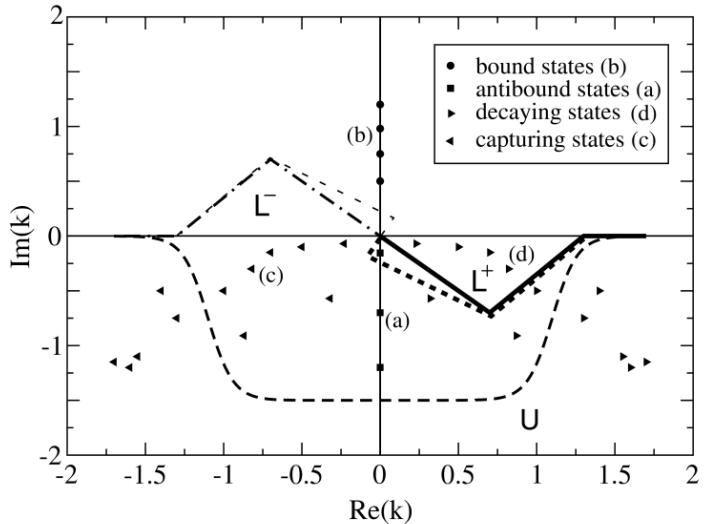


# Threshold effects: Breakup effects on CF



Wang\_Zhao\_Gomes\_Zhao\_SGZ2014\_PRC90-034612  
Wang\_Zhao\_Diaz-Torres\_Zhao\_SGZ2016\_PRC93-014615

# Weakly bound: Continuum Shell Model

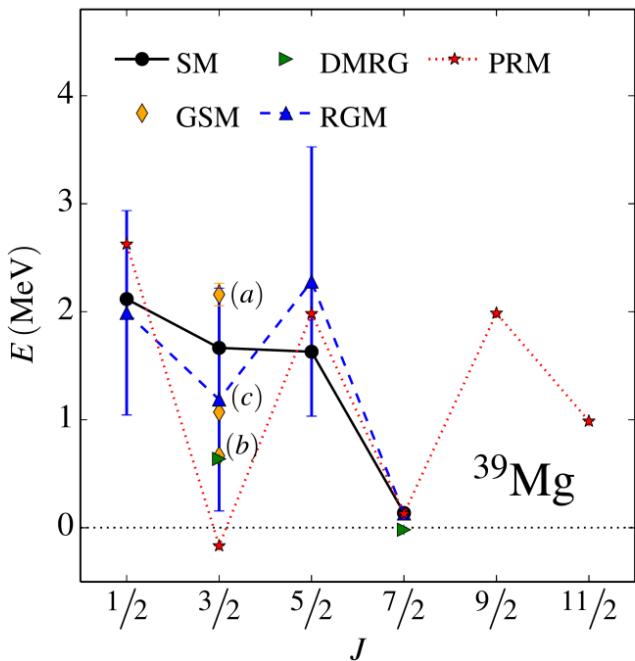


Berggren completeness relation

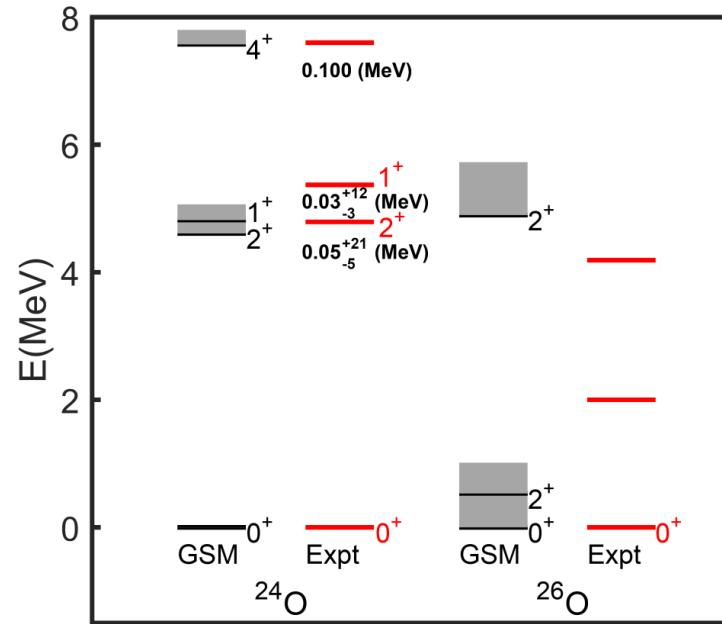
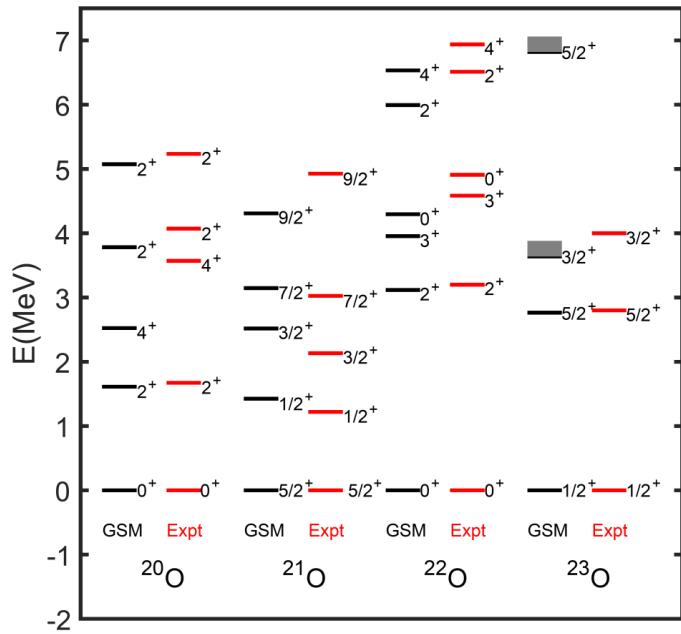
$$\sum_n u_n(E_n, r) u_n(E_n, r') + \int_L dE u(E, r) u(E, r') = \delta(r - r'),$$

Okolowicz\_Ploszajczak\_Rotter2003\_PR374-271  
Michel+2009\_JPG36-013101

Fossez+2016\_arXiv1607.08439



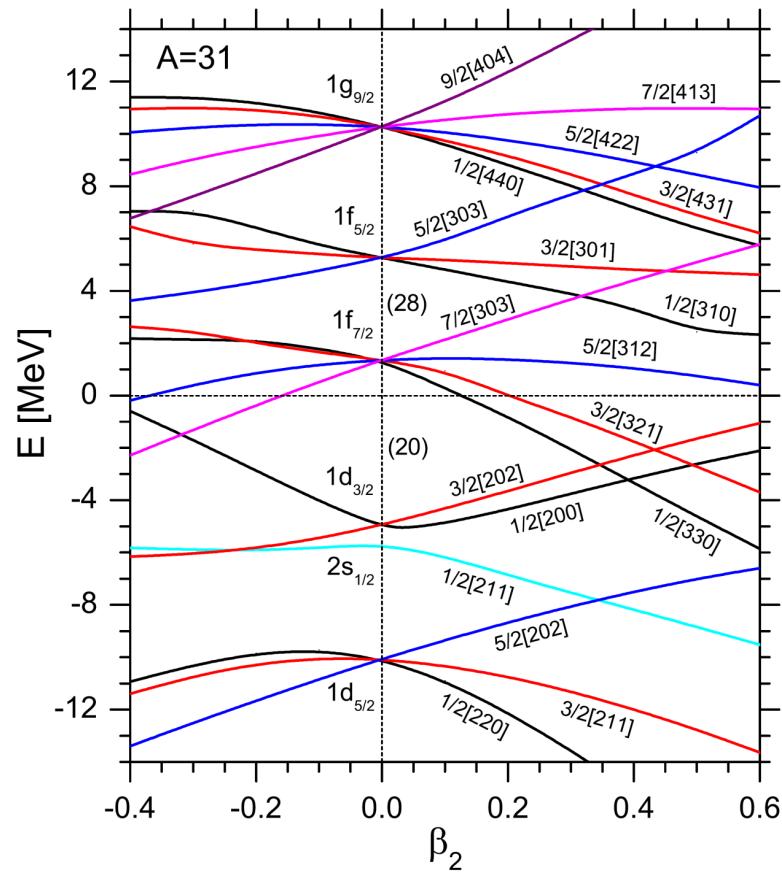
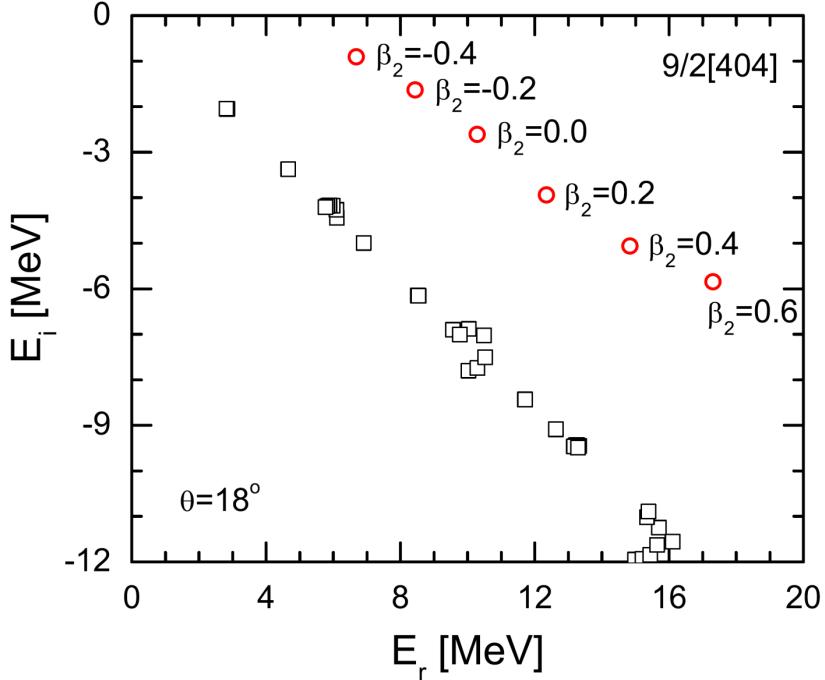
# Oxygen isotopes: Gamow Shell Model



Zhong-Hao Sun, PhD Thesis

# Nilsson Diagram w/ Resonances from CSM

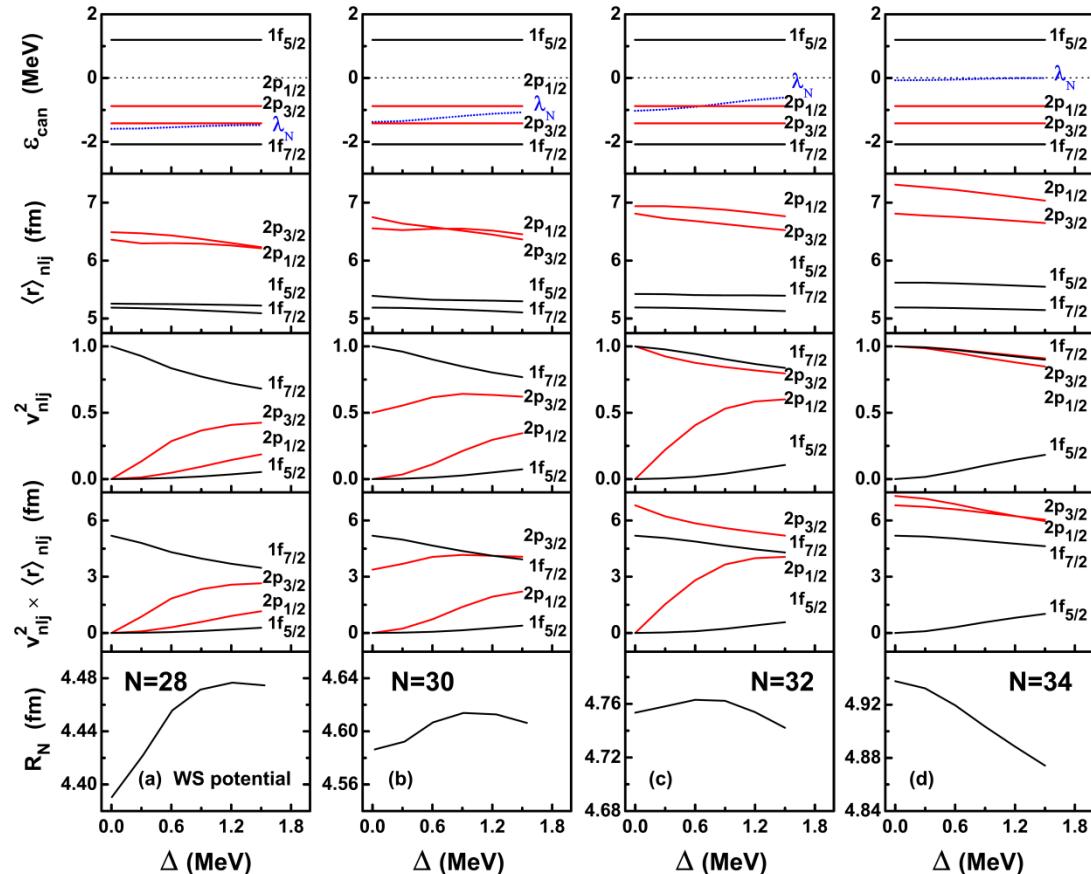
Shi\_Liu\_Niu\_Guo2014\_PRC90-034319



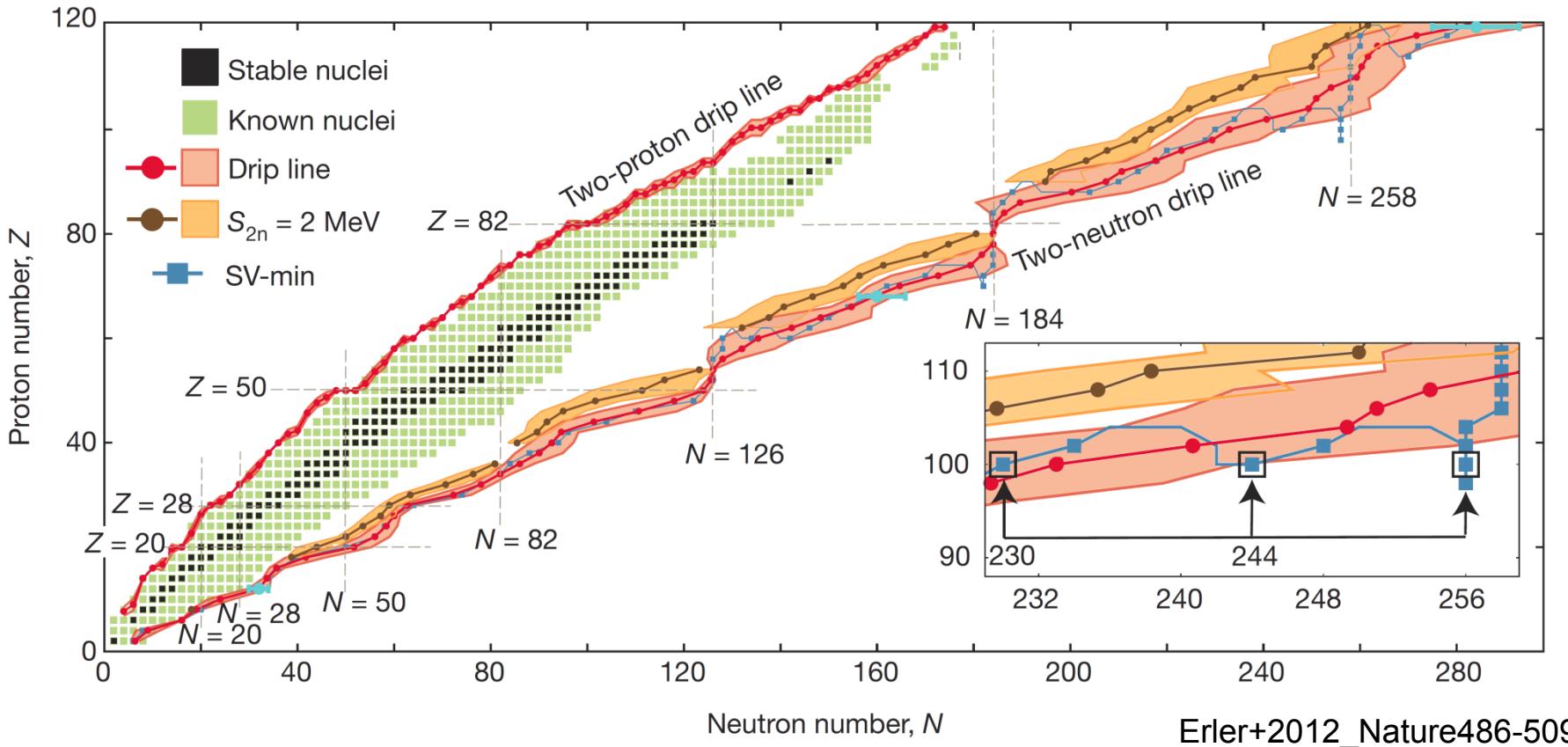
# Pairing Anti-Halo Effect ?

Chen\_Ring\_Meng2014  
PRC89-014312

Pairing correlations have a two-fold influence on the density distribution of the neutrons and therefore on the total nuclear size. First, they can change the root-mean-square radius of the individual weakly bound orbits and, second, they can change the occupation probabilities of these orbits in the nuclear system. Both effects are important, and finally the total radius is dominated by their competition.



# Uncertainties in Predicted Drip Lines



# $^{31}\text{Ne}$

## □ Spherical models

- Ren et al.: DDRMF      [Ren\\_Chen\\_Ma\\_Xu2001\\_CTP35-717](#)
- Zhang et al.: RMF+ACCC+BCS

Zhang\_Smith\_Kang\_Zhao2014\_PLB730-30

## □ Deformed models

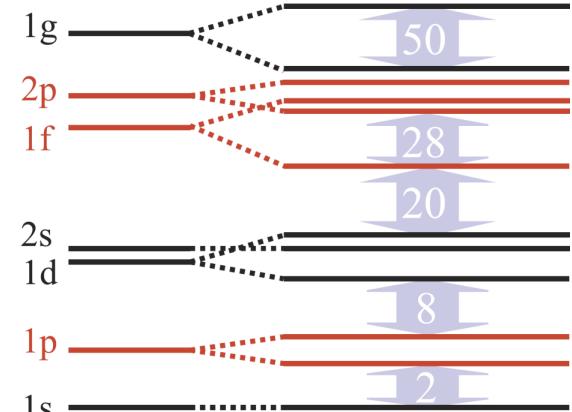
- Qiu & Zhou: deformed Skyrme HF+BCS, tensor

[Qiu\\_Zhou2014\\_CTP61-101](#)

## □ Experiment

- Nakamura et al.: Deformation-driven p-wave halos at the drip-line:  $^{31}\text{Ne}$

[Nakamura ... 2014\\_PRL112-142501](#)



[Liang\\_Meng\\_SGZ2015PhysRep](#)

# Tetraneutron state ? ! ?... !

PRL 116, 052501 (2016)

Selected for a Viewpoint in Physics  
PHYSICAL REVIEW LETTERS

Kisamori...2016\_PRL116-052501  
week ending  
5 FEBRUARY 2016

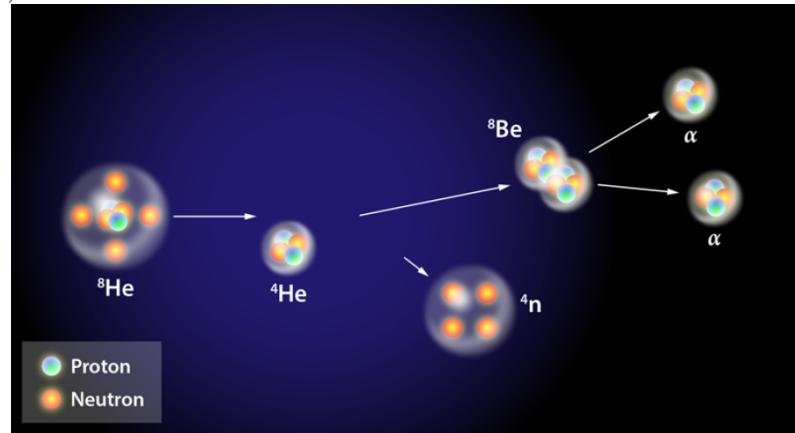


## Candidate Resonant Tetraneutron State Populated by the ${}^4\text{He}({}^8\text{He}, {}^8\text{Be})$ Reaction

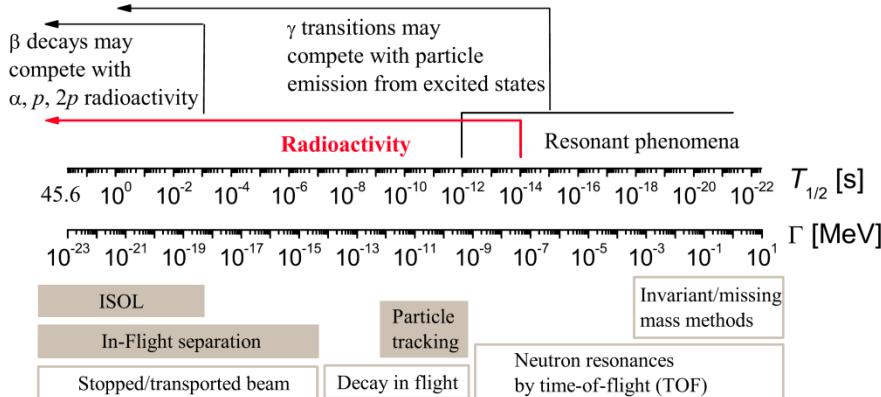
K. Kisamori,<sup>1,2</sup> S. Shimoura,<sup>1</sup> H. Miya,<sup>1,2</sup> S. Michimasa,<sup>1</sup> S. Ota,<sup>1</sup> M. Assie,<sup>3</sup> H. Baba,<sup>2</sup> T. Baba,<sup>4</sup> D. Beaumel,<sup>2,3</sup> M. Dozono,<sup>2</sup> T. Fujii,<sup>1,2</sup> N. Fukuda,<sup>2</sup> S. Go,<sup>1,2</sup> F. Hammache,<sup>3</sup> E. Ideguchi,<sup>5</sup> N. Inabe,<sup>2</sup> M. Itoh,<sup>6</sup> D. Kameda,<sup>2</sup> S. Kawase,<sup>1</sup> T. Kawabata,<sup>4</sup> M. Kobayashi,<sup>1</sup> Y. Kondo,<sup>7,2</sup> T. Kubo,<sup>2</sup> Y. Kubota,<sup>1,2</sup> M. Kurata-Nishimura,<sup>2</sup> C. S. Lee,<sup>1,2</sup> Y. Maeda,<sup>8</sup> H. Matsubara,<sup>12</sup> K. Miki,<sup>5</sup> T. Nishi,<sup>9,2</sup> S. Noji,<sup>10</sup> S. Sakaguchi,<sup>11,2</sup> H. Sakai,<sup>2</sup> Y. Sasamoto,<sup>1</sup> M. Sasano,<sup>2</sup> H. Sato,<sup>2</sup> Y. Shimizu,<sup>2</sup> A. Stoltz,<sup>10</sup> H. Suzuki,<sup>2</sup> M. Takaki,<sup>1</sup> H. Takeda,<sup>2</sup> S. Takeuchi,<sup>2</sup> A. Tamii,<sup>5</sup> L. Tang,<sup>1</sup> H. Tokieda,<sup>1</sup> M. Tsumura,<sup>4</sup> T. Uesaka,<sup>2</sup> K. Yako,<sup>1</sup> Y. Yanagisawa,<sup>2</sup> R. Yokoyama,<sup>1</sup> and K. Yoshida<sup>2</sup>

Orr2016\_Physics9-14

$$E = 0.83 \pm 0.65(\text{stat.}) \pm 1.25(\text{syst.}) \text{ MeV}$$



# Nuclear Radioactivities



Pfutzner\_Karny\_Grigorenko\_Riisager  
2012\_RMP84-567

TABLE VI. Ground-state  $2p$  emitters investigated experimentally. The indicated half-life corresponds to the partial value for the  $2p$  decay.

${}^N_Z$	$E$ (keV)	$\Gamma$ or $T_{1/2}$	Reference
${}^6\text{Be}$	1371(5)	92(6) keV	Whaling (1966)
${}^{12}\text{O}$	1820(120)	400(250) <sup>a</sup> keV	KeKelis <i>et al.</i> (1978)
	1790(40)	580(200) <sup>a</sup> keV	Kryger <i>et al.</i> (1995)
	1800(400)	600(500) <sup>a</sup> keV	Suzuki <i>et al.</i> (2009)
	1350(80)	200(100) <sup>a</sup> keV	KeKelis <i>et al.</i> (1978)
${}^{16}\text{Ne}$	1400(20)	110(40) <sup>a</sup> keV	Woodward, Tribble, and Tanner (1983)
	1350(80)	<200 keV	Mukha <i>et al.</i> (2008b)
${}^{19}\text{Mg}$	750(50)	4.0(15) ps	Mukha <i>et al.</i> (2007)
	1100(100)	$4.0^{+3.3}_{-1.8}$ ms	Pfützner <i>et al.</i> (2002)
	1140(50)	$8.5^{+6.4}_{-3.2}$ ms	Giovinazzo <i>et al.</i> (2002)
	1154(16)	$2.8^{+1.0}_{-0.7}$ ms	Dossat <i>et al.</i> (2005)
${}^{45}\text{Fe}$	3.7 $^{+0.4}_{-0.4}$ ms		Miernik <i>et al.</i> (2007c)
	1350(20)	$8.4^{+12.8}_{-7.0}$ ms <sup>b</sup>	Dossat <i>et al.</i> (2005)
		$3.0^{+2.2}_{-1.2}$ ms	Pomorski <i>et al.</i> (2011b)
${}^{48}\text{Ni}$	1480(20)	$3.7^{+2.2}_{-1.0}$ ms	Blank <i>et al.</i> (2005)
${}^{54}\text{Zn}$			

<sup>a</sup>According to theoretical calculations, much smaller widths are expected (Barker, 1999; Barker, 2001; Grigorenko *et al.*, 2002).

<sup>b</sup>Only one decay event observed.