

Role of Hexadecupole Deformation in the Shape Evolution of Neutron-rich Nd Isotopes

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Collaborators

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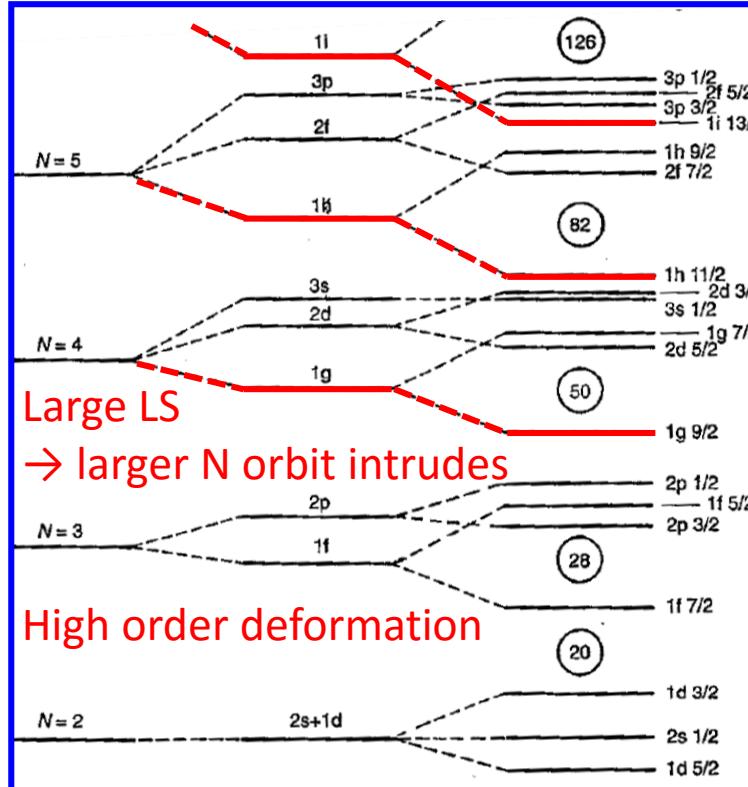
CNS, Univ. of Tokyo, ^ARCNP, Osaka Univ., ^BLPSC, ^CRIKEN, Nishina Center, ^DTohoku Univ., ^EUniv. of Tokyo, ^FUniv. of Brighton, ^GUniv. of Surrey, ^HYork Univ., ^IPeking Univ., ^JBeihang Univ., ^KUniv. of Oslo, ^LATOMKI, ^MUniv. of Madrid, ^NOsaka Univ., ^ORikkyo Univ., ^PTsukuba Univ., ^QHoseo Univ.





Shape of atomic nuclei

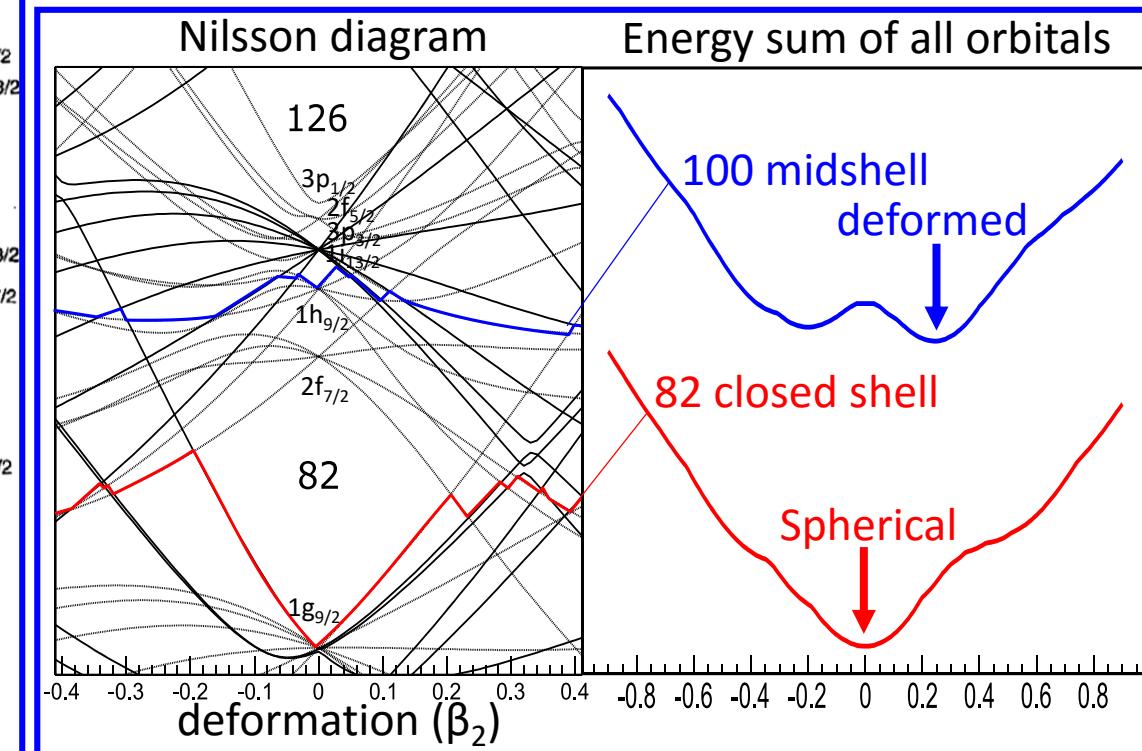
Atomic nuclei:
Finite quantum many-body system
→ shell effect
Shell effect drives macroscopic shape



$$R(\theta, \phi) = R_0 \{ 1 + \sum \alpha_{\lambda\mu} Y_{\lambda\mu}(\theta, \phi) \}$$

$\lambda = 2$ $\lambda = 3$ $\lambda = 4 \dots$

Quadrupole Octupole Hexadecupole





Experimental $E(2^+)$ on midshell nuclei

- $E(2^+)$ relates to deformation
- Lack of experimental data for neutron-rich midshell nuclei at $N \sim 100$, $Z \sim 60$

How does the shape evolve in (N, Z) plane?

Measurement of excited states

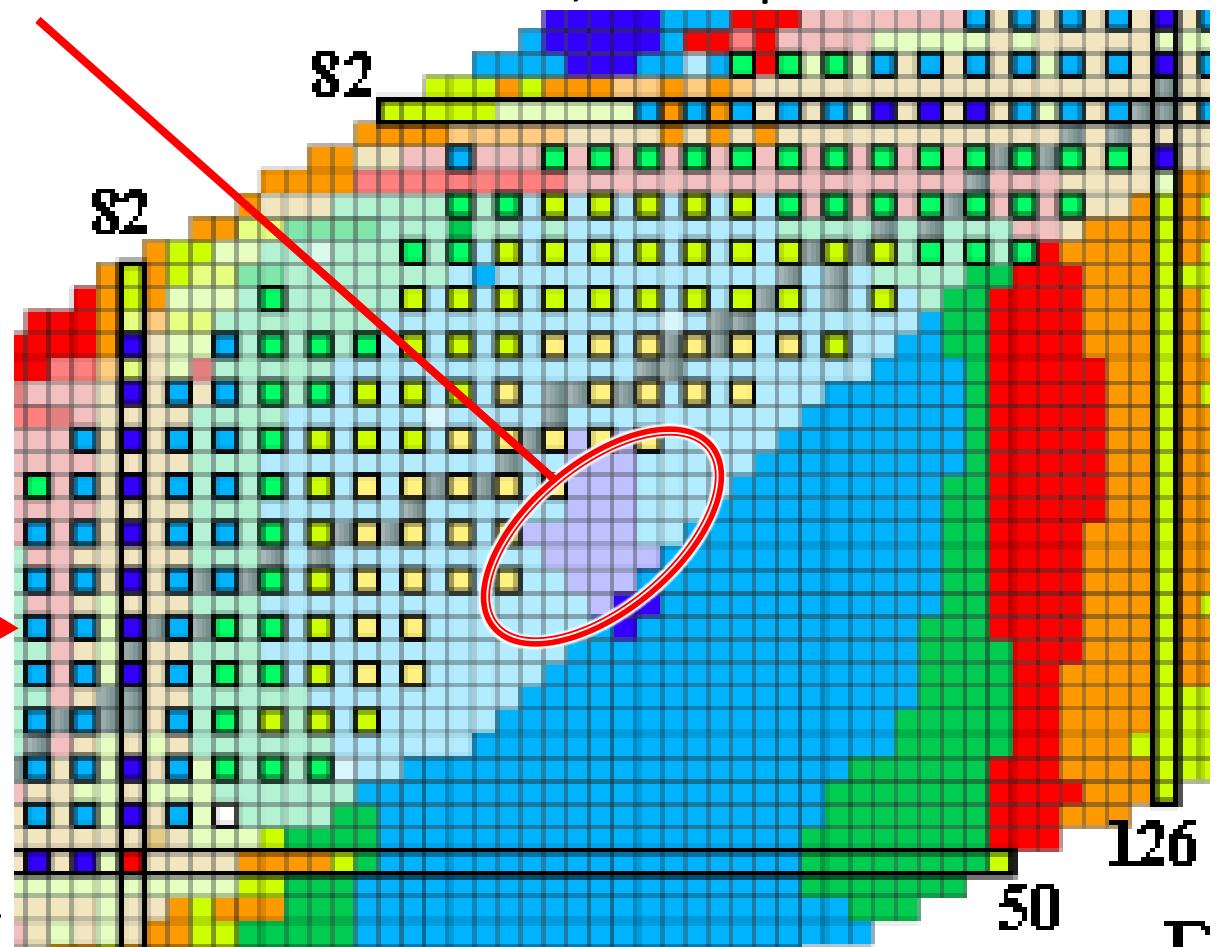
isomer & β - γ spectroscopy

$E(2^+)$ plotted over the theoretical chart →

Hexadecupole

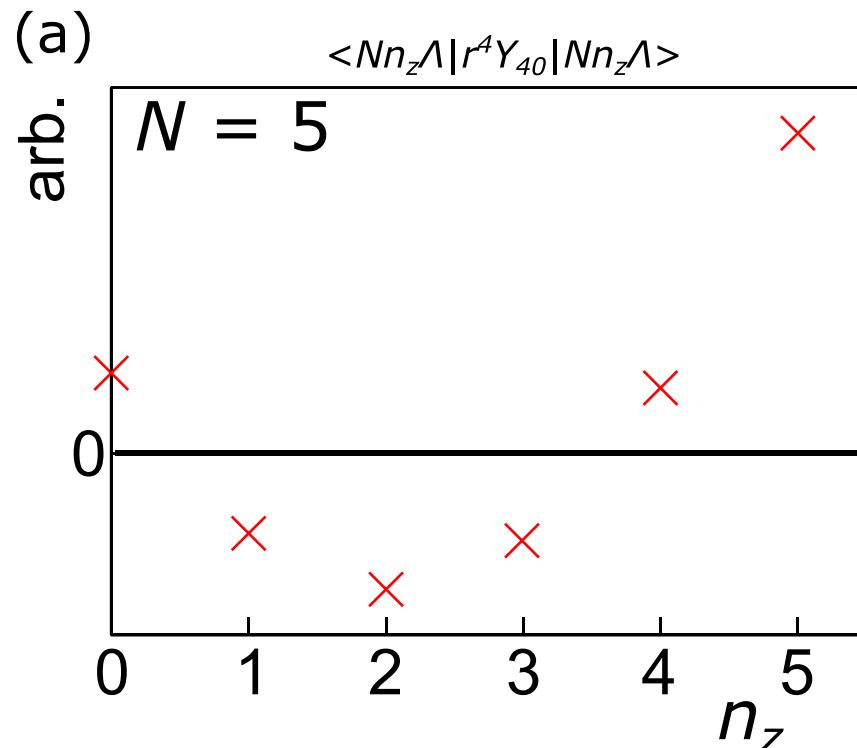
$Z = 60$

max. at $N \sim 102$, $Z \sim 64$ predicted



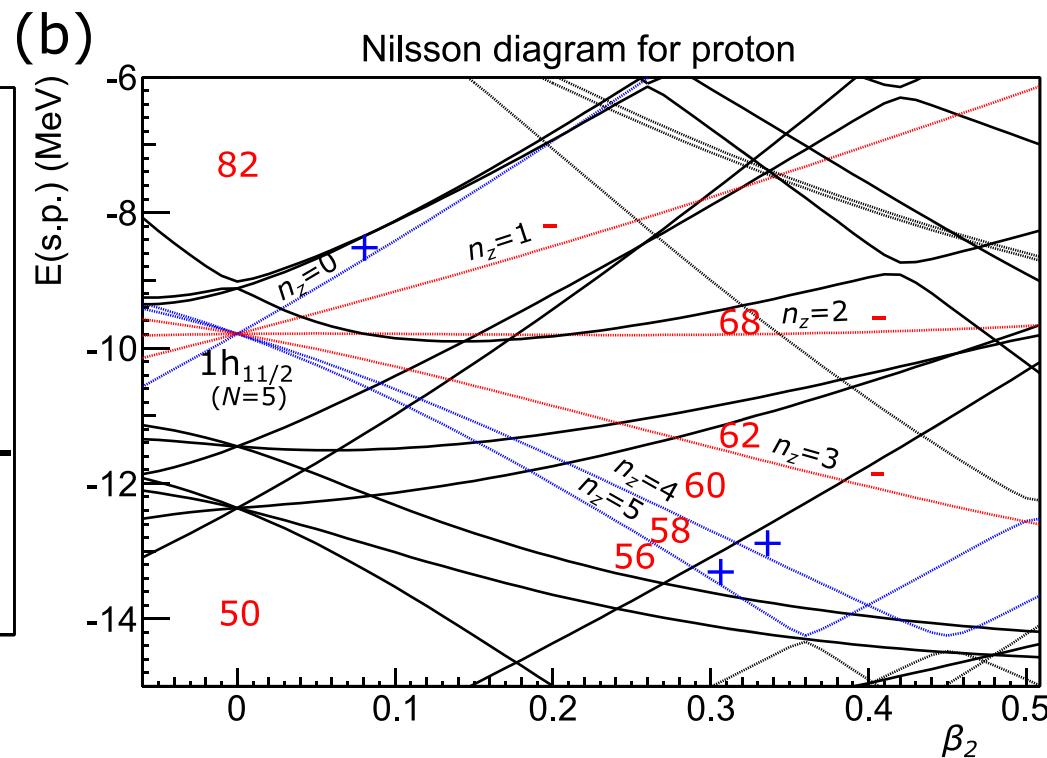
Hexadecupole deformation

$\langle Nn_z \Lambda | r^4 Y_{40} | Nn_z \Lambda \rangle$ for $1h_{11/2}$ orbitals with deformed HO.



- Large n_z are responsible

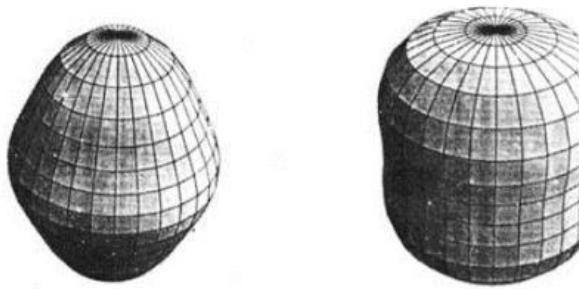
Nilsson diagram for proton with deformed WS.



- When $\beta_2 \sim 0.3$, $Z=60$ (N_d) will have large hexadecupole moment

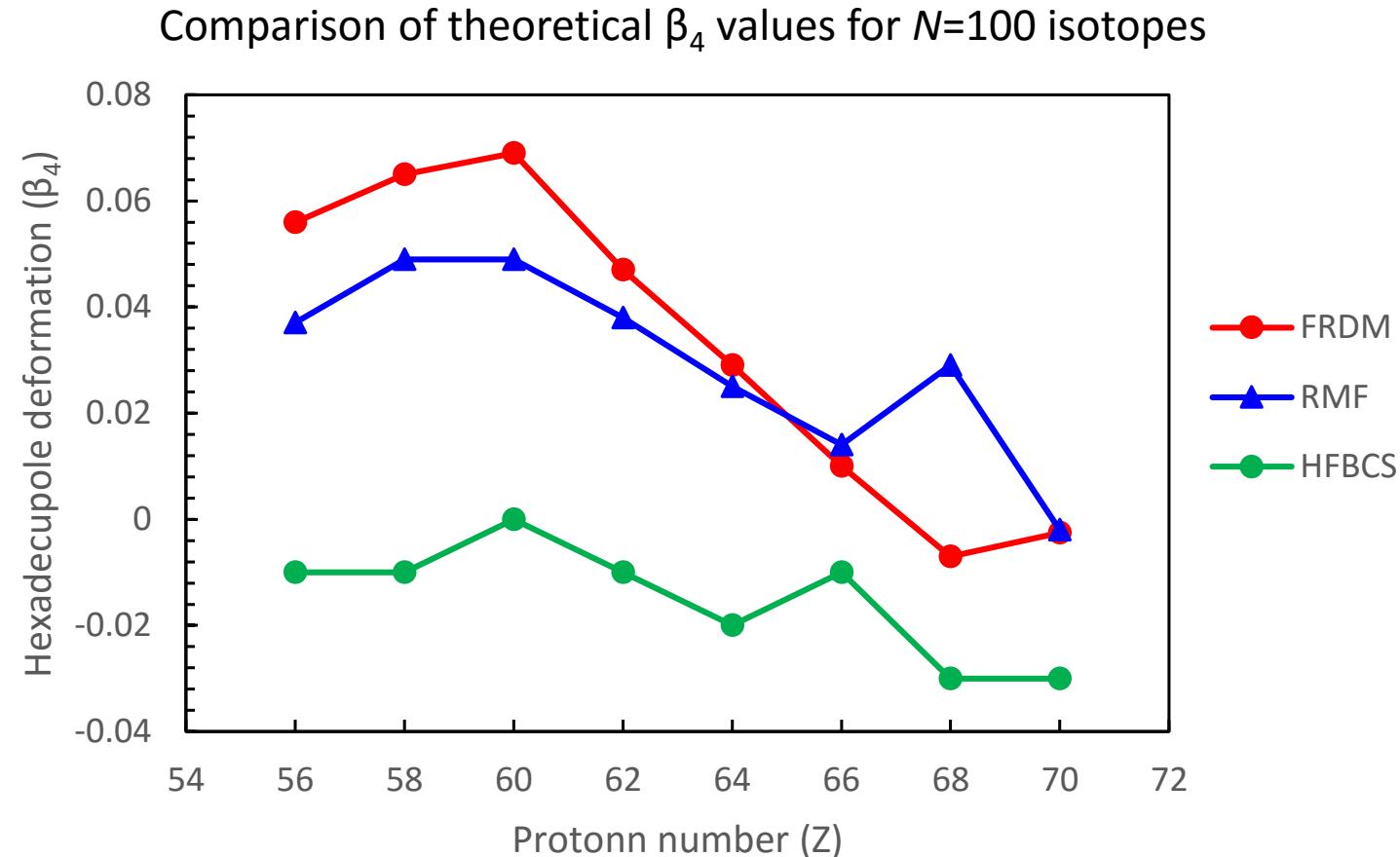


Hexadecupole deformation



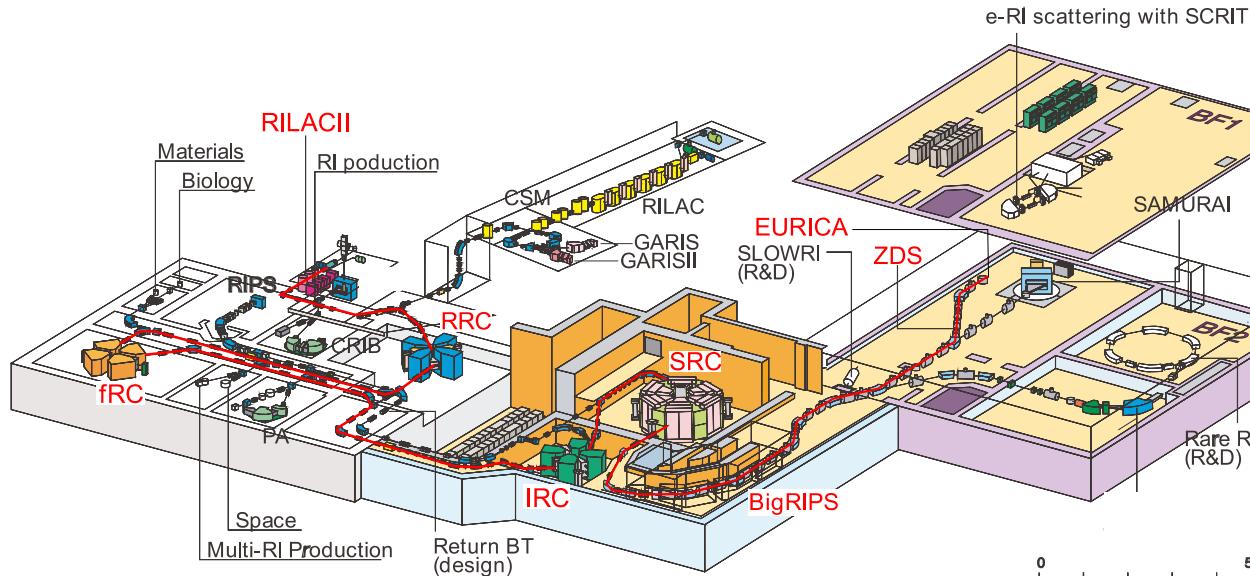
Quadrupole + Hexadecupole
(0.3,0,0.15) Quadrupole + Hexadecupole
(0.3,0,-0.15)

- B(E4) measurement by Coulomb excitation
 - ^{152}Sm : $\beta_4=0.06(3)$,
 - ^{148}Nd : $\beta_4=0.07(2)$
- No exp. data on unstable nuclide
- Theoretical predictions on unstable nuclei differ in theories
Experimental investigations are necessary

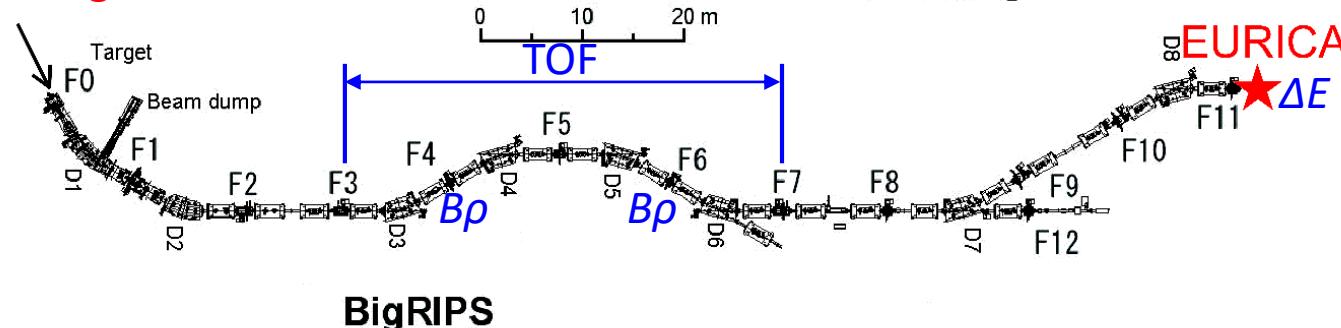




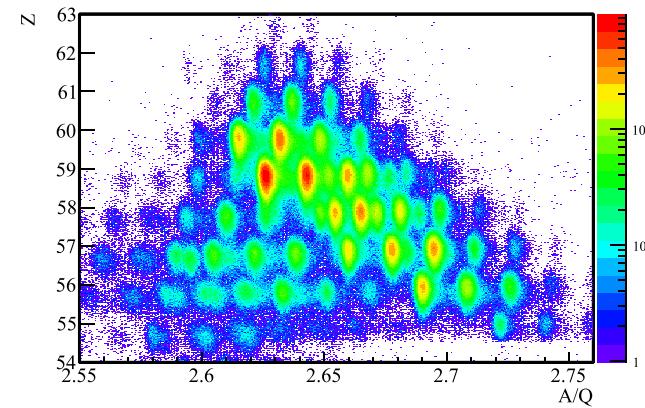
Production of neutron-rich nuclei at RIBF



Be target
in-flight fission



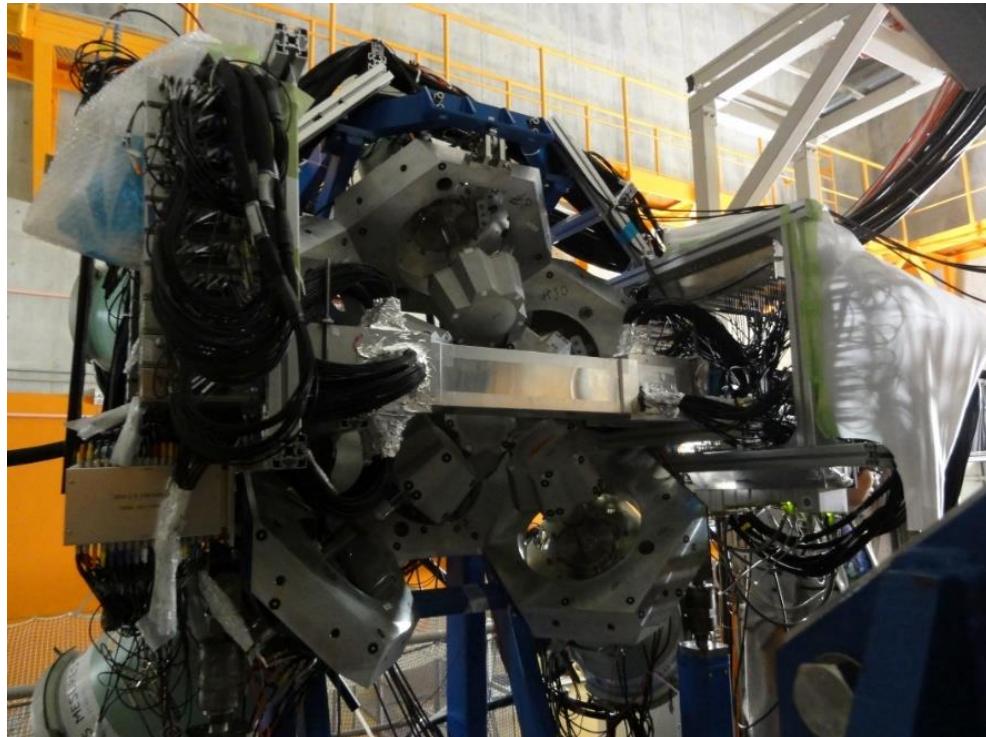
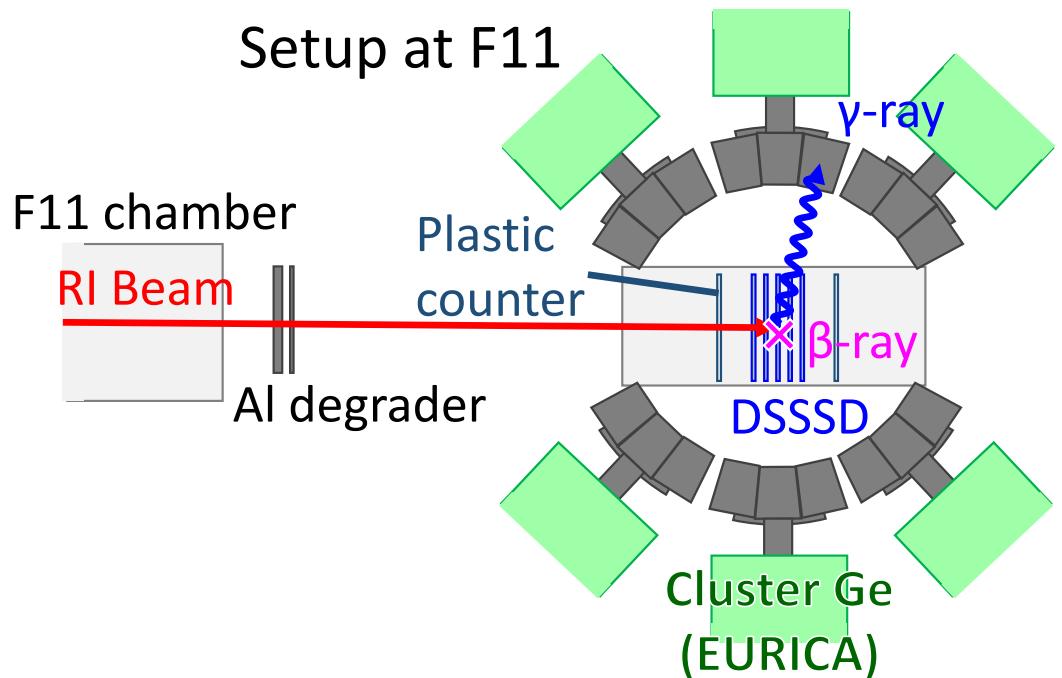
- 5 accelerators for 345 MeV/u ^{238}U beam
- Particle separation and identification at BigRIPS
- $B\bar{\rho}$ -TOF- ΔE method (event-by-event PI)



- transported to F11



Detector setups



- isomer and β - γ measurement
 - EURICA (Euroball Riken cluster array) with 84 Ge crystals
 - for γ -ray energies of isomer and β decay
 - WAS3ABi (Double sided Silicon strip detectors)
 - for position correlation between beam implantation and β -ray emission



Experimental results

Z:N	92	93	94	95	96	97	98	99	100	101	102	103	104	105
67	¹⁵⁹ Ho	¹⁶⁰ Ho	¹⁶¹ Ho	¹⁶² Ho	¹⁶³ Ho	¹⁶⁴ Ho	¹⁶⁵ Ho	¹⁶⁶ Ho	¹⁶⁷ Ho	¹⁶⁸ Ho	¹⁶⁹ Ho	¹⁷⁰ Ho	¹⁷¹ Ho	¹⁷² Ho
66	¹⁵⁸ Dy	¹⁵⁹ Dy	¹⁶⁰ Dy	¹⁶¹ Dy	¹⁶² Dy	¹⁶³ Dy	¹⁶⁴ Dy	¹⁶⁵ Dy	¹⁶⁶ Dy	¹⁶⁷ Dy	¹⁶⁸ Dy	¹⁶⁹ Dy	¹⁷⁰ Dy	¹⁷¹ Dy
65	¹⁵⁷ Tb	¹⁵⁸ Tb	¹⁵⁹ Tb	¹⁶⁰ Tb	¹⁶¹ Tb	¹⁶² Tb	¹⁶³ Tb	¹⁶⁴ Tb	¹⁶⁵ Tb	¹⁶⁶ Tb	¹⁶⁷ Tb	¹⁶⁸ Tb	¹⁶⁹ Tb	¹⁷⁰ Tb
64	¹⁵⁶ Gd	¹⁵⁷ Gd	¹⁵⁸ Gd	¹⁵⁹ Gd	¹⁶⁰ Gd	¹⁶¹ Gd	¹⁶² Gd	¹⁶³ Gd	¹⁶⁴ Gd	¹⁶⁵ Gd	¹⁶⁶ Gd	¹⁶⁷ Gd	¹⁶⁸ Gd	¹⁶⁹ Gd
63	¹⁵⁵ Eu	¹⁵⁶ Eu	¹⁵⁷ Eu	¹⁵⁸ Eu	¹⁵⁹ Eu	¹⁶⁰ Eu	¹⁶¹ Eu	¹⁶² Eu	¹⁶³ Eu	¹⁶⁴ Eu	¹⁶⁵ Eu	¹⁶⁶ Eu	¹⁶⁷ Eu	¹⁶⁸ Eu
62	¹⁵⁴ Sm	¹⁵⁵ Sm	¹⁵⁶ Sm	¹⁵⁷ Sm	¹⁵⁸ Sm	¹⁵⁹ Sm	¹⁶⁰ Sm	¹⁶¹ Sm	¹⁶² Sm	¹⁶³ Sm	¹⁶⁴ Sm	¹⁶⁵ Sm	¹⁶⁶ Sm	¹⁷ Sm
61	¹⁵³ Pm	¹⁵⁴ Pm	¹⁵⁵ Pm	¹⁵⁶ Pm	¹⁵⁷ Pm	¹⁵⁸ Pm	¹⁵⁹ Pm	¹⁶⁰ Pm	¹⁶¹ Pm	¹⁶² Pm	¹⁶³ Pm	¹⁶⁴ Pm	¹⁶⁵ Pm	¹⁶⁶ Pm
60	¹⁵² Nd	¹⁵³ Nd	¹⁵⁴ Nd	¹⁵⁵ Nd	¹⁵⁶ Nd	¹⁵⁷ Nd	¹⁵⁸ Nd	¹⁵⁹ Nd	¹⁶⁰ Nd	¹⁶¹ Nd	¹⁶² Nd	¹⁶³ Nd	¹⁶⁴ Nd	
59	¹⁵¹ Pr	¹⁵² Pr	¹⁵³ Pr	¹⁵⁴ Pr	¹⁵⁵ Pr	¹⁵⁶ Pr	¹⁵⁷ Pr	¹⁵⁸ Pr	¹⁵⁹ Pr	¹⁶⁰ Pr	¹⁶¹ Pr	¹⁶² Pr	¹⁶³ Pr	
58	¹⁵⁰ Ce	¹⁵¹ Ce	¹⁵² Ce	¹⁵³ Ce	¹⁵⁴ Ce	¹⁵⁵ Ce	¹⁵⁶ Ce	¹⁵⁷ Ce	¹⁵⁸ Ce	¹⁵⁹ Ce	¹⁶⁰ Ce			
57	¹⁴⁹ La	¹⁵⁰ La	¹⁵¹ La	¹⁵² La	¹⁵³ La	¹⁵⁴ La	¹⁵⁵ La	¹⁵⁶ La	¹⁵⁷ La	¹⁵⁸ La				
56	¹⁴⁸ Ba	¹⁴⁹ Ba	¹⁵⁰ Ba	¹⁵¹ Ba	¹⁵² Ba	¹⁵³ Ba	¹⁵⁴ Ba	¹⁵⁵ Ba	¹⁵⁶ Ba					

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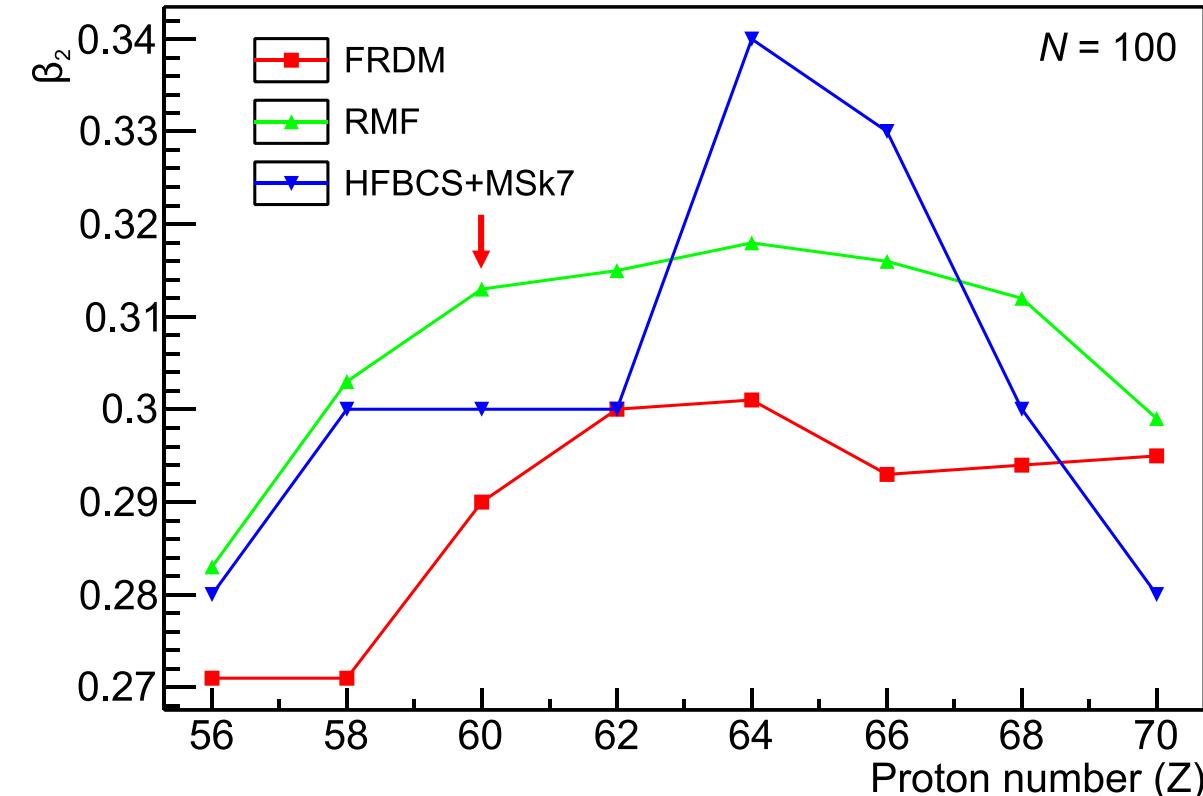
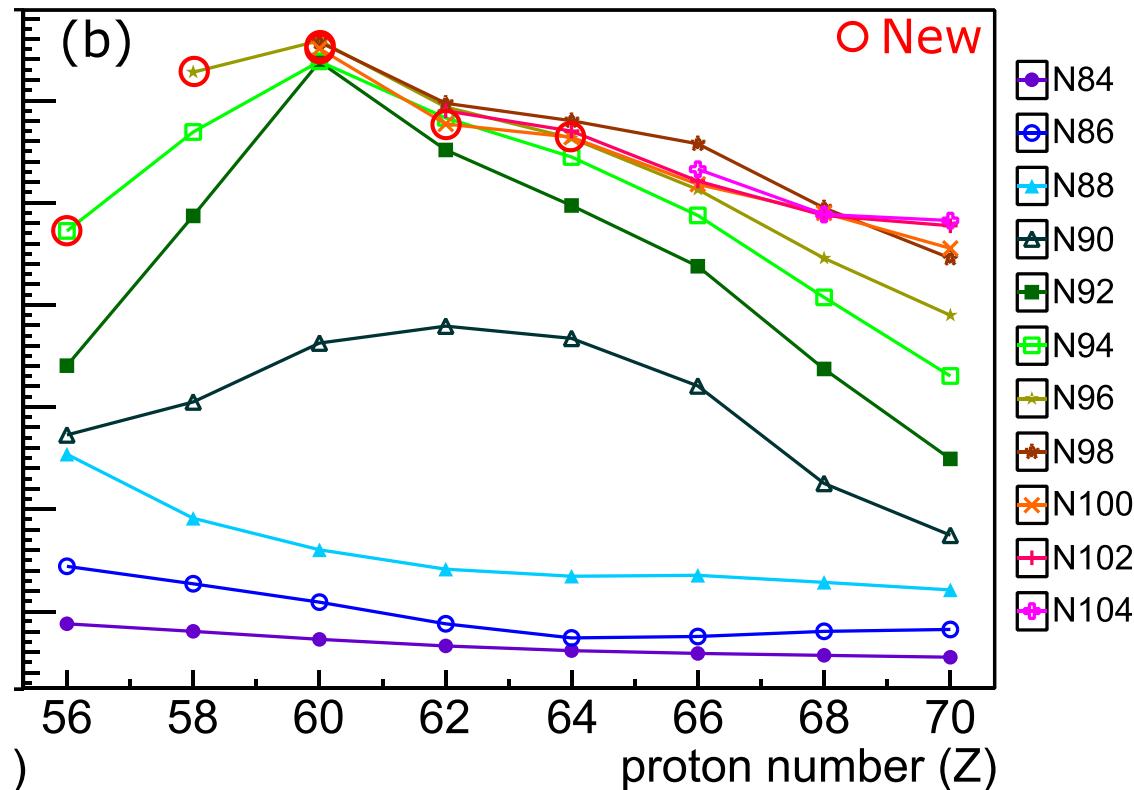
- ^AX Known isomer ($T_{1/2} > 100$ ns)
- ^AX New isomer
- ^AX No isomer (> 10^4 implant)
- ^AX Octupole band
- ^AX stable nuclide
- ^AX New β - γ

- G.s. band systematics
→ quadrupole
- Isomers in $N=100$ and $N=98$ isotones
→ hexadecupole



Systematics of g.s. band

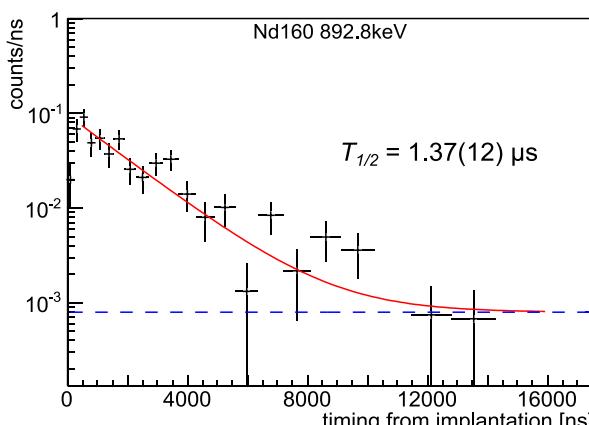
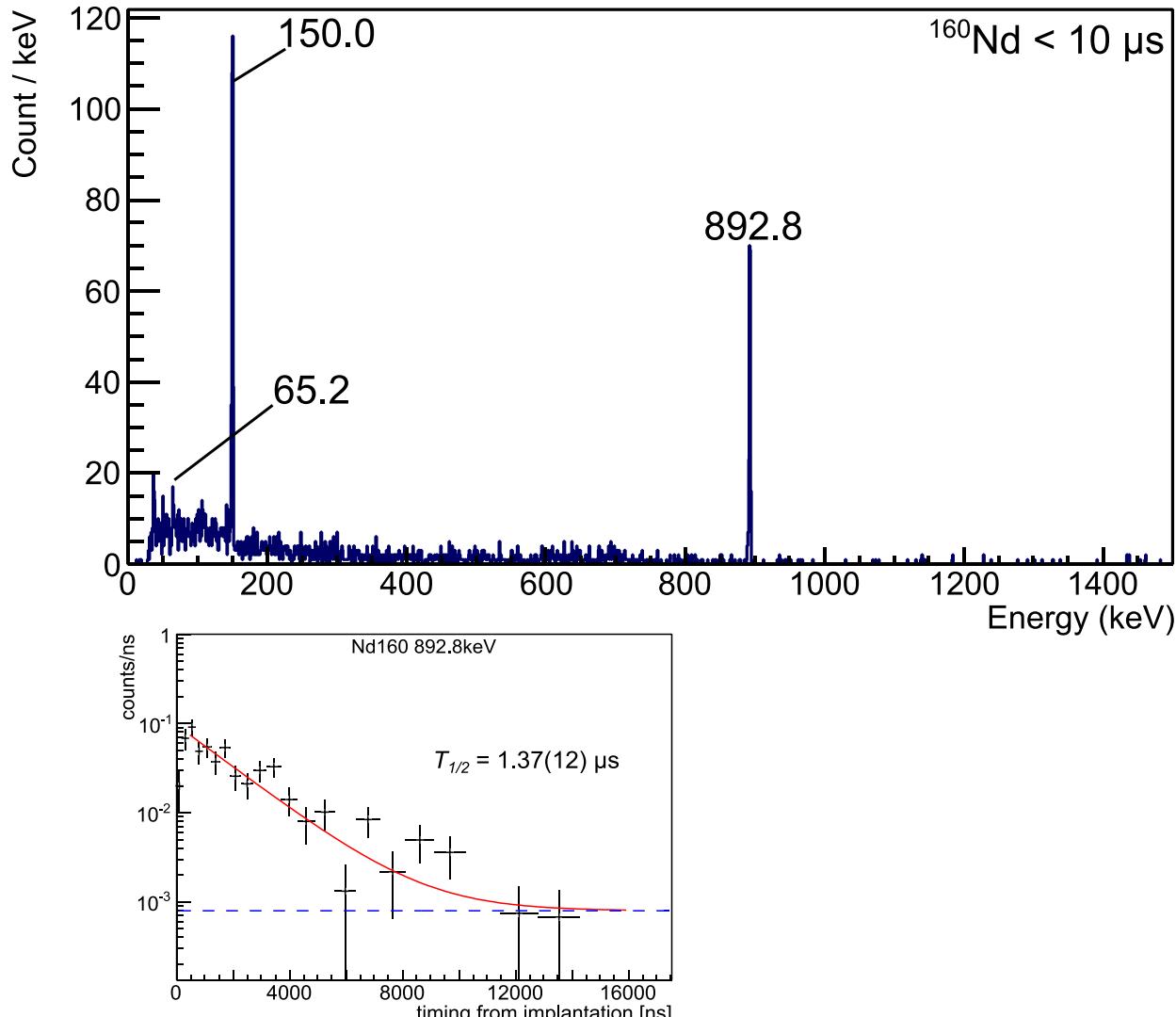
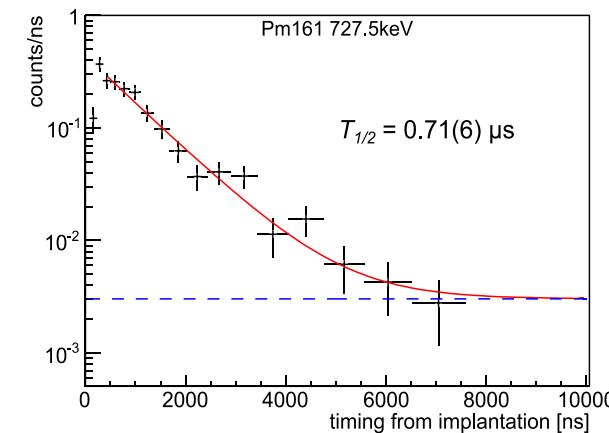
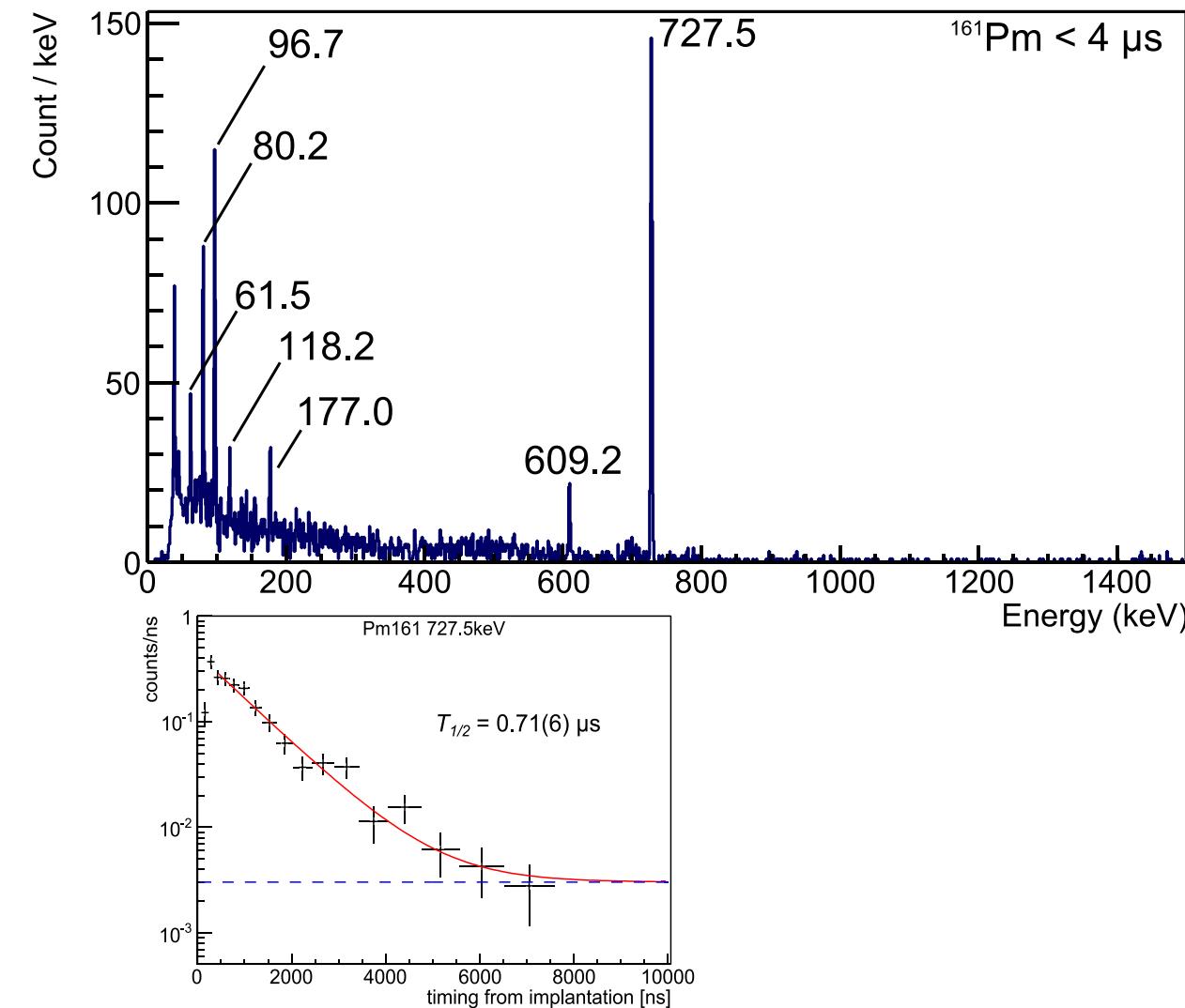
Moment of inertia of g.s. band from $E(2+)$ of even-even nuclei



- Moment of inertia peaks at $Z=60$ (b)
→ No calculation predicts deformation maximum at $Z=60$

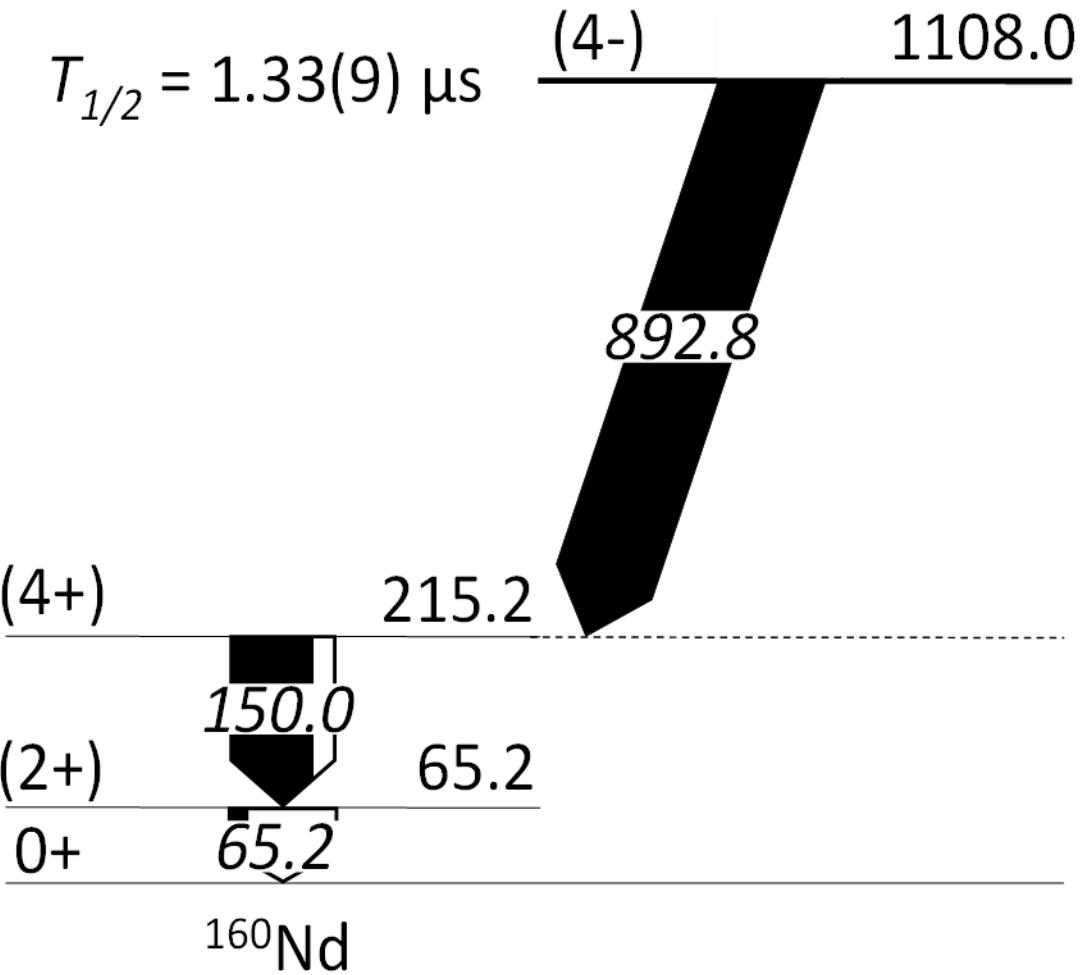
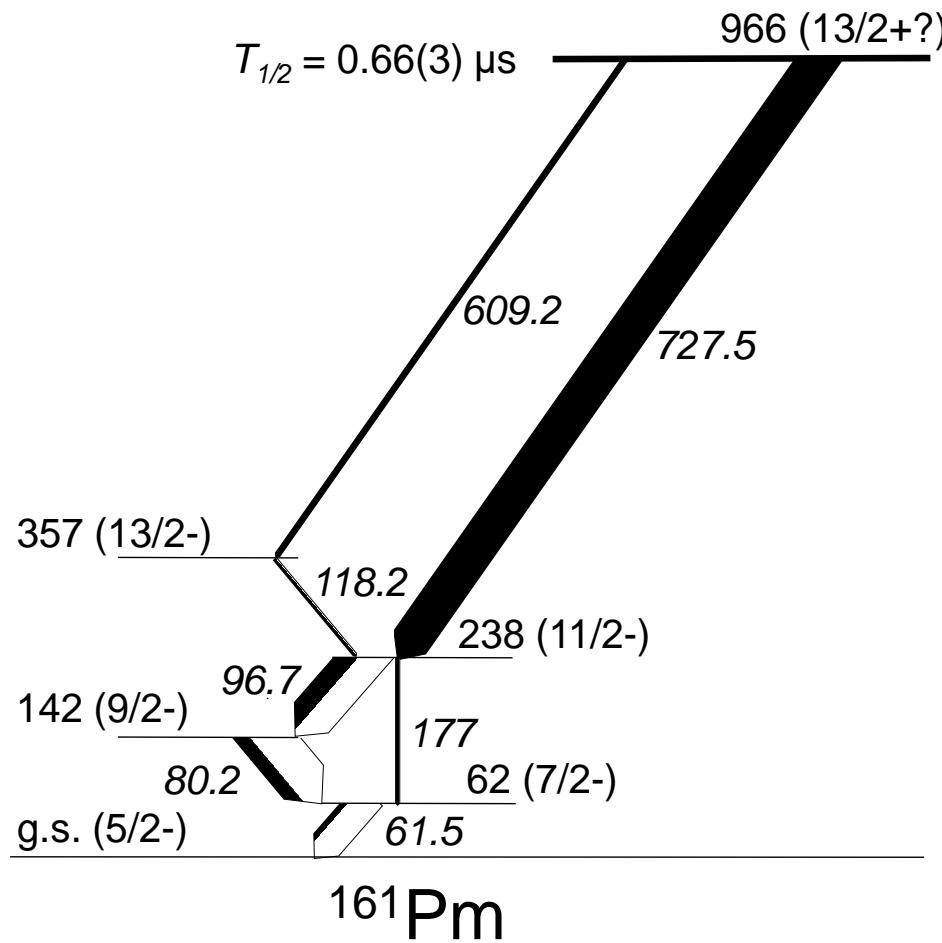


Isomers in $N=100$ isotones: Energy and timing spectra



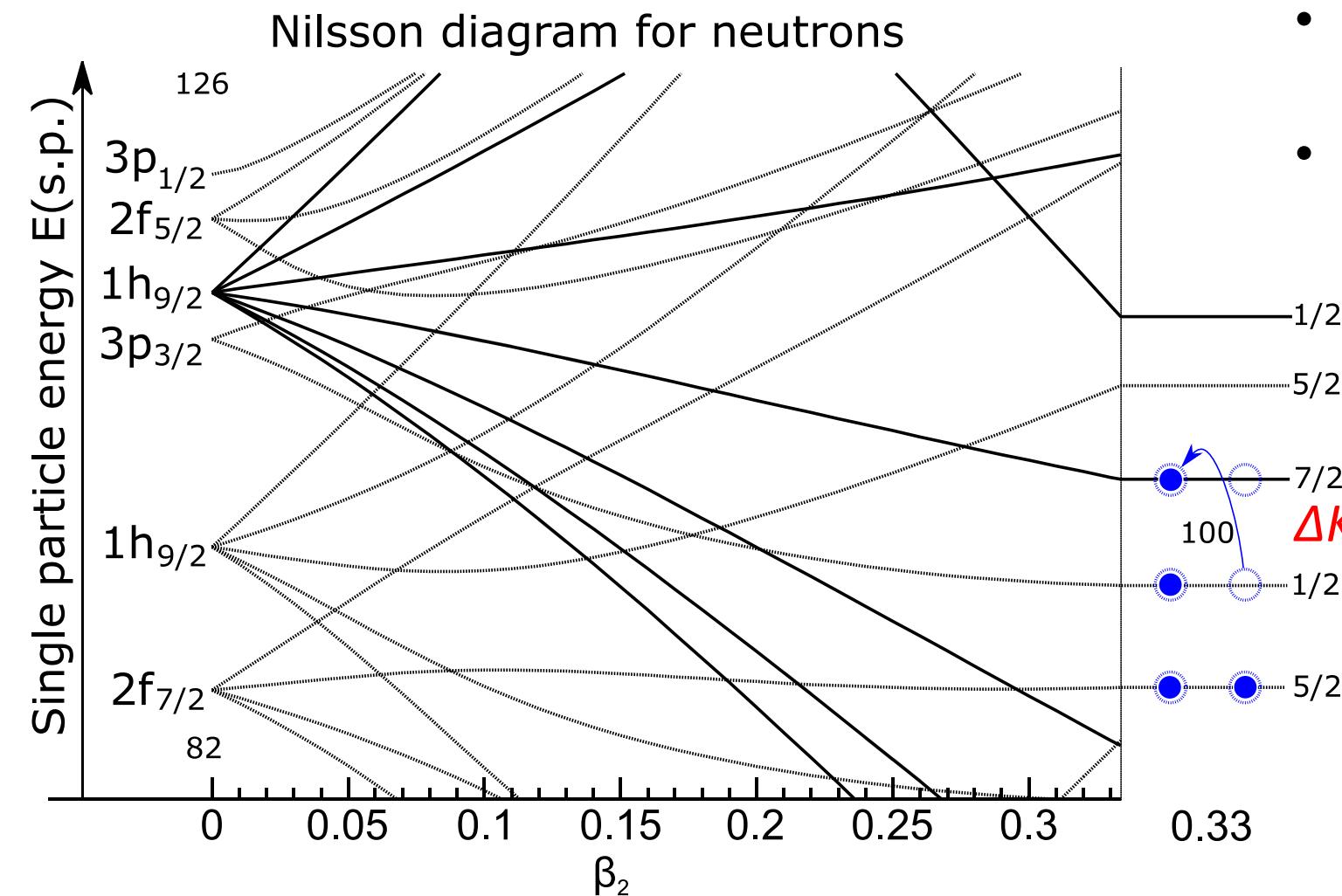


Isomers in $N=100$ isotones: Level schemes

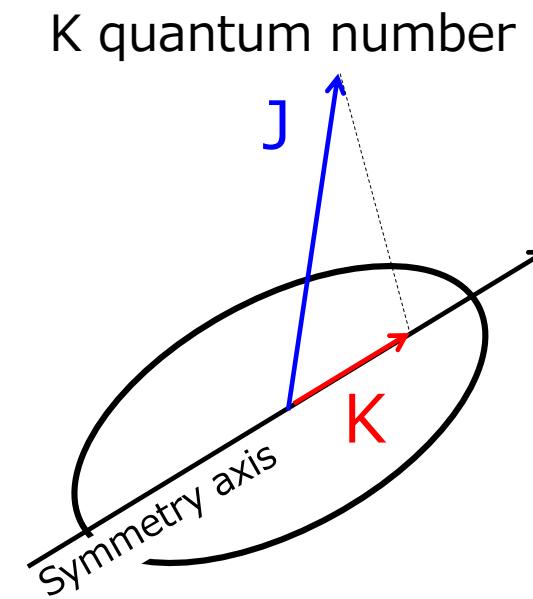




High- K isomers at $N=100$



- K isomers known in $N = 100$ isotones
 ^{170}Yb , ^{168}Er
- quasi-particle excitation:
 $7/2[633] \otimes 1/2[521]$ ($\Omega[Nn, \Lambda]$)





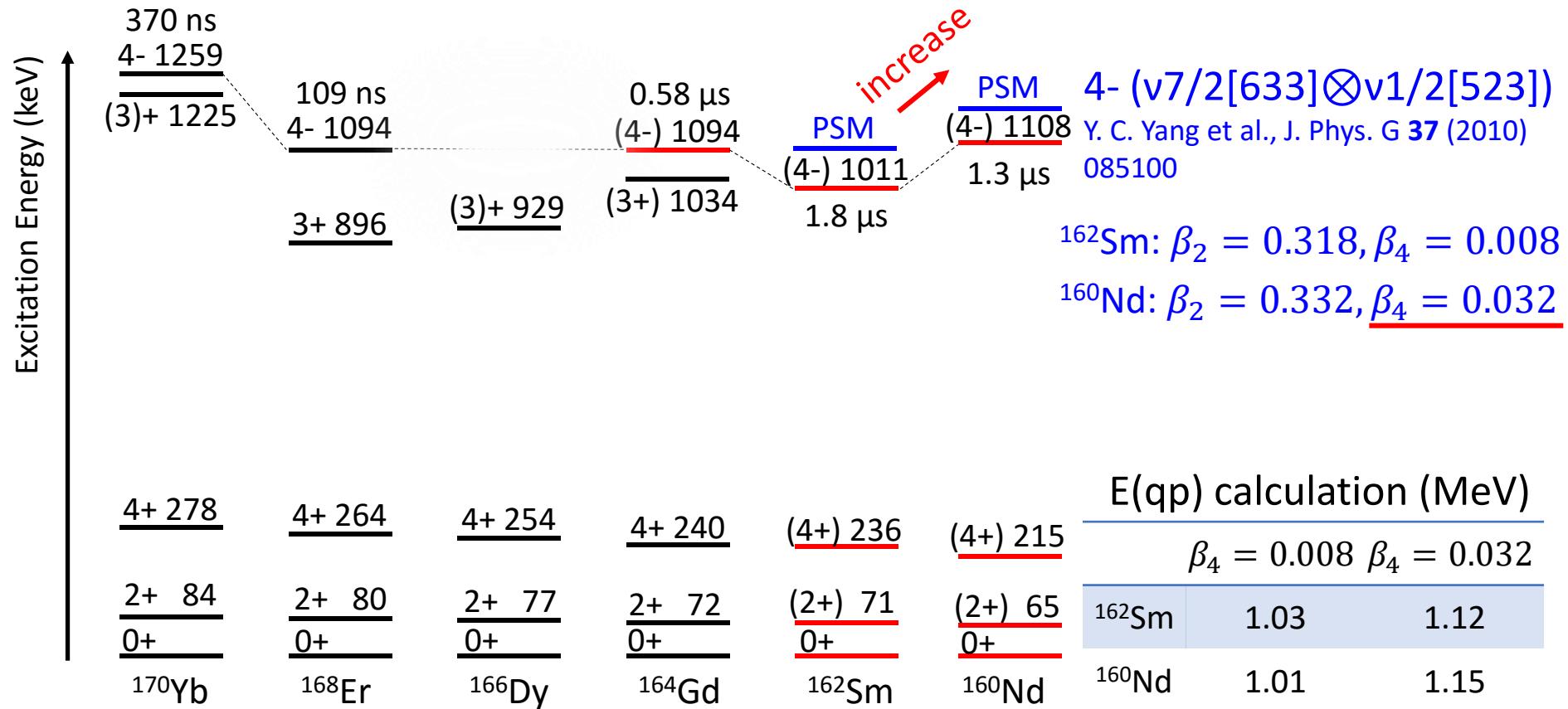
Isomers in $N=100$ isotones: Summary of isomer

Nuclide	E_{isomer} (keV)	E_γ (keV)	$T_{\gamma 1/2}(\text{exp.})$ (s)	F_w W.u. $^{-1}$
^{170}Yb	1259	981.1	3.7×10^{-7}	1.6×10^9
^{168}Er	1094	830.0	1.1×10^{-6}	2.9×10^9
^{164}Gd	1094	854.1	7.1×10^{-7}	2.0×10^9
^{163}Eu	964	674.9	9.1×10^{-7}	1.2×10^9
^{162}Sm	1010	774.5	1.8×10^{-6}	3.6×10^9
^{161}Pm New	966	727.5	7.6×10^{-7}	1.3×10^9
^{160}Nd New	1108	892.8	1.3×10^{-6}	4.0×10^9

- All have 10^9 order of hindrance $\Delta K=4$
- Expected same isomer configuration (neutron 2-qp $K^\pi = 4^-$)
known in ^{170}Yb and ^{168}Er



$N=100$ isomers



- PSM (projected shell model) calculation reproduces the increase of $E(4-)$ with large hexadecupole deformation in Nd



Conclusion

- New excited states found by isomer and β - γ spectroscopy
 - K isomers in $N=100$ ($K^\pi=4^-$), $N=98$ ($K^\pi=6^-$) isotones
 - Ground band of some even-even nuclei (^{150}Ba , ^{154}Ce , etc....)
- Systematics of g.s. band
 - Moment of inertia peaks at $Z=60$ (disagree with FRDM, RMF, HFBCS calc.)
 - Small pairing correlation due to $Z=60$ gap may increase the moment of inertia
- Experimental indications on hexadecupole deformation in Nd ($Z=60$)
 - Energy increase of $K^\pi=4^-$ isomers
 - Change of isomer configuration ($K^\pi=5^-$ to $K^\pi=6^-$) in $N=98$ isotones
- Future perspective
 - Half-life measurement