

Neutron star structure explored with a family of unified equations of state of neutron star matter

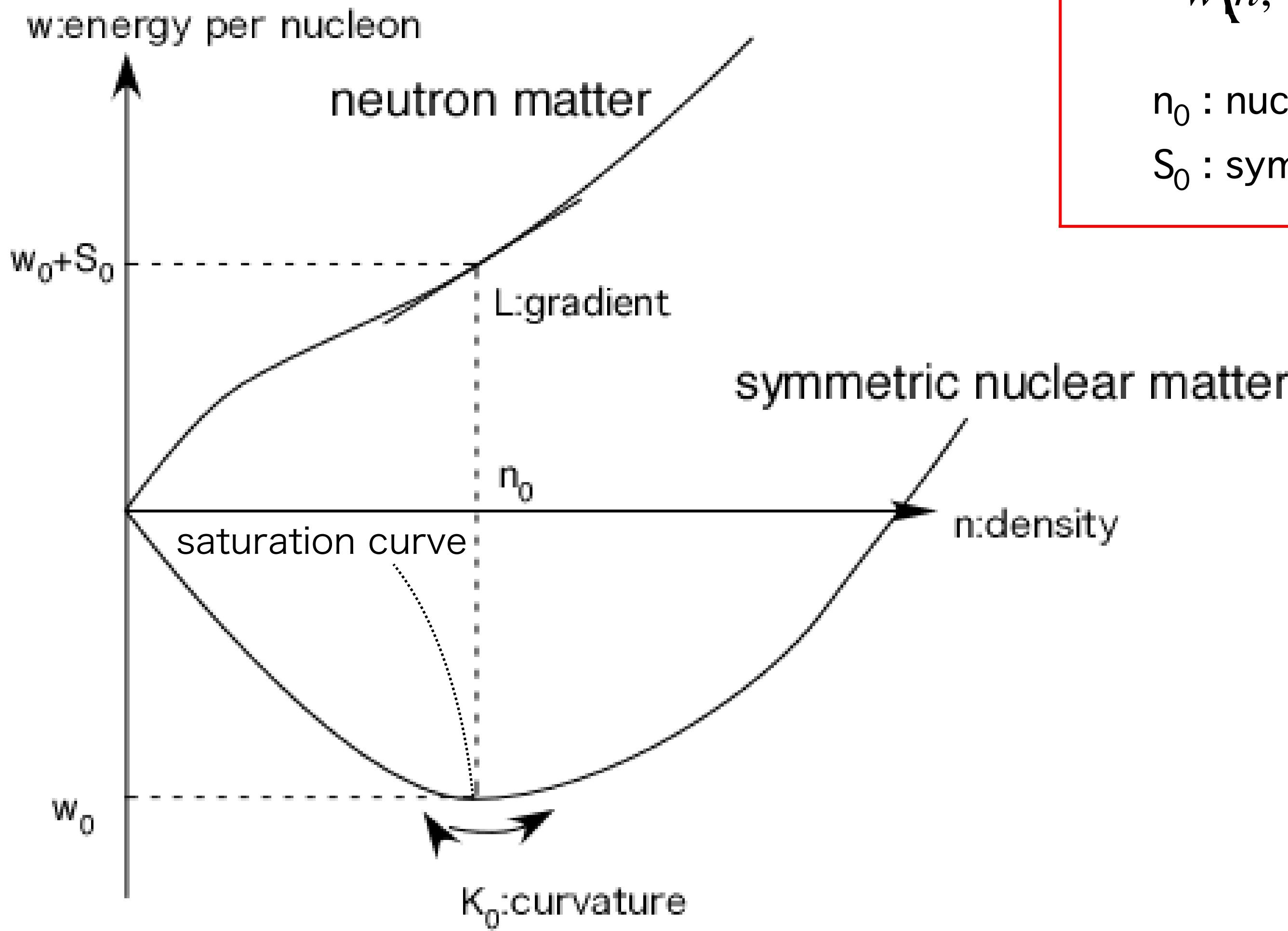
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Oyamatsu-lida (OI) unified EOS family

- Unified EOS family which covers from laboratory nuclei to neutron star matter
- Each EOS is labeled with the empirical uncertain saturation parameters: the incompressibility K_0 , and the density gradient of symmetry energy L
- A simplified Thomas-Fermi model description of nuclei (the same method as popular Shen EOS (NPA1998,2011) for supernova matter)

Saturation parameters and auxiliary empirical constraint



Energy per nucleon of nearly symmetric nuclear matter

$$w(n, x) \approx w_0 + \frac{K_0}{18n_0^2}(n - n_0)^2 + (1 - 2x)^2 \left[S_0 + \frac{L}{3n_0}(n - n_0) \right]$$

n_0 : nuclear density, w_0 :saturation energy, K_0 : incompressibility

S_0 : symmetry energy at $n=n_0$, L : its density derivative coefficient

Symmetry energy S_0 and its density gradient L

$$S_0 = S(n_0) \quad L = \frac{dS(n)}{dn} \Big|_{n=n_0}$$

Saturation point of asymmetric matter ($x \approx 0.5$)

$$n_s = n_0 - \frac{3n_0 L}{K_0} \alpha^2 \quad w_s = w_0 + S_0 \alpha^2 \quad \alpha = 1 - 2x$$

slope of saturation curve

$$y = -\frac{S_0 K_0}{3n_0 L}$$

Auxiliary empirical constraint

$$-1800 \leq y \leq -200$$

Adopted macroscopic mode

Energy per cell

(or Energy of a nucleus

$$W = \int_{\text{cell}} dr \left[\epsilon_0(n_n, n_p) + m_n n_n + m_p n_p \right] + \int_{\text{cell}} dr F_0 |\nabla n_i|^2 + (\text{electron kinetic energy}) + (\text{Coulomb})$$

n_n (n_p): local neutron (proton) density, $n = n_n + n_p$: total density

$\varepsilon_0(n_n, n_p)$: EOS of uniform nuclear matter (energy density)

F_0 : surface energy parameter

Parametrization of the EOS (energy density)

$$\varepsilon_0(n_n, n_p) = \frac{3}{5} \left(3\pi^2 \right)^{2/3} \left(\frac{\hbar^2}{2m_n} n_n^{5/3} + \frac{\hbar^2}{2m_p} n_p^{5/3} \right) + \left[1 - \left(1 - 2Y_p \right)^2 \right] v_s(n) + \left(1 - 2Y_p \right)^2 v_n(n)$$

Fermi kinetic energy density

potential energy density

potential energy densities of symmetric and neutron matte

$$V_s(n) = a_1 n^2 + \frac{a_2 n^3}{1 + a_3 n} \quad V_u(n) = b_1 n^2 + \frac{b_2 n^3}{1 + b_3 n}$$

★ $a_1 \sim b_2$ and F_0 : masses and radii of stable nuclei ($b_3=1.59$ fm 3 , a fit to FP EOS)

★ very flexible function form: a_3 can vary K_0 widely. (better than Skyrme)

The function can be fitted to SIII and TM1 EOS very well

Simplified Thomas-Fermi calculation

energy minimization with respect to parameters of $n_n(r)$ and $n_p(r)$ (and lattice constant)

neutron (proton) density distribution n_n (n_p)

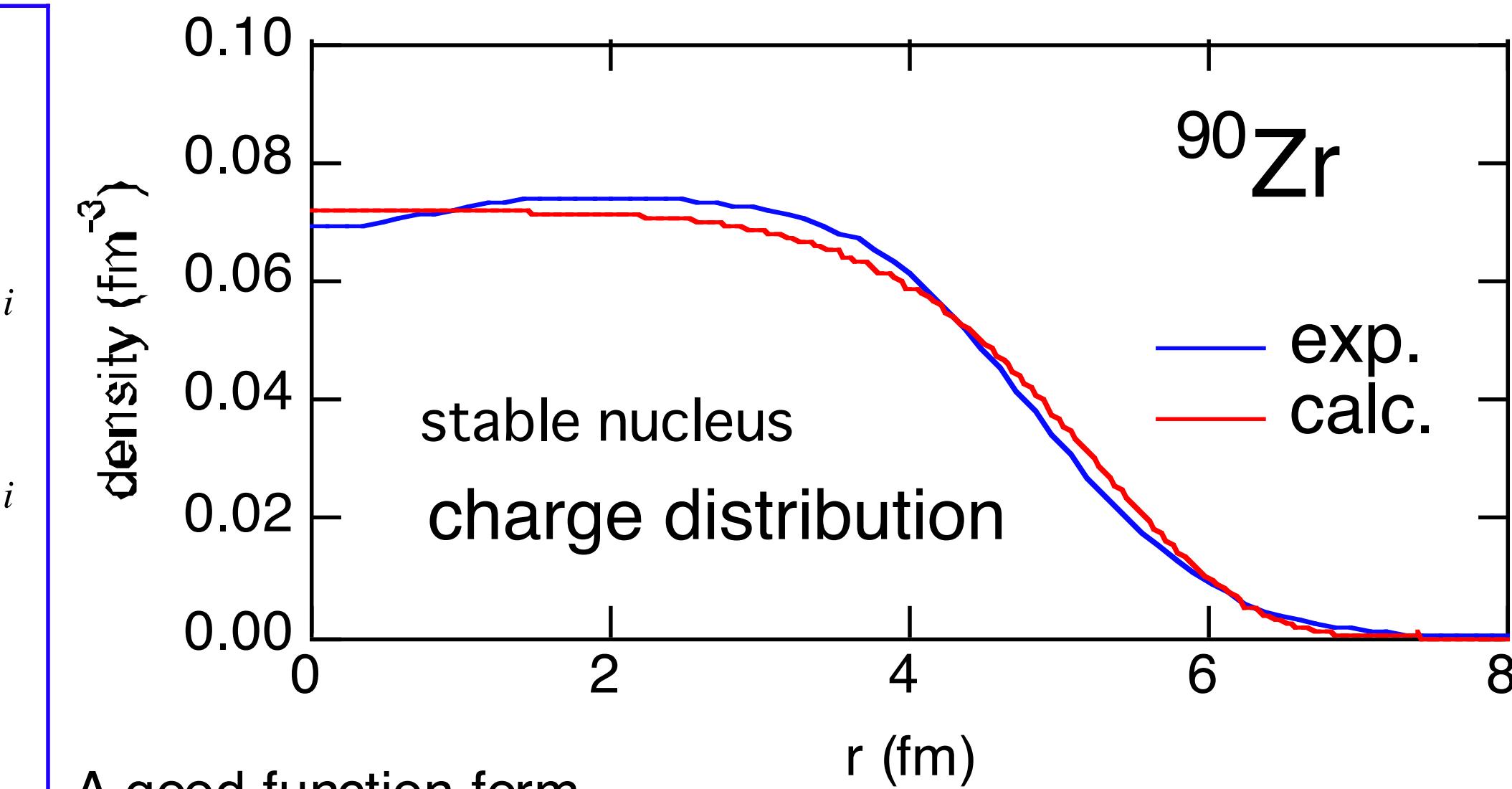
$$n_i(r) = \begin{cases} (n_i^{in} - n_i^{out}) \left[1 - \left(\frac{r}{R_i} \right)^{t_i} \right]^3 + n_i^{out} & r < R_i \\ n_i^{out} & r > R_i \end{cases}$$

R_n (R_p): neutron (proton) radius parameter

t_n (t_p): neutron (proton) surface thickness parameter

n_i^{in} : central density

n_n^{out} : neutron gas density ($n_p^{out}=0$)



A good function form

The n and p distributions are independent.

=> neutron skin

The empirical information is limited: radius and thickness.

The gradient term in Euler Eq. is continuous.

The density is zero beyond the classical turning point.

The values of parameters $a_1 \sim b_3$ (EOS) and F_0 are determined

to fit masses and radii of stable nuclei.

=> about 200 sets of empirical EOS+ F_0

EOS parameters and liquid drop mass formula

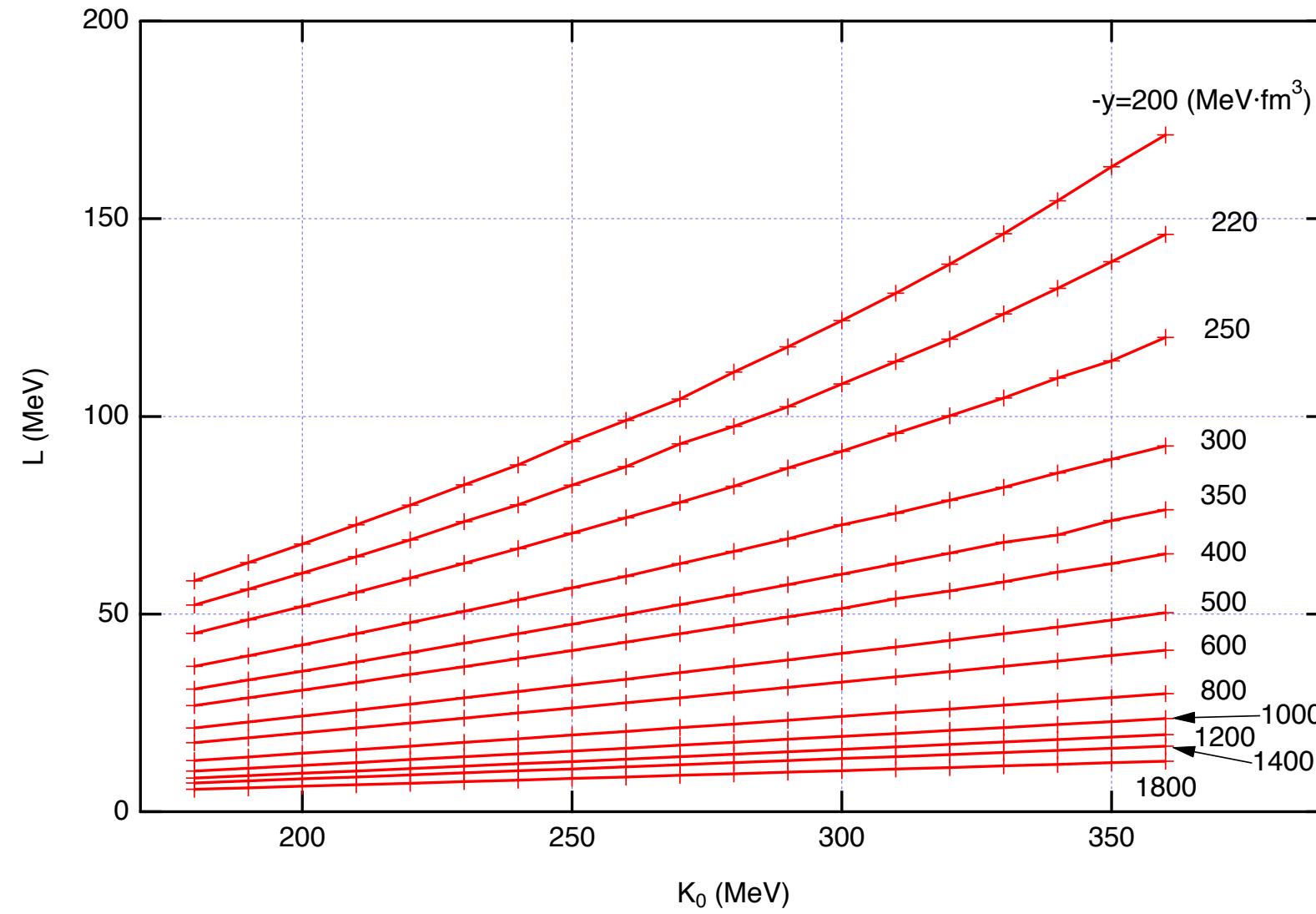
	OI EOS	saturation parameters	liquid drop mass formula
symmetric matter	a_1, a_2, a_3	n_0, w_0, K_0	a_v (volume) $\Rightarrow w_0$ a_c (Coulomb) $\Rightarrow n_0$
Symmetry energy neutron matter	$b_1, b_2, b_3 (=1.59)$	S_0, L w_{n0}, L (, K_{n0})	a_i (symmetry)
surface	F_0	(F_0)	a_s (surafce)

K_0 and L are not constrained well from nuclear masses.
=> Each OI EOS is labeled with (K_0, L) .

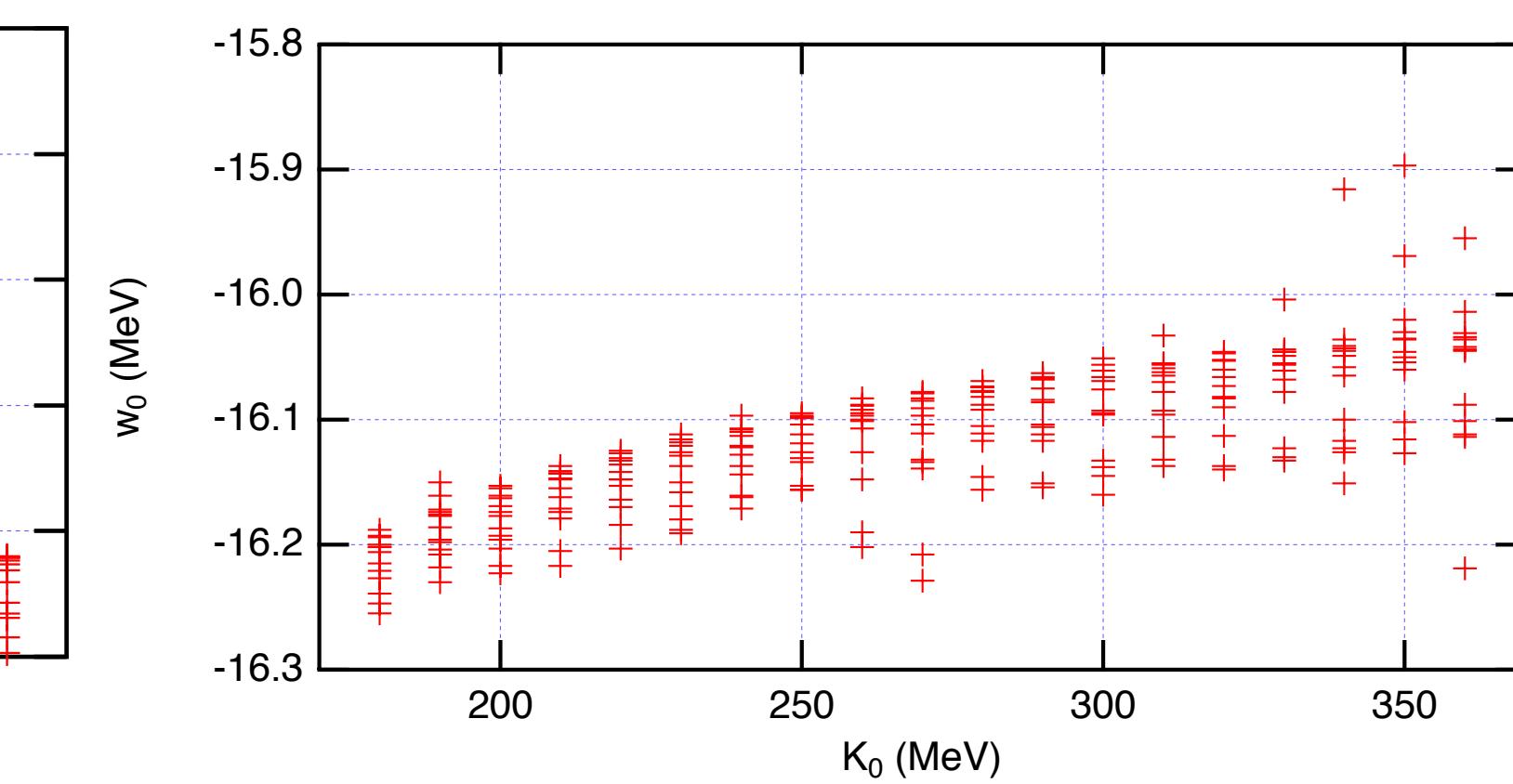
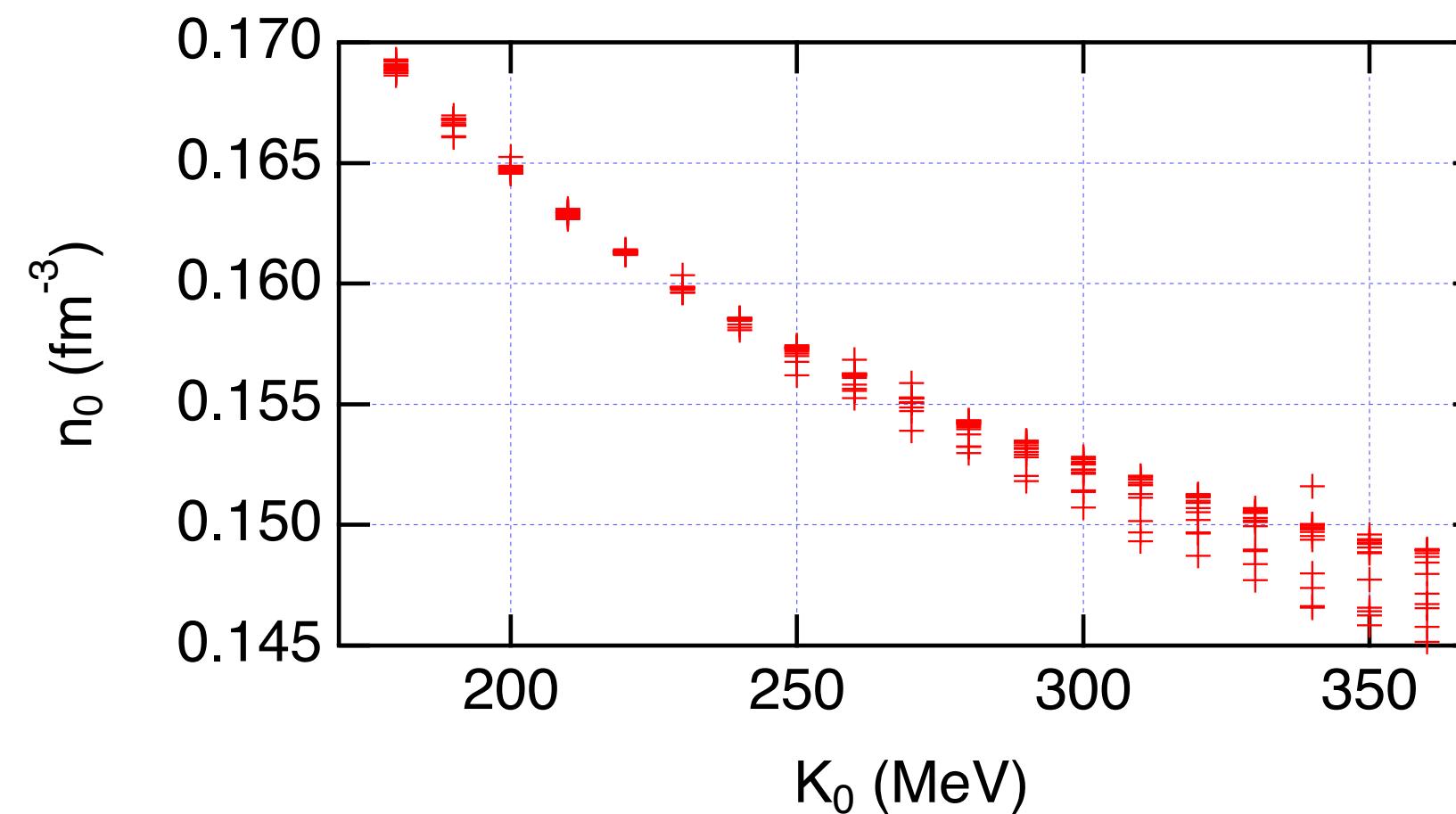
Saturation parameters of OI EOS family

Values of n_0 , w_0 and F_0 are almost constant.

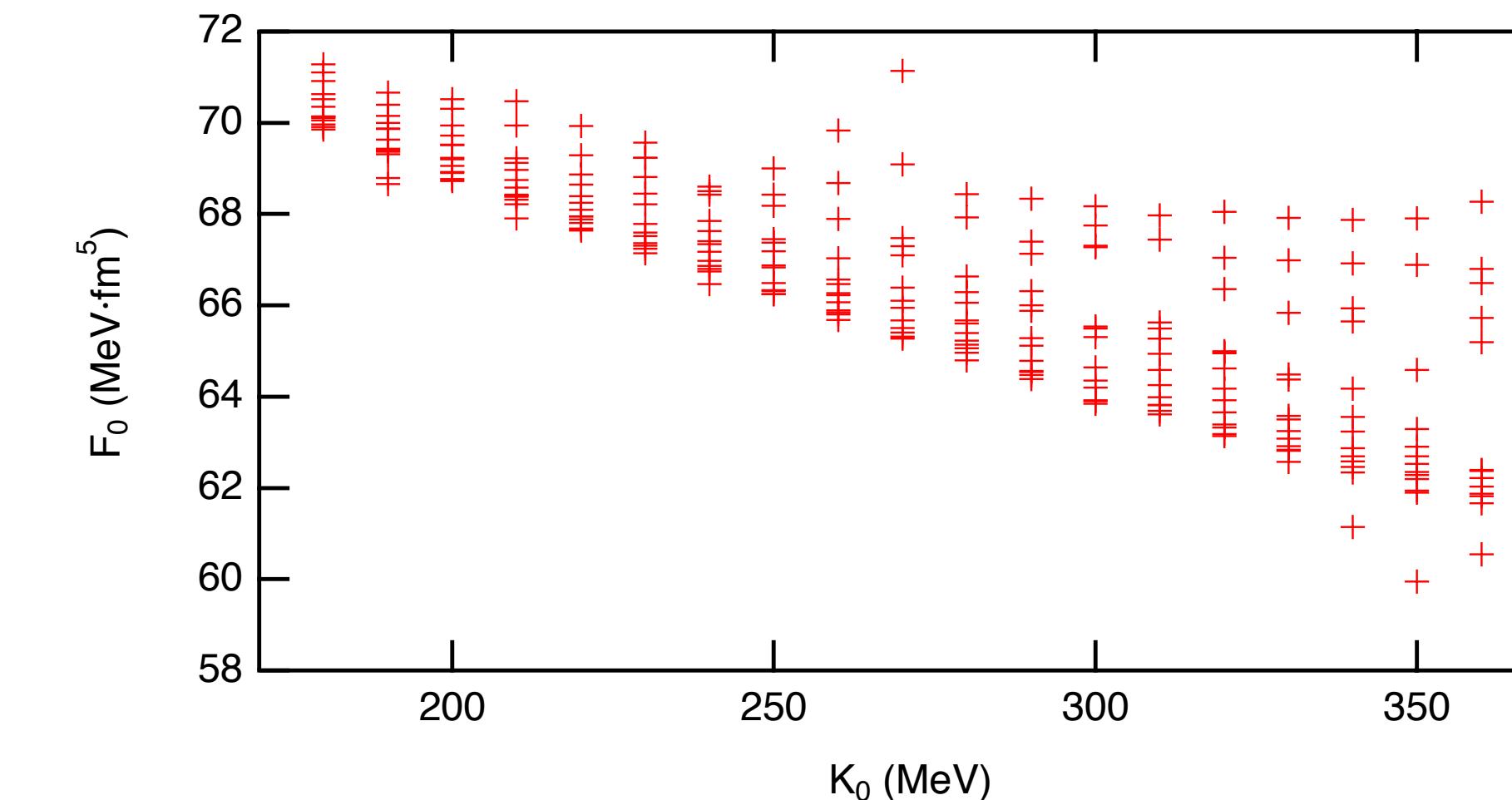
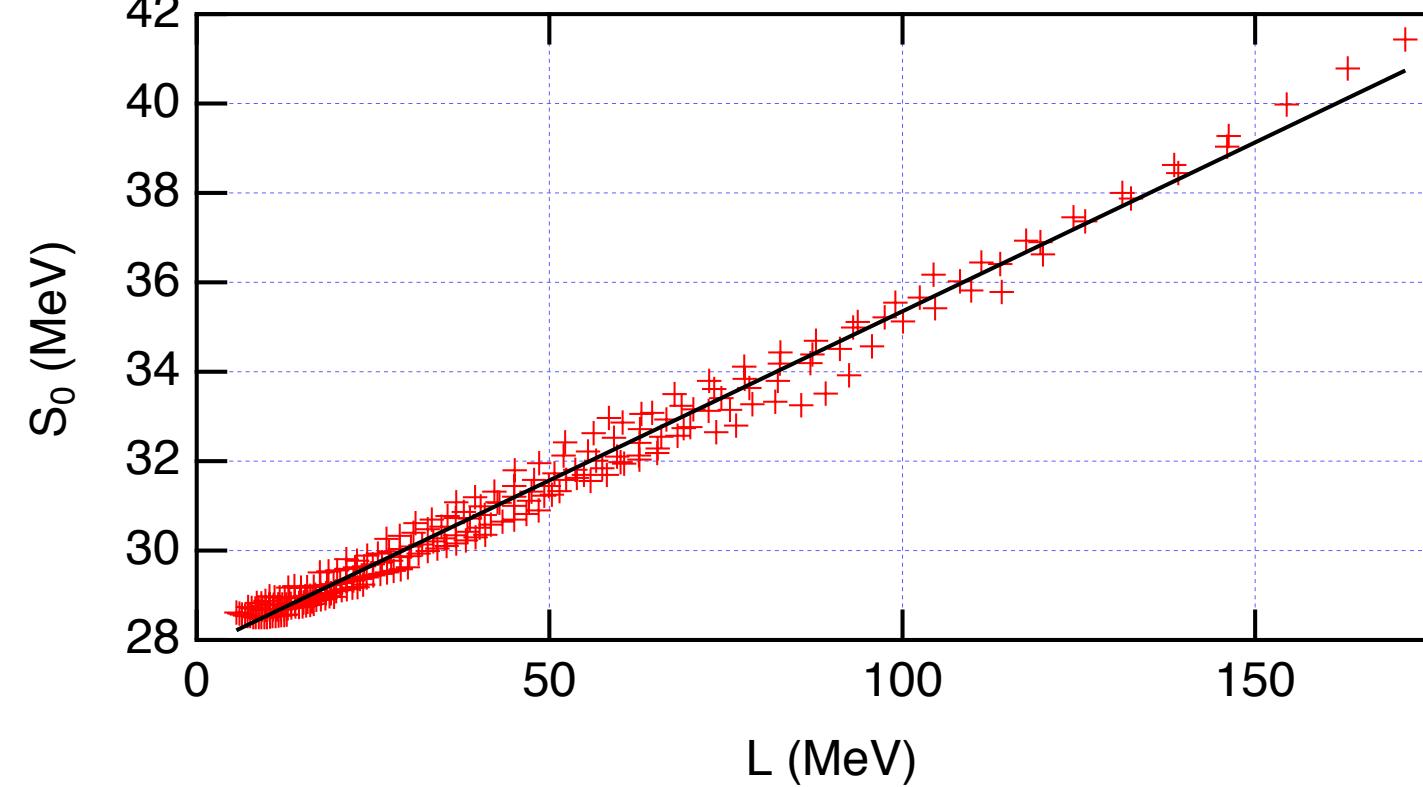
(K_0, L) values (crosses)



They have slight K_0 dependence
and their L dependence is much smaller.



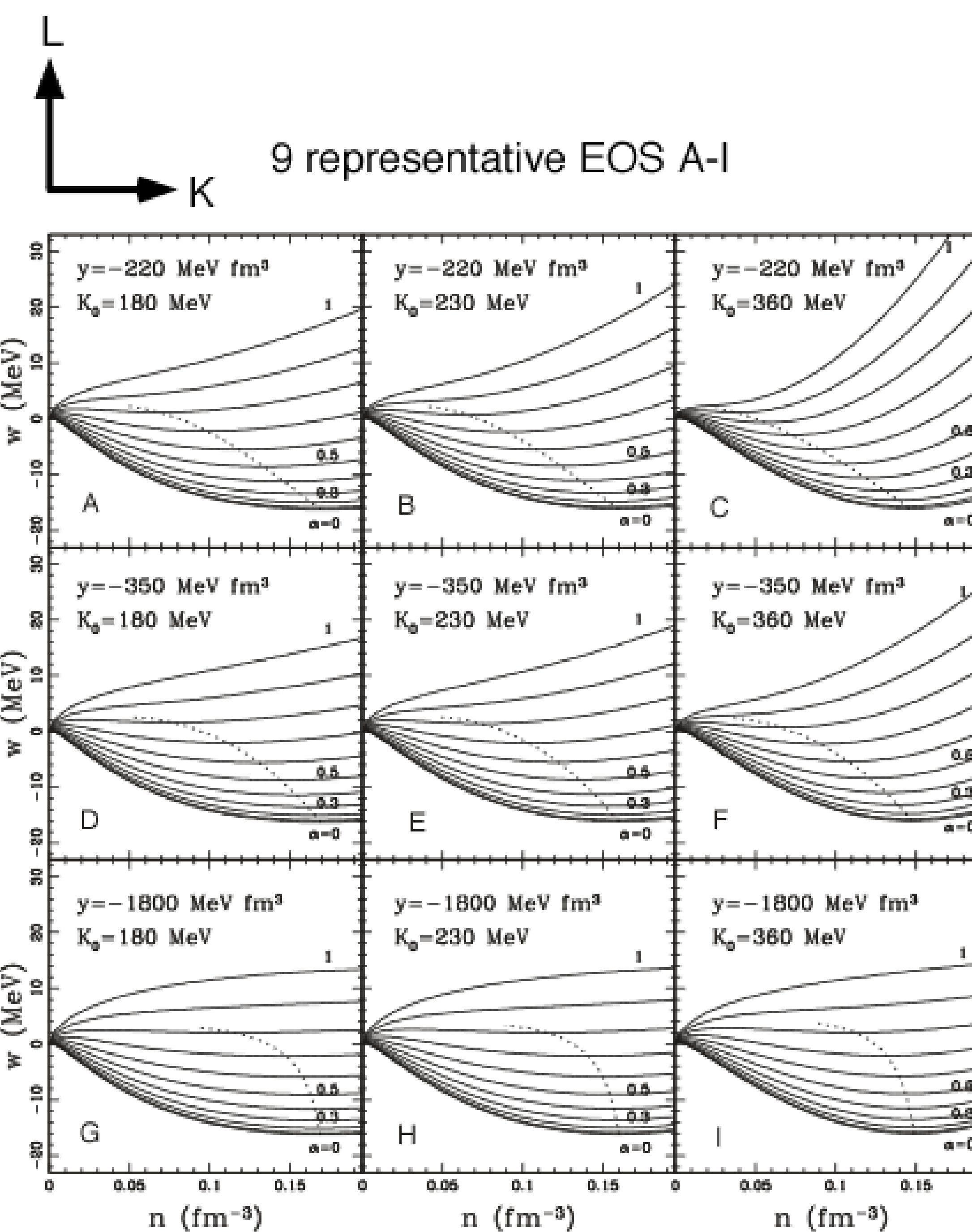
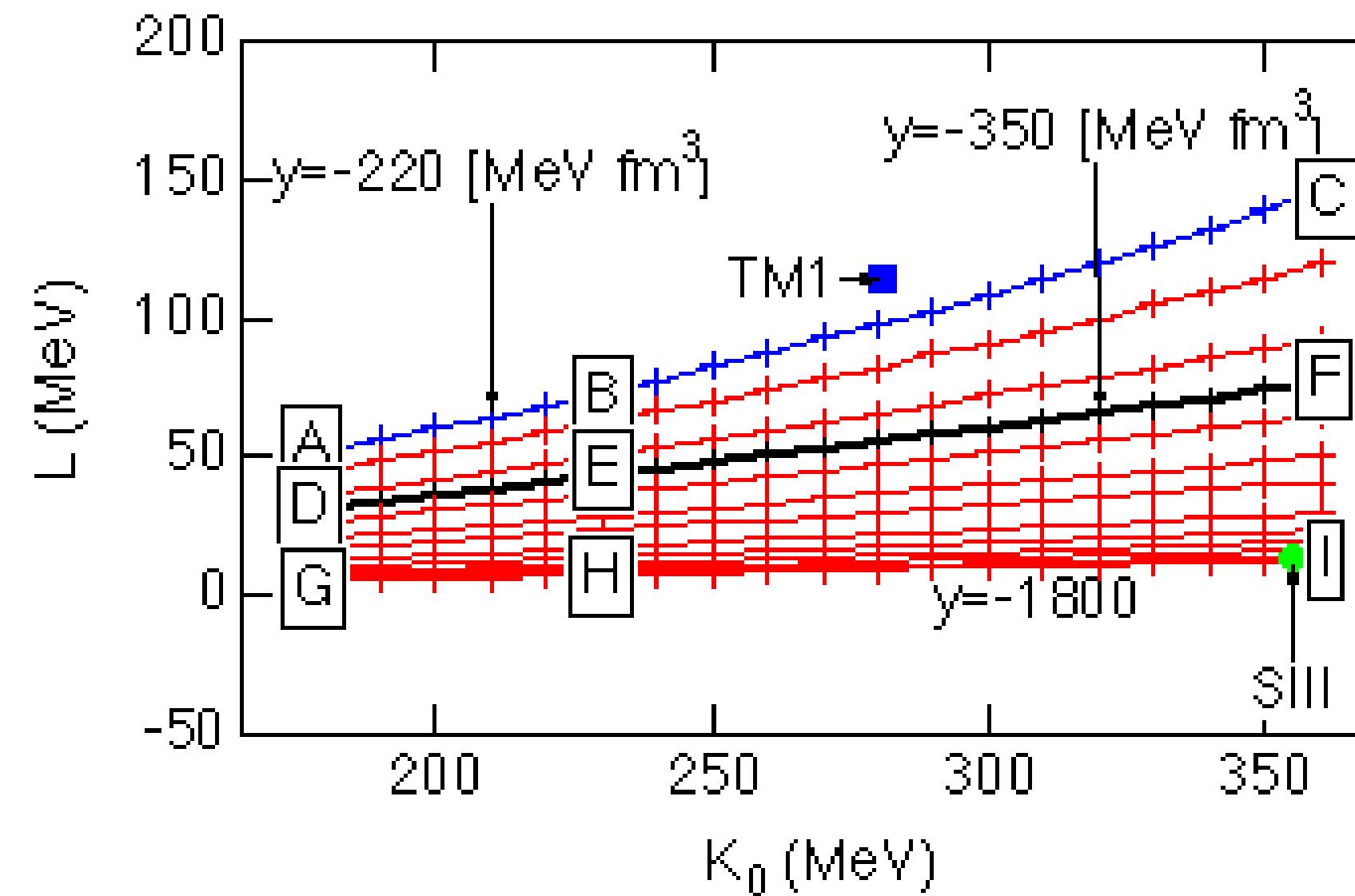
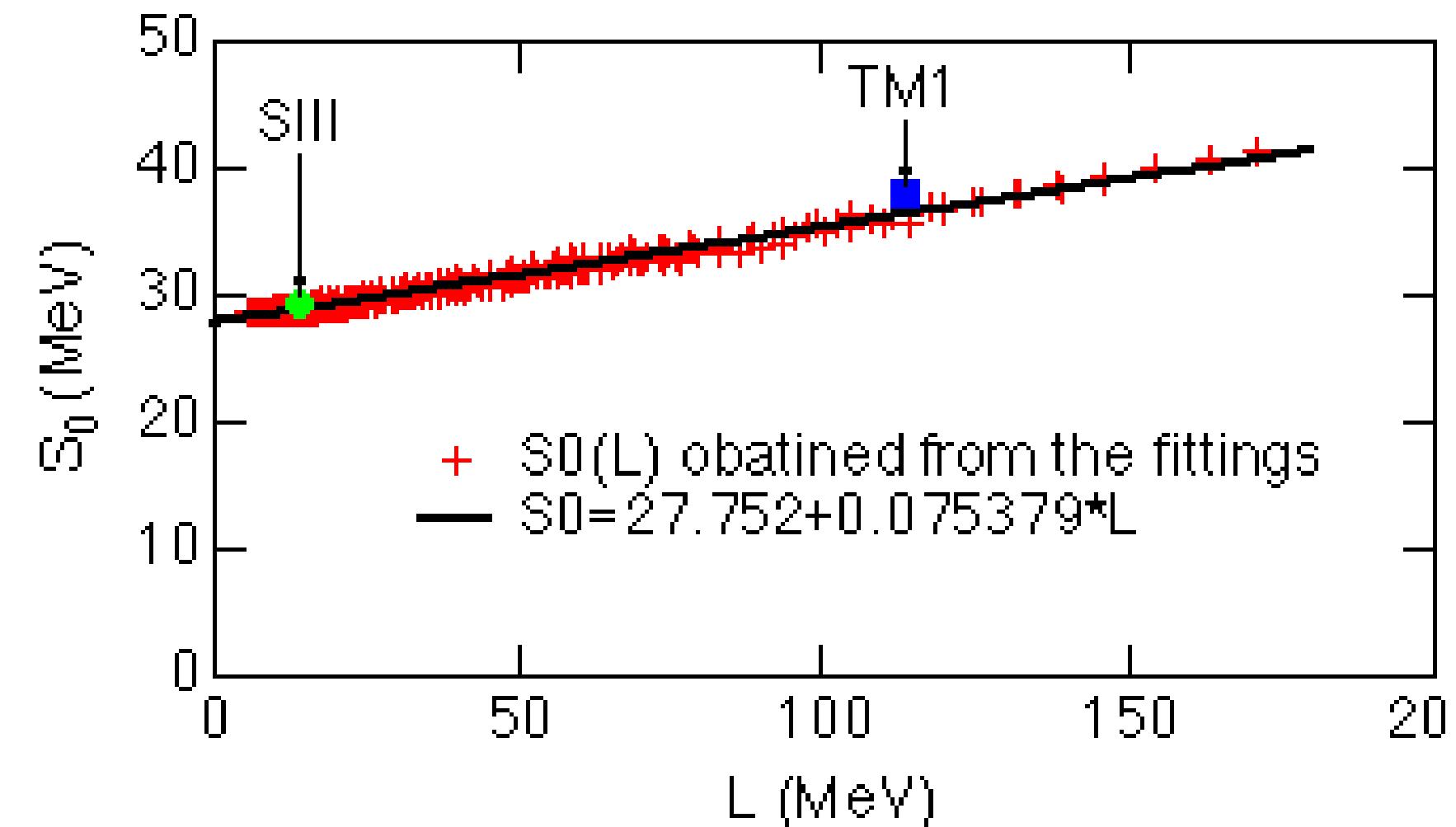
S_0 has strong correlation with L .



EOS parameter values obtained
from stable nuclei

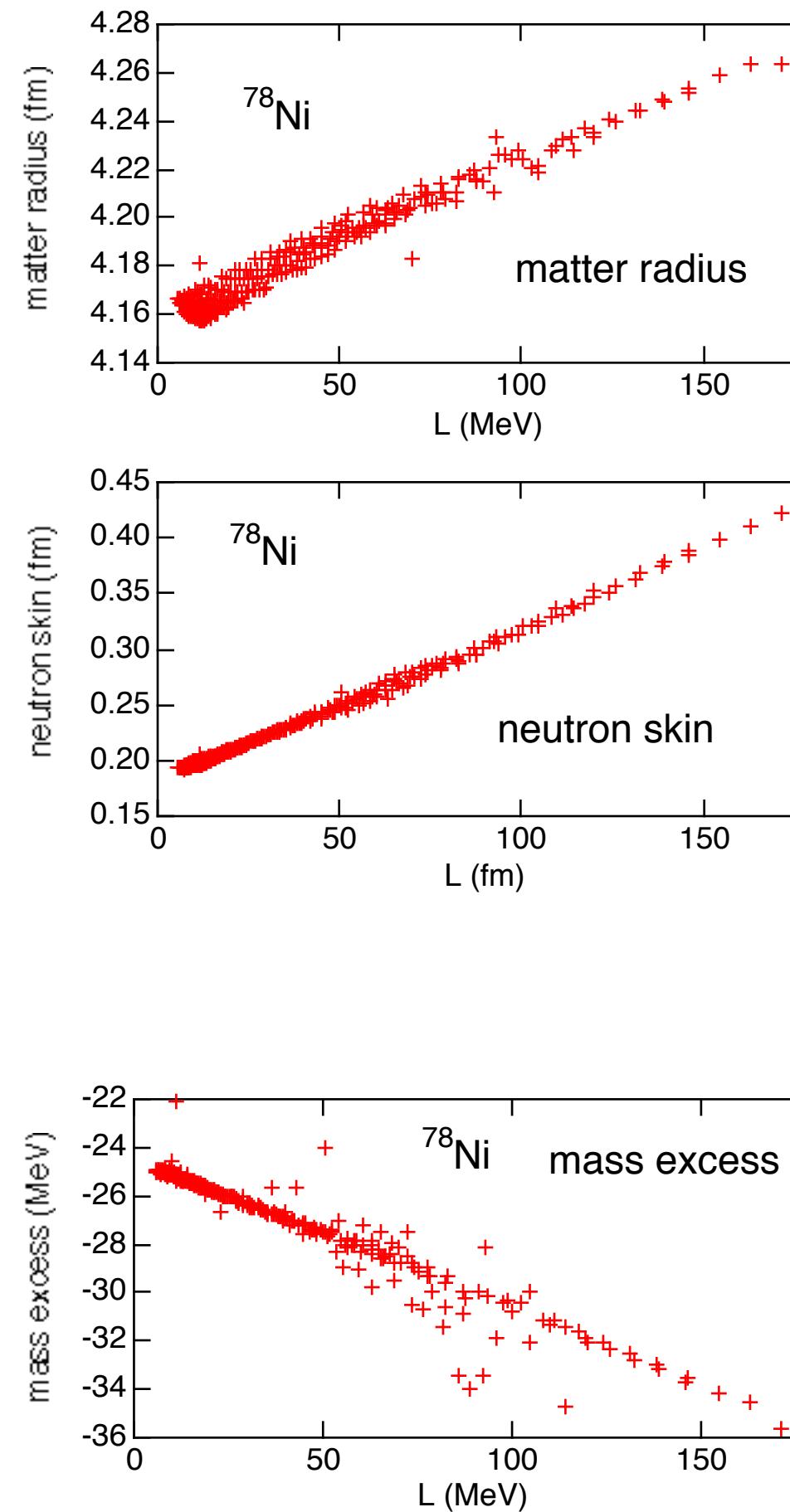
S_0 :symmetry energy

L : density symmetry coefficient



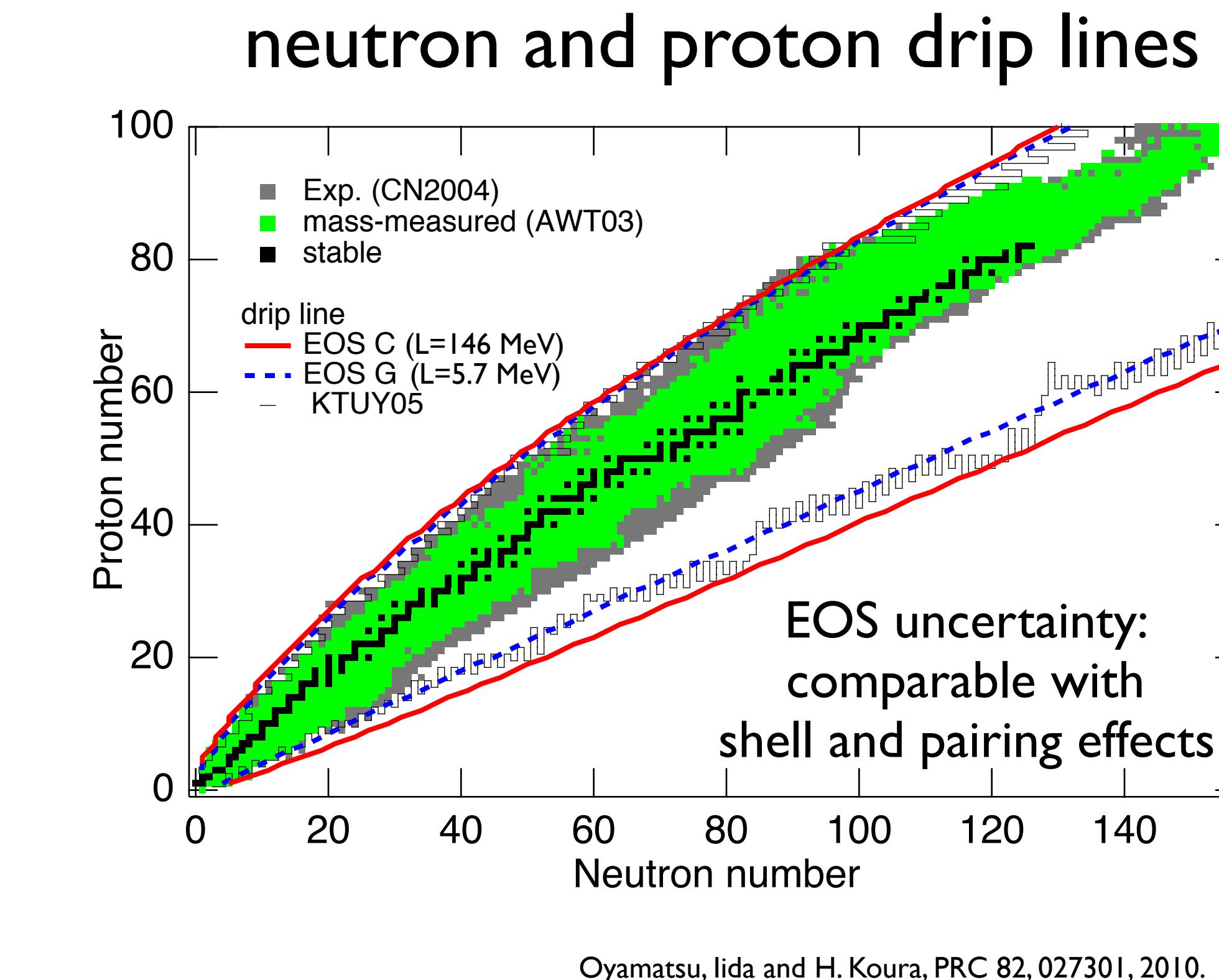
neutron rich nuclei in laboratory

mass, radius and neutron skin are sensitive to L but not to K_0 .



Larger L \Rightarrow larger neutron radius
and neutron skin

Larger L \Rightarrow smaller mass
not simple
(surface symmetry)

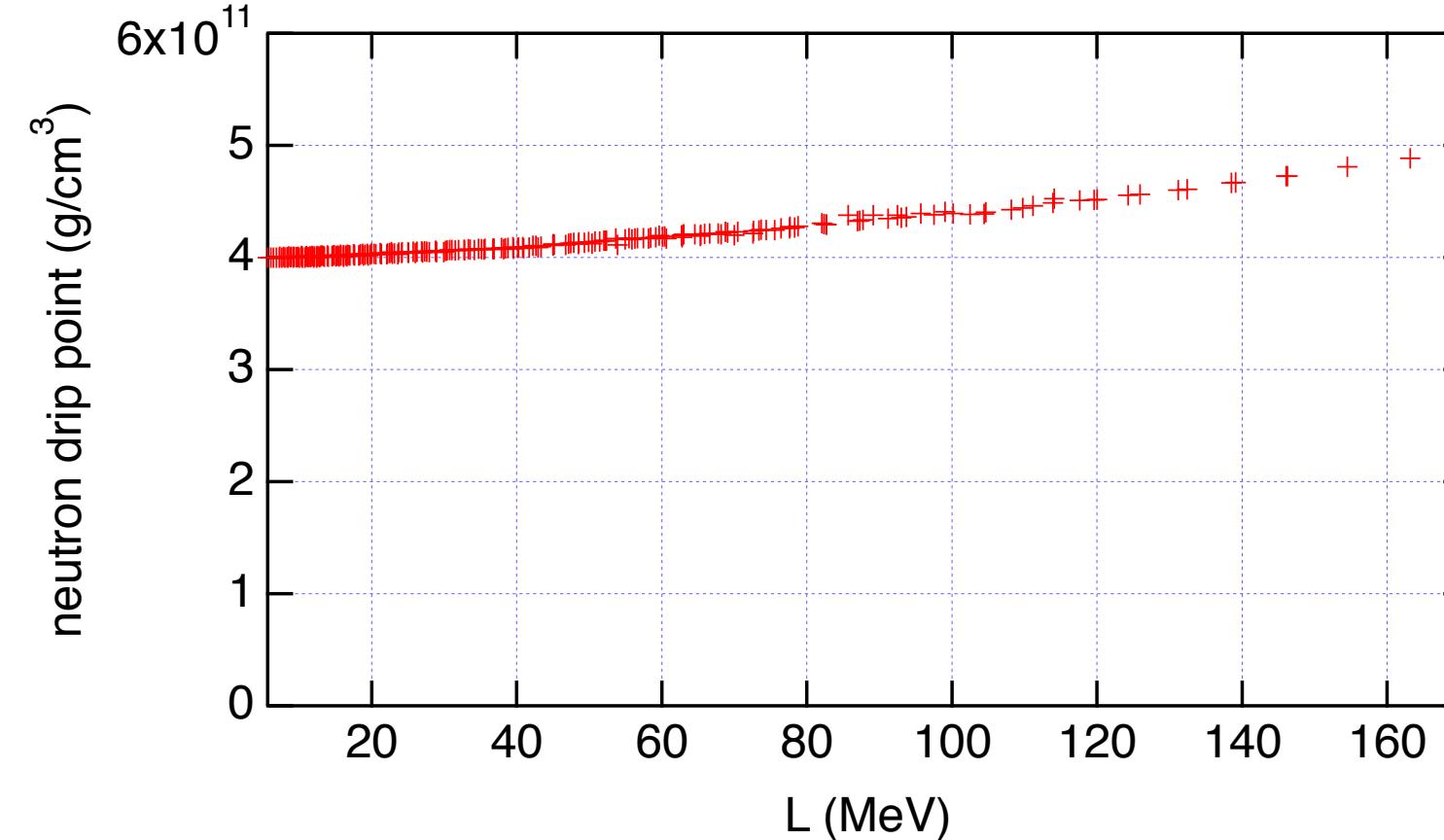


neutron star crust

nuclei in neutron-star crusts

neutron drip point (NDP)

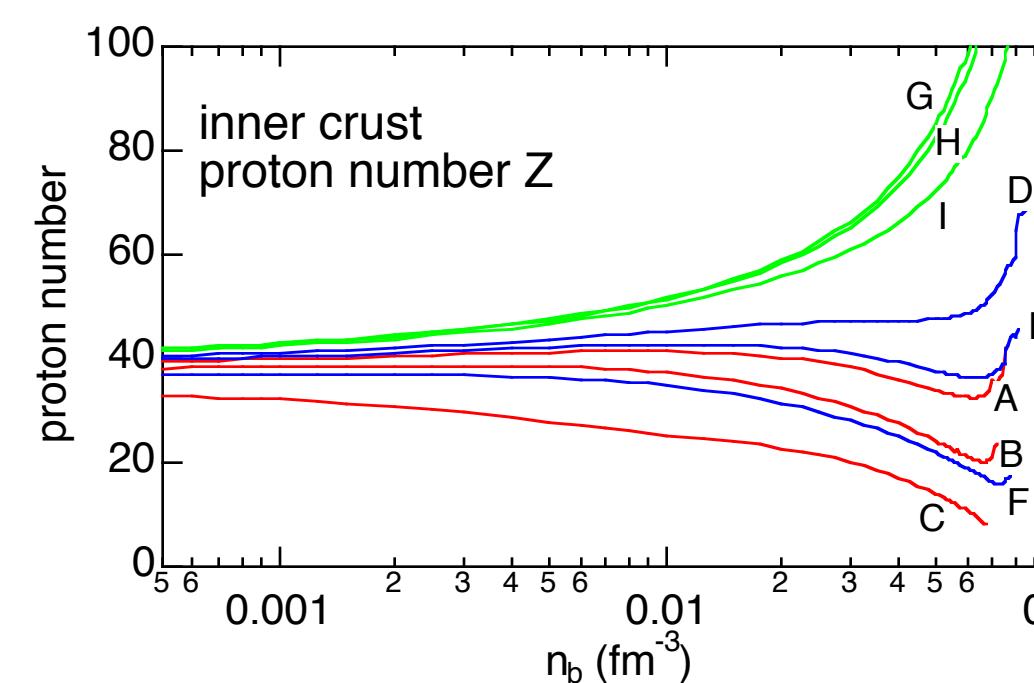
onset density of neutron drip
boundary of outer and inner crust



NDP slightly increases with L.

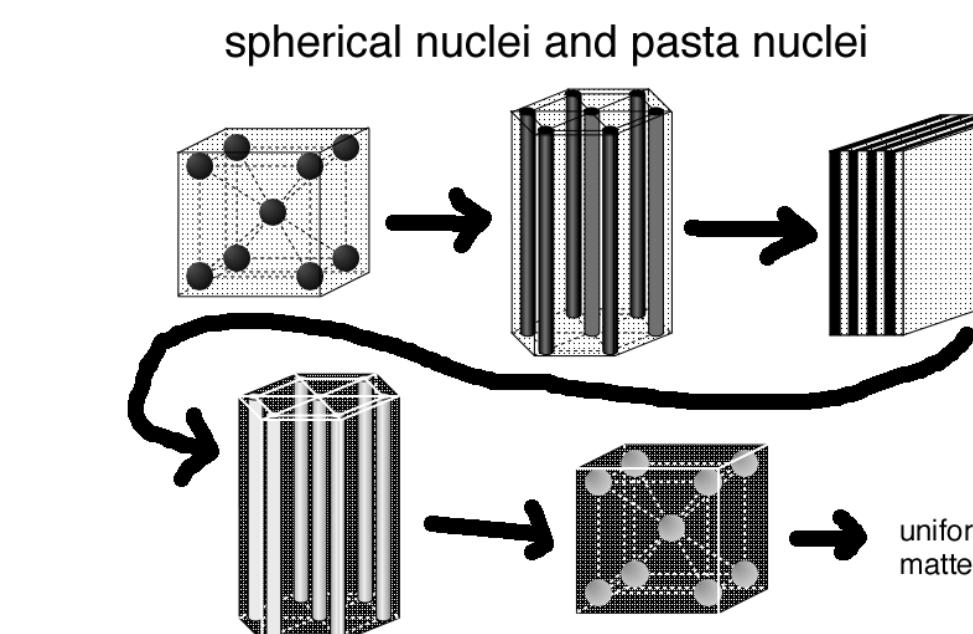
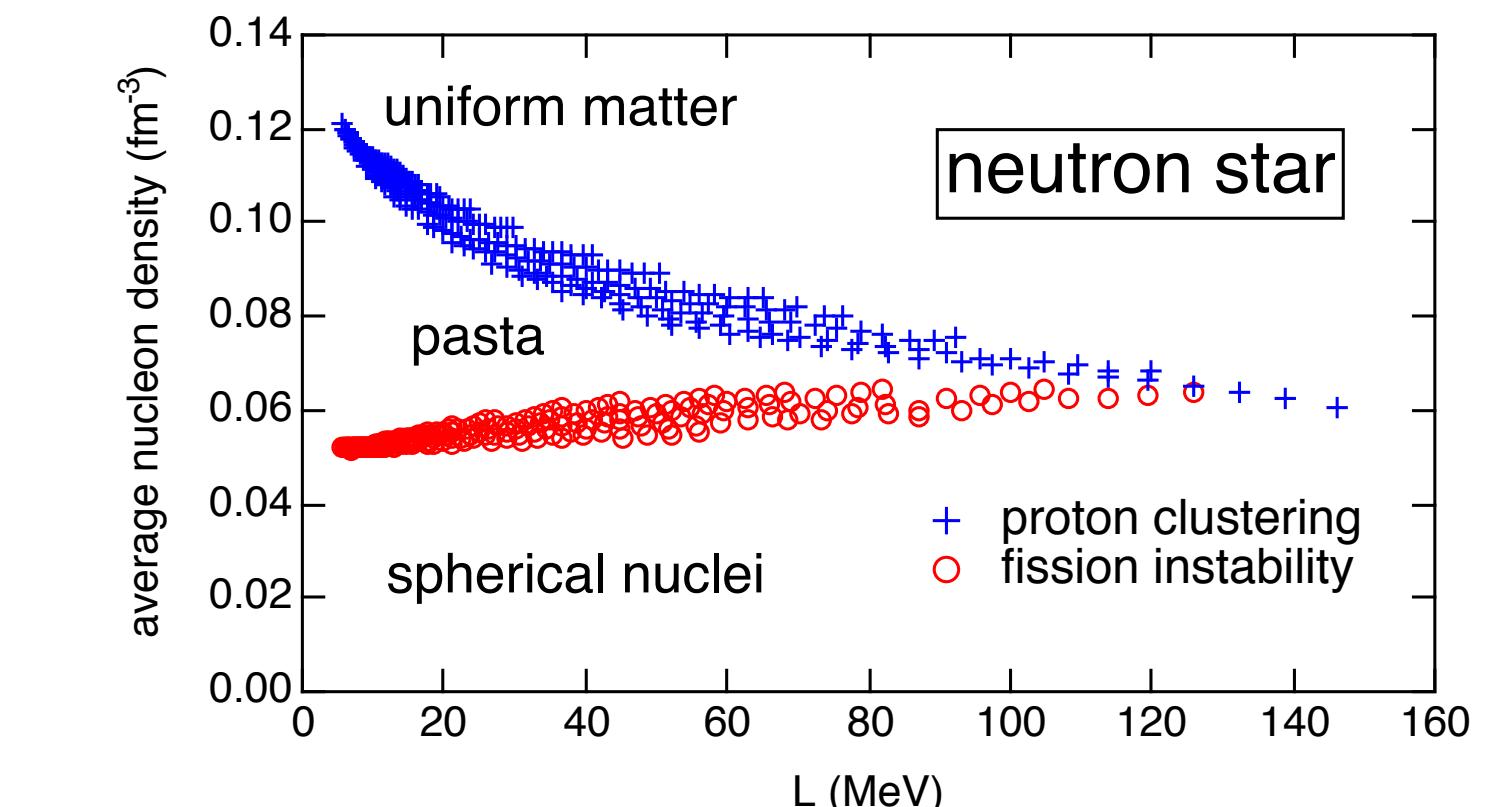
Inner crust nuclei

Z and Y_p decrease with L.



For large L, S(n) at $n < n_0$ is small
so that nuclei become more neutron-rich.

crust-core boundary density
decrease with L.



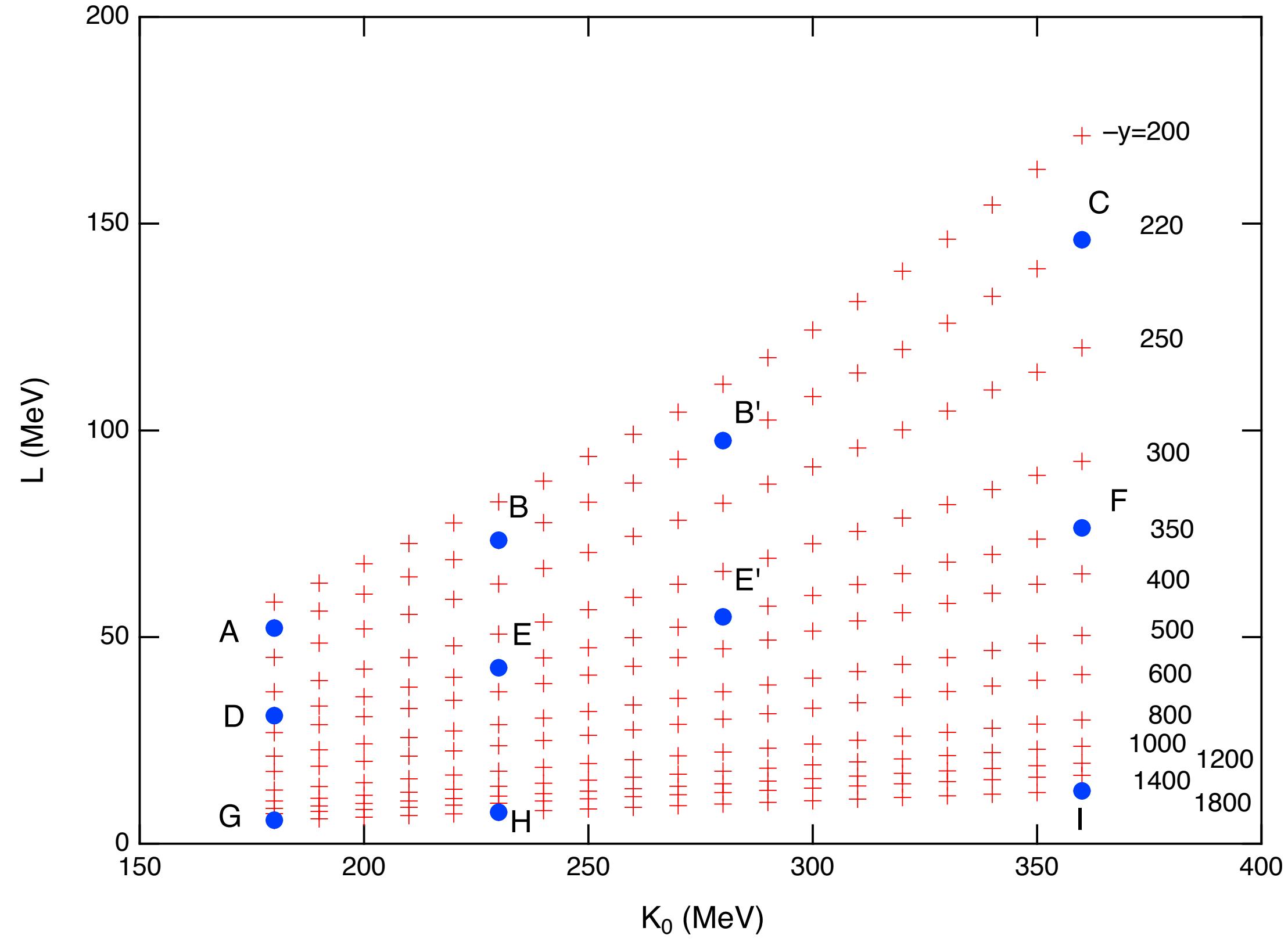
K.Oyamatsu, NPA561, 431 (1993)

Existence of pasta nuclei depends on the EOS.

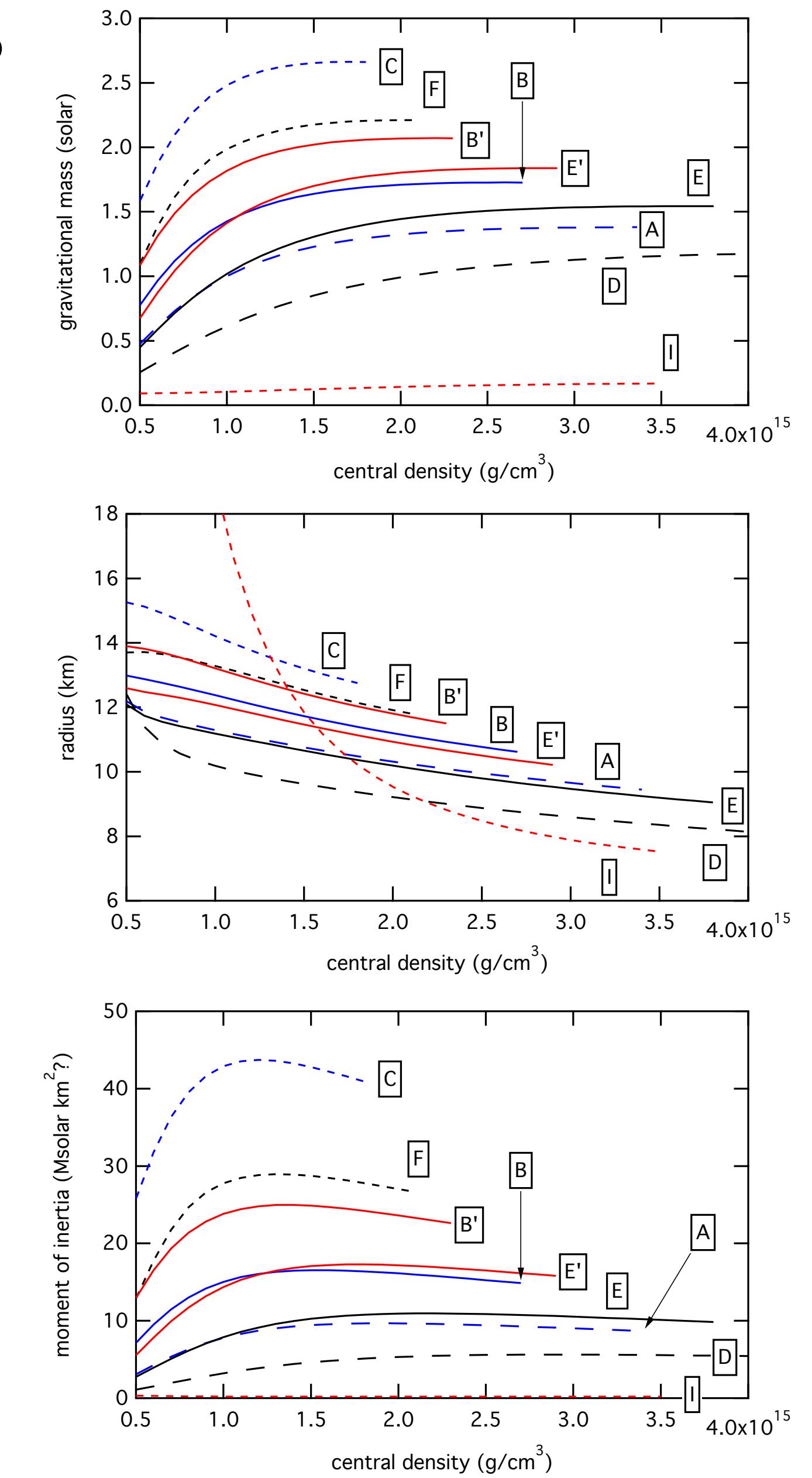
Neutron star mass

Neutron Star with typical EOS's

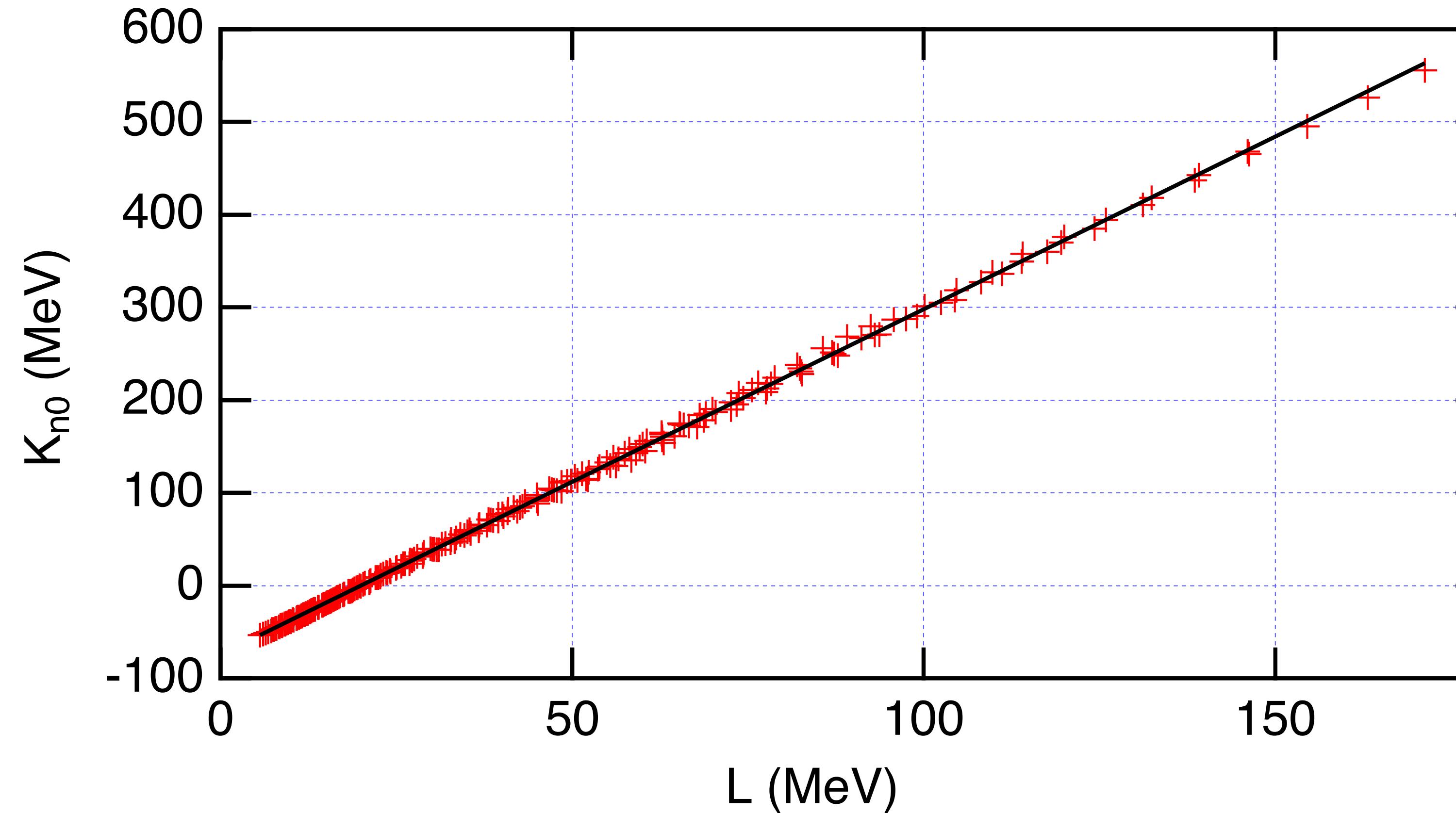
(K_0, L) and y values for typical EOS's



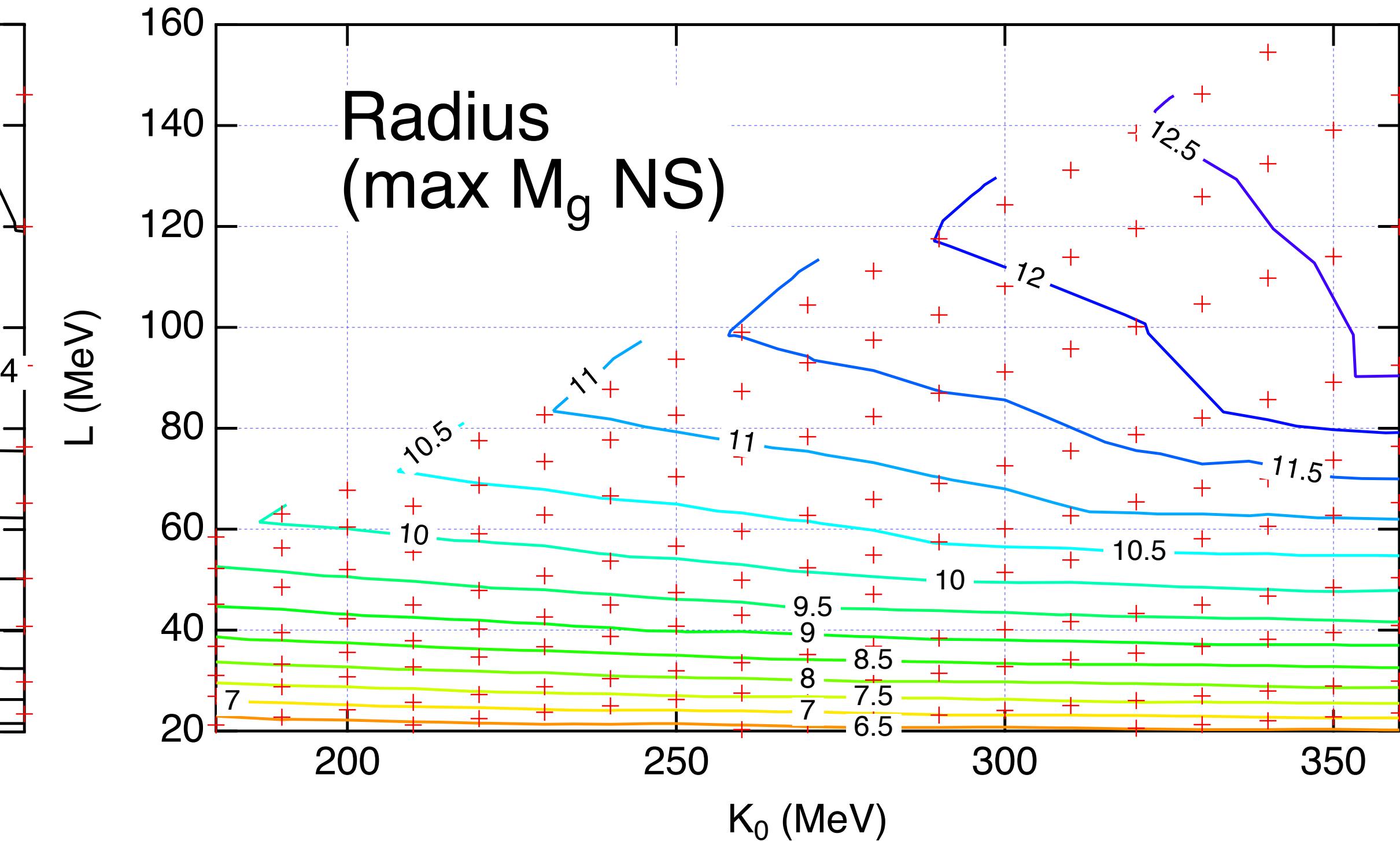
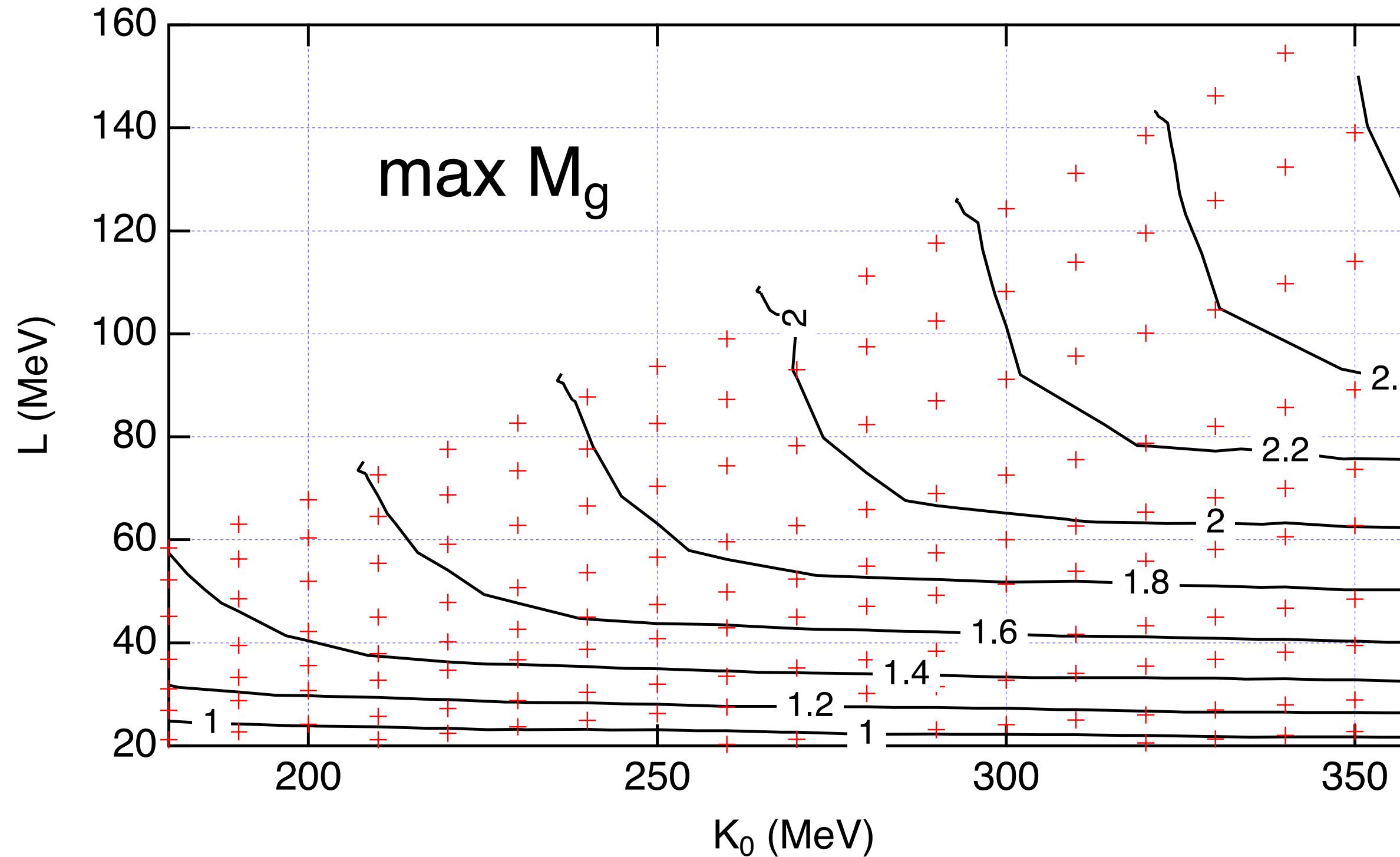
The neutron star mass increases with L , and also with K_0 .
EOS's G and H (smallest L) can't support a neutron star.



Incompressibility of neutron matter $K_{n0} > 0$,
then $L > 20$ MeV.



Mass and radius of max Mg neutron Star with OI EOS family



$L > 20$ MeV from $K_{n0} > 0$.

EOS's with $L > 40$ MeV can support 1.4 solar mass star.

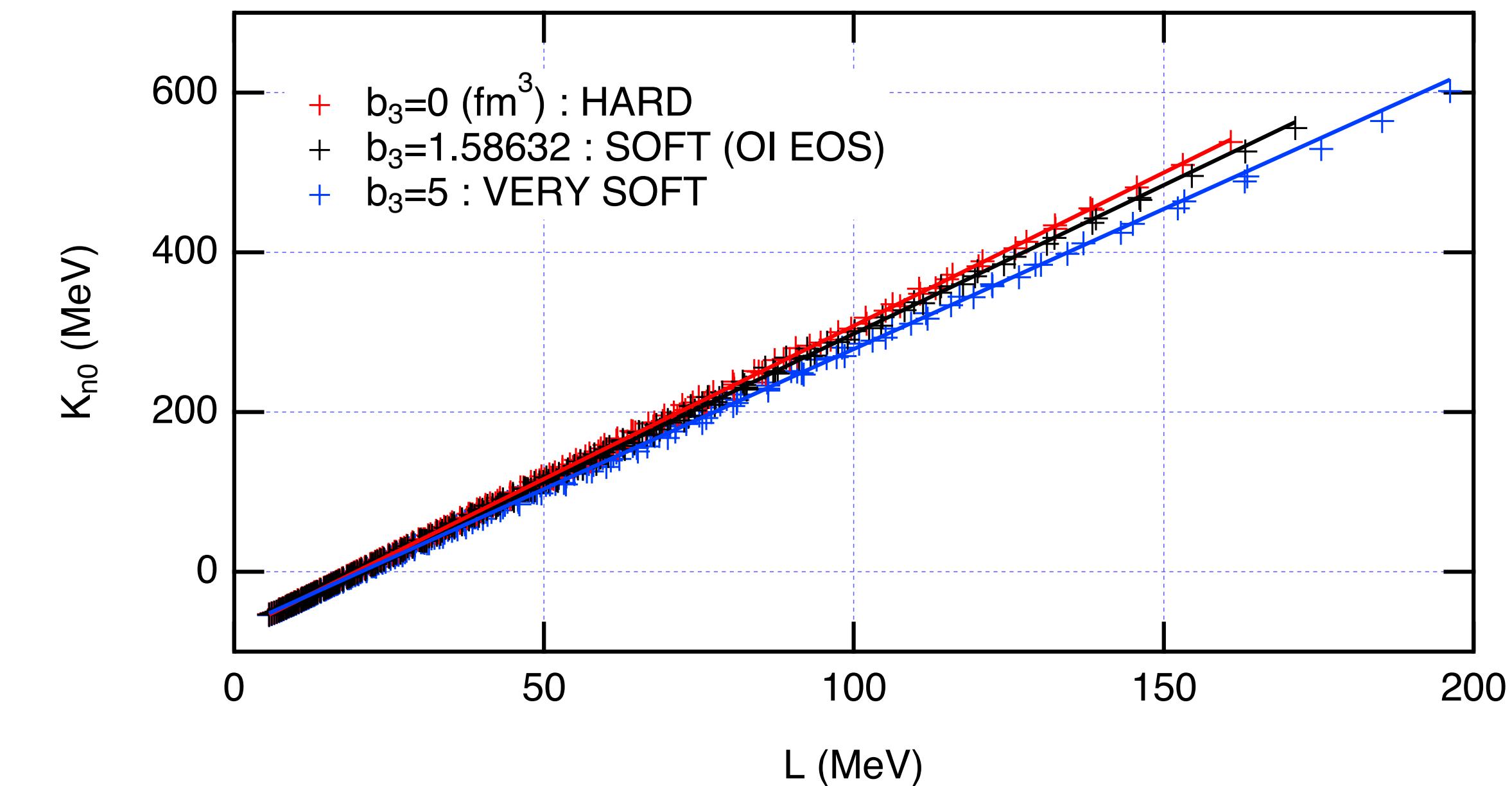
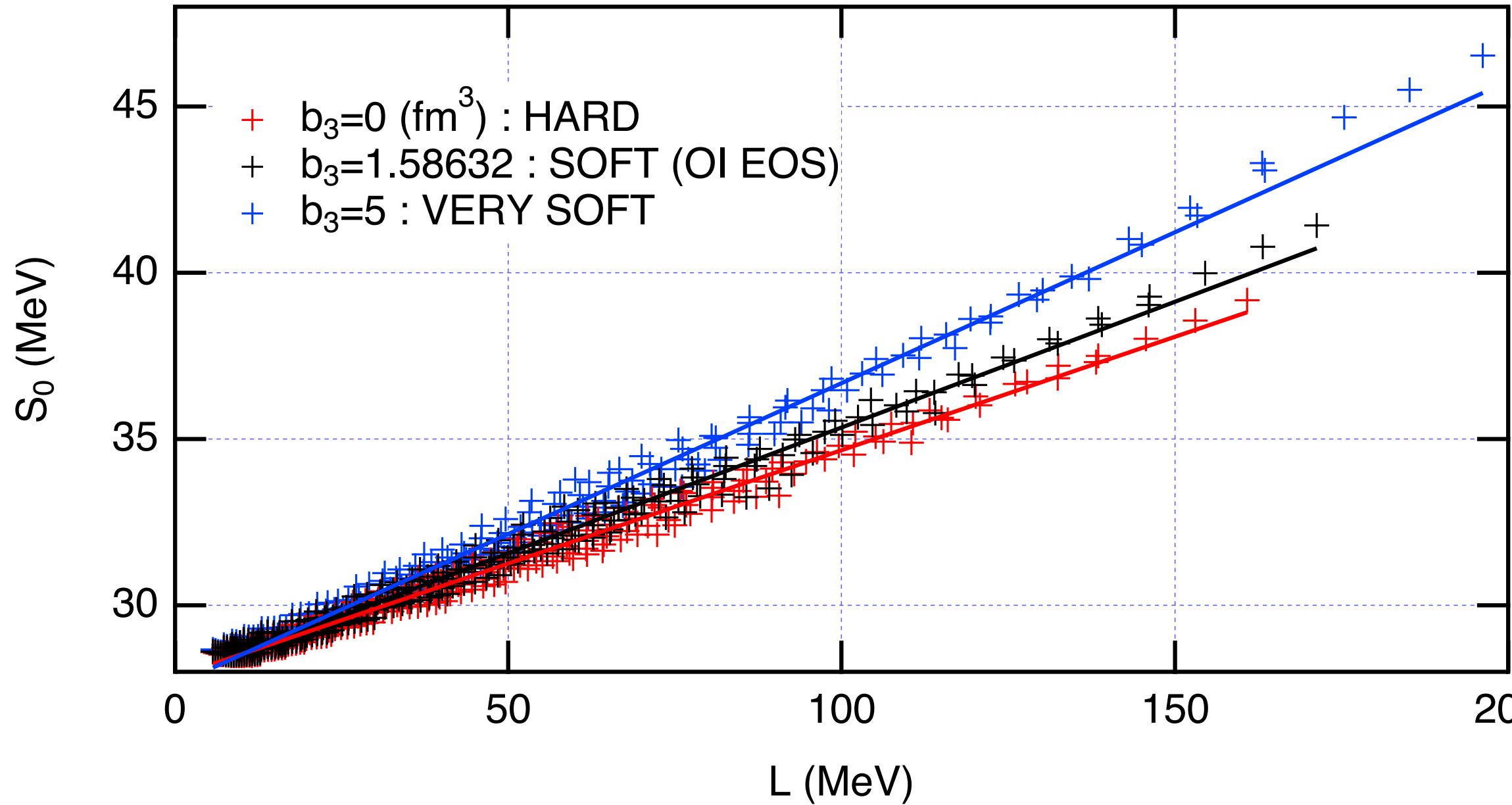
Summary

- OI EOS family describes the structure of neutron rich nuclei and neutron stars as function of (K_0, L) related to nuclear compressibility.
- The structure of neutron rich nuclei and neutron star crusts are mainly dominated by L .
 - This is the result of nuclear saturation properties.
- The neutron star mass and radius increase with L and also with K_0 .^{*}
 - This depends on the behavior of high density EOS ($b_3=1.59$).

* For low mass neutron stars,
see Sotani, Iida, Oyamatsu and Ohnishi, Prog. Theor. Exp. Phys. (2014) 051E01.

NEXT : High Density => Oyamatsu-Sotani-Iida EOS family

- Empirical description of high density EOS using different value for 3 body energy coefficient b_3 in the potential energy density.
- Each EOS is labeled with (K_0, L, b_3) .
- Values of saturation parameters are almost the same as OI EOS's ($b_3=1.59$).
 - $L > 20$ MeV from $K_{n0}>0$ independently of b_3 .
- The choice of b_3 value does not affect nuclei and crusts very much but will alter core structure.



$$v_n(n) = b_1 n^2 + \frac{b_2 n^3}{1 + b_3 n}$$