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# **Microscopic studies on nuclear spin-isospin properties** *--- a personal perspective on covariant density functional theory*

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*September 14, 2016*



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# Acknowledgments



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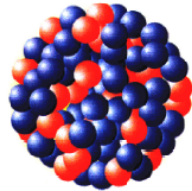
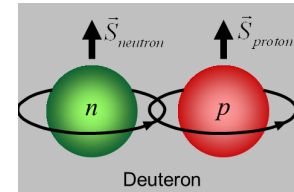


Y. Tanizaki, P.W. Zhao

# Research interests and tools

Research interests: **Spin and Isospin properties in atomic nuclei**

**Spin** and **Isospin** are essential degrees of freedom in nuclear physics

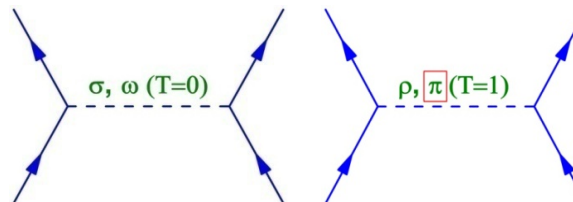


*Relevant studies in nuclear physics × nuclear astrophysics × particle physics*

Research tools: **Covariant density functional theory (CDFT)**

- Fundamental: **Kohn-Sham** Density Functional Theory
- Scheme: **Yukawa** meson-exchange nuclear interactions

$$\begin{aligned} \mathcal{L} = & \bar{\psi} \left[ i\gamma^\mu \partial_\mu - M - g_\sigma \sigma - \gamma^\mu \left( g_\omega \omega_\mu + g_\rho \vec{\tau} \cdot \vec{\rho}_\mu + e \frac{1 - \tau_3}{2} A_\mu \right) - \frac{f_\pi}{m_\pi} \gamma_5 \gamma^\mu \partial_\mu \vec{\pi} \cdot \vec{\tau} \right] \psi \\ & + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 - \frac{1}{4} \Omega^{\mu\nu} \Omega_{\mu\nu} + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu - \frac{1}{4} \vec{R}_{\mu\nu} \cdot \vec{R}^{\mu\nu} + \frac{1}{2} m_\rho^2 \vec{\rho}^\mu \cdot \vec{\rho}_\mu \\ & + \frac{1}{2} \partial_\mu \vec{\pi} \cdot \partial^\mu \vec{\pi} - \frac{1}{2} m_\pi^2 \vec{\pi} \cdot \vec{\pi} - \frac{1}{4} F^{\mu\nu} F_{\mu\nu} \end{aligned}$$

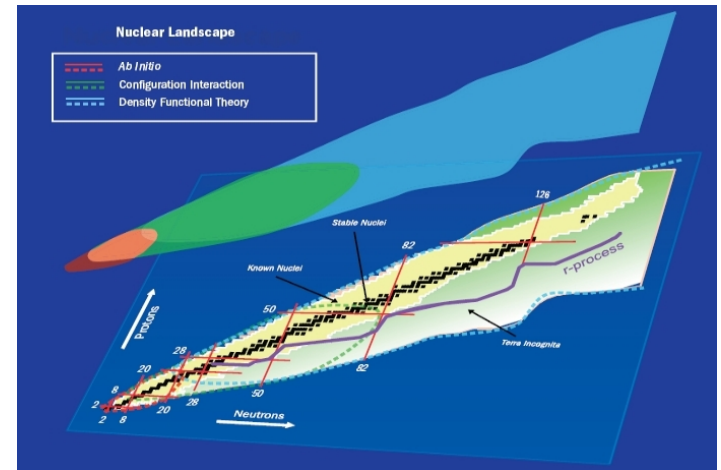


Nobel Prize 1949  
Nobel Prize 1998

# Covariant density functional theory

## Why DFT?

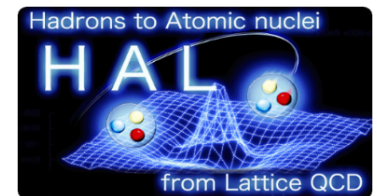
- applicable to almost whole nuclear chart (*ground states* × *excited states*)
- no other method achieves comparable accuracy at the similar computational costs



<http://www.unedf.org/>

## Why covariant (relativistic)?

- Dirac equation  
consistent treatment of **spin** d.o.f. & nuclear saturation properties (**3-body effect**)
- Lorentz covariant symmetry  
unification of time-even and **time-odd** components
- Effective Lagrangian  
connections to underlying theories, QCD at low energy



cf. HAL QCD Collaboration

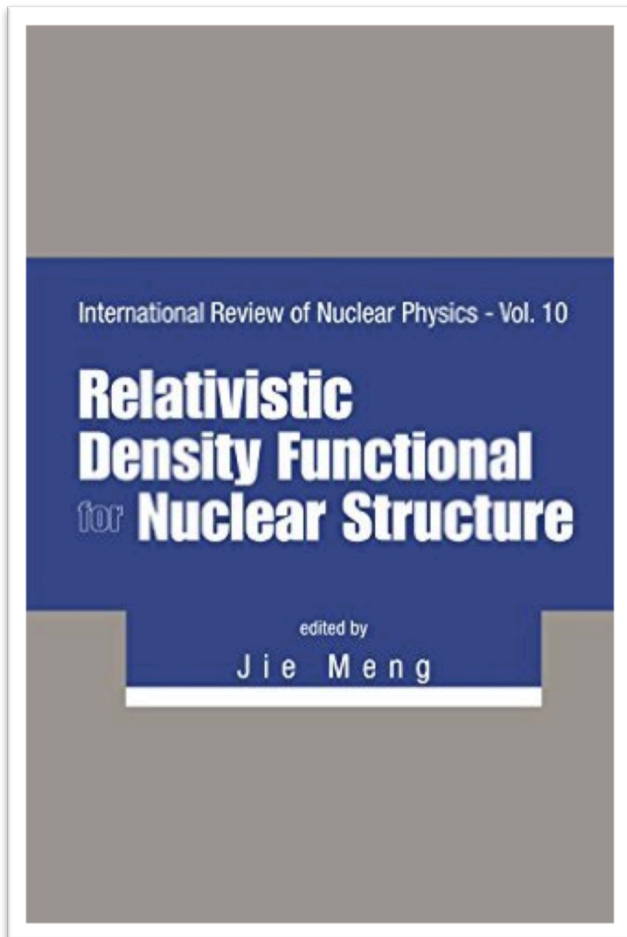


# Covariant density functional theory

From Walecka model in 1974 ..... to now

cf. S.-G. Zhou's plenary talk

**in Jan 2016**



- ❑ Concept of Covariant Density Functional Theory ([P Ring](#))
- ❑ Relativistic Mean-Field Theory ([J Meng](#), [P Ring](#) and [P W Zhao](#))
- ❑ Relativistic Mean Field Description of Exotic Nuclei ([J Meng](#), [P Ring](#), [P W Zhao](#) and [S G Zhou](#))
- ❑ Relativistic Hartree–Fock–Bogoliubov Theory: Ground States and Excitations ([W H Long](#), [J Meng](#) and [N Van Giai](#))
- ❑ Superheavy Nuclei and Fission Barriers ([B N Lu](#), [J Zhao](#), [E G Zhao](#) and [S G Zhou](#))
- ❑ Relativistic Symmetries in Nuclear Single-Particle Spectra ([J Y Guo](#), [H Z Liang](#), [J Meng](#) and [S G Zhou](#))
- ❑ Structure of Hypernuclei in Relativistic Approaches ([K Hagino](#) and [J M Yao](#))
- ❑ Rotating Nuclei: From Ground State to the Extremes of Spin and Deformation ([A V Afanasjev](#))
- ❑ Novel Rotational Excitations ([J Meng](#), [S Q Zhang](#) and [P W Zhao](#))
- ❑ Small Amplitude Motion ([N Paar](#) and [Y Niu](#))
- ❑ Nuclear Shell Structure and Response with Quasiparticle-Vibration Coupling ([E Litvinova](#) and [P Ring](#))
- ❑ Beyond the Relativistic Mean-Field Approximation — Collective Correlations ([Z P Li](#), [T Nikšić](#), [D Vretenar](#) and [J M Yao](#))
- ❑ Heavy Element in Astrophysical Nucleosynthesis ([B H Sun](#) and [Z M Niu](#))
- ❑ Relativistic Density Functional Theory for Finite Nuclei and Neutron Stars ([J Piekarewicz](#))
- ❑ Relativistic Versus Non-Relativistic Mean Field ([P-G Reinhard](#))

# Our studies on pseudospin symmetry

Physics Reports 570 (2015) 1–84



Contents lists available at ScienceDirect

Physics Reports

journal homepage: [www.elsevier.com/locate/physrep](http://www.elsevier.com/locate/physrep)



Hidden pseudospin and spin symmetries and their origins in atomic nuclei



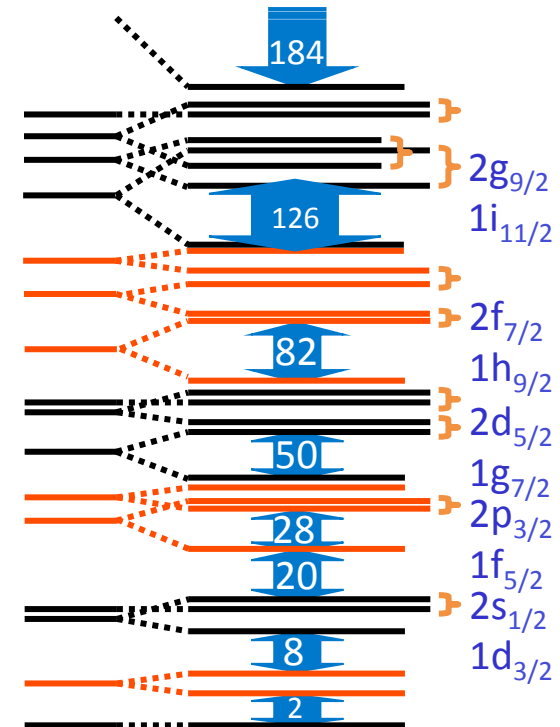
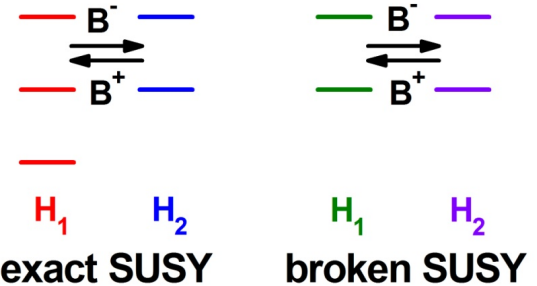
CrossMark

Haozhao Liang<sup>a,b</sup>, Jie Meng<sup>a,c,d,\*</sup>, Shan-Gui Zhou<sup>e,f</sup>

with 58 figs, 10 tables, & 378 refs

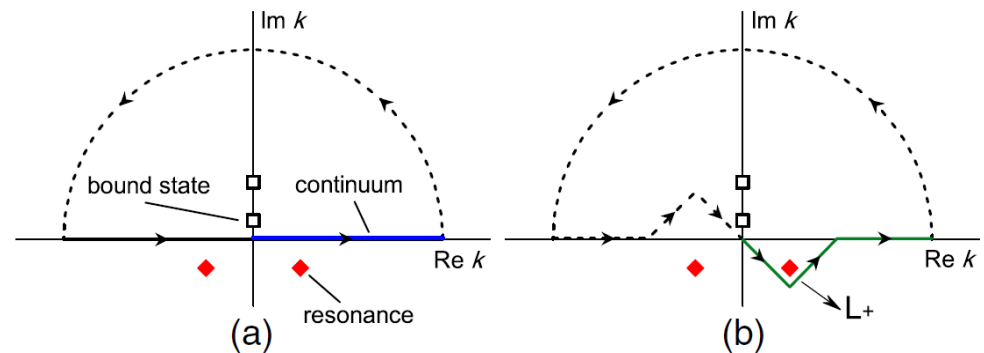
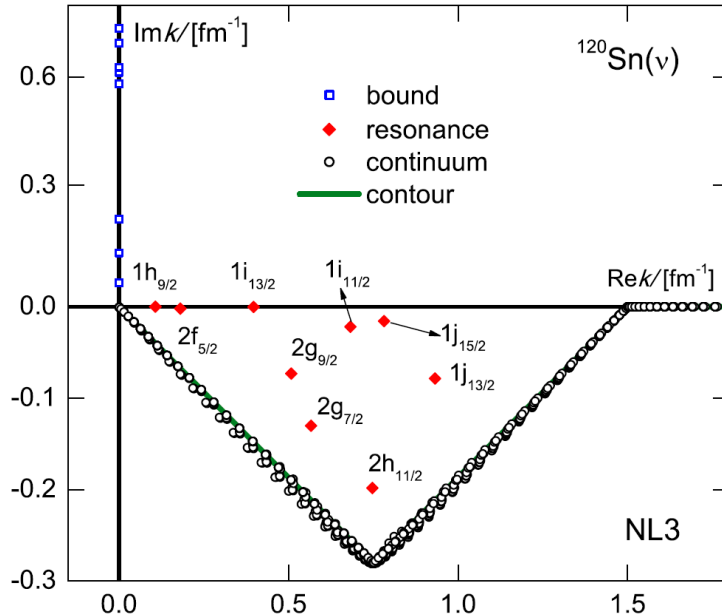
- **Pseudospin symmetry**  $\begin{cases} (n-1, l+2, j=l+3/2) \\ (n, l, j=l+1/2) \end{cases}$   
near degeneracy between  
----- *a relativistic symmetry*

- The origin of PSS deeply hidden in original Hamiltonian  $H_1$  can be traced in its SUSY partner Hamiltonian  $H_2$ .
- $\Delta E_{\text{PSO}}$  can be understood in an explicit and quantitative way.



# Our studies on single-particle resonances

## ➤ Resonances in relativistic scheme



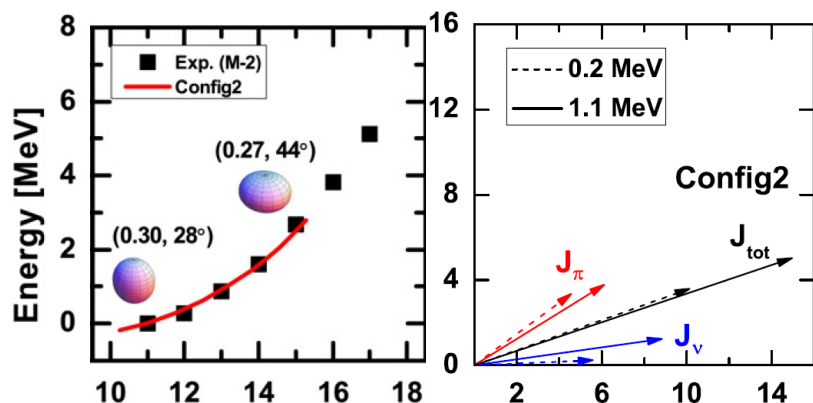
Li, Shi, Guo, Niu, HZL, *Phys. Rev. Lett.* **117**, 062502 (2016)

- solving nucleon equation of motion in complex momentum space → single-particle resonances in relativistic scheme
- This method is not only very effective for narrow resonances, but also can be reliably applied to broad resonances.

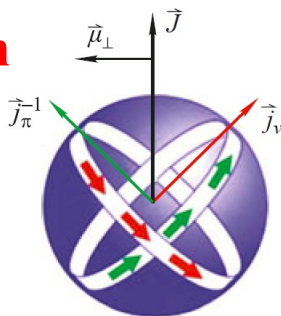
→ halo nuclei

# Our studies on (anti-)magnetic rotations

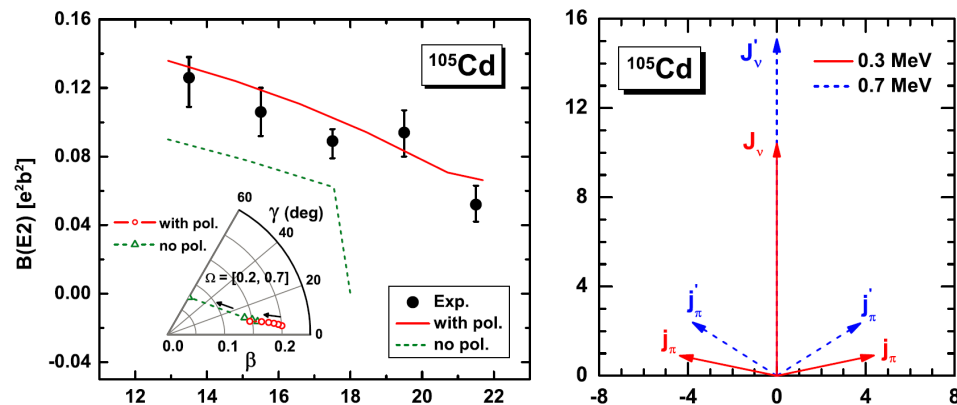
## ➤ Magnetic rotation in $^{60}\text{Ni}$



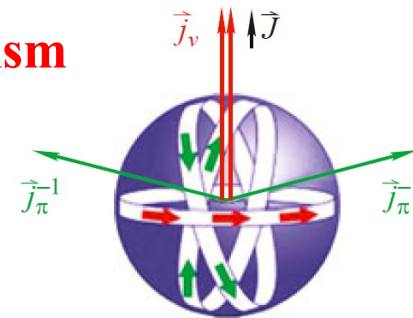
**shears mechanism**



## ➤ Anti-magnetic rotation in $^{105}\text{Cd}$



**two-shears-like mechanism**



Zhao et al., *Phys. Lett. B* **699**, 181 (2011); *Phys. Rev. Lett.* **107**, 122501 (2011)

- ❑ 2D tilted axis cranking model with CDFT → nuclear rotations
- ❑ Shears and two-shears-like mechanisms are described and understood self-consistently and microscopically.

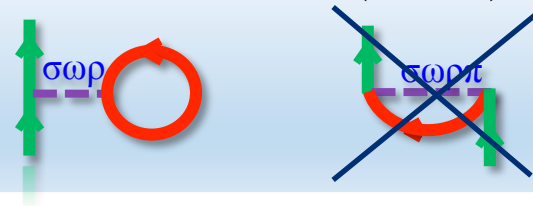
# Covariant density functional theory

From Walecka model in 1974 ..... to now

CDFT achieves a great success in nuclear **ground-state** and **excited-state** properties

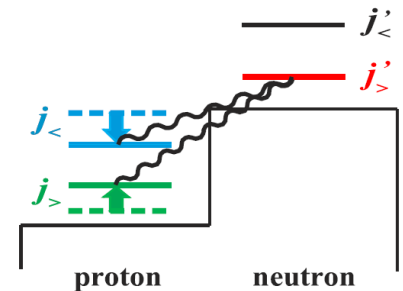
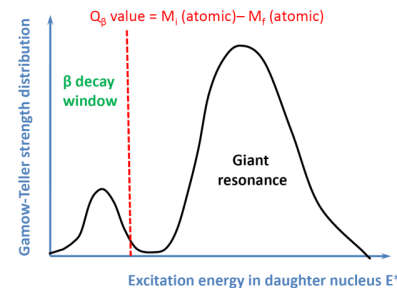
For simplicity, in most of versions ← relativistic mean-field (**RMF**) theory

- with local Hartree terms ✓
- without non-local Fock terms ✗



However, “Hartree terms only” show limitations in

- properties in spin-isospin channel
- effects of tensor interaction

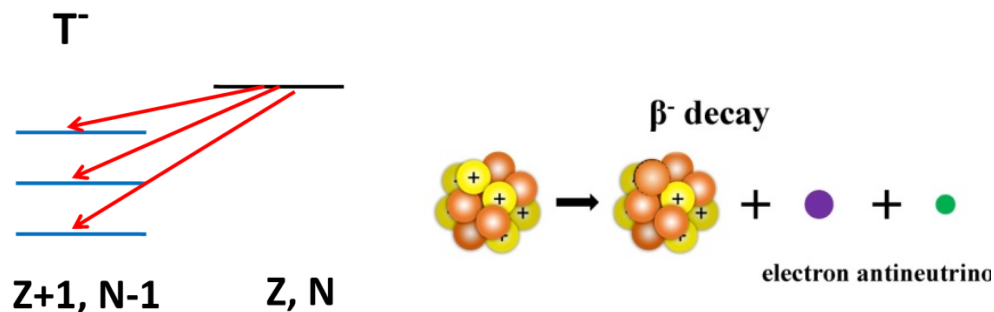


Our works: both **Hartree** and **Fock** terms

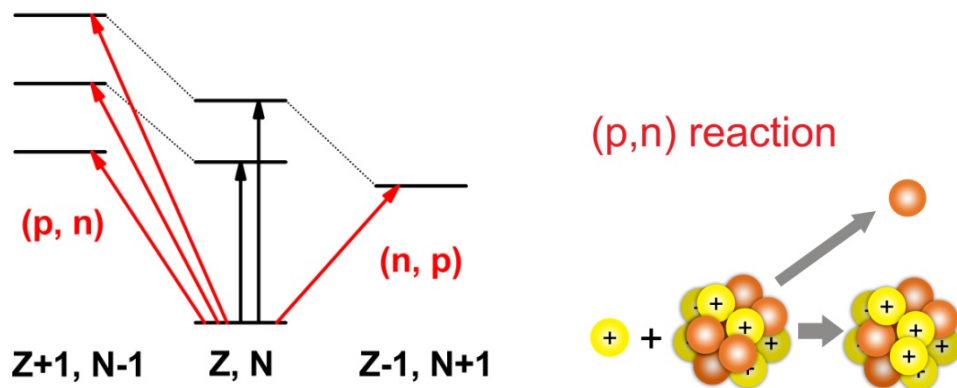
# Nuclear spin-isospin properties

## Nuclear spin-isospin excitations

### ➤ $\beta$ -decays in nature



### ➤ charge-exchange reactions in lab



Bell  
Hammers  
(iron, wooden)  
Sounds of the Bell

Nucleus  
Probes  
 $(e, \gamma, \alpha, p, n)$   
Modes of collective  
vibrations of nucleus



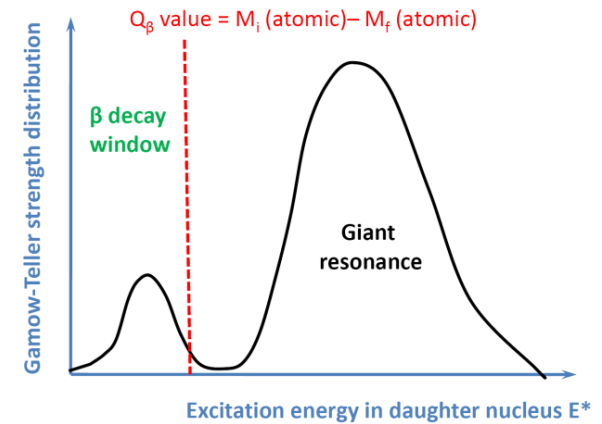
# Spin-isospin excitations

These excitations are important to understand

"What are the spin and isospin properties of nuclear force and nuclei?" (*nuclear physics*)

"Where and how does the rapid neutron-capture process (*r*-process) happen?" (*nuclear astrophysics*)

"Does Cabibbo-Kobayashi-Maskawa matrix satisfy the unitary condition?" (*particle physics*)



**Key exp. @**

RIKEN

RCNP

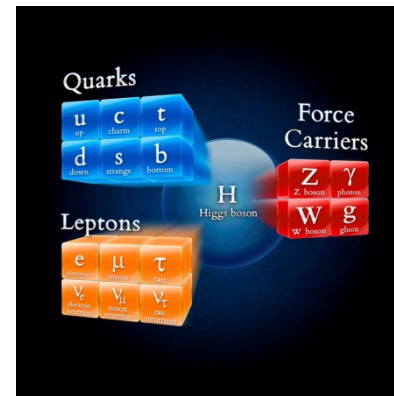
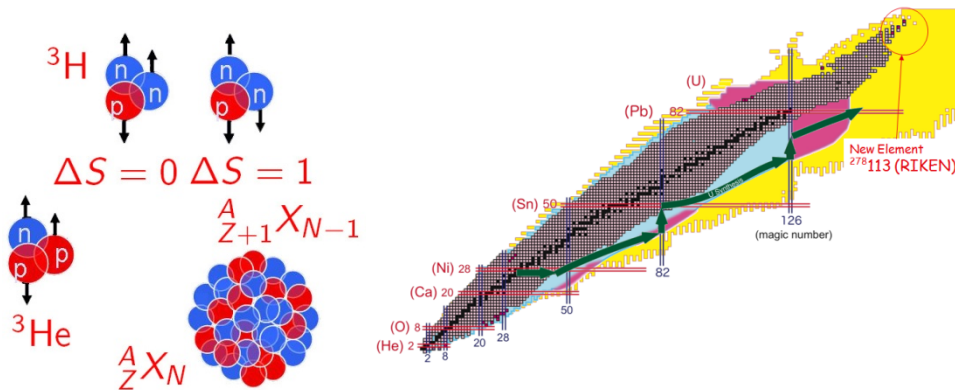
MSU

GSU

TRIUMF

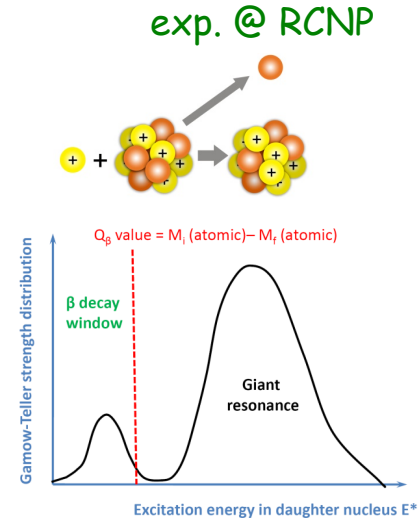
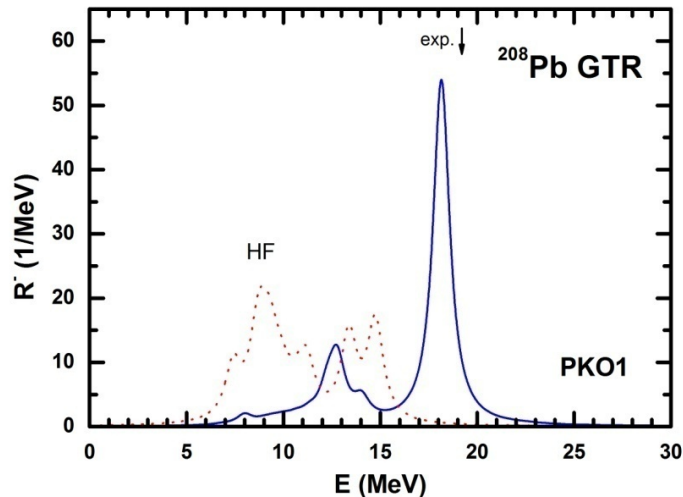
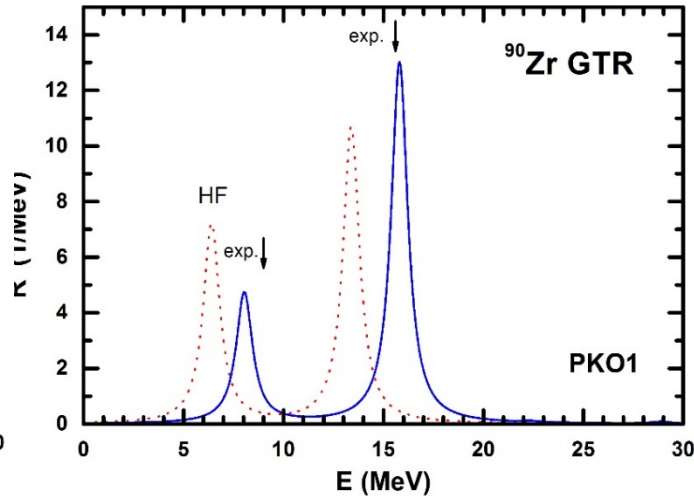
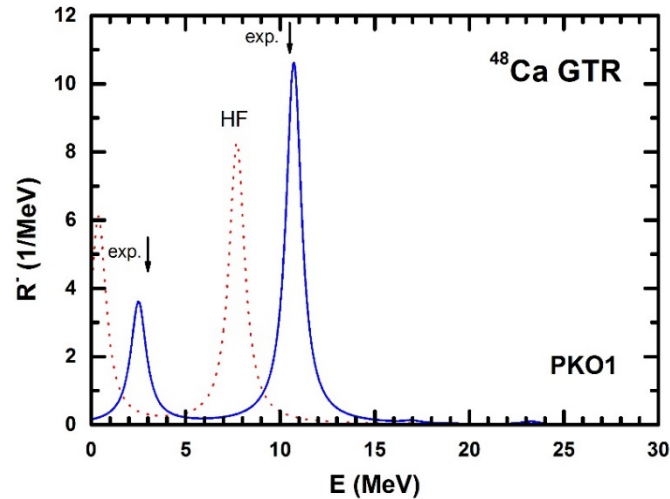
CERN

.....



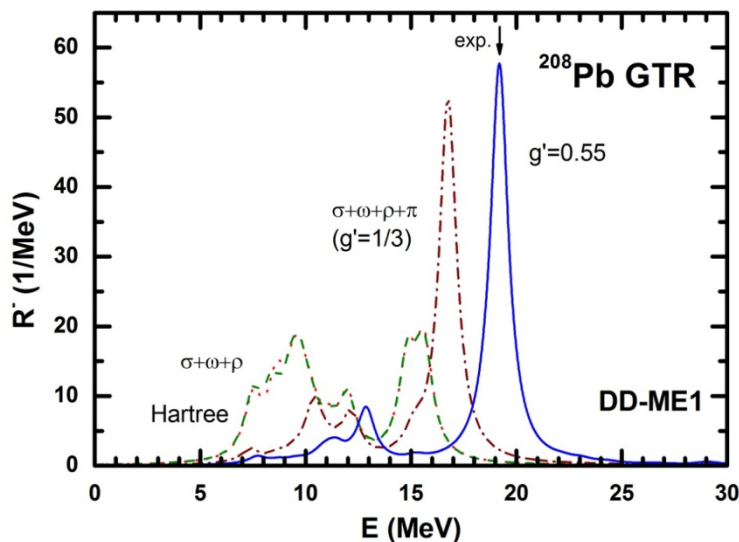
# Gamow-Teller resonances

CDFT+RPA for Gamow-Teller resonances ( $\Delta S = 1, \Delta L = 0, J^\pi = 1^+$ )



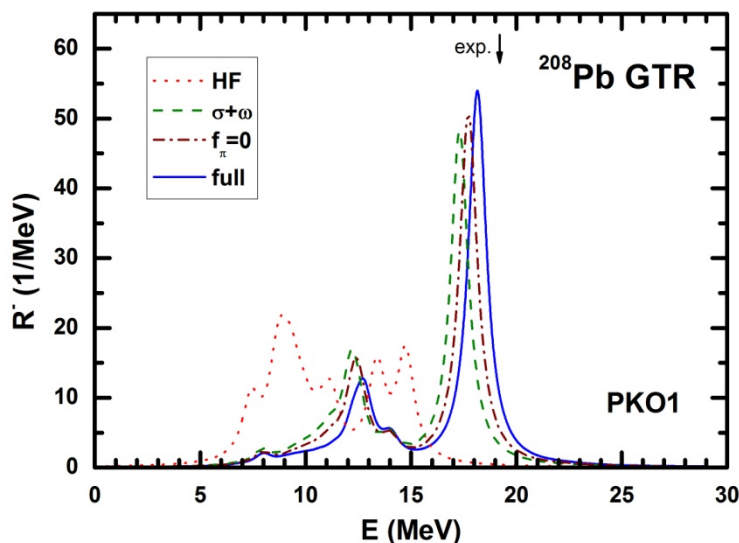
- ✓ GTR excitation energies can be reproduced in a fully self-consistent way.
- New and most important ingredient:  
**Fock terms** in CDFT

# Physical mechanisms of GTR



## With only Hartree terms

- No contribution from isoscalar  $\sigma$  and  $\omega$  mesons, because exchange terms are missing.
- $\pi$ -meson is dominant in this resonance.
- $g'$  has to be re-fitted to reproduce the experimental data.



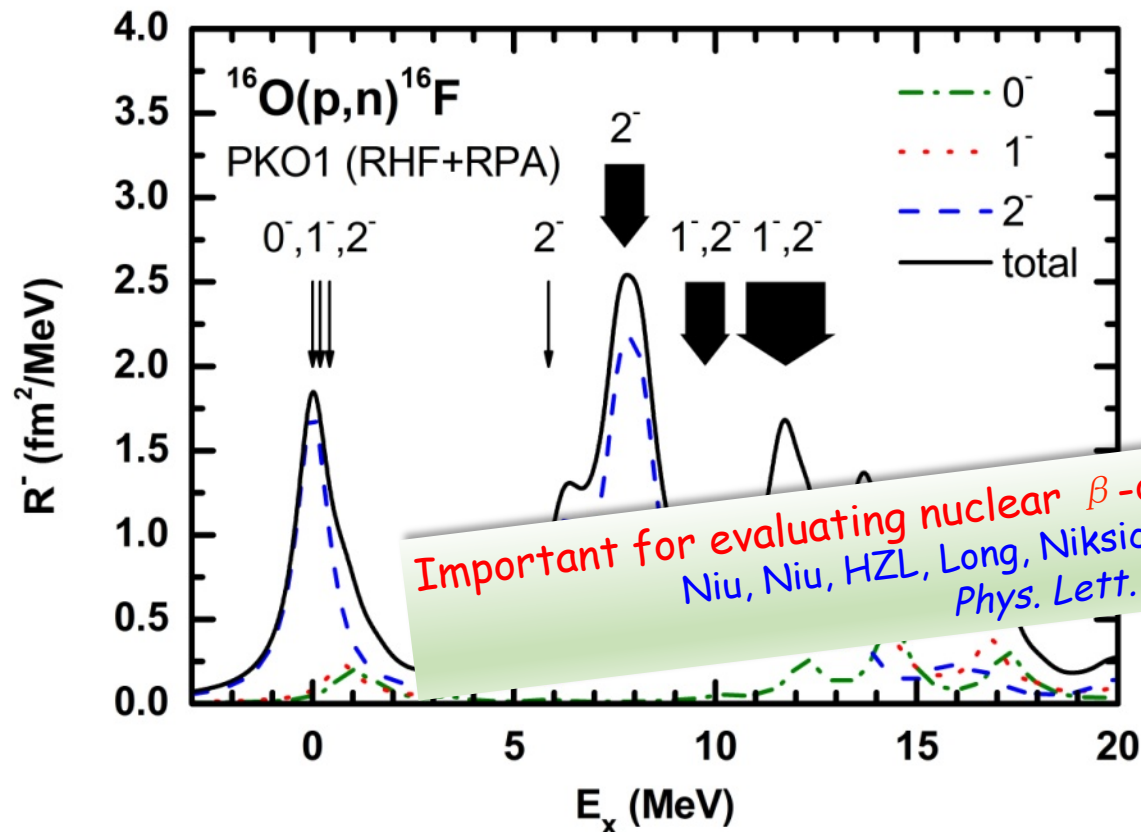
## With both Hartree & Fock terms

- Isoscalar  $\sigma$  and  $\omega$  mesons play an essential role via the exchange terms.
- $\pi$ -meson plays a minor role.
- $g' = 1/3$  is kept for self-consistency.

HZL, Giai, Meng, *Phys. Rev. Lett.* **101**, 122502 (2008)  
 HZL, Zhao, Ring, Roca-Maza, Meng, *Phys. Rev. C* **86**, 021302(R) (2012)

# Spin-dipole resonances

CDFT+RPA for spin-dipole resonances ( $\Delta S = 1, \Delta L = 1, J^\pi = 0^-, 1^-, 2^-$ )



(Exp.) Wakasa *et al.*, PRC 84, 014614 (2011); (Theory) HZL, Zhao, Meng, Phys. Rev. C 85, 064302 (2012)

□ a crucial test for the theoretical predictive power

# CKM matrix and its unitarity test

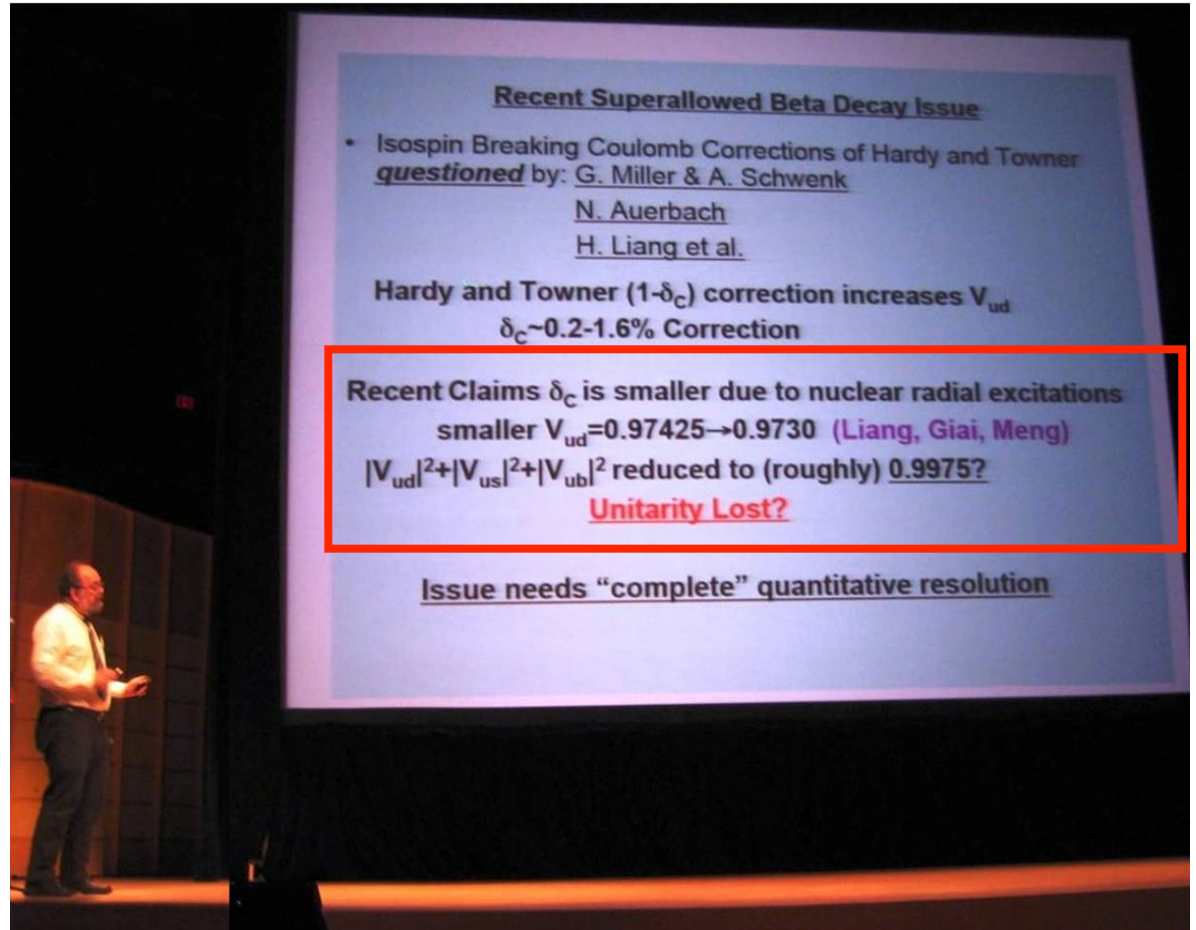
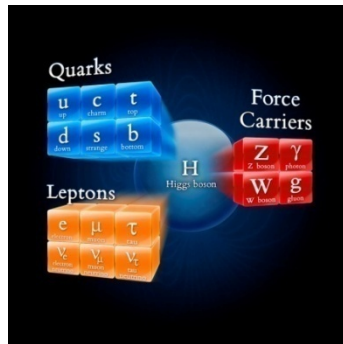
## Cabibbo-Kobayashi-Maskawa matrix



Nobel Prize 2008

"There exist *at least* three families of quarks in nature."

"Only three?"



Plenary talk in INPC2010 "Precision Electroweak Tests of the Standard Model" by Professor William Marciano

# CKM matrix and its unitarity test

## Cabibbo-Kobayashi-Maskawa matrix

- quark eigenstates of weak interaction  $\longleftrightarrow$  quark mass eigenstates
- unitarity of CKM matrix  $\longleftrightarrow$  test of Standard Model

$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| & |V_{ts}| & |V_{tb}| \end{pmatrix} = \begin{pmatrix} 0.97425 \pm 0.00022 & 0.2252 \pm 0.0009 & 0.00415 \pm 0.00049 \\ 0.230 \pm 0.011 & 1.006 \pm 0.023 & 0.0409 \pm 0.0011 \\ 0.0084 \pm 0.0006 & 0.0429 \pm 0.0026 & 0.89 \pm 0.07 \end{pmatrix}$$

## Unitarity test Particle Data Group 2014

- the most precise test comes from  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2$
- the most precise  $|V_{ud}|$  comes from nuclear  $0^+ \rightarrow 0^+$  superallowed  $\beta$  transitions

## Nuclear superallowed $\beta$ transitions

$$|M_F|^2 = |\langle f | T_+ | i \rangle|^2 = |M_0|^2(1 - \delta_c)$$

- experimental measurements
- theoretical corrections (isospin symmetry-breaking corrections)

"Only three families of quarks in nature?"



# Isospin symmetry-breaking corrections $\delta_c$

◆ Isospin symmetry-breaking corrections  $\delta_c$ . All values are expressed in %.

	with Fock terms			w/o Fock terms			
	PKO1	PKO2	PKO3	DD-ME1	DD-ME2	NL3	TM1
$^{10}\text{C} \rightarrow ^{10}\text{B}$	0.082	0.083	0.088	0.149	0.150	0.124	0.133
$^{14}\text{O} \rightarrow ^{14}\text{N}$	0.114	0.134	0.110	0.189	0.197	0.181	0.159
$^{18}\text{Ne} \rightarrow ^{18}\text{F}$	0.270	0.277	0.288	0.424	0.430	0.344	0.373
$^{26}\text{Si} \rightarrow ^{26}\text{Al}$	0.176	0.176	0.184	0.252	0.252	0.213	0.226
$^{30}\text{S} \rightarrow ^{30}\text{P}$	0.497	0.550	0.507	0.612	0.633	0.551	0.648
$^{34}\text{Ar} \rightarrow ^{34}\text{Cl}$	0.268	0.281	0.267	0.368	0.376	0.438	0.320
$^{38}\text{Ca} \rightarrow ^{38}\text{K}$	0.313	0.330	0.313	0.431	0.441	0.390	0.572
$^{42}\text{Ti} \rightarrow ^{42}\text{Sc}$	0.384	0.387	0.390	0.515	0.523	0.436	0.443
$^{26}\text{Al} \rightarrow ^{26}\text{Mg}$	0.139	0.138	0.144	0.198	0.198	0.172	0.179
$^{34}\text{Cl} \rightarrow ^{34}\text{S}$	0.234	0.242	0.231	0.302	0.307	0.289	0.267
$^{38}\text{K} \rightarrow ^{38}\text{Ar}$	0.278	0.290	0.276	0.363	0.371	0.334	0.484
$^{42}\text{Sc} \rightarrow ^{42}\text{Ca}$	0.333	0.334	0.336	0.442	0.448	0.377	0.383
$^{54}\text{Co} \rightarrow ^{54}\text{Fe}$	0.319	0.317	0.321	0.395	0.393	0.355	0.368
$^{66}\text{As} \rightarrow ^{66}\text{Ge}$	0.475	0.475	0.469	0.568	0.572	0.560	0.524
$^{70}\text{Br} \rightarrow ^{70}\text{Se}$	1.140	1.118	1.107	1.232	1.268	1.230	1.226
$^{74}\text{Rb} \rightarrow ^{74}\text{Kr}$	1.088	1.091	1.071	1.233	1.258	1.191	1.234

# Isospin corrections & $V_{ud}$

PHYSICAL REVIEW C **79**, 064316 (2009)

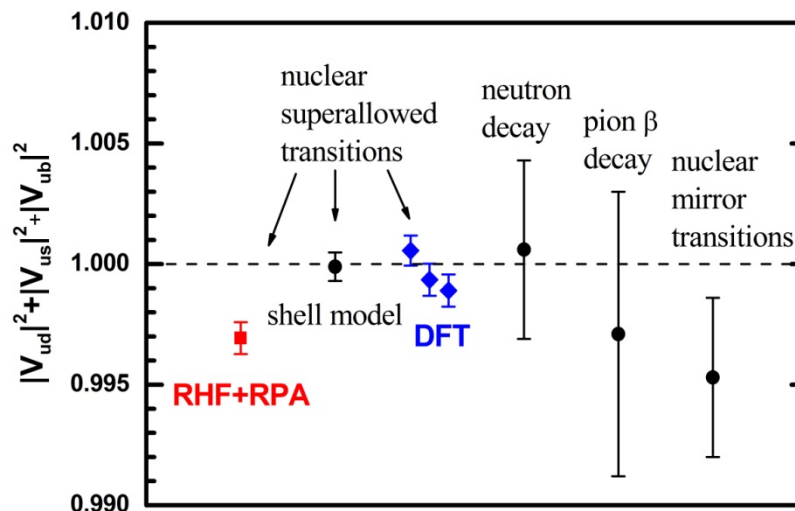
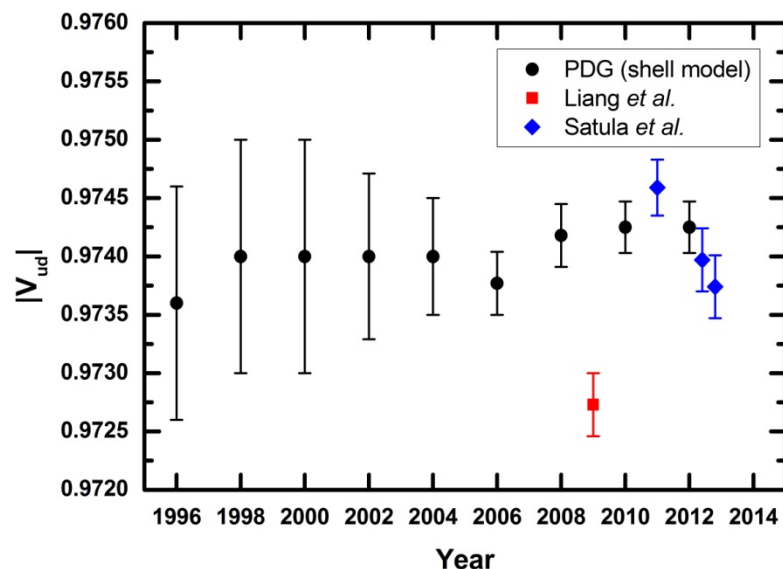
## Isospin corrections for superallowed Fermi $\beta$ decay in self-consistent relativistic random-phase approximation approaches

Haozhao Liang (梁豪兆),<sup>1,2</sup> Nguyen Van Giai,<sup>2</sup> and Jie Meng (孟杰)<sup>1,3</sup>



cited by PDG 2010, 2012, 2014, ...

## Isospin corrections by self-consistent CDFT

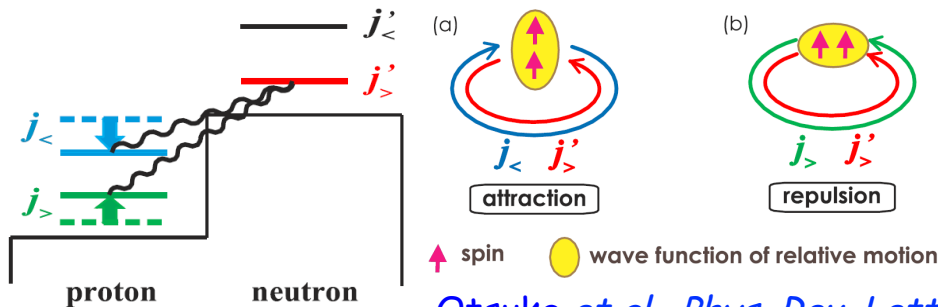


HZL, Giai, Meng, *PRC* **79**, 064316 (2009); Satula et al., *PRL* **106**, 132502 (2011); *PRC* **86**, 054316 (2012)

- To our best knowledge:  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2$ : 0.997 ~ 1.000 (the 4<sup>th</sup> family?)
- ongoing studies .....

# Tensor effects in CDFT?

Tensor effects are crucial, in particular, for properties of exotic nuclei

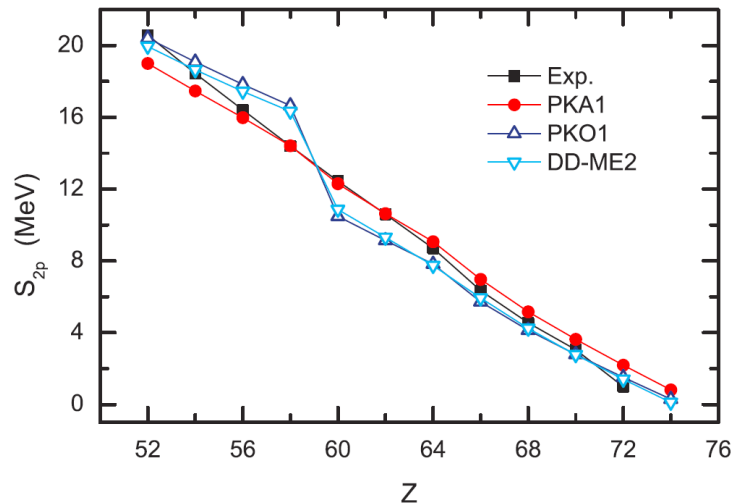


new magic numbers



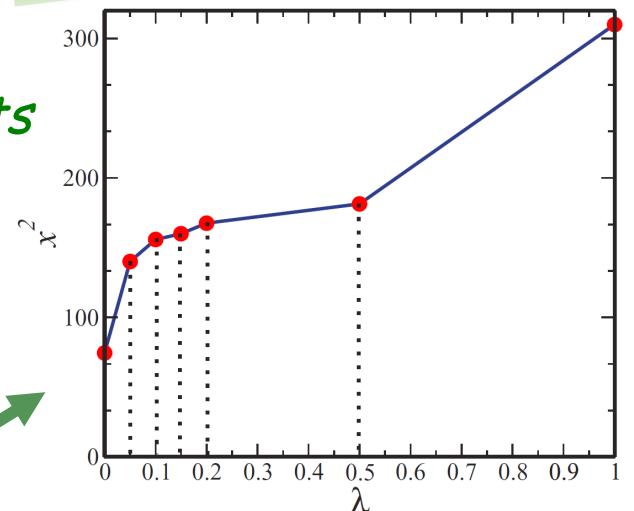
Otsuka et al., *Phys. Rev. Lett.* **95**, 232502 (2005)

What are the tensor effects in CDFT?



some fingerprints

Ab initio for CDFT

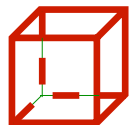
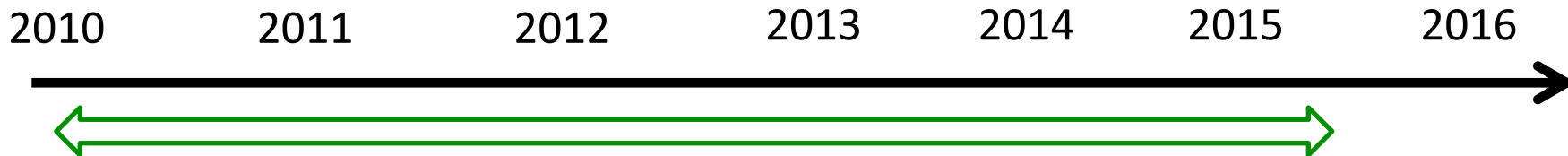


$\pi$  meson (tensor) is not welcomed in

CDFT Talazissis et al., *Phys. Rev. C* **80**, 041301(R) (2009)

Long et al., *Phys. Rev. C* **76**, 034314 (2007)

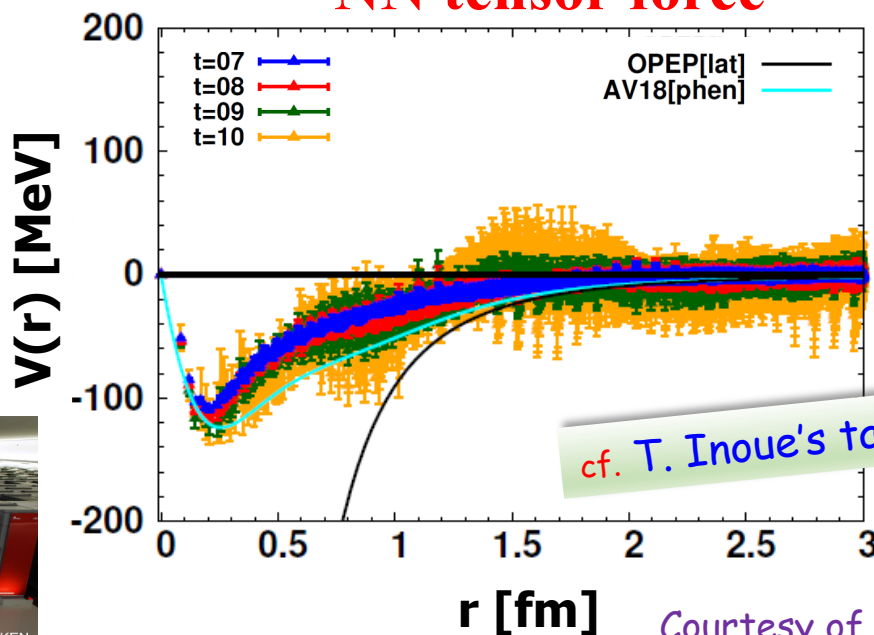
# CDFT from lattice QCD?



$M_\pi = 800 \text{ MeV}$   
 $L = 2 \text{ fm}$

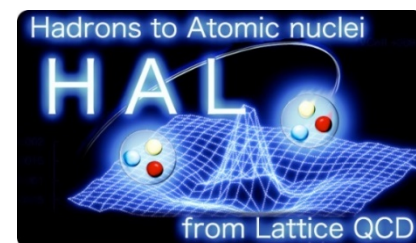
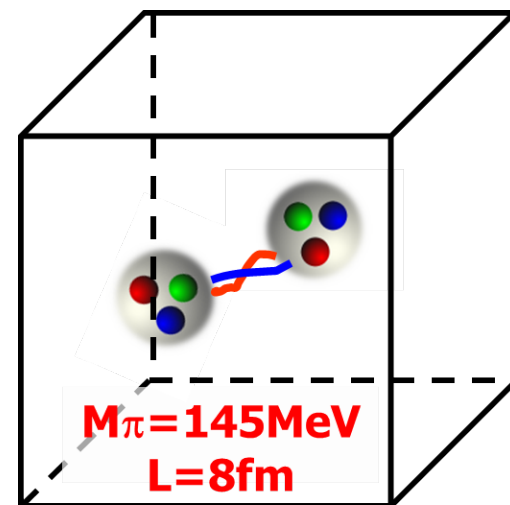
“Unphysical” QCD

*The world's 1st  
calculation of  
Baryon Forces in “Real”  
NN tensor force*



cf. T. Inoue's talk

Courtesy of T. Doi



# *Ab initio* for CDFT

- Brueckner-Hartree-Fock theory (*ladder diagrams to all order*)

(with exchange terms as well)

$$\begin{aligned}
 & c \text{---} \text{HF} \text{---} d + c \text{---} \text{---} m \text{---} n \text{---} d + c \text{---} \text{---} m' \text{---} n' \text{---} d + \dots \\
 & = c \text{---} \text{BHF} \text{---} d
 \end{aligned}$$

- Bethe-Goldstone equation → **finite nuclei**

$$\langle ab | G(W) | cd \rangle = \langle ab | V | cd \rangle + \sum_{mn} \langle ab | V | mn \rangle \frac{Q(m, n)}{W - \varepsilon_m - \varepsilon_n} \langle mn | G(W) | cd \rangle$$

where the starting energy  $W = \varepsilon_c + \varepsilon_d$

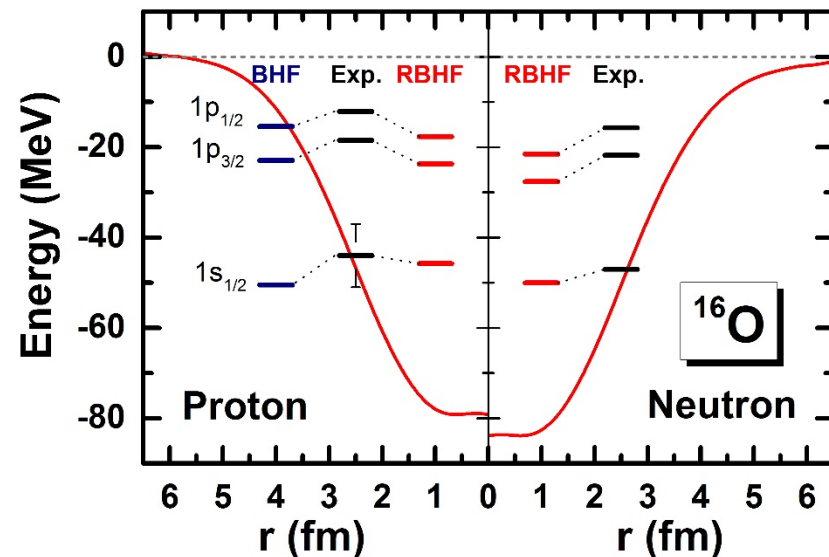
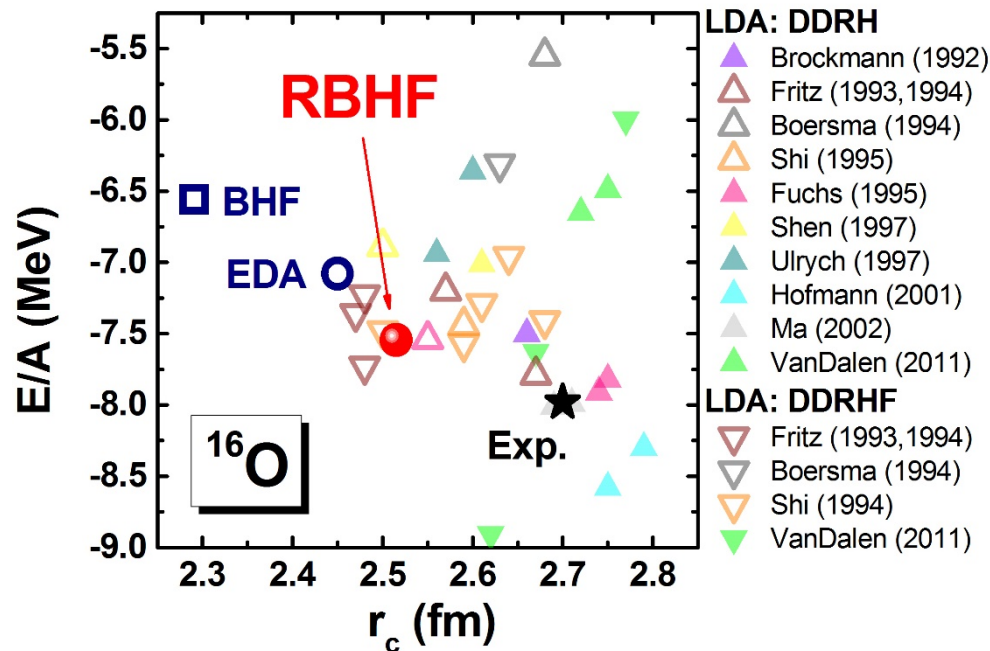
For the first time, **Bethe-Goldstone equation** is solved **self-consistently**

- in the **two-body** frame
- in pure **relativistic** scheme

RIKEN IPA project  
Shen, Hu, HZL, Meng, Ring, Zhang, arXiv:1609.01866

# Relativistic BHF for finite nuclei

## ➤ Relativistic BHF calculations for $^{16}\text{O}$ with Bonn A interaction



EDA = effective density approximation [Müther(1990)]

LDA = local density approximation

RIKEN IPA project

Shen, Hu, HZL, Meng, Ring, Zhang, arXiv:1609.01866

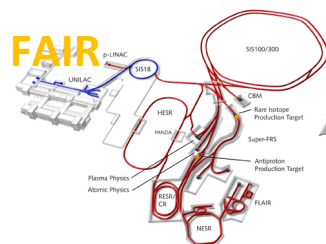
- a first *ab initio* calculations for finite nuclei in **relativistic** scheme
- **Spin-orbit** splitting is reproduced well from the bare interaction.
- benchmark for various LDA calculations



# A dream for another 10 years

quantum-field-theory  
oriented DFT

Exp. facilities:



EDF from  
**effective action**  
 $E_{\text{HK}}[\rho] \sim \Gamma[\rho]/\beta$   
(Legendre transform)

non-perturbative  
nature by  
**renormalization  
group**  
 $\partial_k \Gamma_k[\rho] = \text{Tr}\{\dots\}$   
(flow eq.)

theoretical  
uncertainties  
from **EFT**  
 $\Gamma^{(2)}, \Gamma^{(3)}, \Gamma^{(4)} \dots$   
(power counting)

**Interdisciplinary:**  
**(lattice) QCD**  
**hadron**  
**cold atom**  
**condensed matter**  
**quantum chemistry**

.....

**Supercomputers**



also cf. Nazarewicz' talk  
Schwenk & Polonyi, arXiv:0403011 [nucl-th]  
Kutzelnigg, JMS 768, 163 (2006)  
Drut, Furnstahl, Platter, PPNP 64, 120 (2010)  
Braun, JPG 39, 033001 (2012)  
Metzner et al., RMP 84, 299 (2012)

# Acknowledgments

*To Jun & our first baby*

*(~in a month)*



# Acknowledgments

*Thank you very much for your  
encouragement and supports!*