

Hyperon-Nucleon Scattering

In A Covariant Chiral Effective Field Theory Approach

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1. Background and significance

2. Chiral effective field theory

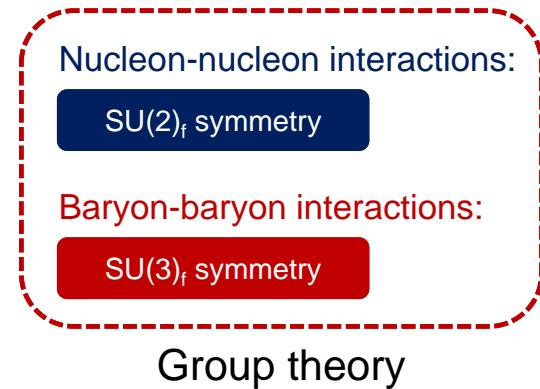
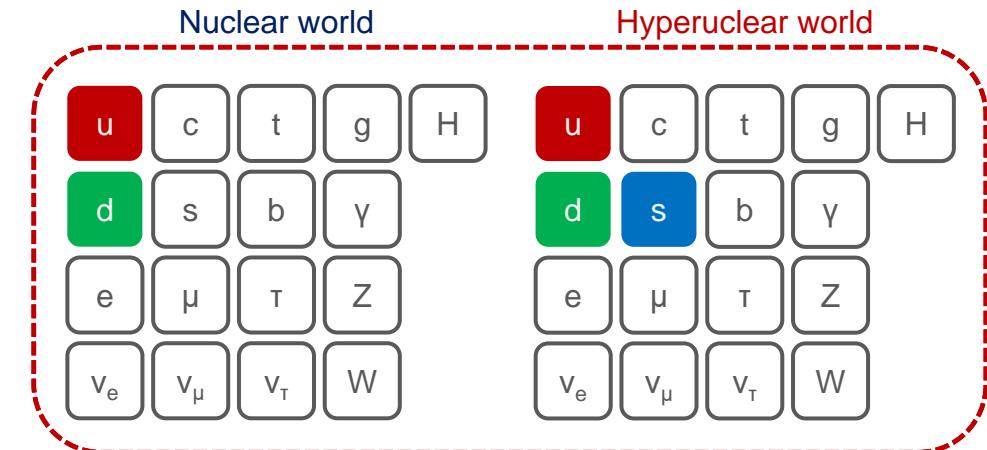
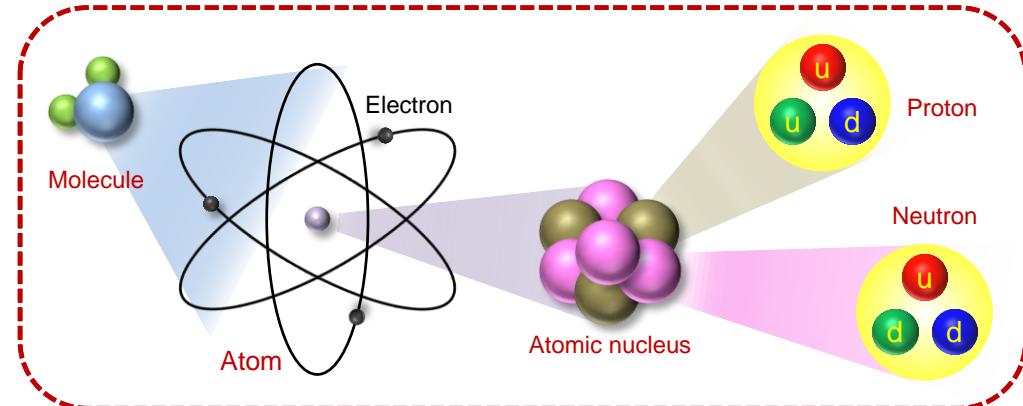
3. A covariant ChEFT approach

4. Results and discussion

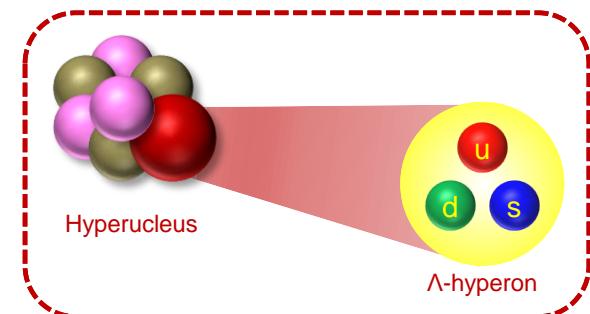
5. Summary and outlook

Baryon-baryon interactions

- Extension of nuclear force



Extension

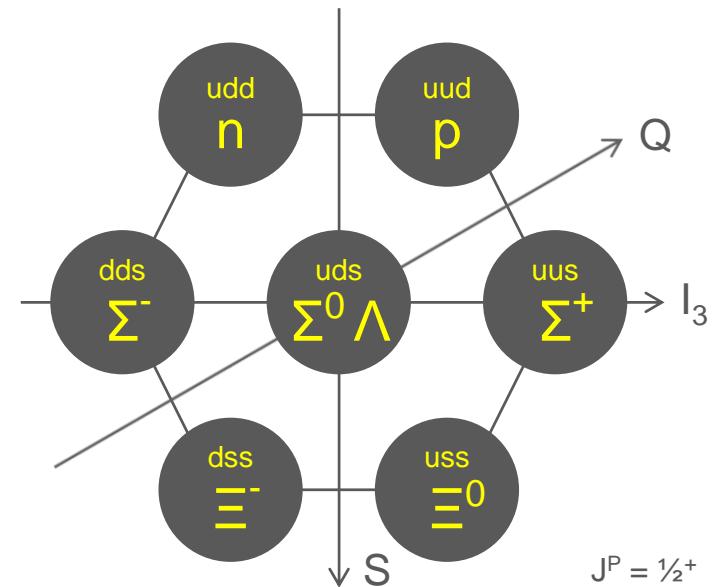


Quark level extension

Octet baryons

Characterized by:

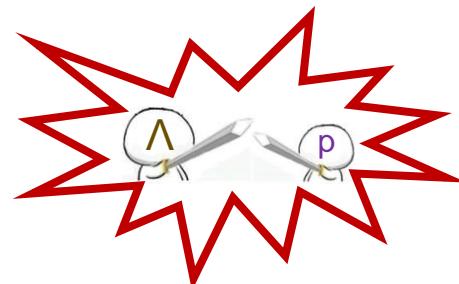
- Charge (Q)
- Strangeness (S)
- Third component of isospin (I_3)



Why baryon-baryon interactions?

Role of strangeness

$SU(3)_f$ symmetry



Hypernuclear physics

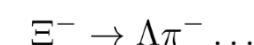
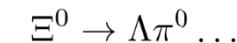
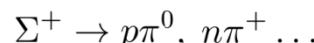
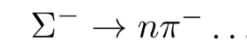
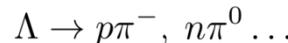
Astrophysics

Experimental status: YN

- Poor

1. Small quantity (36, S=-1, YN)
2. Age-old (1960s - 1970s)
3. Poor quality (large error bar)

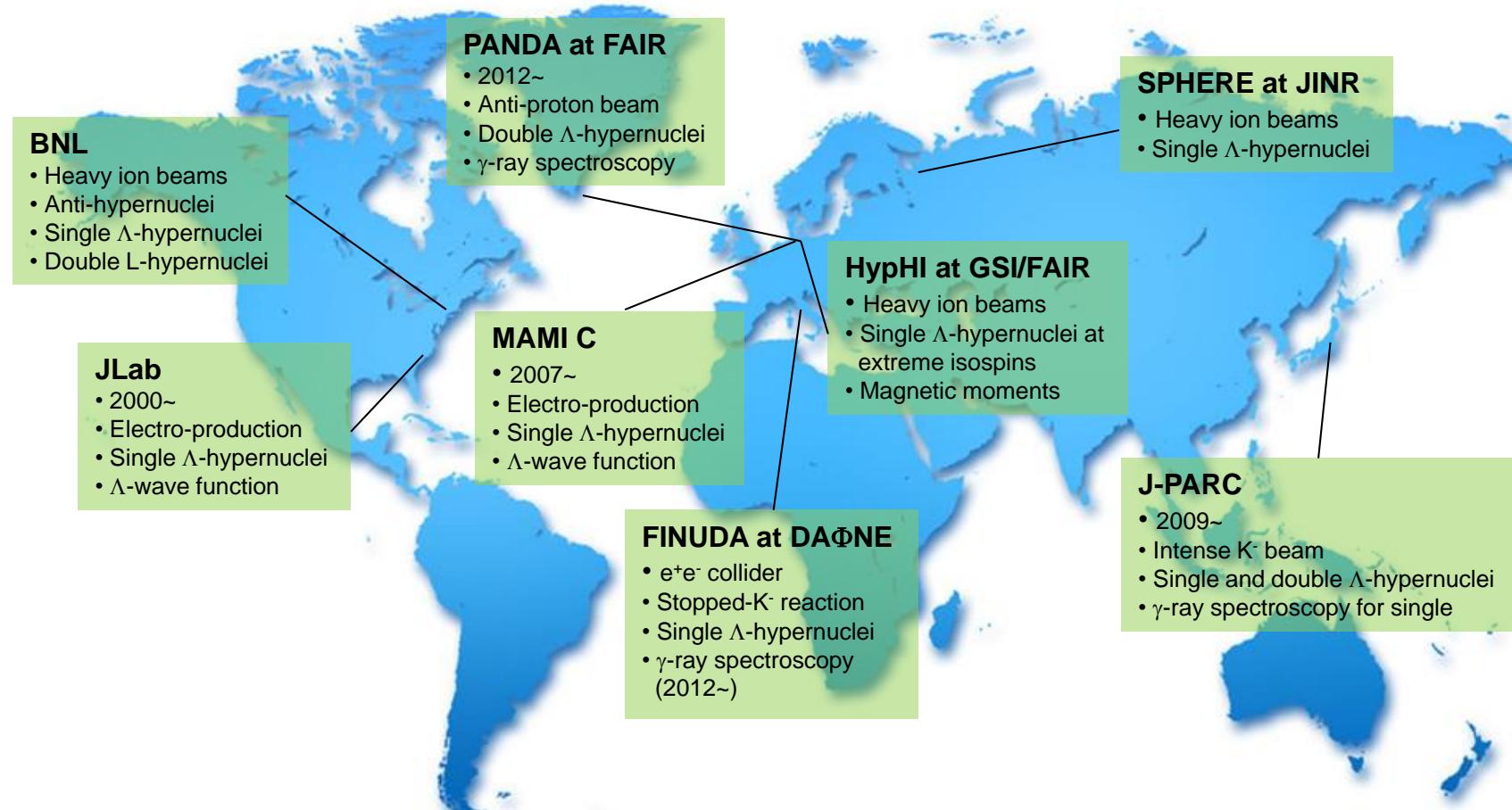
- R. Engelmann, et al., Phys. Lett. **21** (1966) **587**
- G. Alexander, et al., Phys. Rev. **173** (1968) **1452**
- B. Sechi-Zorn, et al., Phys. Rev. **175** (1968) **1735**
- F. Eisele, et al., Phys. Lett. **37B** (1971) **204**
- V. Hepp and H. Schleich, Z. Phys. **214** (1968) **71**
- Short lifetime of hyperons! ($\leq 10^{-10}$ s)



$\Lambda p \rightarrow \Lambda p$		$\Lambda p \rightarrow \Lambda p$		$\Sigma^- p \rightarrow \Lambda n$	
p_{lab}^Λ	σ_{exp}	p_{lab}^Λ	σ_{exp}	$p_{\text{lab}}^{\Sigma^-}$	σ_{exp}
135 ± 15	209 ± 58	145 ± 25	180 ± 22	110 ± 5	174 ± 47
165 ± 15	177 ± 38	185 ± 15	130 ± 17	120 ± 5	178 ± 39
195 ± 15	153 ± 27	210 ± 10	118 ± 16	130 ± 5	140 ± 28
225 ± 15	111 ± 18	230 ± 10	101 ± 12	140 ± 5	164 ± 25
255 ± 15	87 ± 13	250 ± 10	83 ± 13	150 ± 5	147 ± 19
300 ± 30	46 ± 11	290 ± 30	57 ± 9	160 ± 5	124 ± 14
$\Sigma^+ p \rightarrow \Sigma^+ p$		$\Sigma^- p \rightarrow \Sigma^- p$		$\Sigma^- p \rightarrow \Sigma^0 n$	
$p_{\text{lab}}^{\Sigma^+}$	σ_{exp}	$p_{\text{lab}}^{\Sigma^-}$	σ_{exp}	$p_{\text{lab}}^{\Sigma^-}$	σ_{exp}
145 ± 5	123 ± 62	135 ± 5	184 ± 52	110 ± 5	396 ± 91
155 ± 5	104 ± 30	142.5 ± 5	152 ± 38	120 ± 5	159 ± 43
165 ± 5	92 ± 18	147.5 ± 5	146 ± 30	130 ± 5	157 ± 34
175 ± 5		81 ± 12	152.5 ± 5	142 ± 25	140 ± 5
			157.5 ± 5	164 ± 32	150 ± 5
			162.5 ± 5	138 ± 19	160 ± 5
			167.5 ± 5	113 ± 16	
$\Sigma^- p$ inelastic capture ratio at rest				$r_R = 0.468 \pm 0.010$	

Units for p and σ : MeV/c and mb

Prospects: very promising



...

Theoretical status

- In about recent 2 decades

Group / Place	Model / Method	Reference
Phenomenological model		
□ Beijing-Tübingen:	Quark cluster model	Zhang NPA 578 (1994) 573
□ Kyoto-Niigata:	Quark cluster model (FSS, fss2)	Fujiwara PRL 76 (1996) 2242
□ Nanjing:	Quark delocalization and color screening model	Ping NPA 657 (1999) 95
□ Nijmegen:	Meson exchange model (NSC, ESC...)	Rijken PRC 59 (1999) 21
□ Bonn-Jülich:	Meson exchange model (Jülich 94, 04)	Haidenbauer PRC 72 (2005) 044005
□ Valencia:	Meson exchange model (UChPT)	Sasaki PRC 74 (2006) 064002
□
Effective field theory		
□ Pecs-Groningen:	KSW approach	Korpa PRC 65 (2002) 015208
□ Bonn-Jülich:	Heavy baryon chiral effective field theory	Haidenbauer NPA 915 (2013) 24
□ Beihang-Peking:	Covariant chiral effective field theory	Li PRD 94 (2016) 014029
□
Lattice QCD simulation		
□ NPLQCD:	Lüscher's finite volume method (phase shifts)	Beane NPA 794 (2007) 62
□ HAL QCD:	HAL QCD method (non-local potential)	Inoue PTP 124 (2010) 591
□

Some of the representative works

1. Background and significance

2. Chiral effective field theory

3. A covariant ChEFT approach

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Weinberg's approach

- Chiral Effective Field Theory

Advantages:

- ✓ Improve calculations systematically
- ✓ Estimate theoretical uncertainties
- ✓ Consistent three- and multi-baryon forces

First proposed
by
Steven Weinberg



Phys. Lett. B 251 (1990) 288

Nuclear forces from chiral lagrangians

Steven Weinberg¹

Theory Group, Department of Physics, University of Texas, Austin, TX 78712, USA

Received 14 August 1990

Nucl. Phys. B 363 (1991) 3

EFFECTIVE CHIRAL LAGRANGIANS FOR NUCLEON–PION INTERACTIONS AND NUCLEAR FORCES

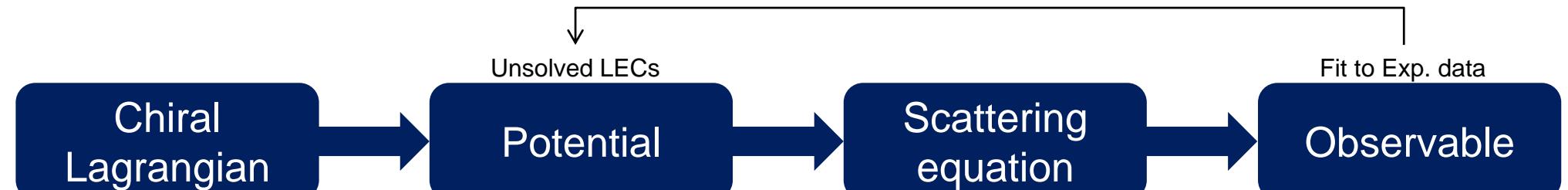
Steven WEINBERG*

Theory Group, Department of Physics, University of Texas, Austin, TX 78712, USA

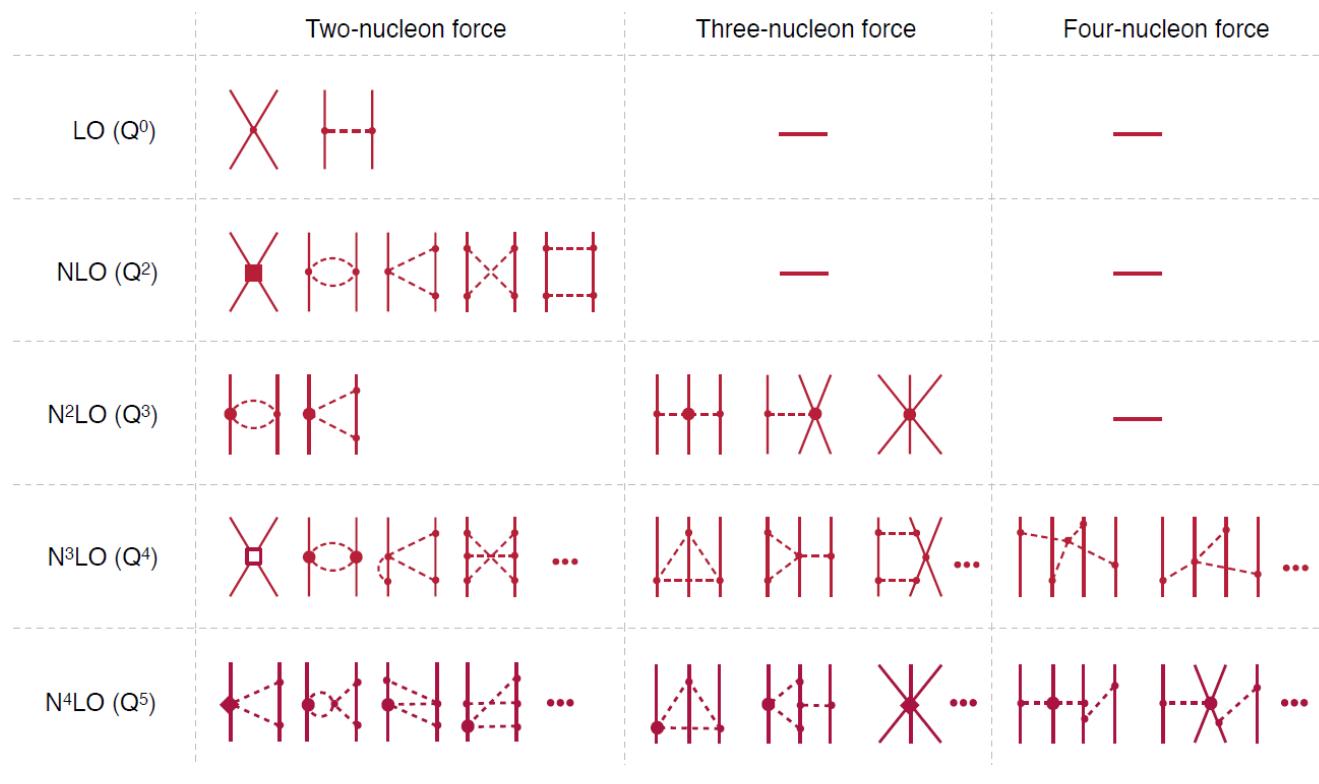
Received 2 April 1991

In **YN** and **YY** interactions: Korpa '01, Polinder '06 '07, Haidenbauer '07 '10 '13 '15, Li '16...

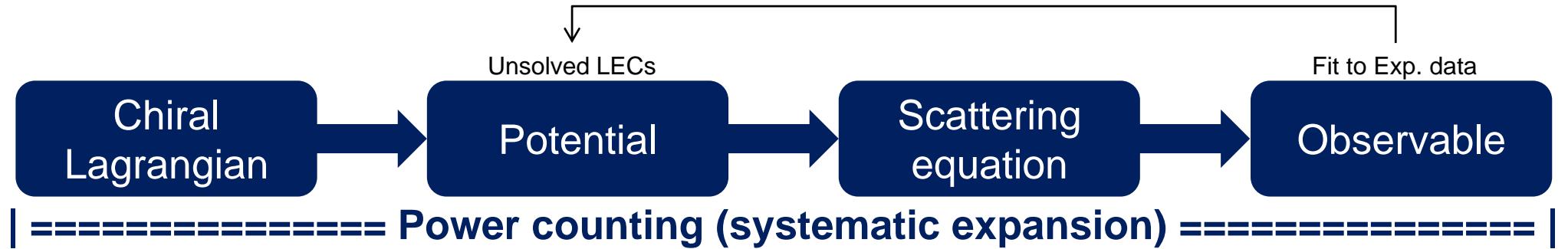
Weinberg's approach



| ====== Power counting (systematic expansion) ====== |



Weinberg's approach



However,

(1) Lippmann-Schwinger equation

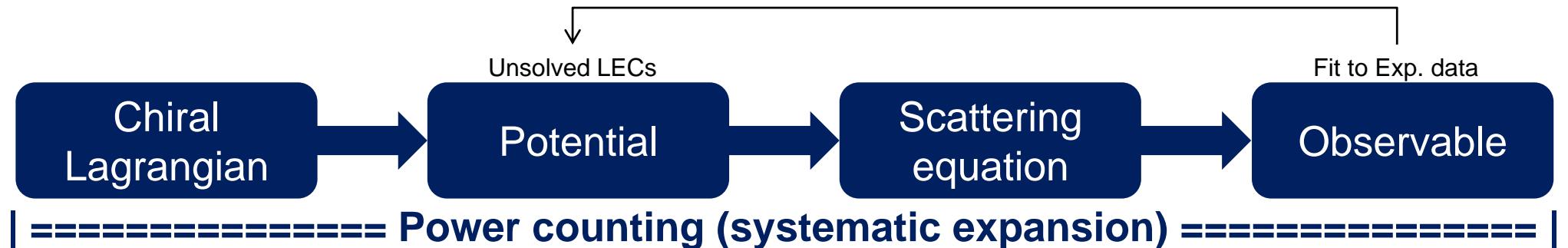
$$T(p, p') = V(p, p') + \int \frac{dp'' p''^2}{(2\pi)^3} V(p, p'') \frac{2\mu}{q_\nu^2 - p''^2 + i\epsilon} T(p'', p')$$

- Singular
 - Cutoff
 - Modified power counting

(2) Reductions

- The missing of relativistic effects

Weinberg's approach



However,

(1) Lippmann-Schwinger equation

$$T(p, p') = V(p, p') + \int \frac{dp'' p''^2}{(2\pi)^3} V(p, p'') \frac{2\mu}{q_\nu^2 - p''^2 + i\epsilon} T(p'', p')$$

- Singular
 - Cutoff
 - Modified power counting

(2) Reductions

- The missing of relativistic effects

Relativistic effects in
one-baryon and heavy-light systems

- Geng PRL 101 (2008) 222002
- Geng PRD 79 (2009) 094022
- Geng PRD 84 (2011) 074024
- Ren JHEP 12 (2012) 073
- Ren PRD 91 (2015) 051502
- ...
- Geng PRD 82 (2010) 054022
- Geng PLB 696 (2011) 390
- Altenbuchinger PLB 713 (2012) 453
- ...

Faster convergence!

Will it happen in the two-baryon system?

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Power counting

Naive dimensional analysis (Weinberg's proposal)

$$\nu = 2 - \frac{B}{2} + 2L + \sum_i v_i \Delta_i \quad \Delta_i = d_i + \frac{1}{2} b_i - 2$$

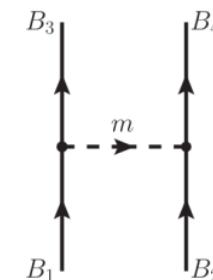
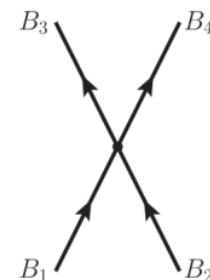
- **v – chiral order**

- B – number of external baryons
- L – number of goldstone boson loops
- i – number of types of the vertices

- v_i – number of vertices with dimension Δ_i
- d_i – number of derivatives
- b_i – number of internal baryon lines

Leading order ($\sim Q^{v=0}$) Feynman diagrams

B=4, L=0, i=1,
v=1, d=0, b=4.



B=4, L=0, i=1,
v=2, d=1, b=2.

Covariant chiral Lagrangians

Mesonic part

$$\mathcal{L}_M^{(2)} = \frac{f_0^2}{4} \langle \partial_\mu U \partial^\mu U^\dagger \rangle + \frac{1}{2} B_0 f_0^2 \langle M U^\dagger + U M \rangle$$

$$U(x) = \text{Exp} \left(i \frac{\phi(x)}{f_0} \right)$$

$$M \equiv \text{diag} (m_u, m_d, m_s)$$

$$\phi(x) = \sum_{a=1}^8 \phi_a(x) \lambda_a \equiv \begin{pmatrix} \pi^0 + \frac{\eta}{\sqrt{3}} & \sqrt{2}\pi^+ & \sqrt{2}K^+ \\ \sqrt{2}\pi^- & -\pi^0 + \frac{\eta}{\sqrt{3}} & \sqrt{2}K^0 \\ \sqrt{2}K^- & \sqrt{2}\bar{K}^0 & -\frac{2\eta}{\sqrt{3}} \end{pmatrix}$$

Meson-baryon interaction

$$\mathcal{L}_{MB}^{(1)} = \left\langle \bar{B} (i \not{D} - M_B) B - \frac{D}{2} \bar{B} \gamma^\mu \gamma_5 \{u_\mu, B\} - \frac{F}{2} \bar{B} \gamma^\mu \gamma_5 [u_\mu, B] \right\rangle$$

Covariant derivative:

$$D^\mu B = (\partial_\mu + \Gamma_\mu - iv_\mu^{(s)}) B$$

$$B = \sum_a \frac{B_a \lambda_a}{\sqrt{2}} \equiv \begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & \Sigma^+ & p \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & n \\ \Xi^- & \Xi^0 & -\frac{2\Lambda}{\sqrt{6}} \end{pmatrix}$$

Four-baryon contact terms

$$\mathcal{L}_{CT}^1 = C_i^1 \langle \bar{B}_a \bar{B}_b (\Gamma_i B)_b (\Gamma_i B)_a \rangle \quad \mathcal{L}_{CT}^2 = C_i^2 \langle \bar{B}_a (\Gamma_i B)_a \bar{B}_b (\Gamma_i B)_b \rangle \quad \mathcal{L}_{CT}^3 = C_i^3 \langle \bar{B}_a (\Gamma_i B)_a \rangle \langle \bar{B}_b (\Gamma_i B)_b \rangle$$

Clifford algebra: $\Gamma_1 = 1, \quad \Gamma_2 = \gamma^\mu, \quad \Gamma_3 = \sigma^{\mu\nu}, \quad \Gamma_4 = \gamma^\mu \gamma_5, \quad \Gamma_5 = \gamma_5.$

Leading order potentials (1st improvement)

- In Weinberg's approach

$$V_{\text{LO}}(\mathbf{p}', \mathbf{p}) = \mathcal{C}_S + \mathcal{C}_T \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 + N_1 N_2 \frac{\boldsymbol{\sigma}_1 \cdot (\mathbf{p}' - \mathbf{p}) \boldsymbol{\sigma}_2 \cdot (\mathbf{p}' - \mathbf{p})}{(\mathbf{p}' - \mathbf{p})^2 + m^2 - i\epsilon}$$

Nonderivative four-baryon contact terms + One-pseudoscalar-meson-exchange

- Baryon spinors

Weinberg's approach

$$u_i(\mathbf{p}, s) = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \chi_s$$

Covariant ChEFT approach

$$u_i(\mathbf{p}, s) = \sqrt{\frac{E + M_i}{2M_i}} \begin{pmatrix} 1 \\ \frac{\boldsymbol{\sigma} \cdot \mathbf{p}}{E + M_i} \end{pmatrix} \chi_s$$

The ‘small’ components are NOT omitted!!!

Leading order potentials (1st improvement)

- Nondervative four-baryon contact terms (helicity basis)

$$V_1^{\text{CT}}(\mathbf{p}', \mathbf{p}) = \textcolor{red}{C}_1 \frac{(E_{p'} + M_B)(E_p + M_B)}{4M_B^2} \left(1 - \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_1\lambda_1}{(E_{p'} + M_B)(E_p + M_B)} \right) \left(1 - \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_2\lambda_2}{(E_{p'} + M_B)(E_p + M_B)} \right) \langle \lambda'_1\lambda'_2 | \lambda_1\lambda_2 \rangle$$

$$\begin{aligned} V_2^{\text{CT}}(\mathbf{p}', \mathbf{p}) = & \textcolor{red}{C}_2 \frac{(E_{p'} + M_B)(E_p + M_B)}{4M_B^2} \left[\left(1 + \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_1\lambda_1}{(E_{p'} + M_B)(E_p + M_B)} \right) \left(1 + \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_2\lambda_2}{(E_{p'} + M_B)(E_p + M_B)} \right) \langle \lambda'_1\lambda'_2 | \lambda_1\lambda_2 \rangle \right. \\ & \left. - \left(\frac{2|\mathbf{p}'|\lambda'_1}{E_{p'} + M_B} + \frac{2|\mathbf{p}|\lambda_1}{E_p + M_B} \right) \left(\frac{2|\mathbf{p}'|\lambda'_2}{E_{p'} + M_B} + \frac{2|\mathbf{p}|\lambda_2}{E_p + M_B} \right) \langle \lambda'_1\lambda'_2 | \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 | \lambda_1\lambda_2 \rangle \right] \end{aligned}$$

$$\begin{aligned} V_3^{\text{CT}}(\mathbf{p}', \mathbf{p}) = & 2\textcolor{red}{C}_3 \frac{(E_{p'} + M_B)(E_p + M_B)}{4M_B^2} \left[\left(1 - \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_1\lambda_1}{(E_{p'} + M_B)(E_p + M_B)} \right) \left(1 - \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_2\lambda_2}{(E_{p'} + M_B)(E_p + M_B)} \right) \right. \\ & \left. - \left(\frac{2|\mathbf{p}'|\lambda'_1}{E_{p'} + M_B} - \frac{2|\mathbf{p}|\lambda_1}{E_p + M_B} \right) \left(\frac{2|\mathbf{p}'|\lambda'_2}{E_{p'} + M_B} - \frac{2|\mathbf{p}|\lambda_2}{E_p + M_B} \right) \right] \langle \lambda'_1\lambda'_2 | \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 | \lambda_1\lambda_2 \rangle \end{aligned}$$

$$\begin{aligned} V_4^{\text{CT}}(\mathbf{p}', \mathbf{p}) = & \textcolor{red}{C}_4 \frac{(E_{p'} + M_B)(E_p + M_B)}{4M_B^2} \left[\left(\frac{2|\mathbf{p}'|\lambda'_1}{E_{p'} + M_B} + \frac{2|\mathbf{p}|\lambda_1}{E_p + M_B} \right) \left(\frac{2|\mathbf{p}'|\lambda'_2}{E_{p'} + M_B} + \frac{2|\mathbf{p}|\lambda_2}{E_p + M_B} \right) \langle \lambda'_1\lambda'_2 | \lambda_1\lambda_2 \rangle \right. \\ & \left. - \left(1 + \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_1\lambda_1}{(E_{p'} + M_B)(E_p + M_B)} \right) \left(1 + \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_2\lambda_2}{(E_{p'} + M_B)(E_p + M_B)} \right) \langle \lambda'_1\lambda'_2 | \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 | \lambda_1\lambda_2 \rangle \right] \end{aligned}$$

$$V_5^{\text{CT}}(\mathbf{p}', \mathbf{p}) = \textcolor{red}{C}_5 \frac{(E_{p'} + M_B)(E_p + M_B)}{4M_B^2} \left(\frac{2|\mathbf{p}'|\lambda'_1}{E_{p'} + M_B} - \frac{2|\mathbf{p}|\lambda_1}{E_p + M_B} \right) \left(\frac{2|\mathbf{p}'|\lambda'_2}{E_{p'} + M_B} - \frac{2|\mathbf{p}|\lambda_2}{E_p + M_B} \right) \langle \lambda'_1\lambda'_2 | \lambda_1\lambda_2 \rangle$$

Leading order potentials (1st improvement)

- One-pseudoscalar-meson-exchange (helicity basis)

$$\begin{aligned} V^{\text{OME}}(\mathbf{p}', \mathbf{p}) &= -N_1 N_2 \frac{(E_{p'} + M_B)(E_p + M_B)}{M_B^2} \\ &\quad \times \left[(E_{p'} - E_p) \left(\frac{|\mathbf{p}'| \lambda'_2}{E_{p'} + M_B} + \frac{|\mathbf{p}| \lambda_2}{E_p + M_B} \right) - (|\mathbf{p}'| \lambda'_2 - |\mathbf{p}| \lambda_2) \left(1 + \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_2\lambda_2}{(E_{p'} + M_B)(E_p + M_B)} \right) \right] \\ &\quad \times \left[(E_{p'} - E_p) \left(\frac{|\mathbf{p}'| \lambda'_1}{E_{p'} + M_B} + \frac{|\mathbf{p}| \lambda_1}{E_p + M_B} \right) - (|\mathbf{p}'| \lambda'_1 - |\mathbf{p}| \lambda_1) \left(1 + \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_1\lambda_1}{(E_{p'} + M_B)(E_p + M_B)} \right) \right] \\ &\quad \times \frac{\langle \lambda'_1 \lambda'_2 | \lambda_1 \lambda_2 \rangle}{(E_{p'} - E_p)^2 - (\mathbf{p}' - \mathbf{p})^2 - m^2 + i\epsilon} \\ &\simeq N_1 N_2 \frac{(E_{p'} + M_B)(E_p + M_B)}{M_B^2} \\ &\quad \times \left[(E_{p'} - E_p) \left(\frac{|\mathbf{p}'| \lambda'_2}{E_{p'} + M_B} + \frac{|\mathbf{p}| \lambda_2}{E_p + M_B} \right) - (|\mathbf{p}'| \lambda'_2 - |\mathbf{p}| \lambda_2) \left(1 + \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_2\lambda_2}{(E_{p'} + M_B)(E_p + M_B)} \right) \right] \\ &\quad \times \left[(E_{p'} - E_p) \left(\frac{|\mathbf{p}'| \lambda'_1}{E_{p'} + M_B} + \frac{|\mathbf{p}| \lambda_1}{E_p + M_B} \right) - (|\mathbf{p}'| \lambda'_1 - |\mathbf{p}| \lambda_1) \left(1 + \frac{4|\mathbf{p}'||\mathbf{p}|\lambda'_1\lambda_1}{(E_{p'} + M_B)(E_p + M_B)} \right) \right] \\ &\quad \times \frac{\langle \lambda'_1 \lambda'_2 | \lambda_1 \lambda_2 \rangle}{(\mathbf{p}' - \mathbf{p})^2 + m^2 - i\epsilon} \end{aligned}$$

Energy-dependent term in the propagator is omitted, same as in the scattering equation!

Scattering equation (2nd improvement)

- Lippmann-Schwinger equation (Weinberg's approach)

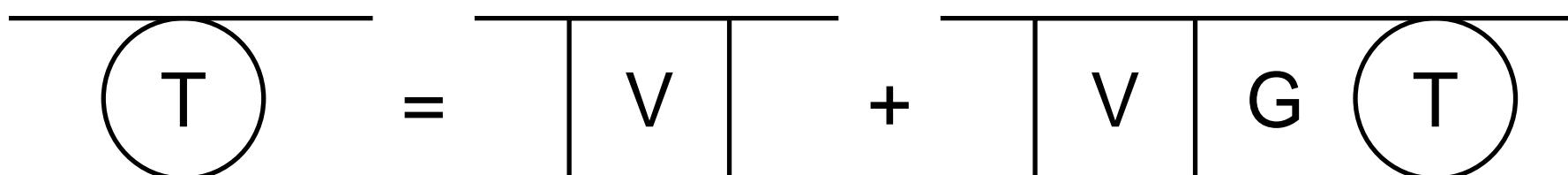
$$T_{\rho''\rho'}^{\nu''\nu',J}(p'', p'; \sqrt{s}) = V_{\rho''\rho'}^{\nu''\nu'}(p'', p') + \sum_{\rho,\nu} \int_0^\infty \frac{dp}{(2\pi)^3} \frac{p^2}{V_{\rho''\rho}^{\nu''\nu}(p'', p)} \frac{2\mu_\nu}{q_\nu^2 - p^2 + i\epsilon} T_{\rho\rho'}^{\nu\nu',J}(p, p'; \sqrt{s})$$

ρ : partial wave ν : particle channel

- Kadyshevsky equation* (More relativistic effects involved)

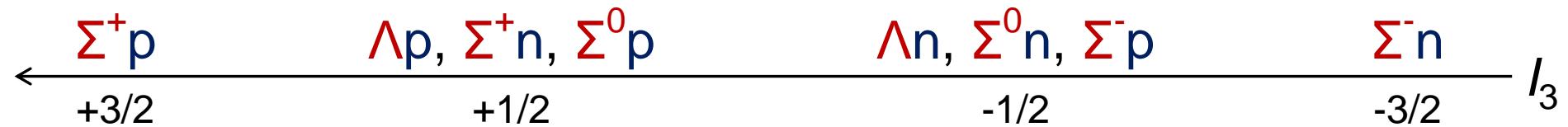
$$T_{\rho''\rho'}^{\nu''\nu',J}(p'', p'; \sqrt{s}) = V_{\rho''\rho'}^{\nu''\nu'}(p'', p') + \sum_{\rho,\nu} \int_0^\infty \frac{dp}{(2\pi)^3} \frac{2\mu_\nu^2 V_{\rho''\rho}^{\nu''\nu}(p'', p)}{(p^2 + 4\mu_\nu^2)(\sqrt{q_\nu^2 + 4\mu_\nu^2} - \sqrt{p^2 + 4\mu_\nu^2} + i\epsilon)} T_{\rho\rho'}^{\nu\nu',J}(p, p'; \sqrt{s})$$

A 3-dimensional reduction of the relativistic Bethe-Salpeter equation

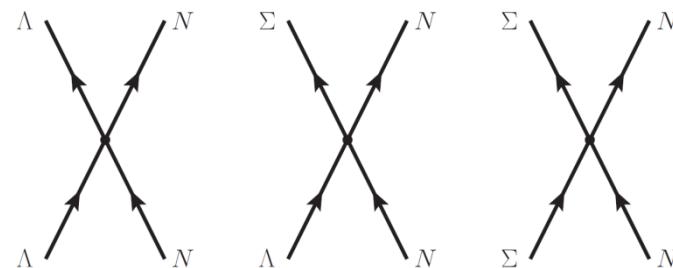


ΛN and ΣN systems

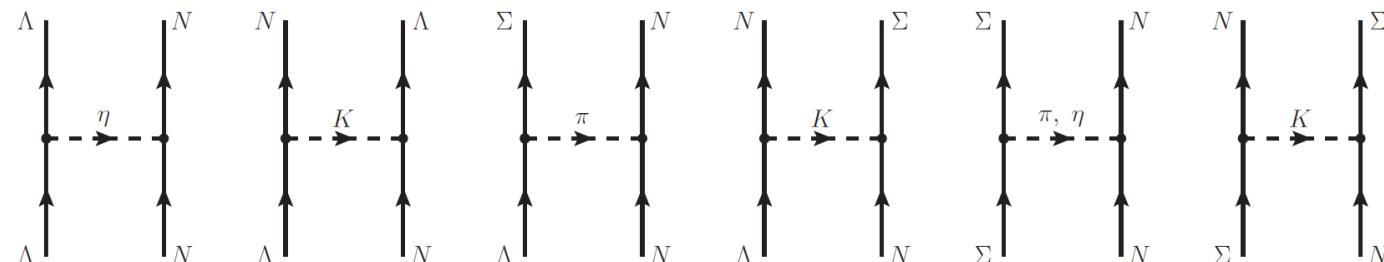
- $S = -1; I = 3/2, 1/2$



- Nonderivative four-baryon contact terms (LO):

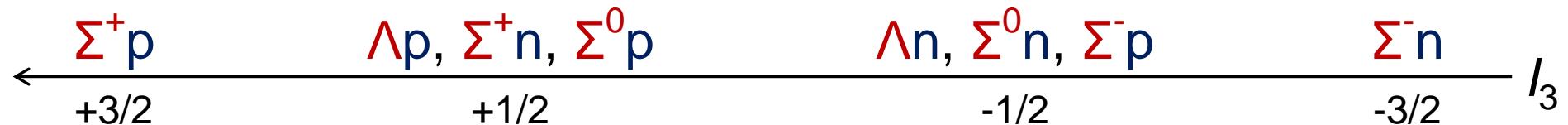


- One-pseudoscalar-meson-exchange (LO)

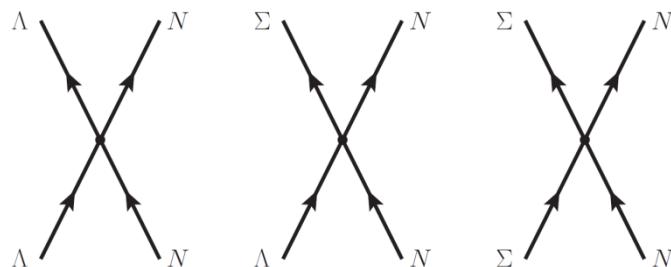


ΛN and ΣN systems

- $S = -1; I = 3/2, 1/2$



- Nonderivative four-baryon contact terms (LO):



Strict SU(3) symmetry is imposed, 12 low energy constants (LECs)

	$C_{1S0}^{\Lambda\Lambda}$	$\hat{C}_{1S0}^{\Lambda\Lambda}$	$C_{1S0}^{\Sigma\Sigma}$	$\hat{C}_{1S0}^{\Sigma\Sigma}$	
$C_{3S1}^{\Lambda\Lambda}$	$\hat{C}_{3S1}^{\Lambda\Lambda}$	$C_{3S1}^{\Sigma\Sigma}$	$\hat{C}_{3S1}^{\Sigma\Sigma}$	$C_{3S1}^{\Lambda\Sigma}$	$\hat{C}_{3S1}^{\Lambda\Sigma}$
	$C_{3P1}^{\Lambda\Lambda}$	$C_{3P1}^{\Sigma\Sigma}$			

1. Background and significance

2. Chiral effective field theory

3. A covariant ChEFT approach

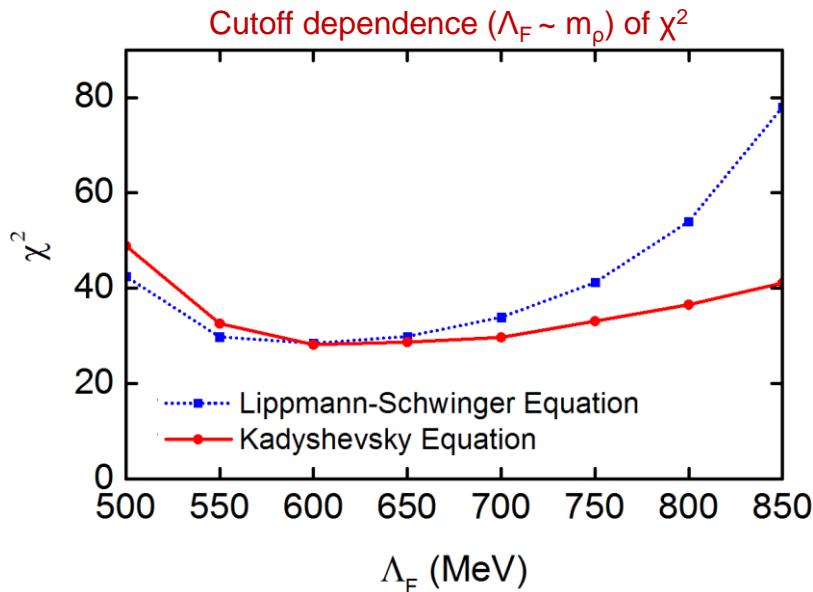
4. Results and discussion

5. Summary and outlook

Relativistic effects in the scattering equation

- χ^2 in the fit (nonrelativistic potentials, 36 YN data)

$$f^{\Lambda_F}(p, p') = \exp \left[- \left(\frac{p}{\Lambda_F} \right)^{2n} - \left(\frac{p'}{\Lambda_F} \right)^{2n} \right]$$

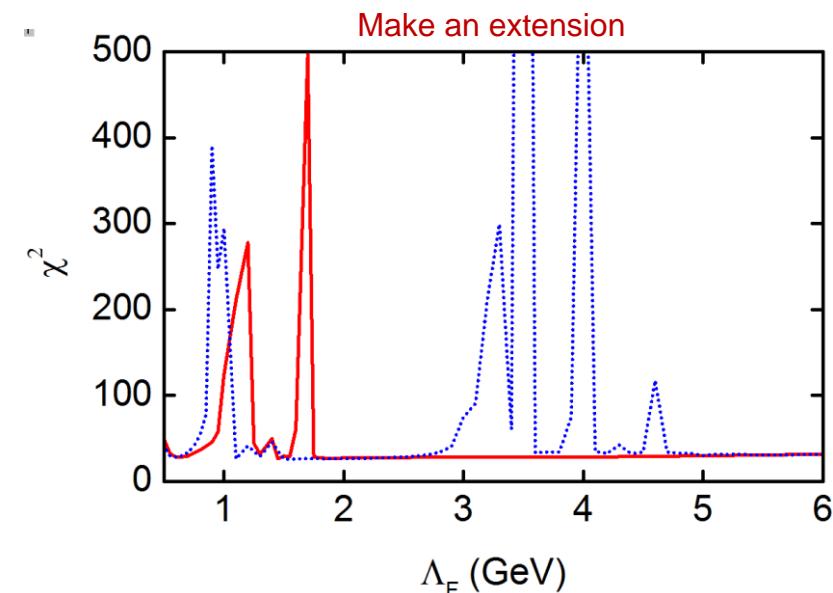
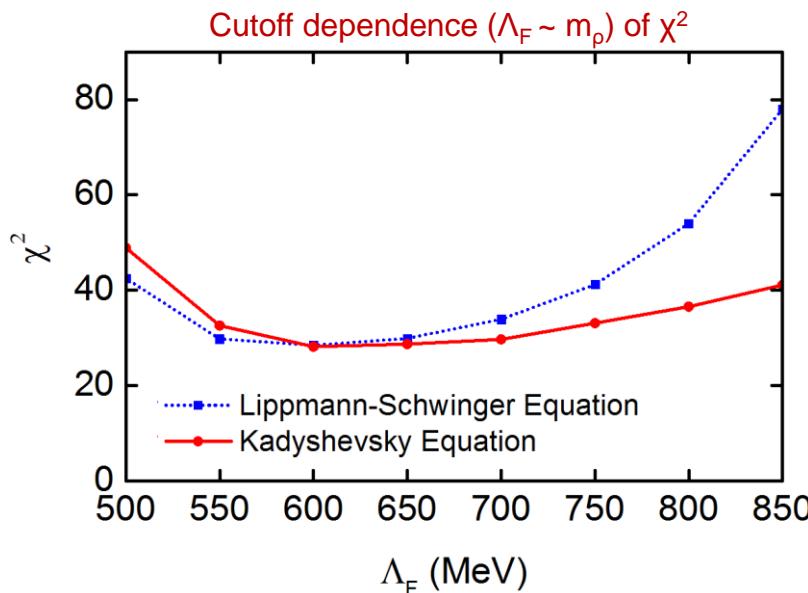


1. Best description of the experimental data: qualitatively similar!

Relativistic effects in the scattering equation

- χ^2 in the fit (nonrelativistic potentials, 36 YN data)

$$f^{\Lambda_F}(p, p') = \exp \left[- \left(\frac{p}{\Lambda_F} \right)^{2n} - \left(\frac{p'}{\Lambda_F} \right)^{2n} \right]$$



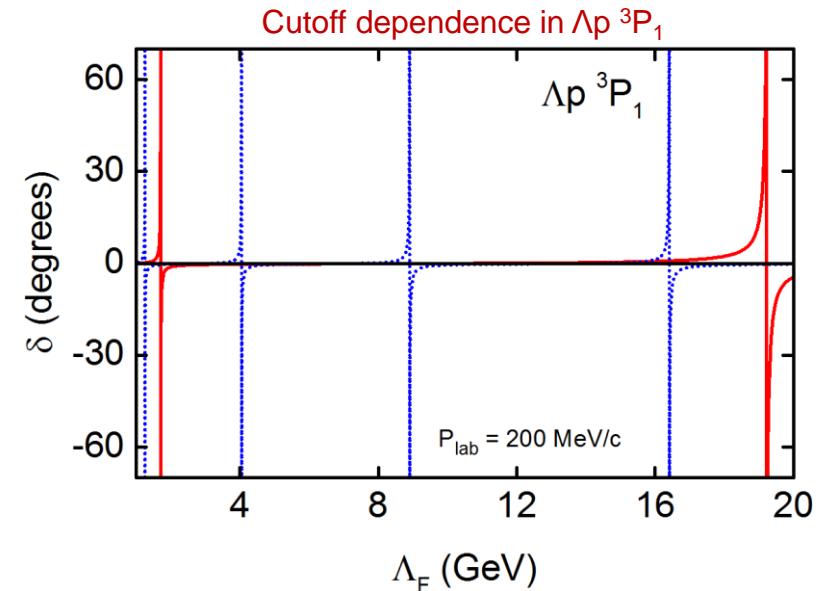
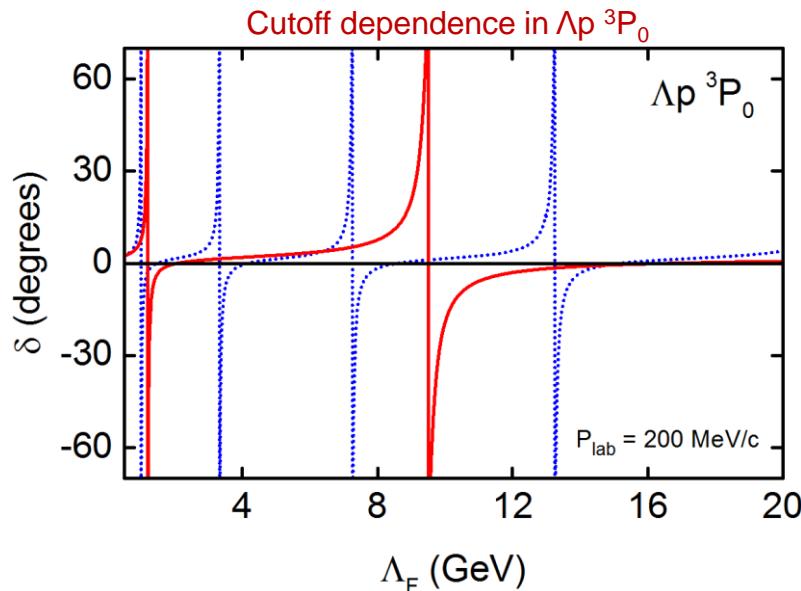
1. Best description of the experimental data: qualitatively similar!
2. Less peaks in using Kadyshevsky equation



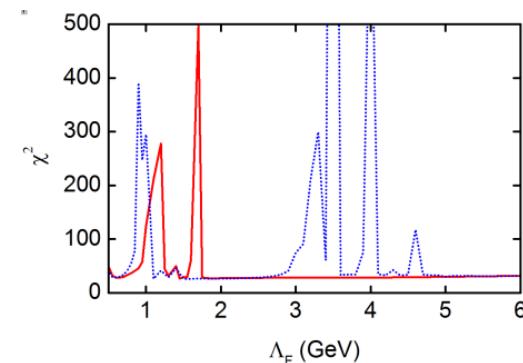
But where do these peaks come from?

Relativistic effects in the scattering equation

- Limit-cycle-like behaviors in the phase shifts

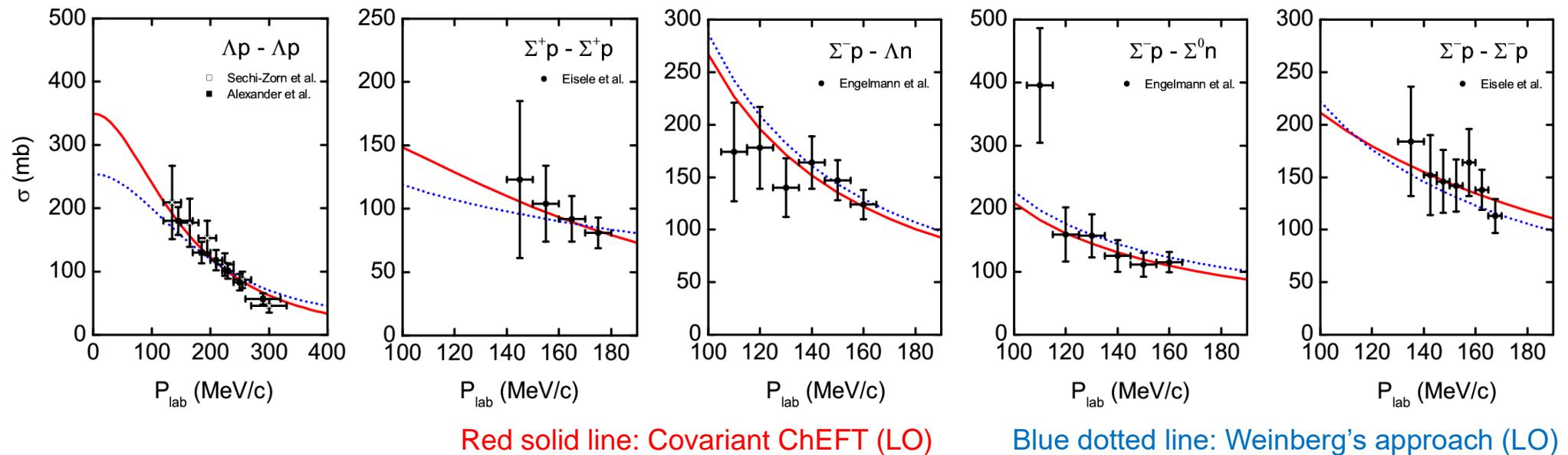


1. Limit-cycle-like behaviors appear
2. Kadyshevsky equation: cutoff dependence is mitigated



Relativistic effects in the potentials (preliminary results)

- Description of experimental data (cross sections) $\Lambda_F = 600 \text{ MeV}$



36 YN data	Weinberg's approach	Covariant ChEFT	NSC97f\$
No. of LECs (or parameters) χ^2	5 (LO*) 28.3	23 (NLO#) 16.2	12 (LO) 16.7

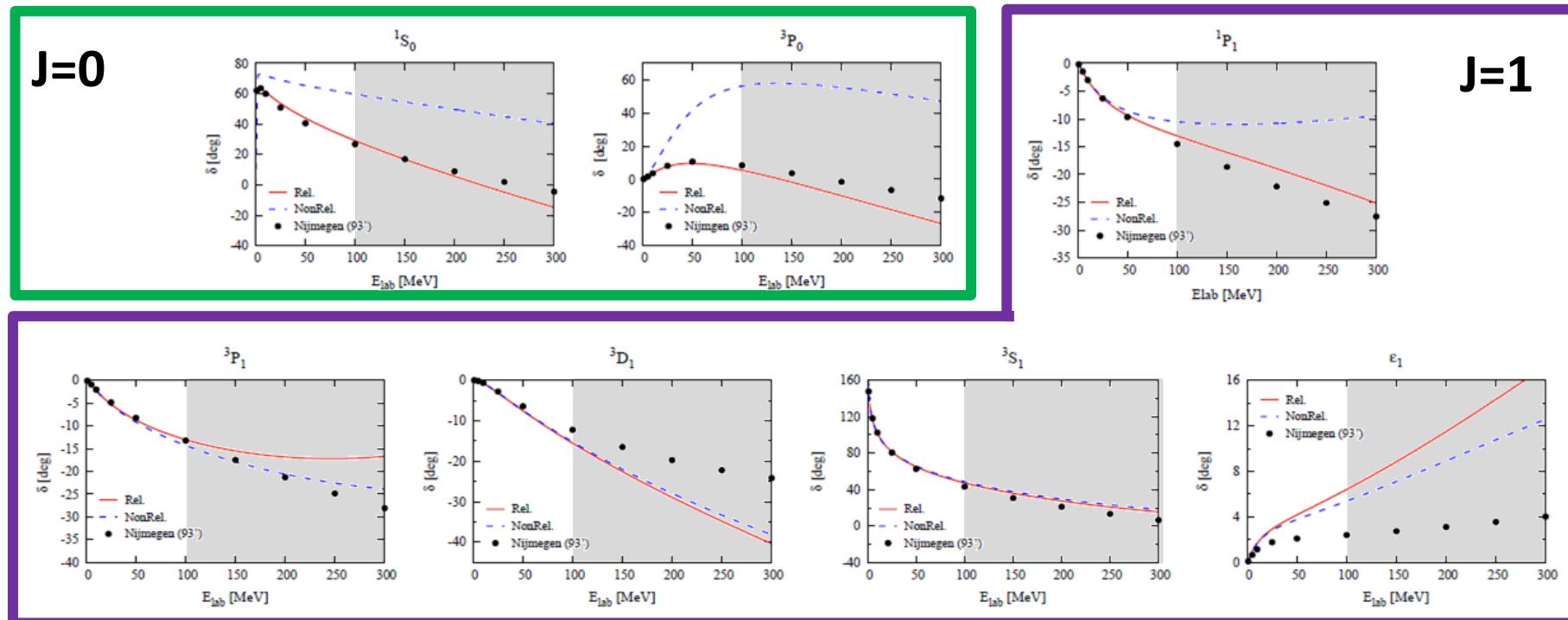
*Polinder NPA 799 (2006) 244

#Haidenbauer NPA 915 (2013) 24

\$Rijken PRC 59 (1999) 21

Covariant ChEFT in NN scattering (preliminary results)

- Phase shifts ($\Lambda_F = 750$ MeV)



	Relativistic Chiral NF	Non-relativistic Chiral NF	
Chiral order	LO	LO	NLO*
No. of LECs	5	2	9
$\chi^2/\text{d.o.f.}$	2.9	147.9	2.5

*Epelbaum NPA 671 (2000) 295

Ren, Li, Geng, Meng and Ring. In preparation

1. Background and significance
2. Chiral effective field theory
3. A covariant ChEFT approach
4. Results and discussion
5. Summary and outlook

Summary and outlook

- Summary
1. Hyperon-nucleon scattering is studied in a covariant ChEFT approach at leading order
 - Covariant chiral Lagrangians
 - Relativistic potentials
 - (Semi-)Relativistic scattering equation
 2. Relativistic effects in the scattering equation: cutoff dependence is mitigated
 3. Relativistic effects in the potentials: better description of experimental data

Summary and outlook

- Outlook
 - 1. Strangeness $S = -2, -3, -4$ systems
 - $\Lambda\Lambda, \Sigma\Lambda, \Sigma\Sigma, \Xi N$ (-2)
 - $\Xi\Lambda, \Xi\Sigma$ (-3)
 - $\Xi\Xi$ (-4)
 - 2. Few/Many-body calculations
 - As further constraints to pin down the LECs
 - Predictions: new $\Lambda/\Lambda\Lambda/\Xi$ hypernuclei?



thanks

Leading order potentials (1st improvement)

- Non-derivative four-baryon contact terms (LSJ basis, all $J=0 \& 1$)

$$\begin{aligned} V_{B_1 B_2}^{\text{CT}}(1S_0) &= 4\pi X_0 [(C_1 + C_2 - 6C_3 + 3C_4)(1 + A^2 B^2) + (3C_2 + 6C_3 + C_4 + C_5)(A^2 + B^2)] \\ &\equiv 4\pi X_0 \left[\textcolor{red}{C}_{1S0}^{B_1 B_2} (1 + A^2 B^2) + \hat{C}_{1S0}^{B_1 B_2} (A^2 + B^2) \right] \end{aligned}$$

$$\begin{aligned} V_{B_1 B_2}^{\text{CT}}(3S_1) &= 4\pi X_0 \left[\frac{1}{9}(C_1 + C_2 + 2C_3 - C_4)(9 + A^2 B^2) + \frac{1}{3}(C_2 + 2C_3 - C_4 - C_5)(A^2 + B^2) \right] \\ &\equiv 4\pi X_0 \left[\frac{1}{9} \textcolor{red}{C}_{3S1}^{B_1 B_2} (9 + A^2 B^2) + \frac{1}{3} \hat{C}_{3S1}^{B_1 B_2} (A^2 + B^2) \right] \end{aligned}$$

$$V_{B_1 B_2}^{\text{CT}}(3P_1) = 4\pi X_0 \left[-\frac{4}{3}(C_1 - 2C_2 + 4C_3 + 2C_4 - C_5)AB \right] \equiv 4\pi X_0 \left[-\frac{4}{3} \textcolor{red}{C}_{3P1}^{B_1 B_2} AB \right]$$

with

$$X_0(\mathbf{p}', \mathbf{p}) = \frac{(E_{p'} + M_B)(E_p + M_B)}{4M_B^2}, \quad A(\mathbf{p}') = \frac{|\mathbf{p}'|}{E_{p'} + M_B}, \quad B(\mathbf{p}) = \frac{|\mathbf{p}|}{E_p + M_B}.$$

We choose the 5 LECs in 1S_0 , 3S_1 and 3P_1 to be independent!
(Others in 3P_0 , 1P_1 , 3S_1 - 3D_1 , 3D_1 - 3S_1 , 3D_1 are not.)

Leading order potentials (1st improvement)

- Non-derivative four-baryon contact terms (LSJ basis, all $J=0 \& 1$)

$$\begin{aligned} V_{B_1 B_2}^{\text{CT}}({}^3P_0) &= 4\pi X_0 [-2(C_1 - 4C_2 - 4C_4 + C_5)AB] \\ &= 4\pi X_0 \left[-2(-\mathbf{C}_{1S0}^{B_1 B_2} - \hat{C}_{1S0}^{B_1 B_2} + 2\mathbf{C}_{3S1}^{B_1 B_2} - 2\hat{C}_{3S1}^{B_1 B_2})AB \right] \end{aligned}$$

$$V_{B_1 B_2}^{\text{CT}}({}^1P_1) = 4\pi X_0 \left[-\frac{2}{3}(C_1 + C_5)AB \right] = 4\pi X_0 \left[-\frac{2}{3}(\mathbf{C}_{3S1}^{B_1 B_2} - \hat{C}_{3S1}^{B_1 B_2})AB \right]$$

$$\begin{aligned} V_{B_1 B_2}^{\text{CT}}({}^3S_1 - {}^3D_1) &= 4\pi X_0 \left[\frac{2}{9}\sqrt{2}(C_1 + C_2 + 2C_3 - C_4)A^2B^2 + \frac{2}{3}\sqrt{2}(C_2 + 2C_3 - C_4 - C_5)B^2 \right] \\ &\equiv 4\pi X_0 \left[\frac{2}{9}\sqrt{2}\mathbf{C}_{3S1}^{B_1 B_2}A^2B^2 + \frac{2}{3}\sqrt{2}\hat{C}_{3S1}^{B_1 B_2}B^2 \right] \end{aligned}$$

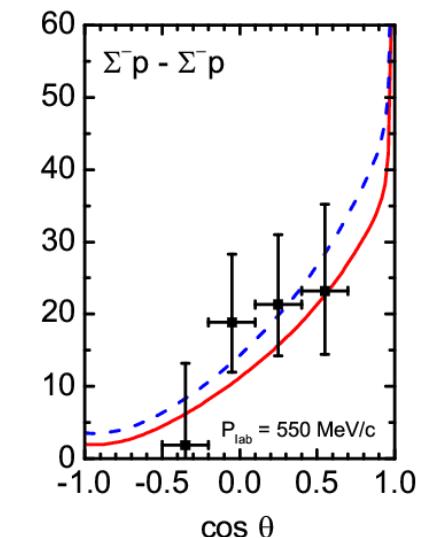
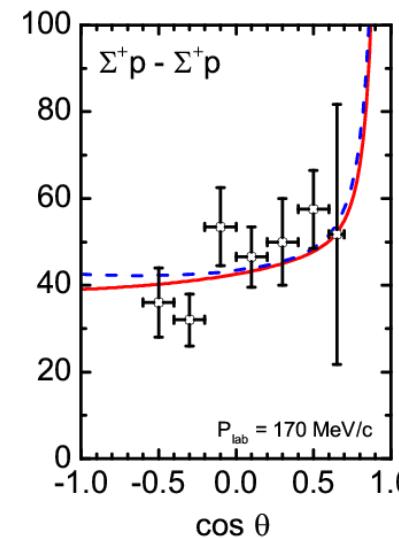
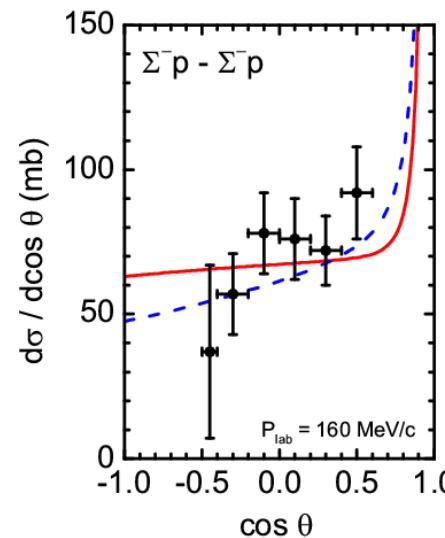
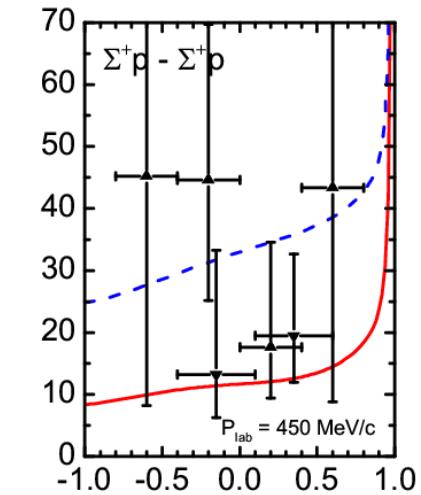
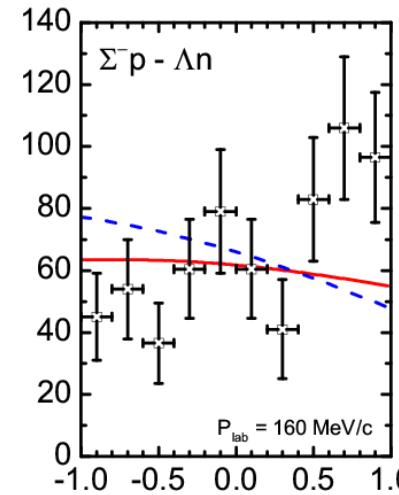
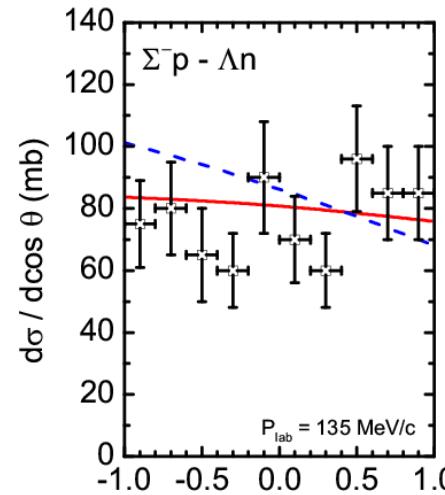
$$\begin{aligned} V_{B_1 B_2}^{\text{CT}}({}^3D_1 - {}^3S_1) &= 4\pi X_0 \left[\frac{2}{9}\sqrt{2}(C_1 + C_2 + 2C_3 - C_4)A^2B^2 + \frac{2}{3}\sqrt{2}(C_2 + 2C_3 - C_4 - C_5)A^2 \right] \\ &\equiv 4\pi X_0 \left[\frac{2}{9}\sqrt{2}\mathbf{C}_{3S1}^{B_1 B_2}A^2B^2 + \frac{2}{3}\sqrt{2}\hat{C}_{3S1}^{B_1 B_2}A^2 \right] \end{aligned}$$

$$V_{B_1 B_2}^{\text{CT}}({}^3D_1) = 4\pi X_0 \left[\frac{8}{9}(C_1 + C_2 + 2C_3 - C_4)A^2B^2 \right] \equiv 4\pi X_0 \left[\frac{8}{9}\mathbf{C}_{3S1}^{B_1 B_2}A^2B^2 \right]$$

Not independent LECs!

Differential cross sections

$\Lambda_F = 600$ MeV

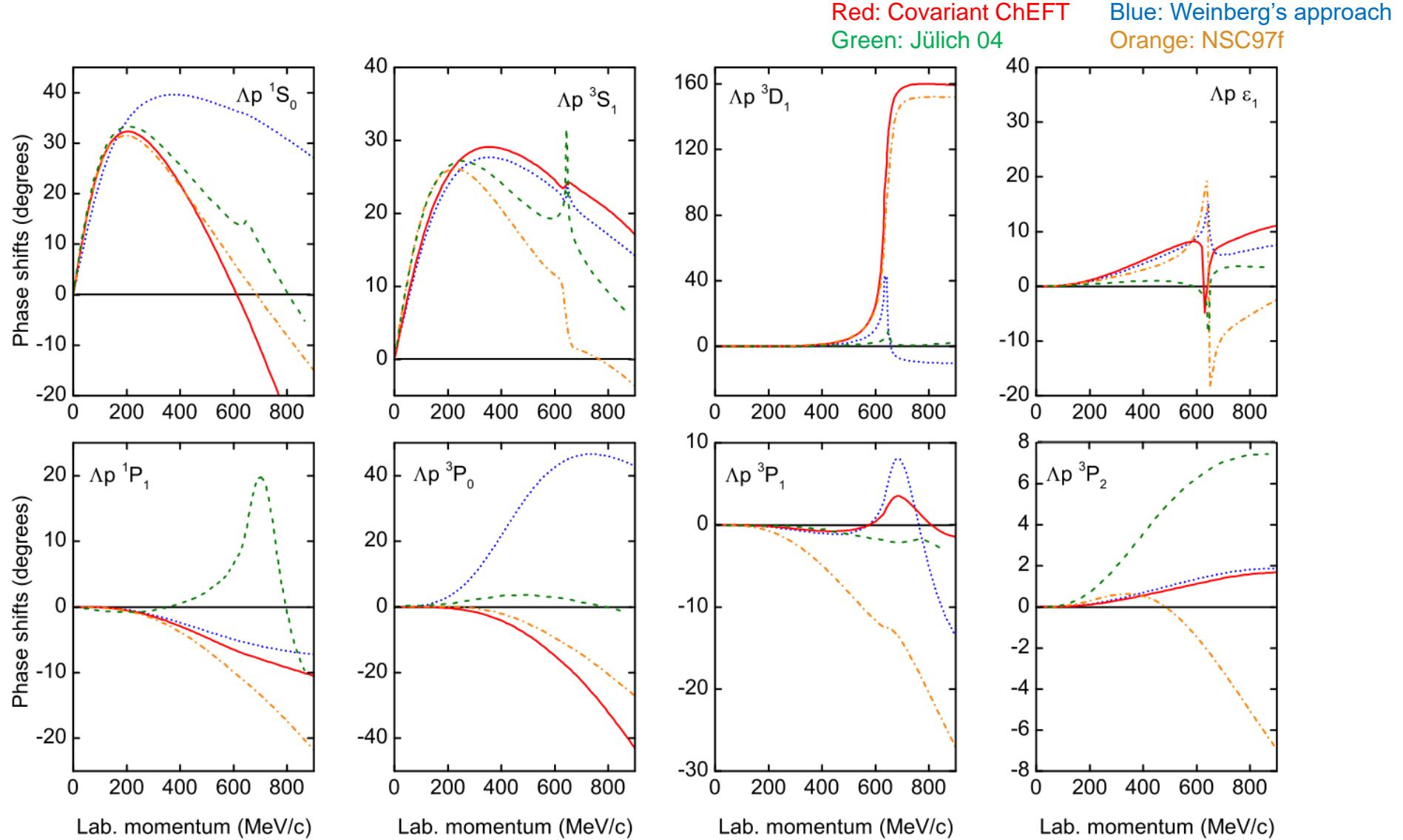


Red solid line: Covariant ChEFT (LO)

Blue dotted line: Weinberg's approach (LO)

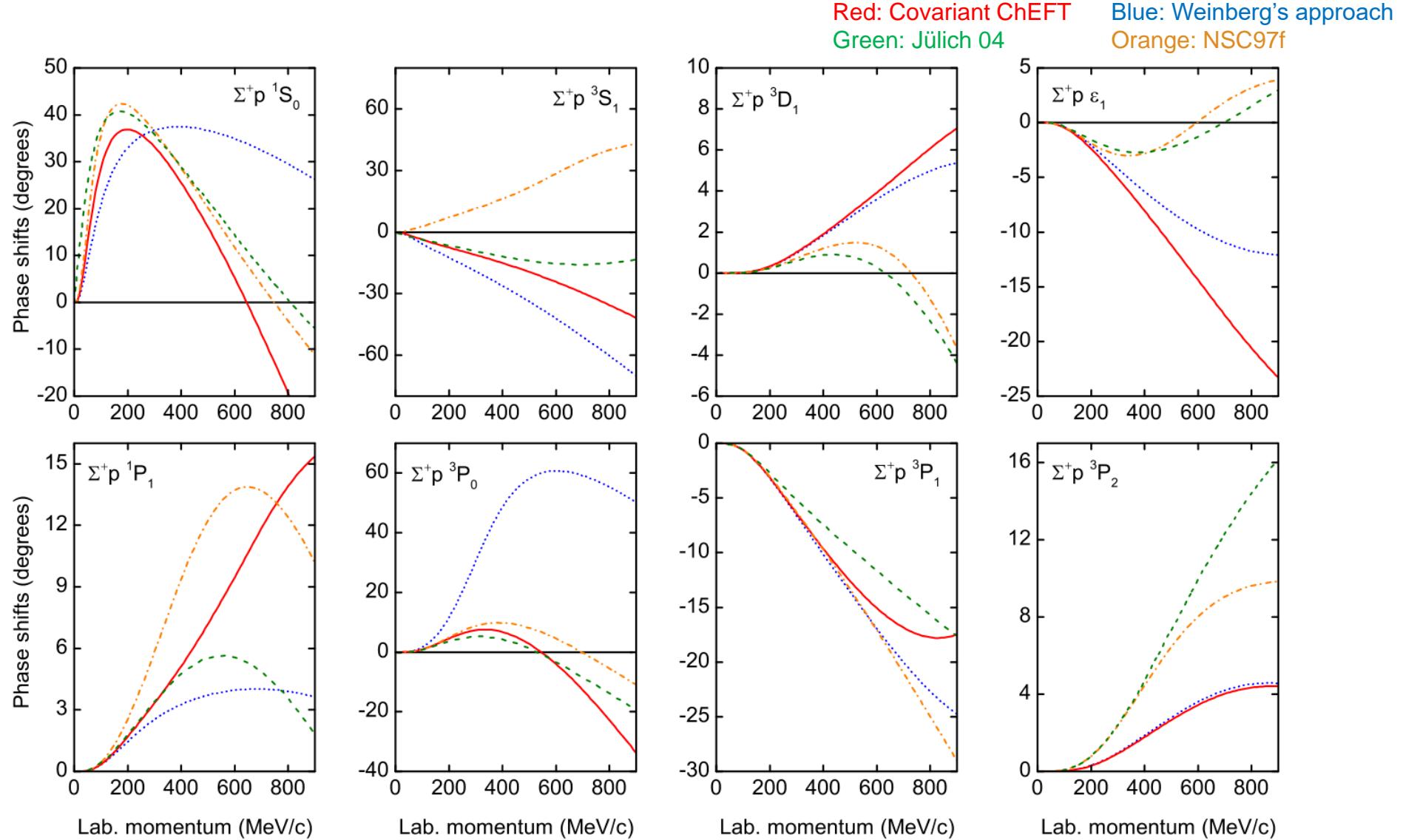
Phase shifts

$\Lambda_F = 600$ MeV



Phase shifts

$\Lambda_F = 600$ MeV



Scattering lengths

Λp	Weinberg's approach	Covariant ChEFT	NSC97f
1S_0	-1.91 (LO) -2.91 (NLO)	-2.45	-2.60
3S_1	-1.23 -1.54	-1.32	-1.72

$$a_s = -1.8 \begin{cases} +2.3 \text{ fm} \\ -4.2 \text{ fm} \end{cases} \quad \text{and} \quad a_t = -1.6 \begin{cases} +1.1 \text{ fm} \\ -0.8 \text{ fm}, \end{cases}$$

A. Gasparyan PRC 69 (2004) 034006, extract from final-state interaction

$\Sigma^+ p$	Weinberg's approach	Covariant ChEFT	NSC97f
1S_0	-2.32 (LO) -3.56 (NLO)	-4.15	-4.35
3S_1	0.65 0.49	0.38	-0.25