

HIGH PRECISION MEASUREMNT OF THE 3-ALPHA DECAY FROM THE HOYLE STATE IN THE $^{12}\text{C}(^{12}\text{C},3\alpha)^{12}\text{C}$ REACTION

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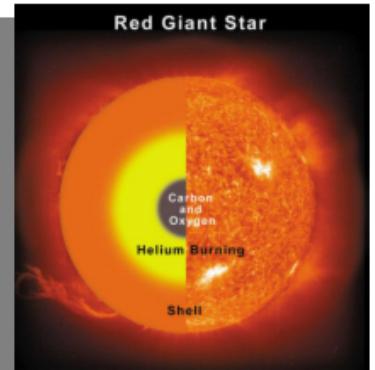
**“The 26th International Nuclear Physics Conference (INPC2016)”,
Adelaide Convention Center, Australia, 11-16 September 2016**

Outline

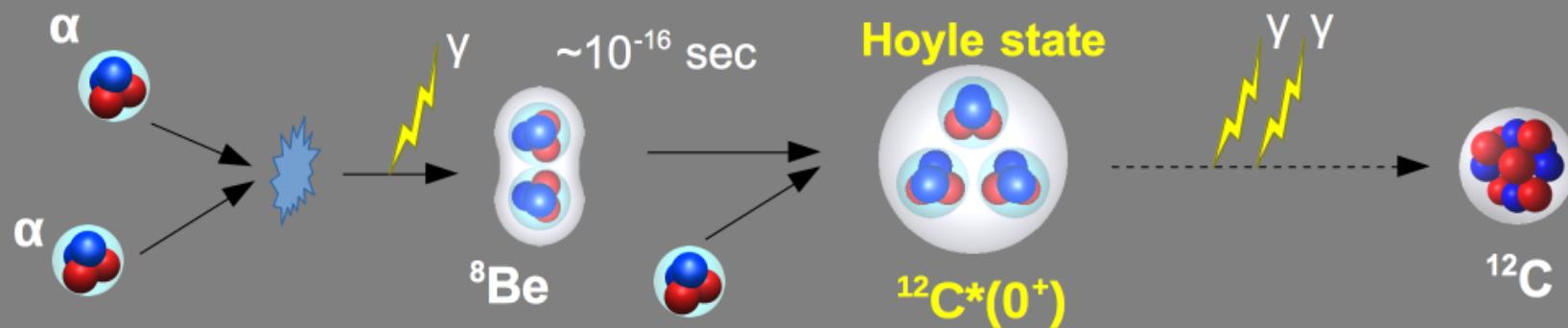
- **Introduction to the Hoyle state**
- **Motivation of this study**
- **Measurement of the 3α decay of the Hoyle state**
- **Summary**

Introduction to the Hoyle state

- The Hoyle state is the second 0^+ state at 7.65 MeV in ^{12}C and a key state to create the carbon nucleus in the star.



- No stable nuclei of $A=5$ and 8 → **Triple-alpha reaction**



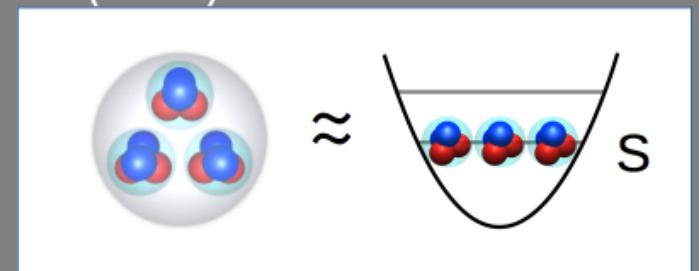
- Structure of the Hoyle state strongly affect the formation of the carbon nucleus.

Structure of the Hoyle state

- Possibility of the α particle condensate in ^{12}C and ^{16}O

A. Tohsaki, H. Horiuchi, P. Schuck, and G. Röpke, PRL 87 (2001) 192501

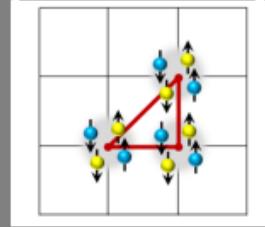
- Gas-like 3α structure = 3α condensate



- Ab initio lattice calculation

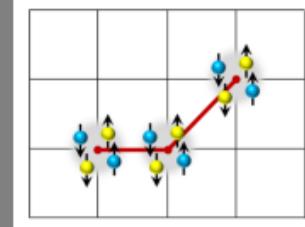
E.Epelbaum, Ulf-G.Meissner et al, PRL109(2012)252501

Compact triangular



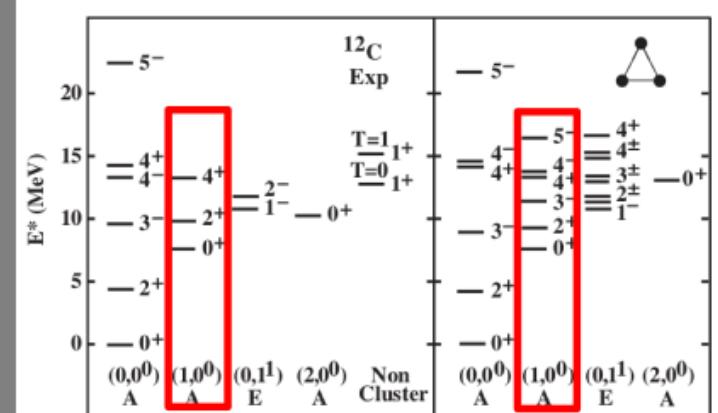
Ground state

Bent-arm



Hoyle state

A symmetric vibration mode
of the triangular configuration

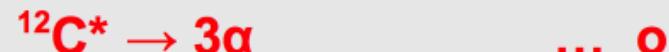


- Algebraic Cluster Model

R.Bijker and F.Iachello, PRC61(2000)067305

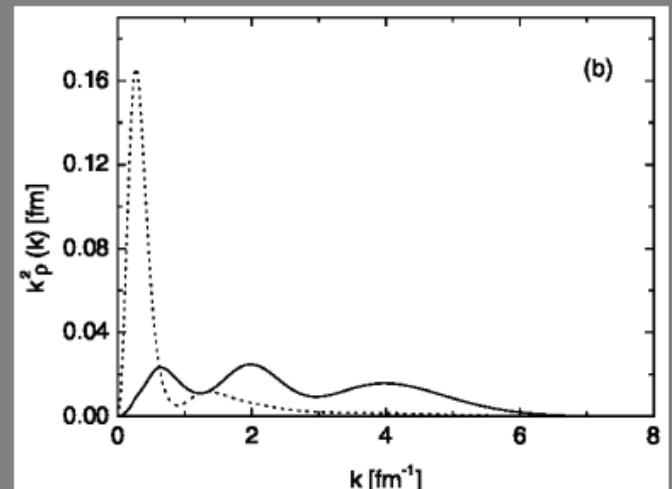
Motivation

- To determine the structure of the Hoyle state experimentally
 - When the Hoyle state decay to three α particles directly, they are supposed to keep the information on the Hoyle state, although it may be very small.



- Momentum distribution of α clusters

Small dispersion = Spatially spreading



T. Yamada and P. Schuck,
Eur. Phys. J. A 26 (2005) 185.

Outline

- Introduction to the Hoyle state
- Motivation of this study
- Measurement of the 3α decay of the Hoyle state
- Summary

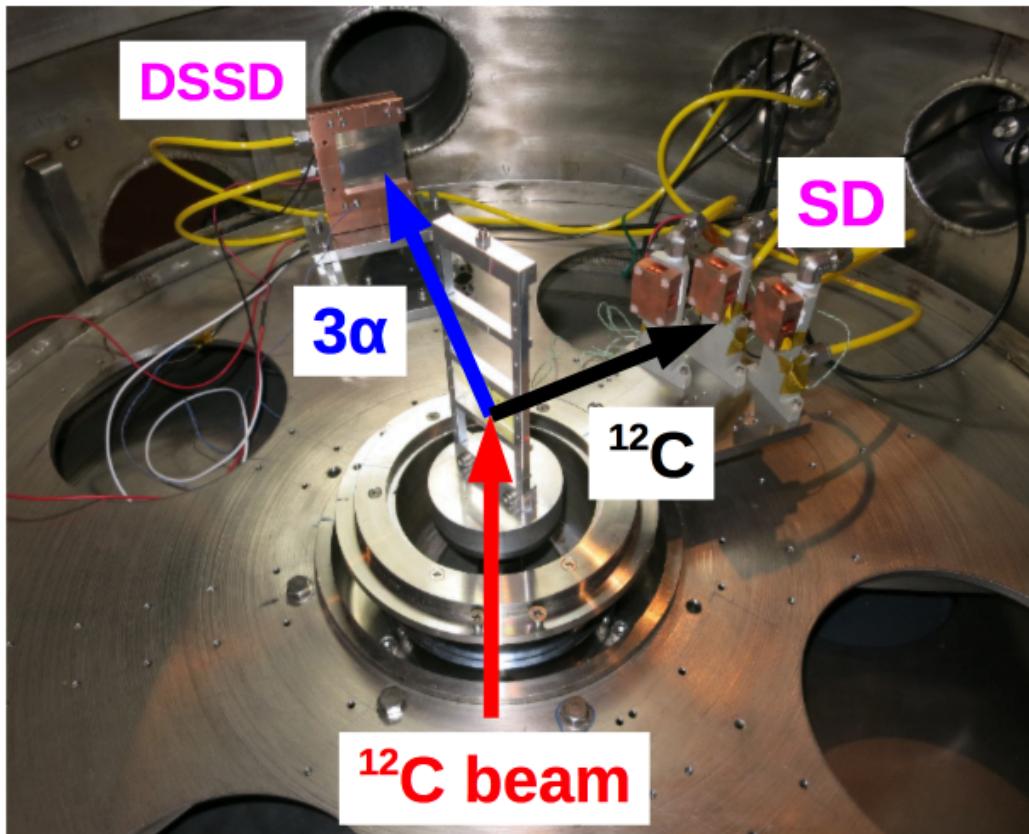
Experimental situation on the direct 3α decay

Exp.	Reaction	Events	Direct Decay branch	comment
M.Freer <i>et al</i> , PRC49,R1751(1994)	$^{12}\text{C}(^{12}\text{C},3\alpha)$	~2000	< 4%	$E_{^{12}\text{C}} = 58 \text{ MeV}$
Ad.R.Raduta <i>et al</i> , PLB705, 65(2011)	$^{40}\text{Ca} + ^{12}\text{C}$	~1000	17(5)%	25 MeV/u
J.Manfredi <i>et al</i> , PRC85,037603(2012)	$^{10}\text{C} + \text{Be, C}$	~4000	<3.9%	10.7 MeV/u
O.S.Kirsebom <i>et al</i> , PRL108,202501(2012)	$^{11}\text{B}(^3\text{He},d3\alpha)$	~5000	<0.5%	$E_{^3\text{He}} = 8.5 \text{ MeV}$
T.K.Rana <i>et al</i> , PRC88,021601(R) (2013)	$^{12}\text{C}(\alpha,\alpha' 3\alpha)$	~20000	0.91(14)%	$E_\alpha = 60 \text{ MeV}$

Experiment at CYRIC

$^{12}\text{C}(\textcolor{red}{^{12}\text{C}}, \text{^{12}\text{C}*}[3\alpha])^{12}\text{C}$ reaction at $E_{^{12}\text{C}} = 110 \text{ MeV}$

Experimental Set-up



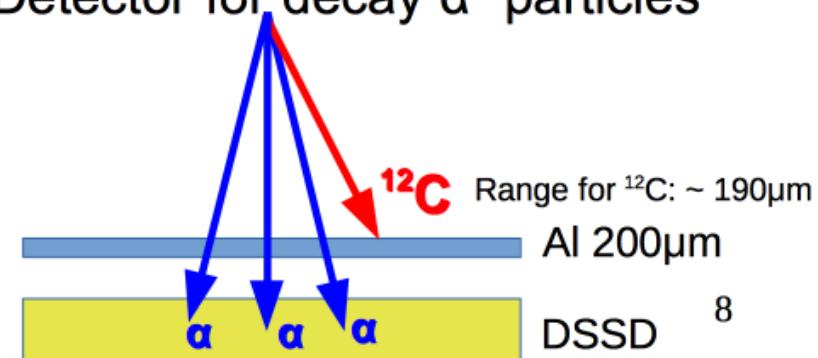
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AVF cyclotron in CYRIC



Detector for decay α particles



8

Symmetric Dalitz plot for the 3α -decay

- To visualize the energy correlation, the **symmetric Dalitz plot** for three equal masses is adopted.

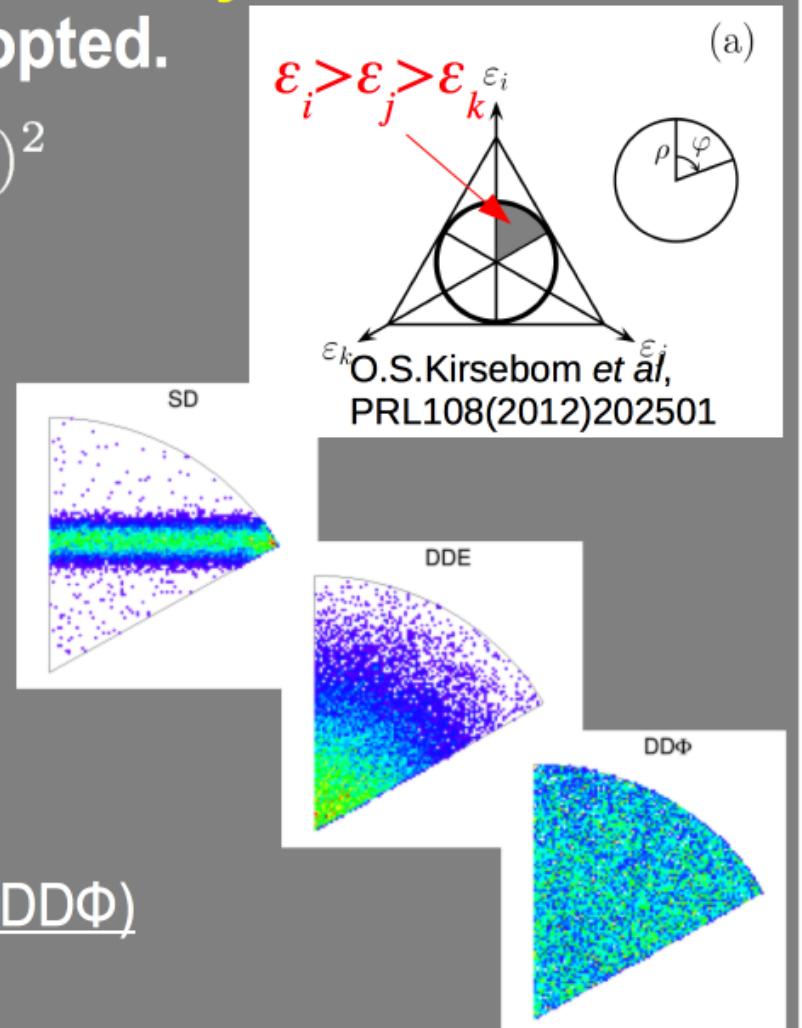
$$(3\rho)^2 = 3(\varepsilon_i - \varepsilon_k)^2 + (2\varepsilon_i - \varepsilon_j - \varepsilon_k)^2$$

$$\varepsilon_{i,j,k} = E_{i,j,k}/(E_i + E_j + E_k)$$

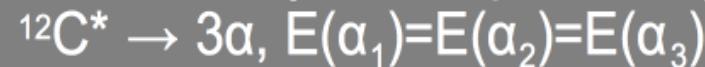
$E_{i,j,k}$: Kinetic energy of α particles

- Three decay mechanisms**

- Sequential decay (SD)



- Direct decay with equal energies(DDE)

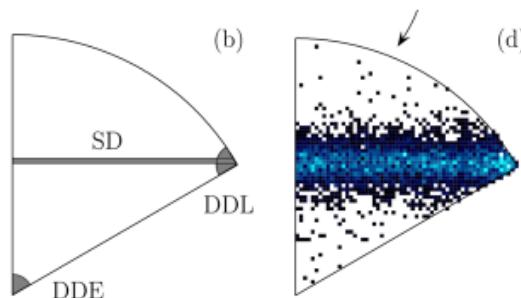
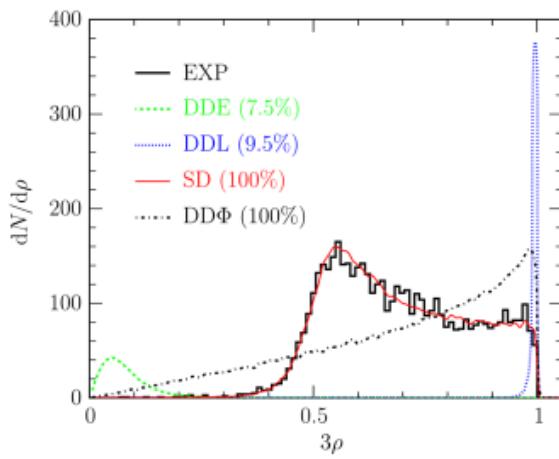


- Direct decay to phase space uniformly(DDΦ)



Comparison with recent experiments

O.S.Kirsebom et al,
PRL108,202501(2012)



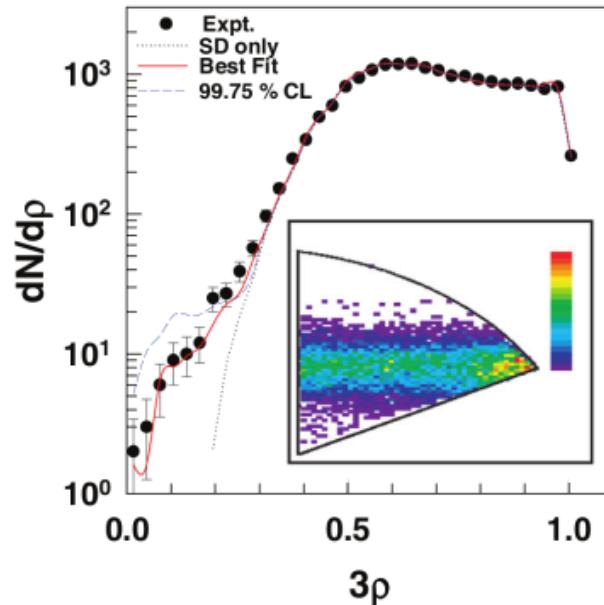
$^{11}\text{B}(\text{d},\text{d}^{\prime }\text{3}\alpha)$

~ 5000 events

Direct decay < 0.5%

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T.K.Rana et al,
PRC88, 021601(R)(2013)



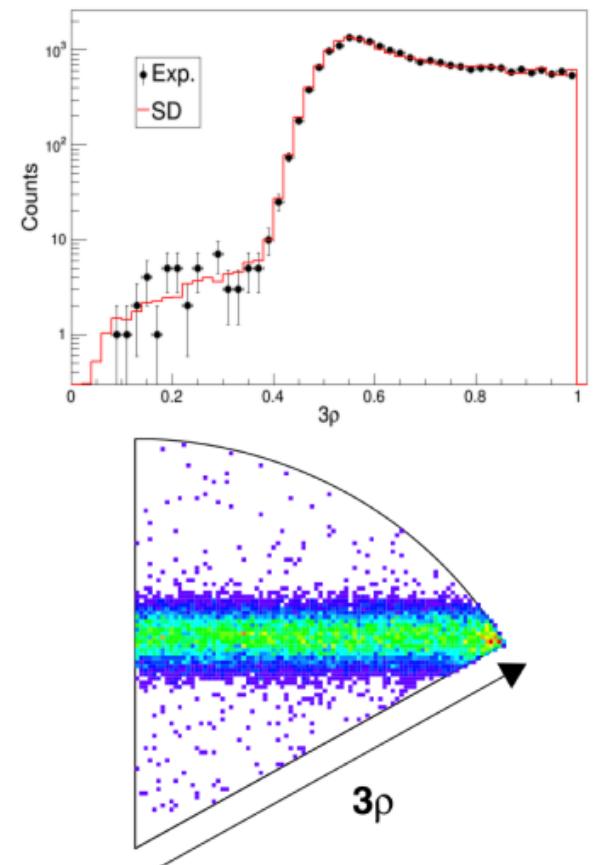
$^{12}\text{C}(\alpha,\alpha'\text{3}\alpha)$

~ 20000 events

Direct decay : 0.9%
(DDΦ:0.6%, DDE:0.3%)

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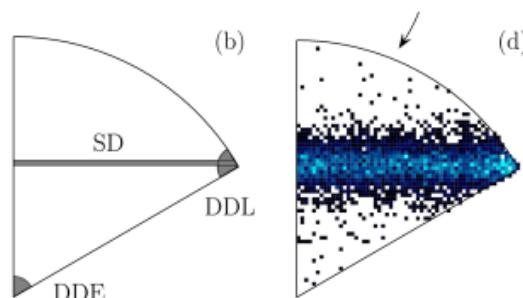
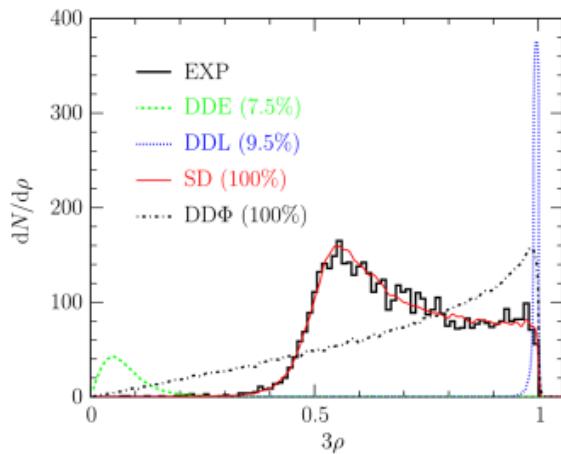
$^{12}\text{C}(\text{d},\text{d}^{\prime }\text{3}\alpha)^{12}\text{C}$

~ 21000 events

10

Comparison with recent experiments

O.S.Kirsebom et al,
PRL108,202501(2012)

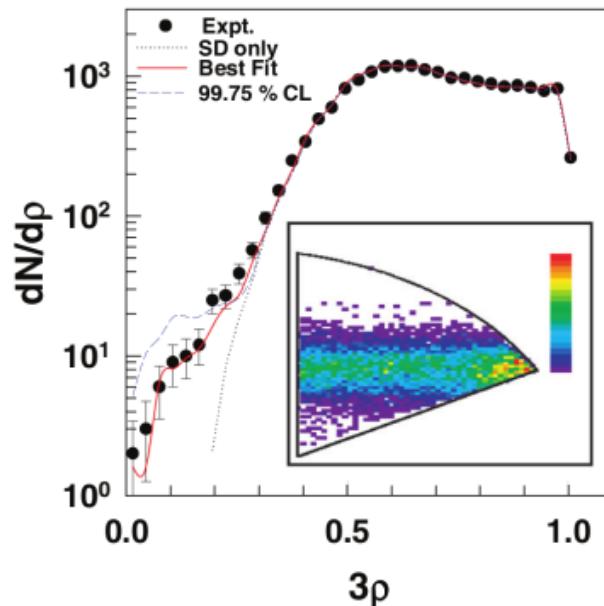


$^{11}\text{B}(\text{He},\text{d}3\alpha)$
~ 5000 events

Direct decay < 0.5%

INPC2016

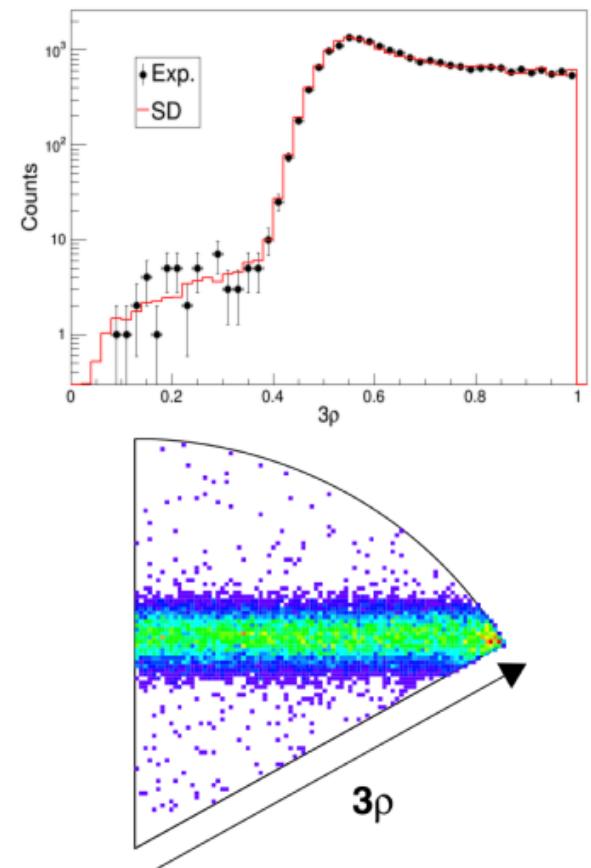
T.K.Rana et al,
PRC88, 021601(R)(2013)



$^{12}\text{C}(\alpha,\alpha'3\alpha)$
~ 20000 events
Direct decay : 0.9%
(DDΦ:0.6%, DDE:0.3%)

M.Itoh

CYRIC



Direct decay < 0.2 %
MI et al, PRL113,102501(2014)

~ 21000 events

11

Decay mode of the Hoyle state in the 3α particle model

- $E_2 < \delta E_{DDL}$ (~ 30 keV)
- $E_{rms} < \delta E_{DDE}$ (~ 30 keV)

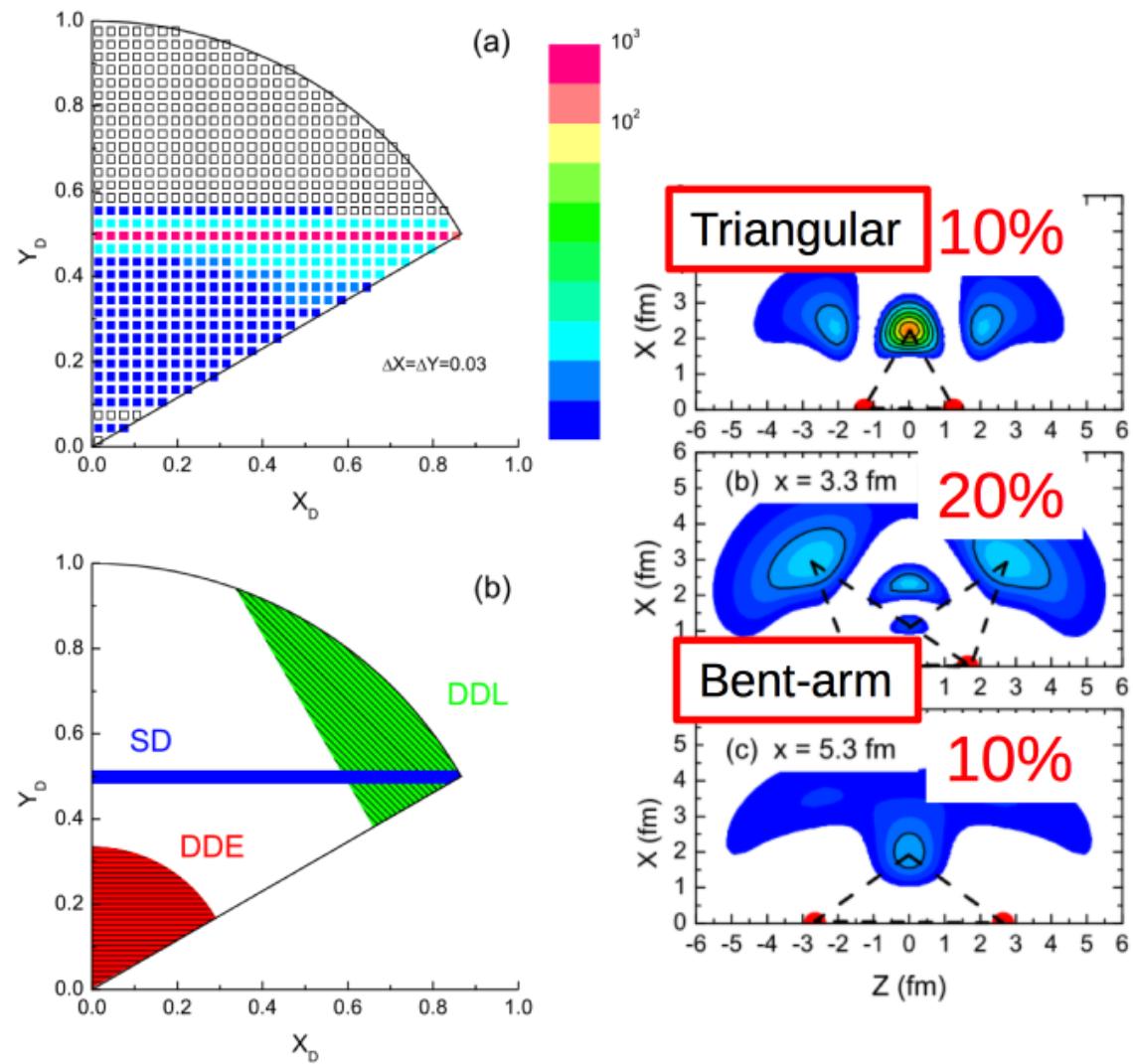
SD: 99.9%

DDE: 0.005%

DDL: 0.03%

Upper limit on Direct Decay
 $DD\Phi < 0.2\%$

M.I et al, Phys.Rev.Lett.113, 102501(2014)



M.Itoh

S.Ishikawa,
Phys.Rev.C90,061604(R)(2014)

Summary

- We performed the precise measurement of decay 3- α particles from the Hoyle state using $^{12}\text{C}(^{12}\text{C},3\alpha)^{12}\text{C}$ reaction at 110 MeV.
- **Direct decay of the Hoyle state**
 - **Further improvement of the upper limit on the direct 3- α decay** : 0.5% → 0.2%
 - In order to observe the direct 3- α decay, the sensitivity need to be improved.

Collaborators

Cyclotron and Radioisotope Center (CYRIC)

Tohoku University

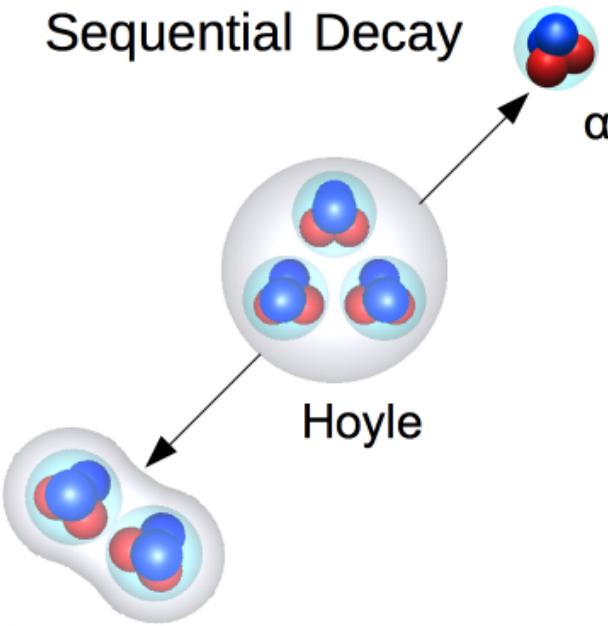
S. Ando, T. Aoki, H. Arikawa, S. Ezure, K. Harada, T. Hayamizu,
T. Inoue, T. Ishikawa, K. Kato, H. Kawamura, A. Uchiyama,
Y. Sakemi

Thank you for your attention!

Energy distribution of decay alpha particles

- “ ε_i ” : Highest normalized energy among three decay- α particles

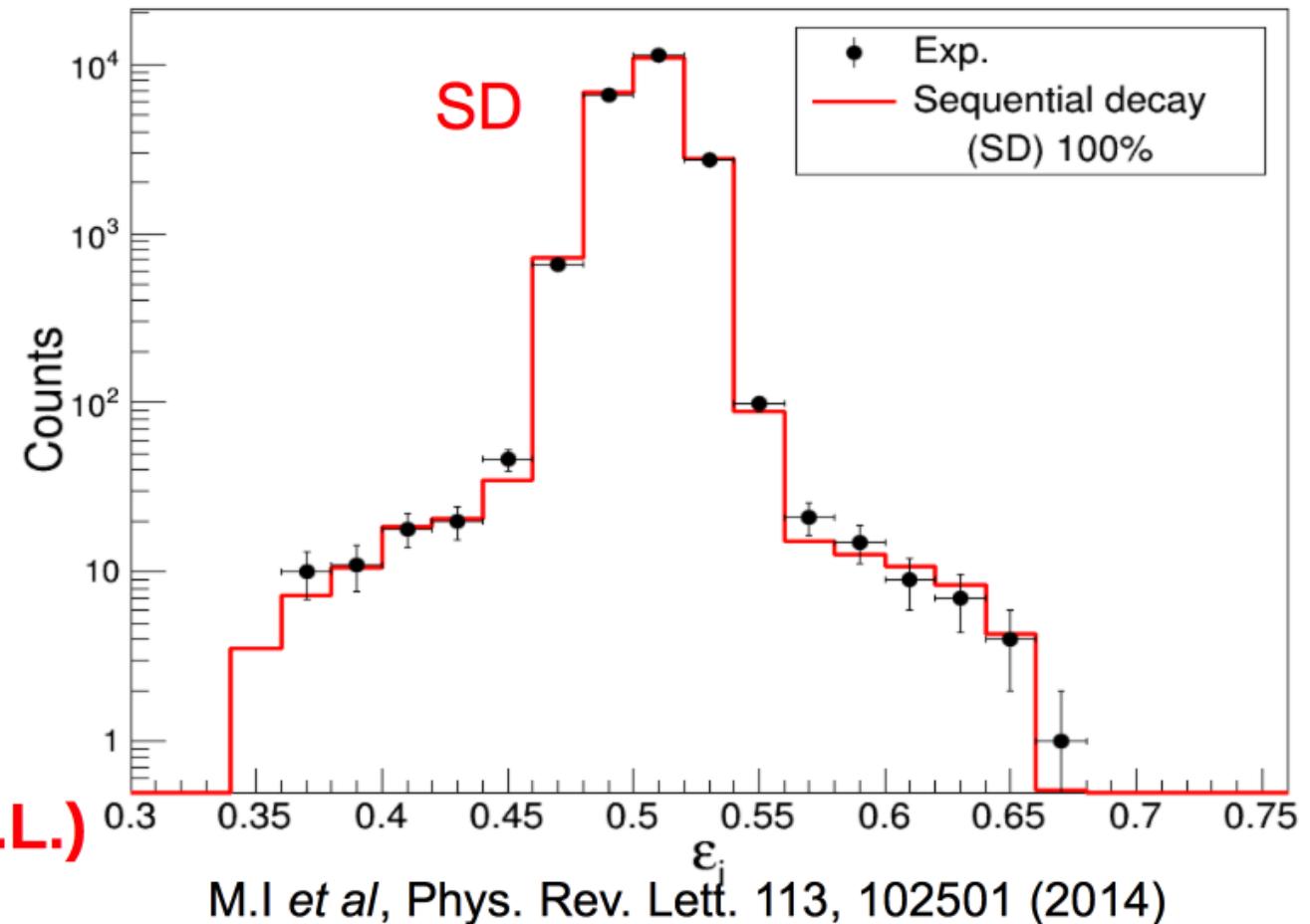
Sequential Decay



$$^{8}\text{Be} \quad \varepsilon_i \sim 0.506$$

Direct decay < 0.2%
(95% C.L.)

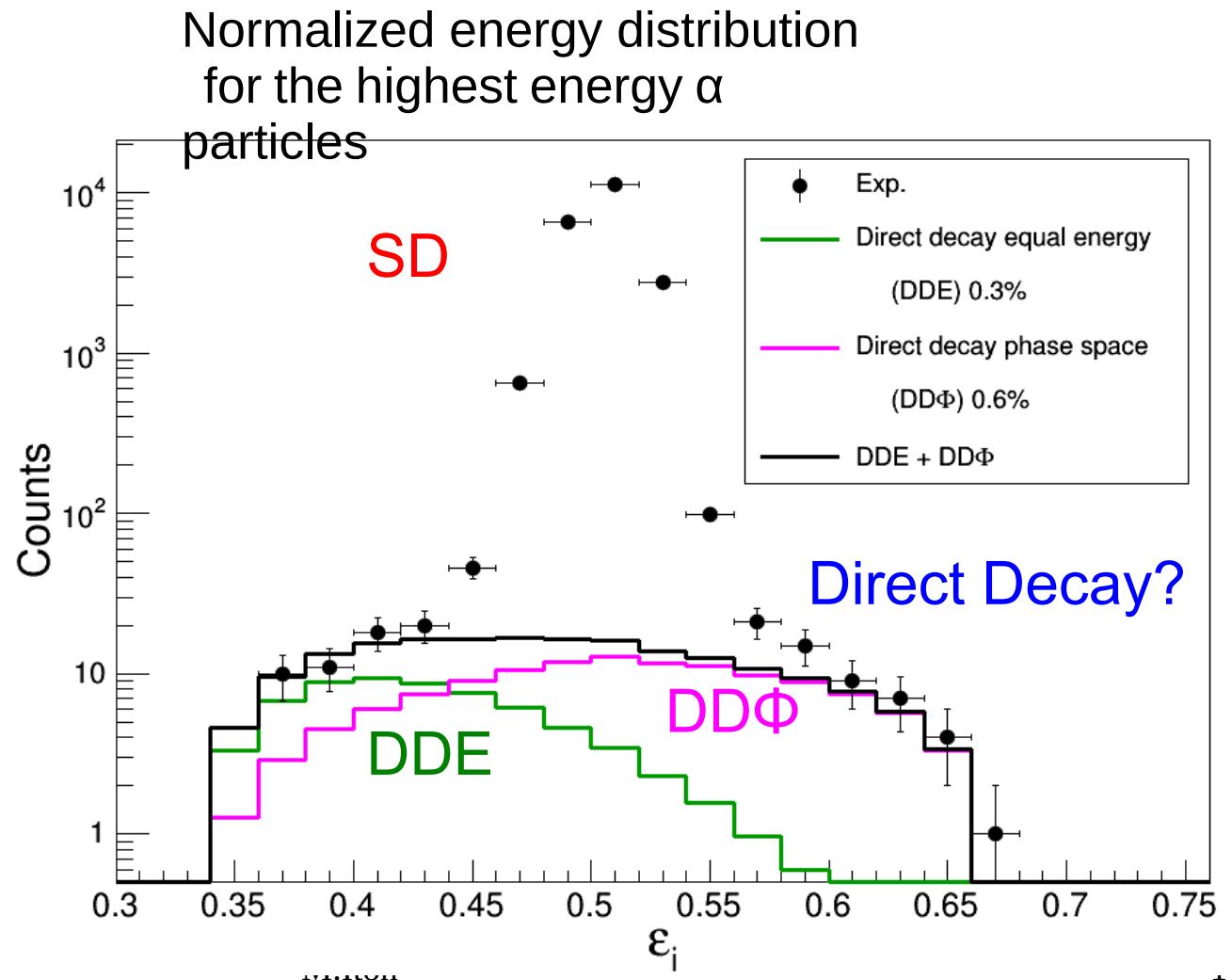
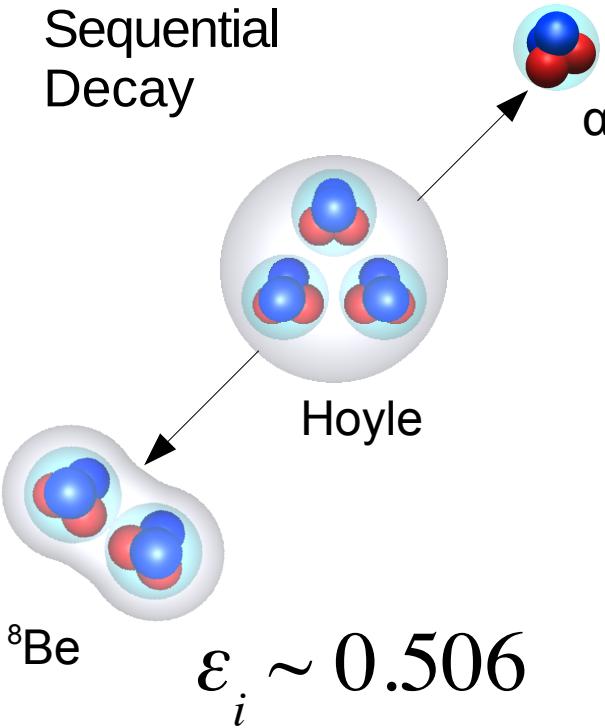
Normalized energy distribution
for the highest energy α particles



Energy distribution of decay alpha particles

- “ ε_i ” : Highest normalized energy among three decay- α particles

Sequential
Decay



$^{12}\text{C}(\alpha, \alpha' 3\alpha)$ experiment in India

- The non-zero direct components of the decay from the Hoyle state have been reported using the $^{12}\text{C}(\alpha, \alpha' 3\alpha)$ reaction.
T.K.Ranæt *et al*/PRC88,021601(R)(2013)

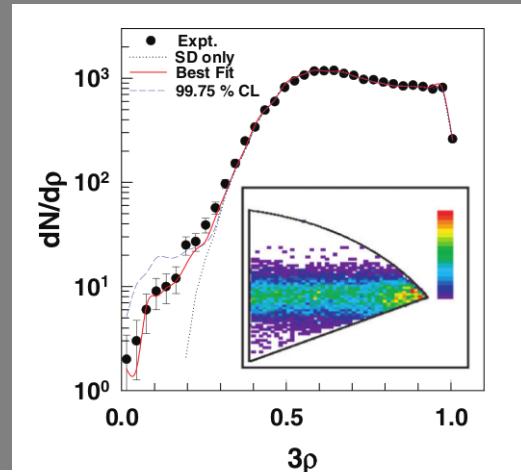
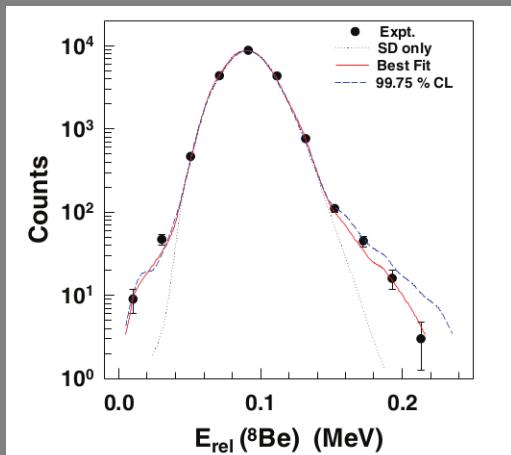


TABLE I. Comparison of different experimental estimates of direct decay modes of the Hoyle state.

Expt.	Total events	DDE (%)	DDL (%)	DDΦ (%)	Total (%)	CL
Ref. [22]	~2000 ^a	—	—	—	<4	99.5
Ref. [23]	~1000 ^b	7.5(4) ^c	9.5(4) ^c	—	17(5) ^c	
Ref. [24]	~4000 ^b	<0.45	—	<3.9	<4.35	99.75
Ref. [25]	~5000 ^a	<0.09	<0.09	<0.5	<0.68	95
Present	~20000 ^a	0.3(1) ^c	0.01(3) ^c	0.60(9) ^c	0.91(14) ^c	

II

^aFully detected events only.

^b3 α reconstructed events.

^cTotal error from statistical, χ^2 , and background.

Recent experiments

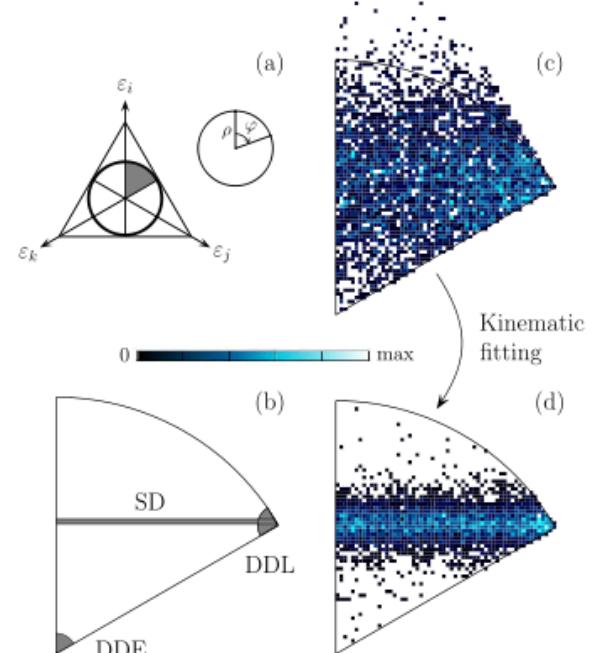
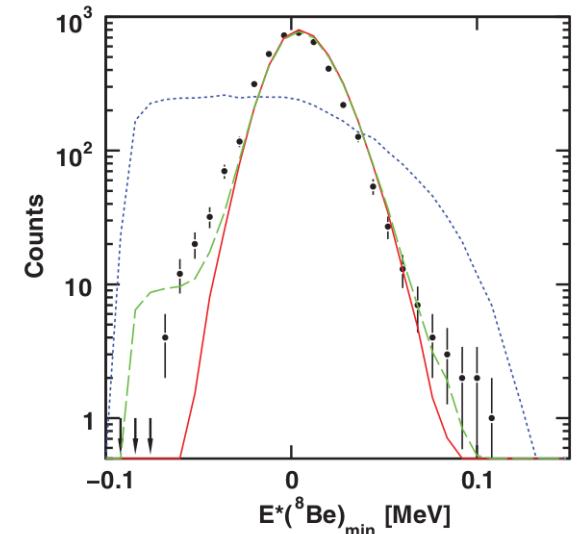
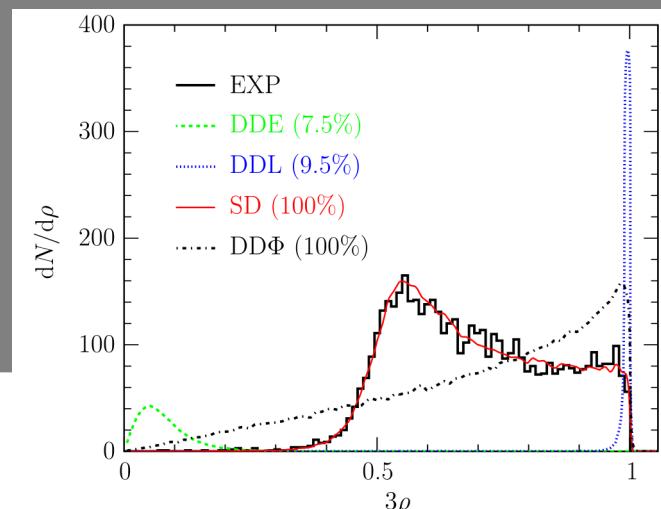
- The $^{10}\text{C} + \text{C(Be)}$ experiment

They obtained the upper limit of 3.9% for the direct 3α decay from the Hoyle state
J.Manfredi et al, PRC85,037603(2012).

- The $^{11}\text{B}(^3\text{He}, d) 3\alpha$ experiment

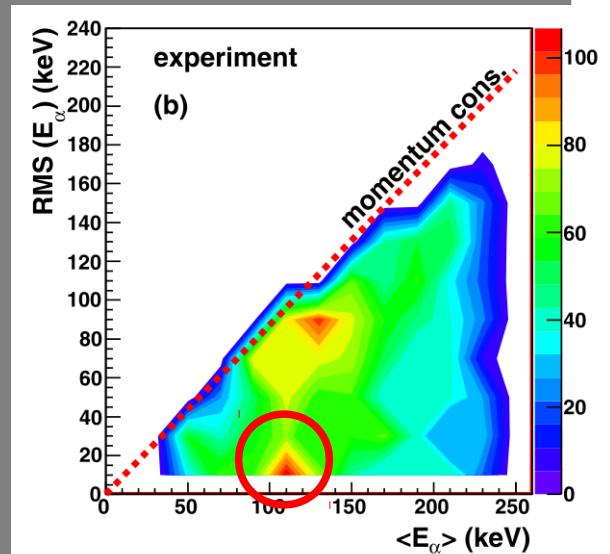
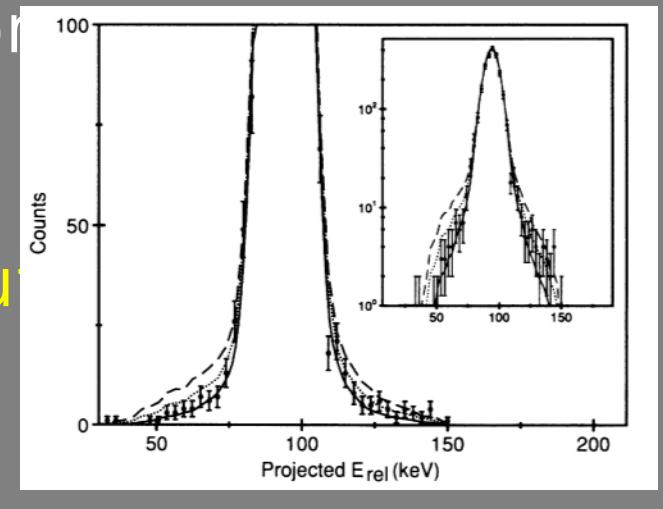
They improved the upper limit of the direct 3α decay to be $\leq 10^{-3}$.

O.S.Kirsebom et al, PRL108,202501(2012).



Experimental situation on the direct 3α decay

- Experiment of the $^{12}\text{C}(^{12}\text{C},3\alpha)^{12}\text{C}$ reaction
M.Freer et al PRC49(1994)R1751
 - Upper limits of 4% for the contribution of the direct decay process to
- In 2011, the direct decay branch of $\pm 5\%$ had been reported by Catania group. Among them, the direct decay with three α particles of equal energies was $\mp 45\%$.
Ad.R.Raduta et al PLB705(2011)65.

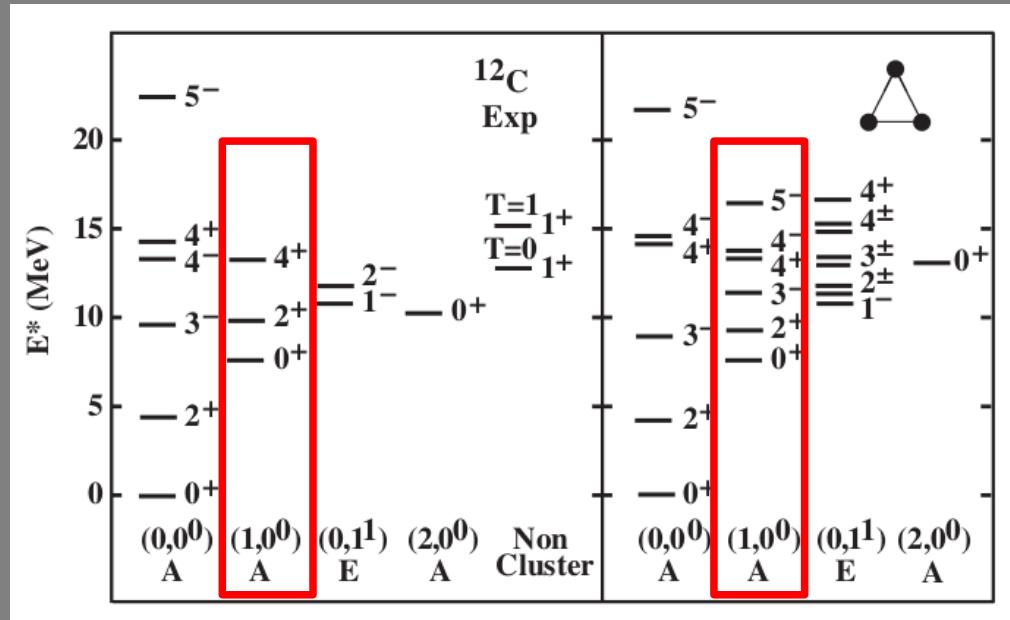


Algebraic Cluster Model in ^{12}C

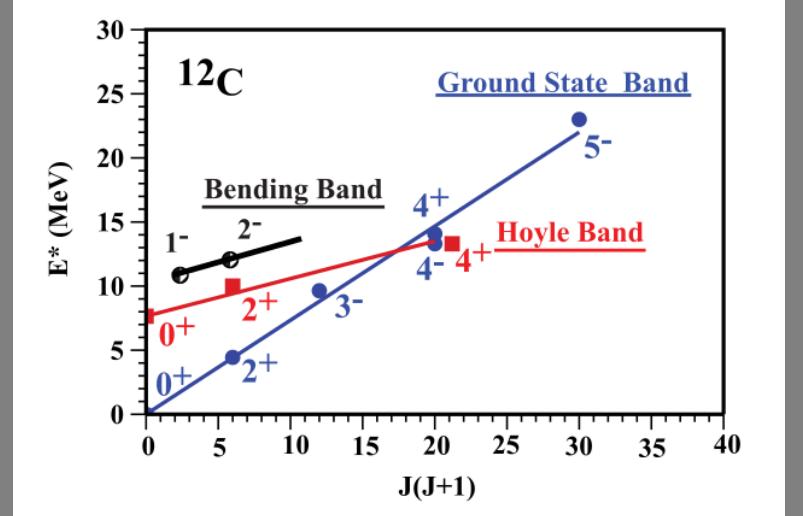
- Hoyle state: the A symmetric stretching vibration (breathing mode) of the triangular configuration

R.Bijker and F.Iachello, PRC61(2000)067305

$^{12}\text{C}(\text{He}^4, \alpha)\text{He}^4$ experiment
at Birmingham



they found 5- state at 22.4 MeV

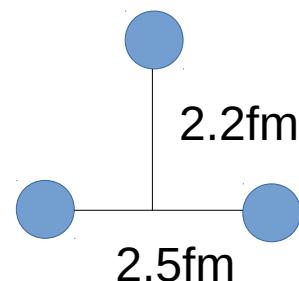


D.J.Marín-Lámbardi *et al*, Phys.Rev.Lett.113, 012502 (2014)

Structure of the Hoyle state

- Root mean square radius

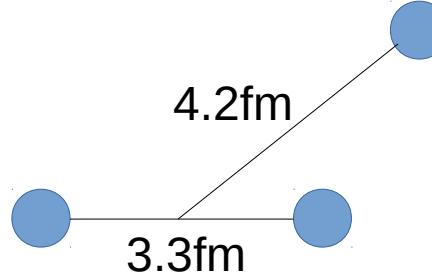
A



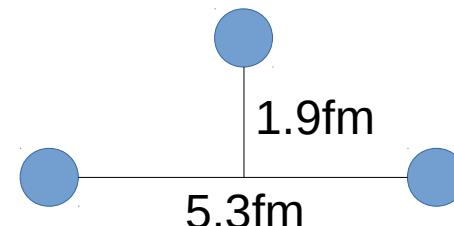
$$R_{rms} = \sqrt{R_\alpha^2 + \frac{1}{6}\langle x^2 \rangle + \frac{2}{9}\langle y^2 \rangle}$$

$$R_{rms} \sim 3.43 \text{ fm}$$

B



C

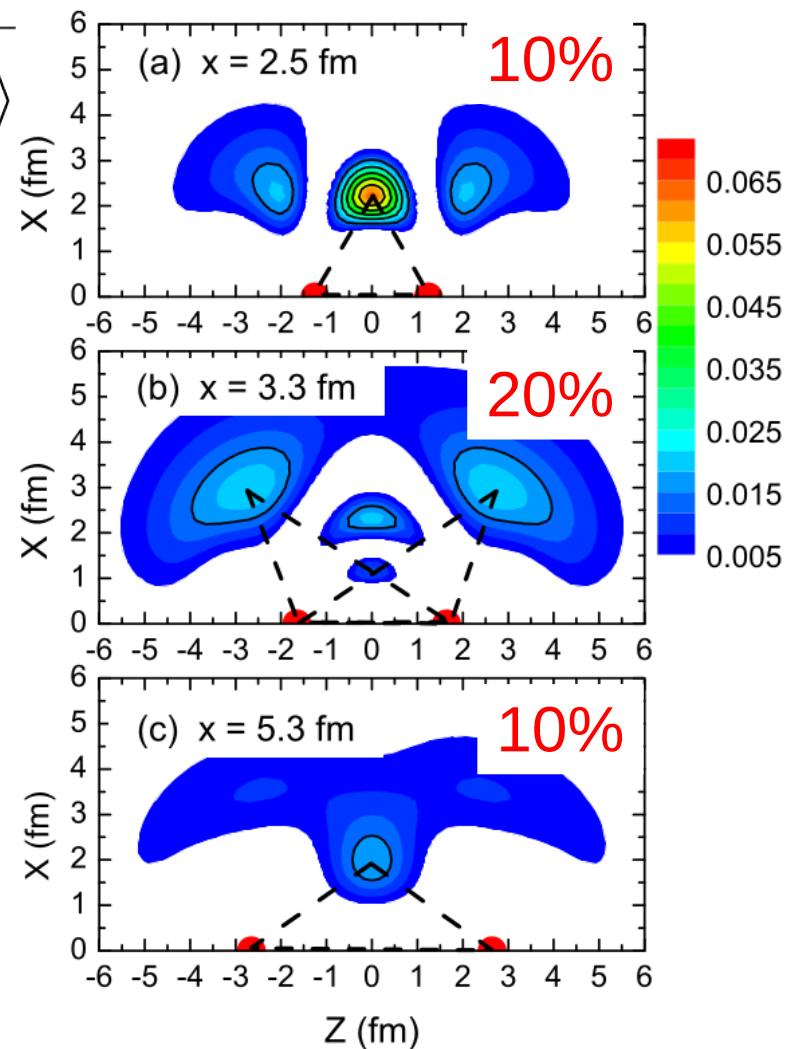


$$B=C$$

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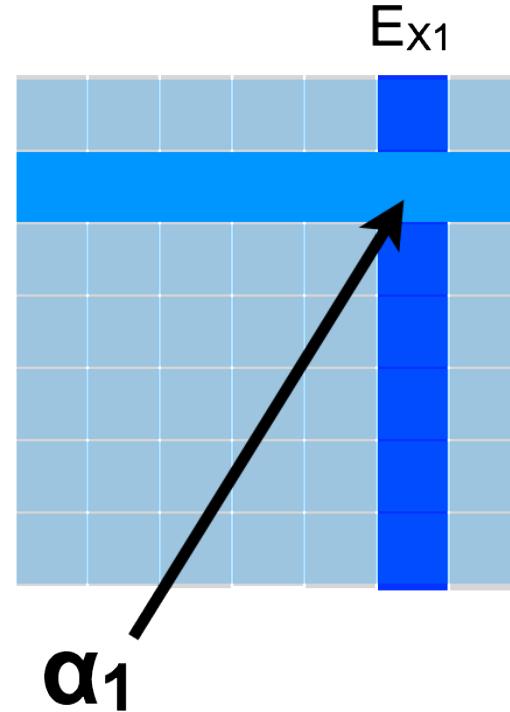
INPC2016

S.Ishikawa,
Phys.Rev.C90, 061604(R)(2014)

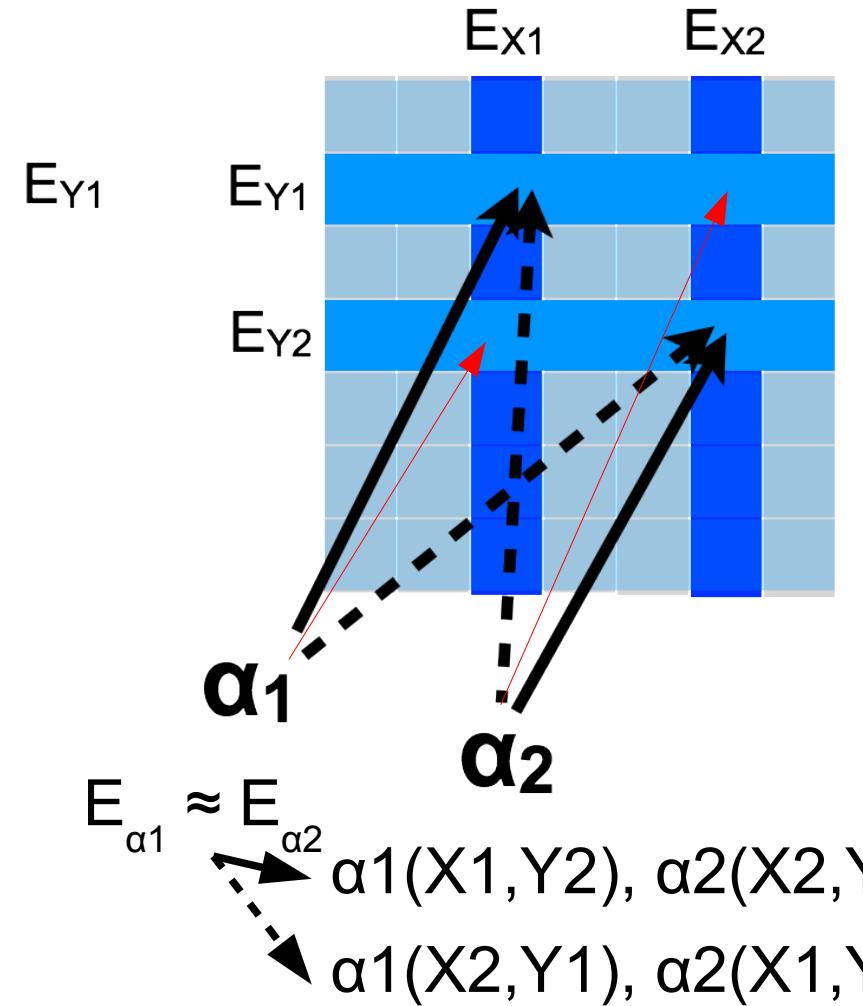


Misassignment of decay alpha particles

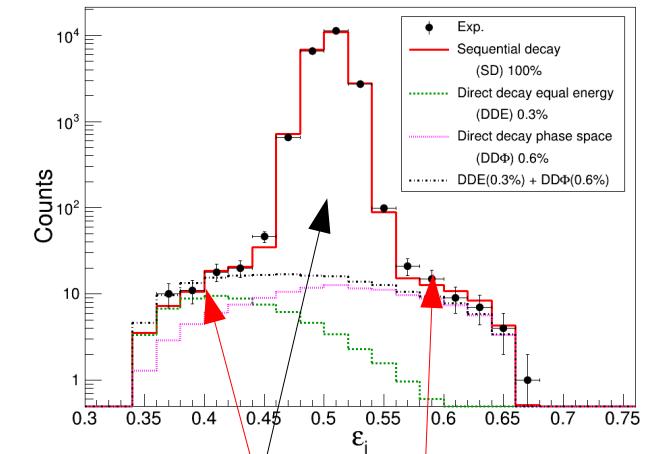
Why do the shoulders appear?



$E_{x_1} \approx E_{y_1}$
 $\rightarrow \alpha_1 (X_1, Y_1)$



... Misassignment of decay alpha particles



M.Itoh

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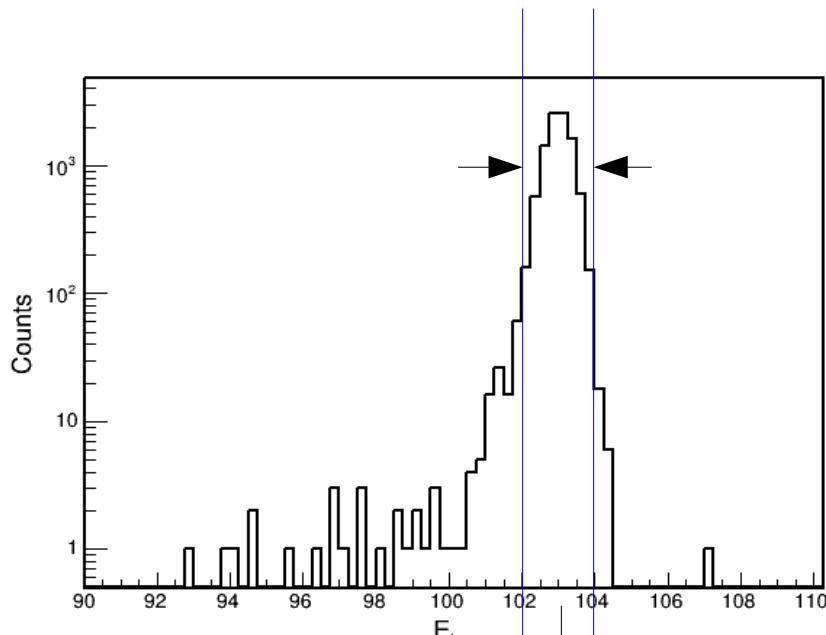
23

Misassignment

Energy spectrum for the decay 3α particles

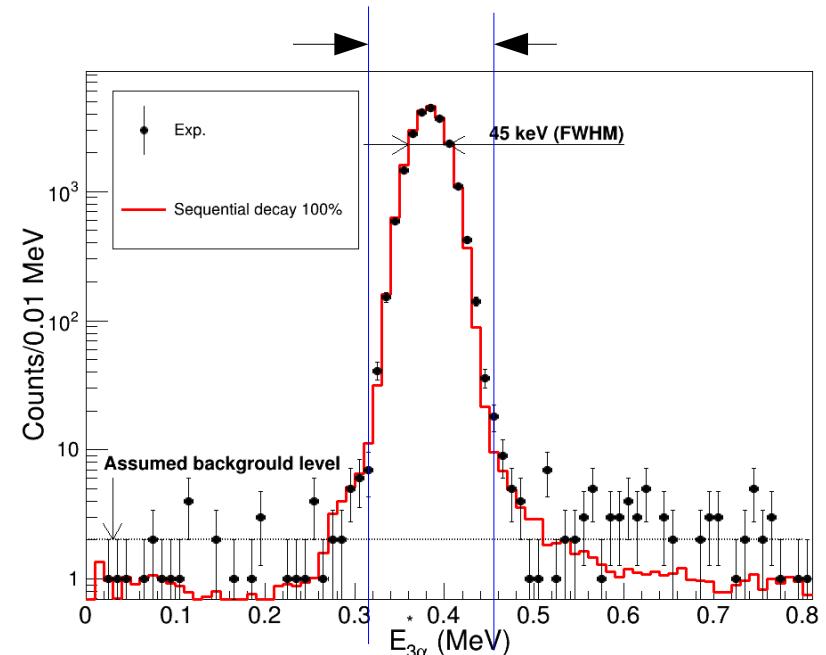
Invariant Mass spectrum

$$E_{\text{inv}} = E_{\text{recoil}^{12}\text{C}} + E_{\alpha 1} + E_{\alpha 2} + E_{\alpha 3}$$



~103 MeV

Total 3α energy spectrum in the $^{12}\text{C}^*$ rest frame

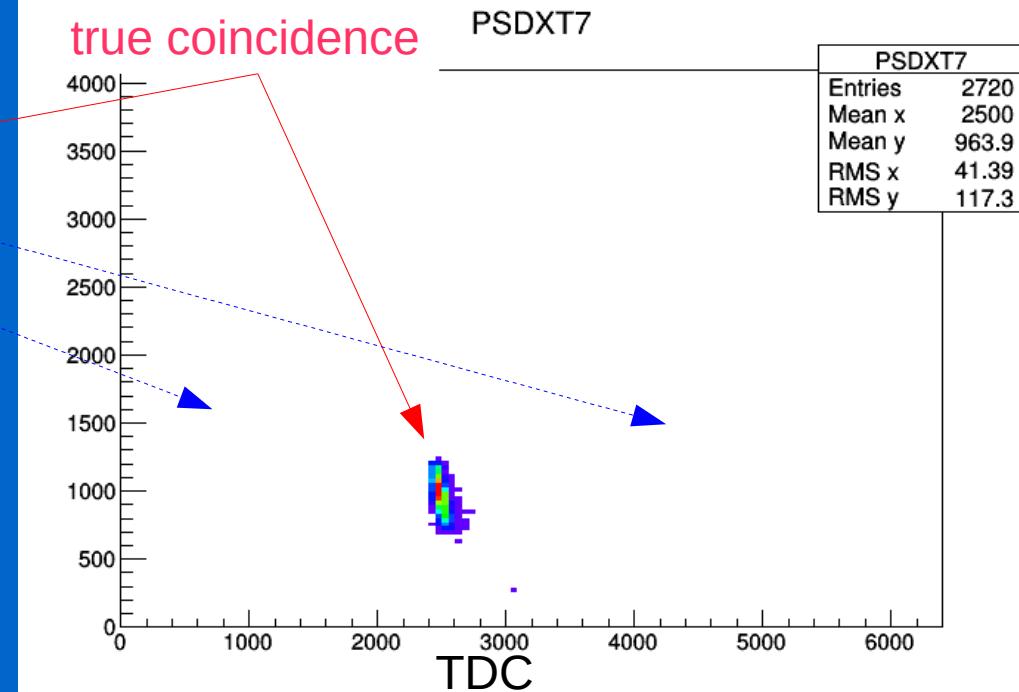
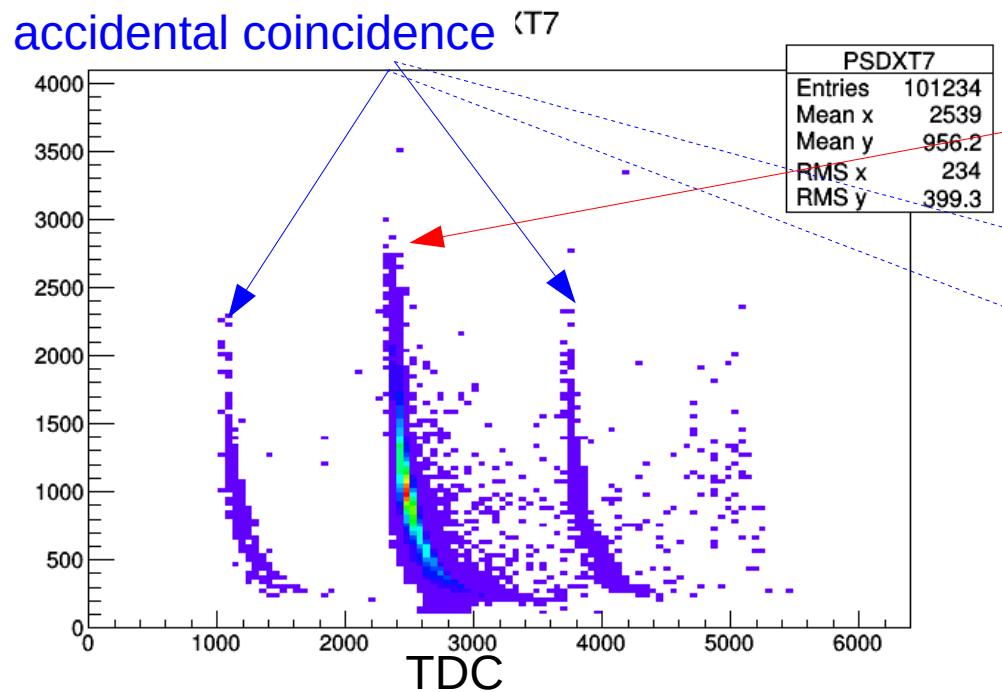


Accidental coincidence

- There was no accidental 3α coincidence.

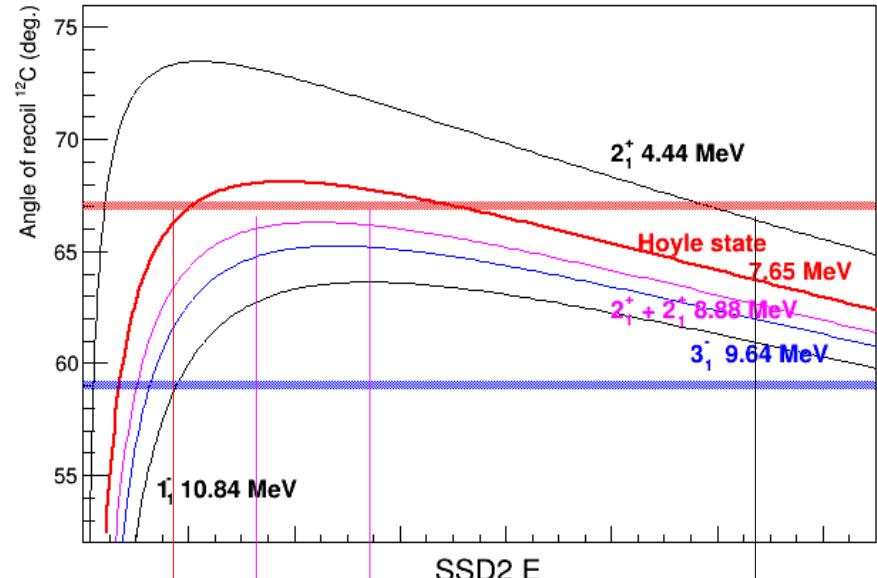
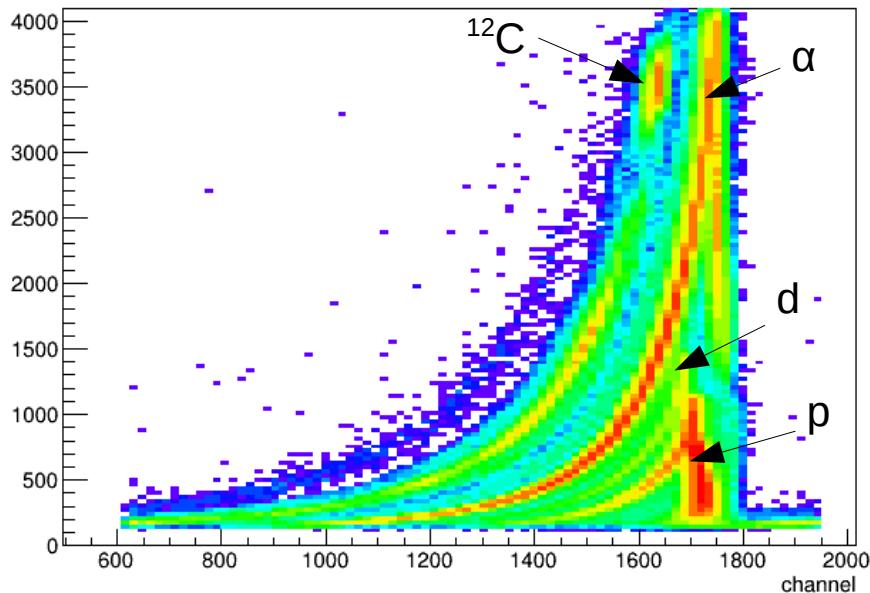
Recoil $^{12}\text{C} + 1-\alpha$

Recoil $^{12}\text{C} + 3-\alpha$

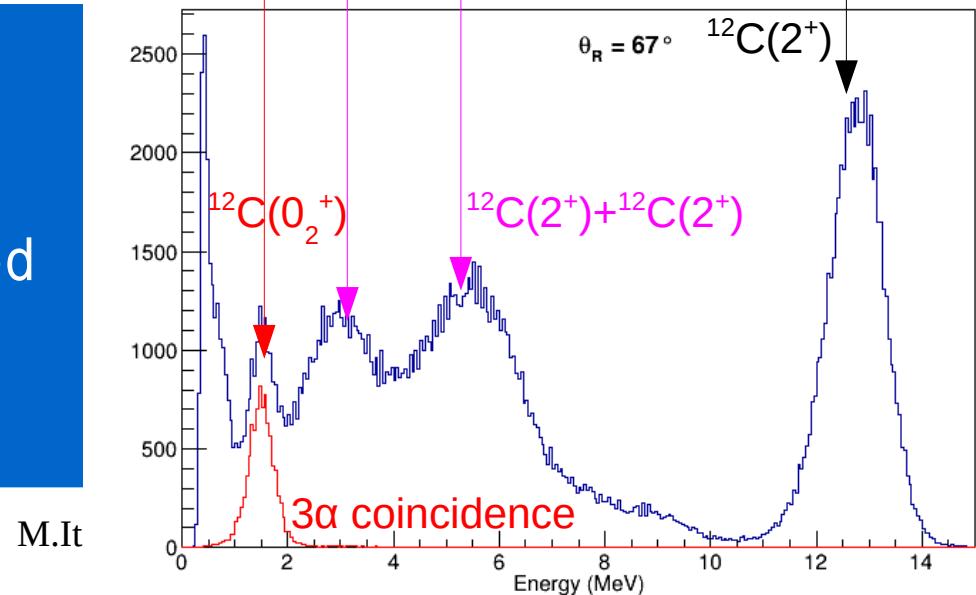


Kinematics and Recoil ^{12}C spectrum

TOF spectrum of SD



- Particle Identification:
TOF method
- Excitation energy is determined
from the energy of the recoil ^{12}C .



Decay and structure of Hoyle state

PHYSICAL REVIEW C **90**, 061604(R) (2014)

Decay and structure of the Hoyle state

S. Ishikawa*

Science Research Center, Hosei University, 2-17-1 Fujimi, Chiyoda, Tokyo 102-8160, Japan

(Received 10 October 2014; revised manuscript received 25 November 2014; published 22 December 2014)

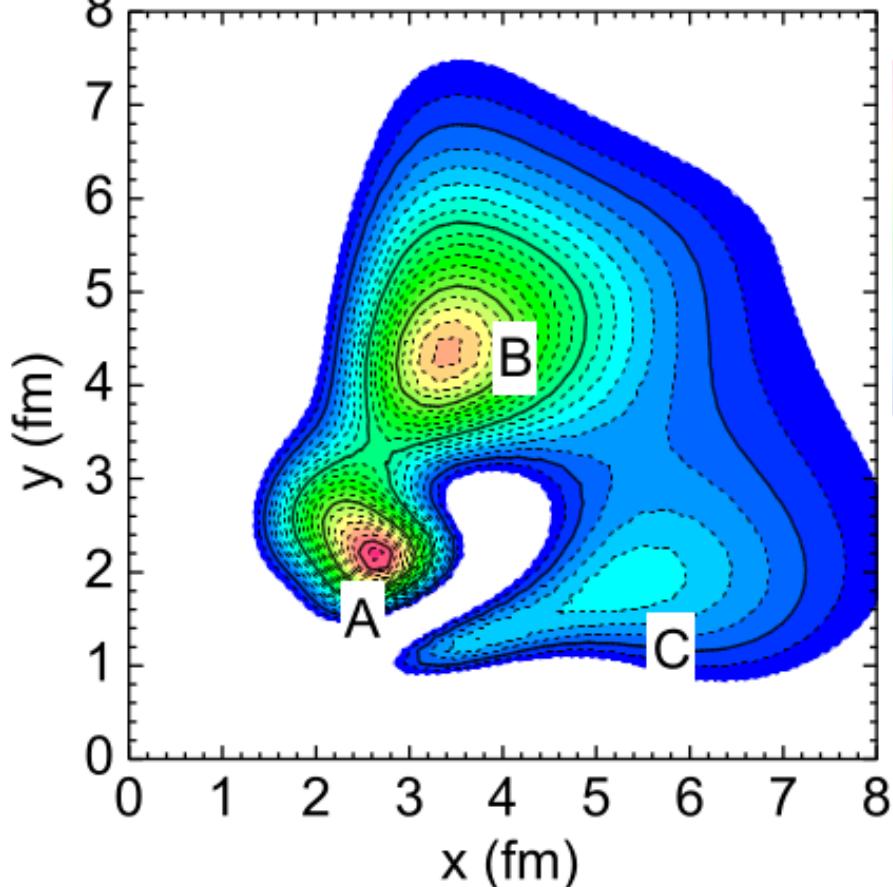
The first 0^+ resonant state of the ^{12}C nucleus, $^{12}\text{C}(0_2^+)$, the so-called Hoyle state, is investigated in a three- α -particle (3- α) model. A wave function for the photodisintegration reaction of a ^{12}C bound state to 3- α final states is defined and calculated by the Faddeev three-body formalism, in which three-body bound and continuum states are treated consistently. From the wave function at the Hoyle state energy, I calculated distributions of outgoing α particles and density distributions at interior region of the Hoyle state. Results show that a process through a two- α resonant state is dominant in the decay and contributions of the rest process are very small, less than 1%. There appear to be some peaks in the interior density distribution corresponding to configurations of equilateral and isosceles triangles. It turns out that these results are obtained independently of the choice of α -particle interaction models, when they are made to reproduce the Hoyle state energy.

DOI: [10.1103/PhysRevC.90.061604](https://doi.org/10.1103/PhysRevC.90.061604)

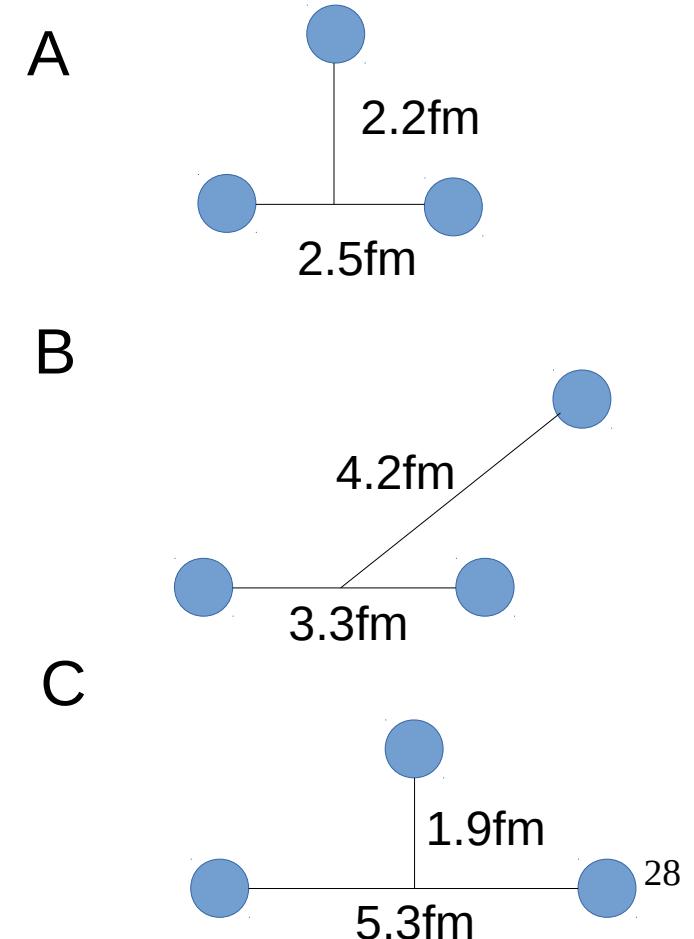
PACS number(s): 21.45.-v, 25.70.Ef, 27.20.+n

Structure of the Hoyle state 1

- Density distribution



$$\rho(x, y) = x^2 y^2 \int d\hat{x} d\hat{y} |\Psi(x, y)|^2$$



S.Ishikawa, Phys.Rev.C90, 061604(R)(2014)