

The $^{40}\text{Ca} + ^{58,64}\text{Ni}$ fusion reactions : interplay between inelastic and transfer channels

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Outline

- Sub-barrier fusion in the Ca + Ni systems. Why ?
- The fusion experiments and results
- Coupled-channels and Hartree-Fock calculations
- The transfer experiment and results
- Conclusions



Glass House Mountains, Australia

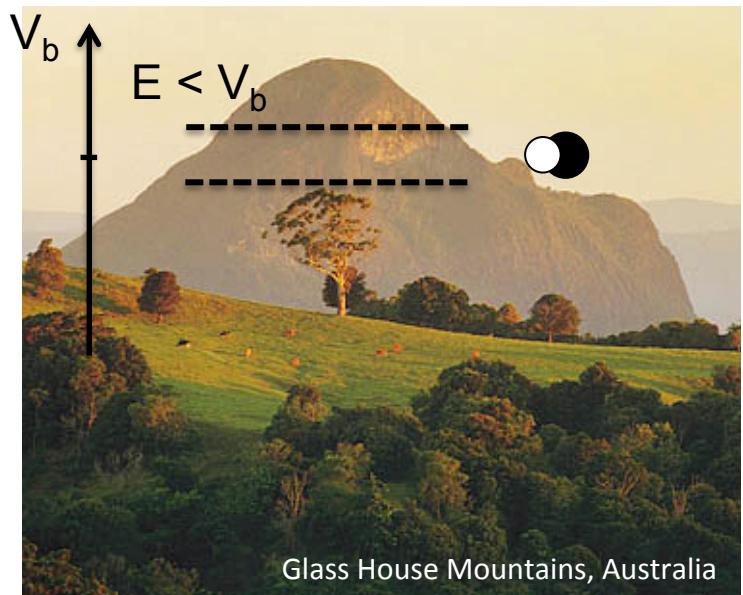
Sub-barrier fusion : Ca + Ni

- Fusion: dominant reaction mechanism in heavy-ion collisions at low bombarding energies
- Sub-barrier fusion



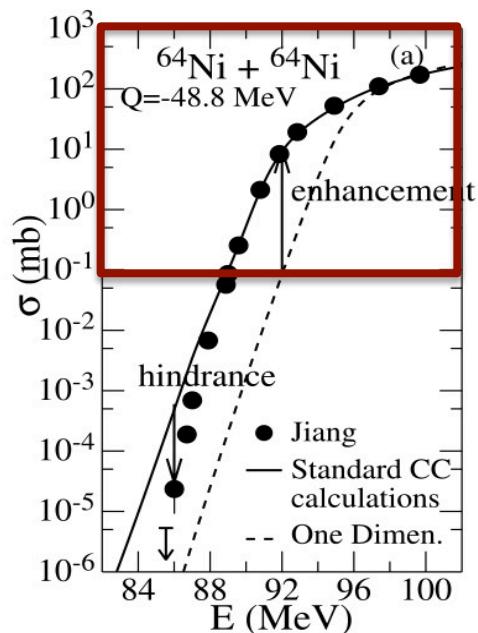
Sub-barrier fusion : Ca + Ni

- Fusion: dominant reaction mechanism in heavy-ion collisions at low bombarding energies
- Sub-barrier fusion
- Nuclear structure vs reaction dynamics in $^{40}\text{Ca} + ^{58,64}\text{Ni}$

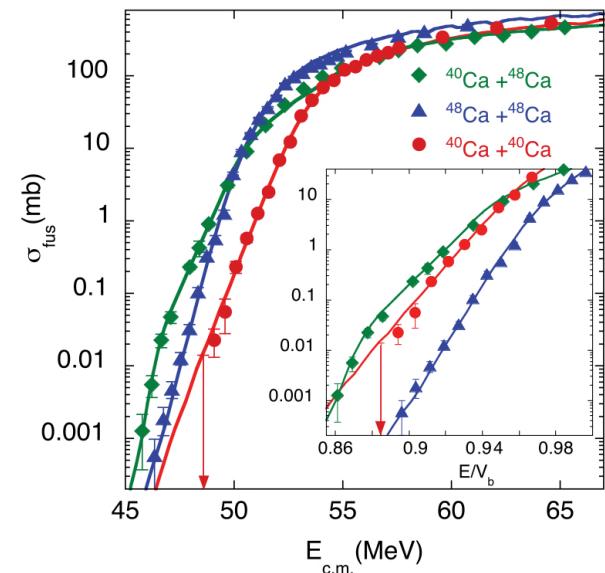
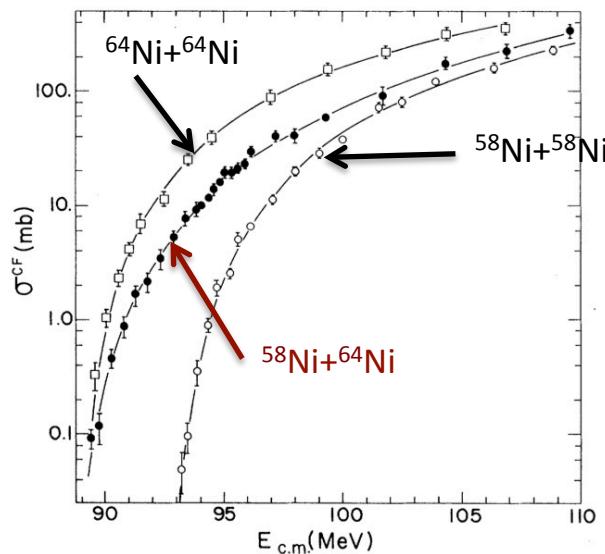


Sub-barrier fusion : Ca + Ni

- Ni + Ni and Ca + Ca



C.L. Jiang et al., Nucl.Phys. A834 (2010) M. Beckerman et al., Phys.Rev.Lett. 45 (1980)



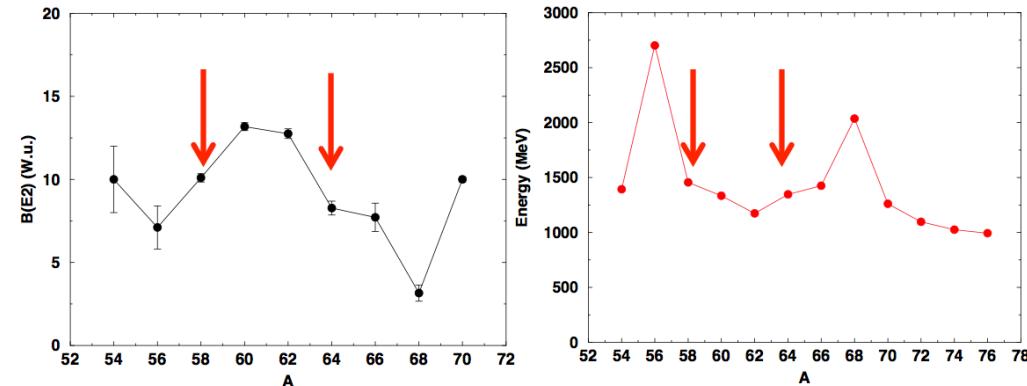
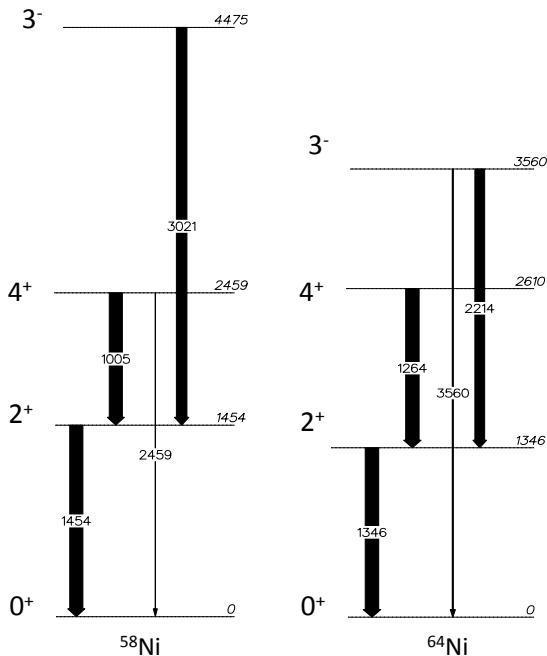
G. Montagnoli et al., Phys.Rev.C85(2012)

- $^{58,60,64}\text{Ni}$ vibrational, well known 1 and 2 phonon states
- $^{64}\text{Ni} + ^{64}\text{Ni}$ 'a textbook example'

- ^{48}Ca 'stiff' / ^{40}Ca 'soft' (strong 3^-)
- $^{40}\text{Ca} + ^{48}\text{Ca}$, hindrance shows up lower
- Q value (transfer) > 0 for $^{40}\text{Ca} + ^{48}\text{Ca}$

Sub-barrier fusion : Ca + Ni

- Effects of couplings on fusion well known for Ca and Ni
- Similar structure features for ^{58}Ni and ^{64}Ni / 6 neutrons

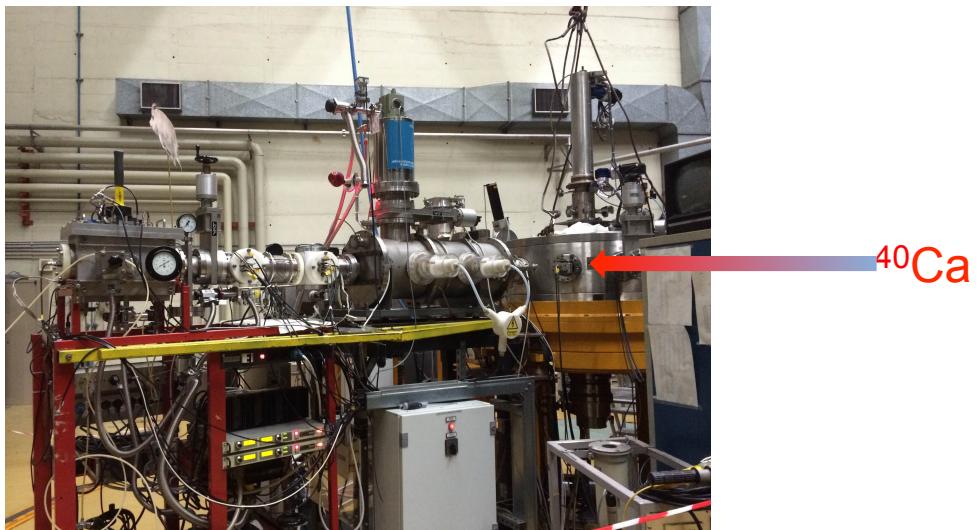


B. Pritychenko et al., Update of $B(E2)$ and $E(2^+)$ evaluation near $N \approx Z \approx 28$, At. Dat. Nucl. Dat. Tables (2012)

- Fusion of Ca+Ni below and around CB almost unknown (except Rochester data for $^{40}\text{Ca} + ^{58}\text{Ni}$, Sikora et al. (1979))
- Positive Q value for transfers for $^{40}\text{Ca} + ^{64}\text{Ni}$ (+2n to +6n and -2p), negative for all transfers in $^{40}\text{Ca} + ^{58}\text{Ni}$

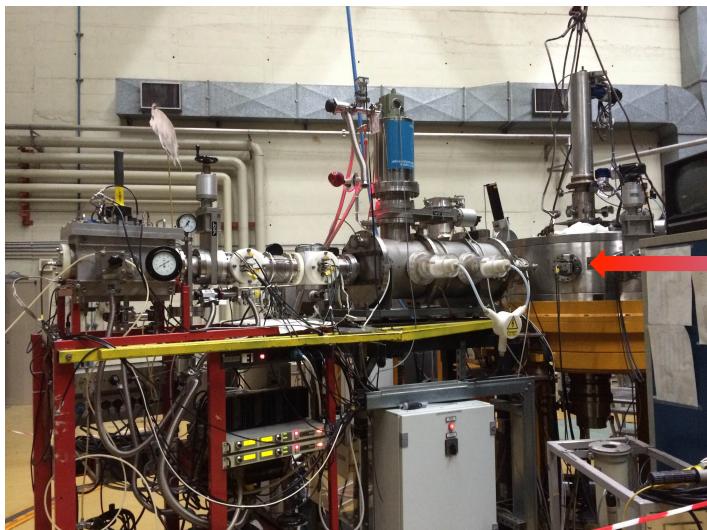
The fusion experiment

- Fusion cross section measurements from above to below the Coulomb barrier in at $^{40}\text{Ca} + ^{58,64}\text{Ni}$ INFN-LNL in Italy
- Electrostatic deflector



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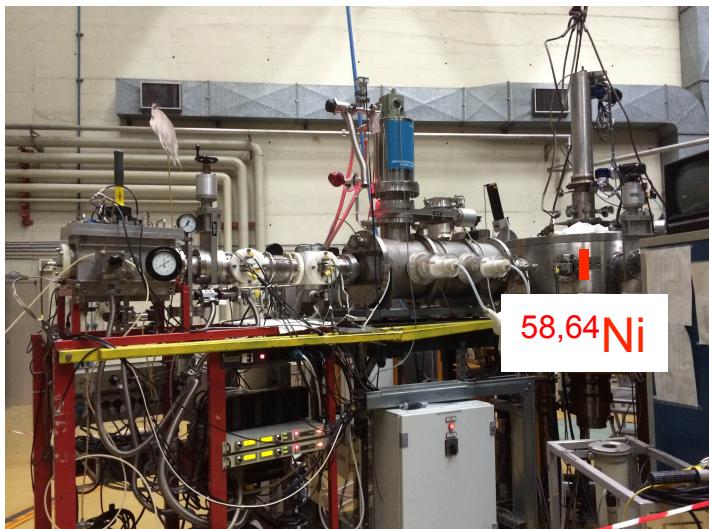
high-quality and intense ^{40}Ca beam
of $\approx 9 \text{ p nA}$ intensity ($\approx 6 \times 10^{10} \text{ p s}^{-1}$)

^{40}Ca

XTU Tandem accelerator

The fusion experiment

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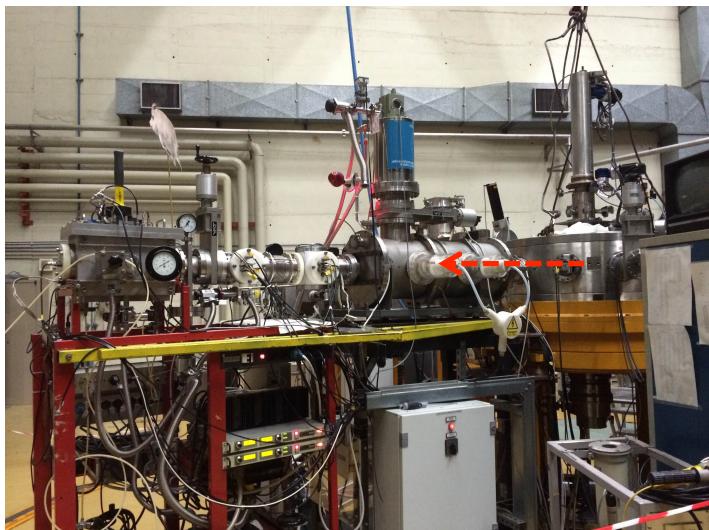
reaction chamber

$^{58,64}\text{Ni}$ targets of $50 \mu\text{g}/\text{cm}^2$ thickness deposited on a $20 \mu\text{g}/\text{cm}^2$ ^{12}C backing

4 silicon detectors used as monitors

The fusion experiment

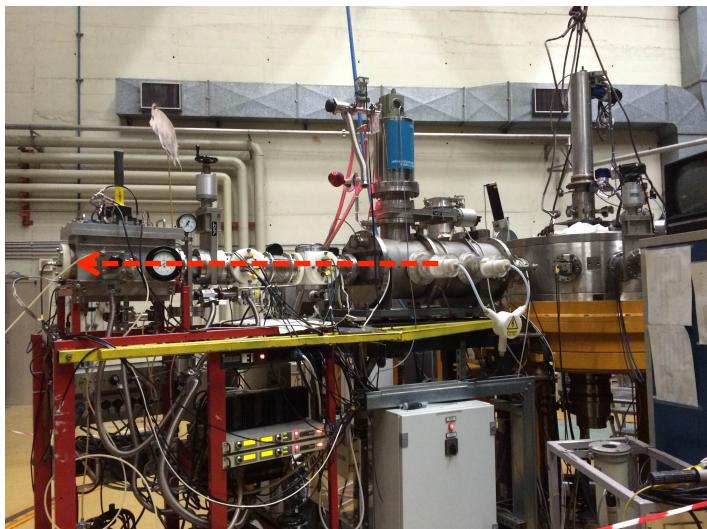
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electrostatic deflector

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detection system for the evaporation residues

2 MCP detectors $t_{1,2}$

ionisation chamber: ΔE

Si detector: E_R, t_3

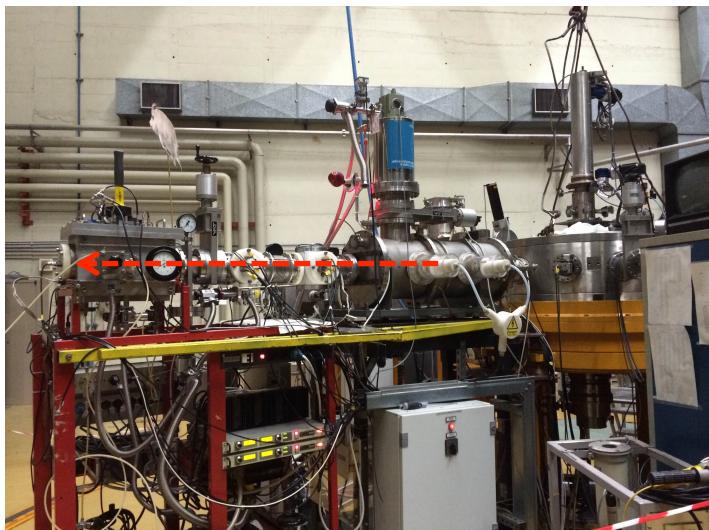
$$\text{TOF}_1 = t_3 - t_1$$

$$\text{TOF}_2 = t_2 - t_1$$

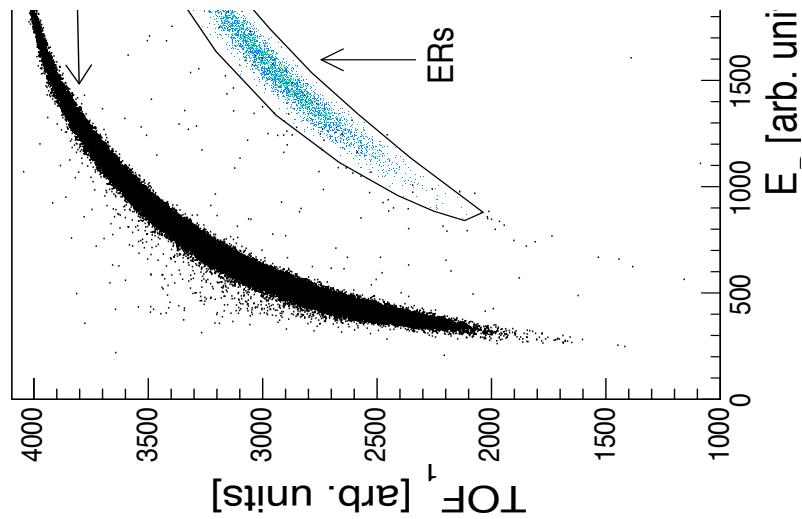
$$\text{TOF}_3 = t_3 - t_2$$

The fusion experiment

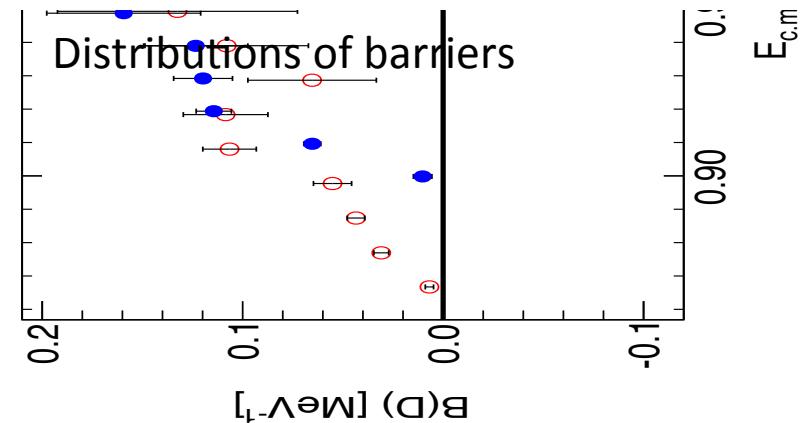
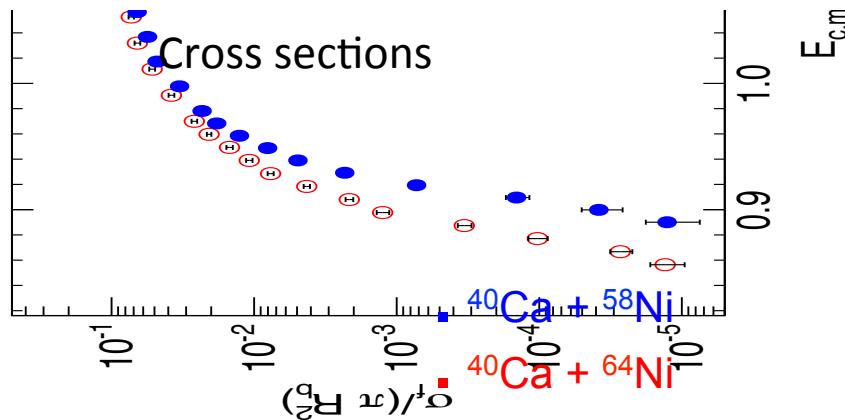
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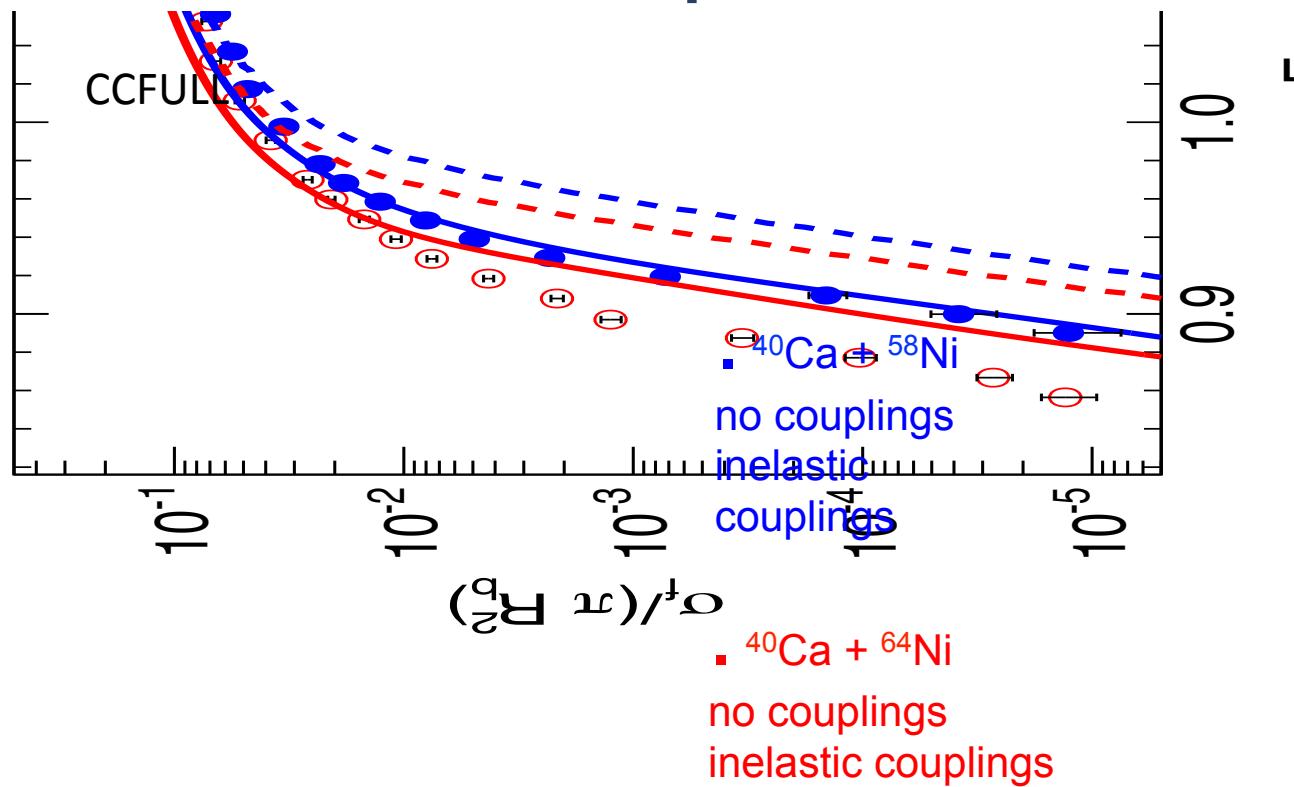


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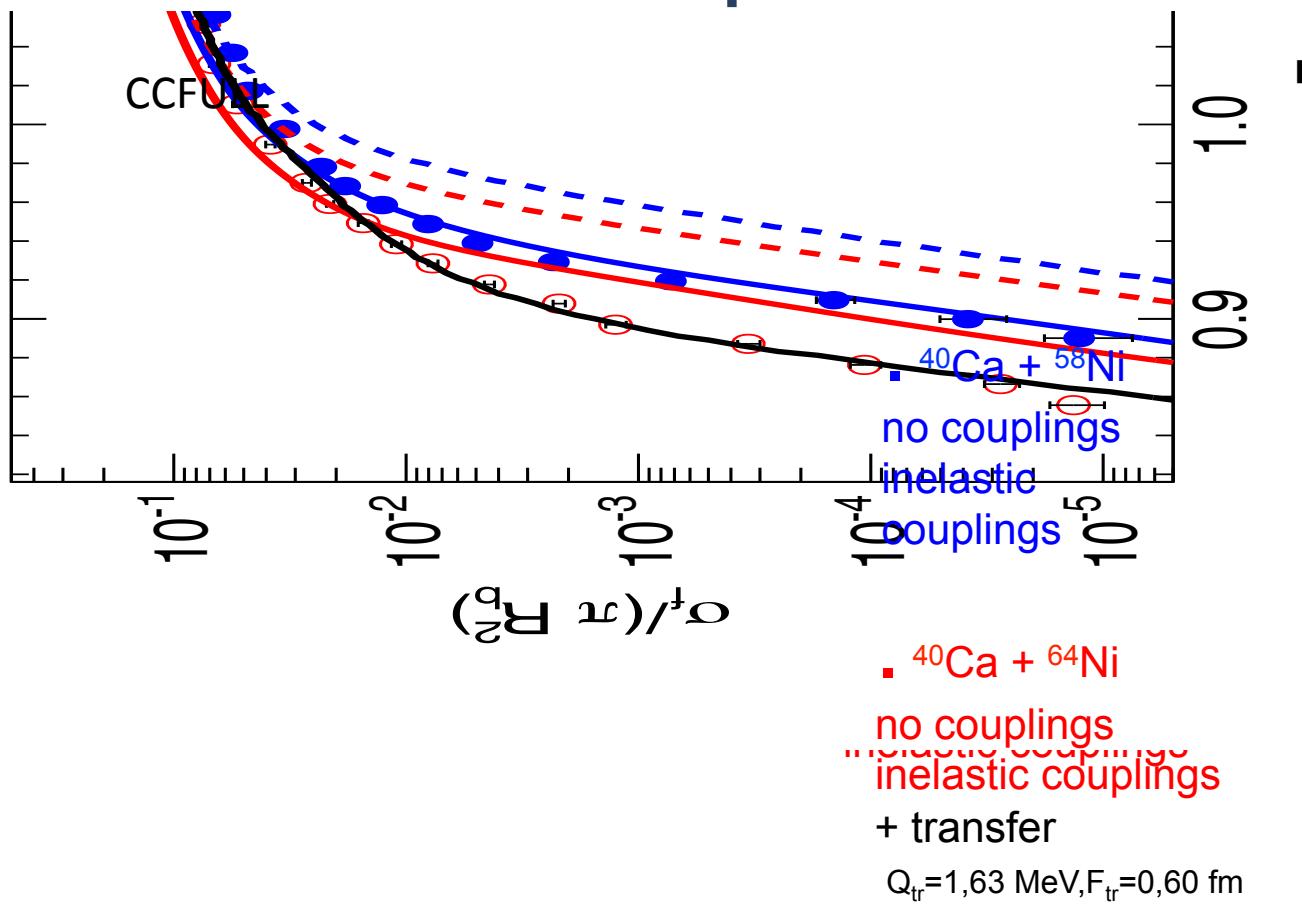


PhD : D. Bourgin, University of Strasbourg

The fusion experiment

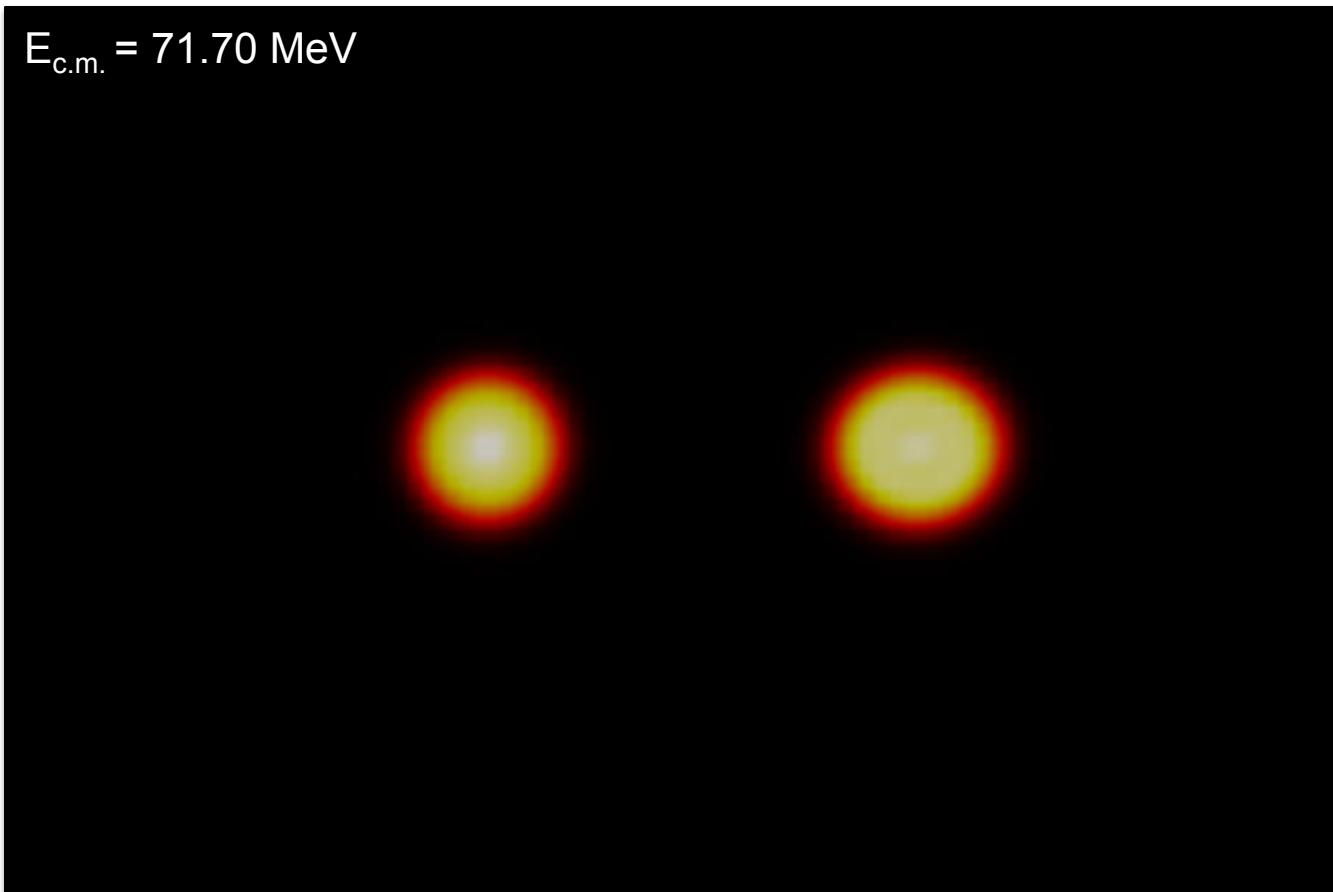


The fusion experiment



TDHF calculations

TDHF + BCS calculations / 1 parameter (Skyrme) / dynamical effects at the mean-field level



In collaboration with C. Simenel, Australian National University, Australia

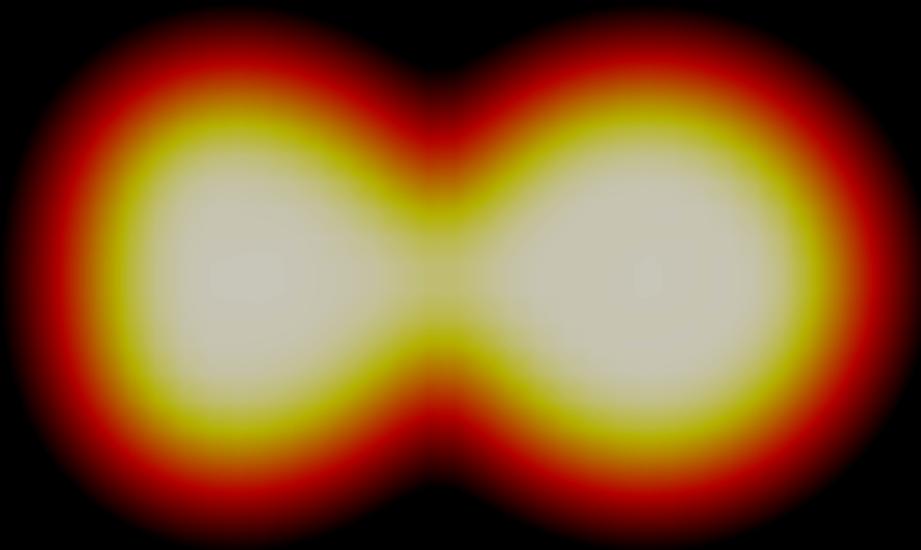
TDHF calculations

TDHF + BCS

$E_{c.m.} = 71.70 \text{ MeV}$

$t = 1,425 \text{ zs}$

$r = 11,24 \text{ fm}$



⁴⁰Ca

⁵⁸Ni

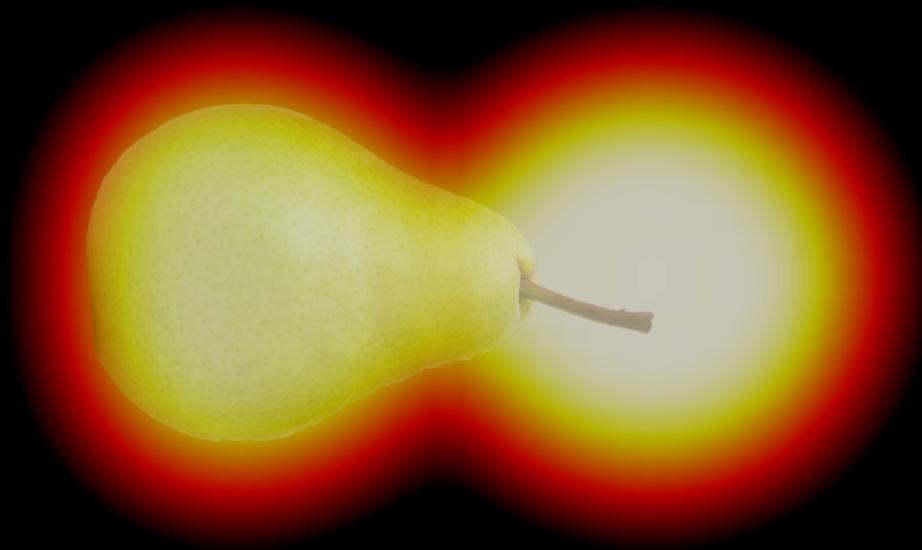
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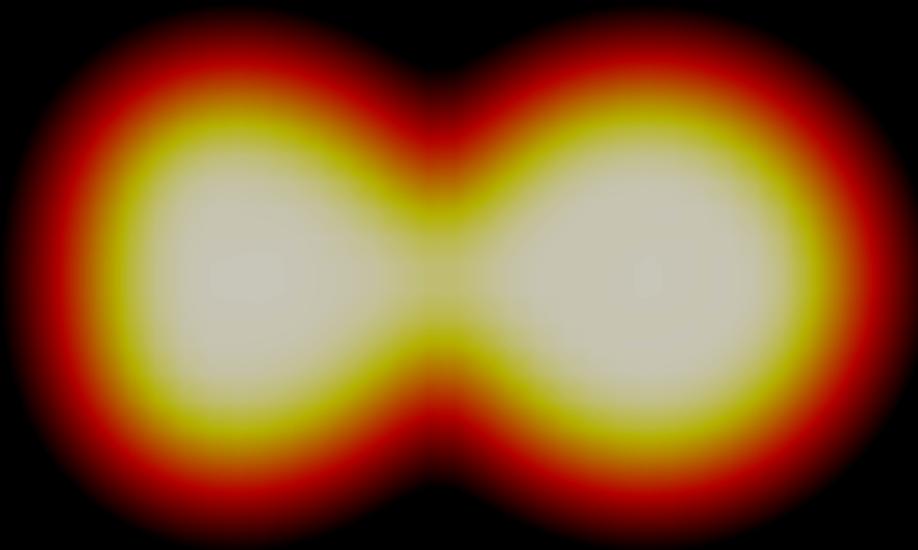
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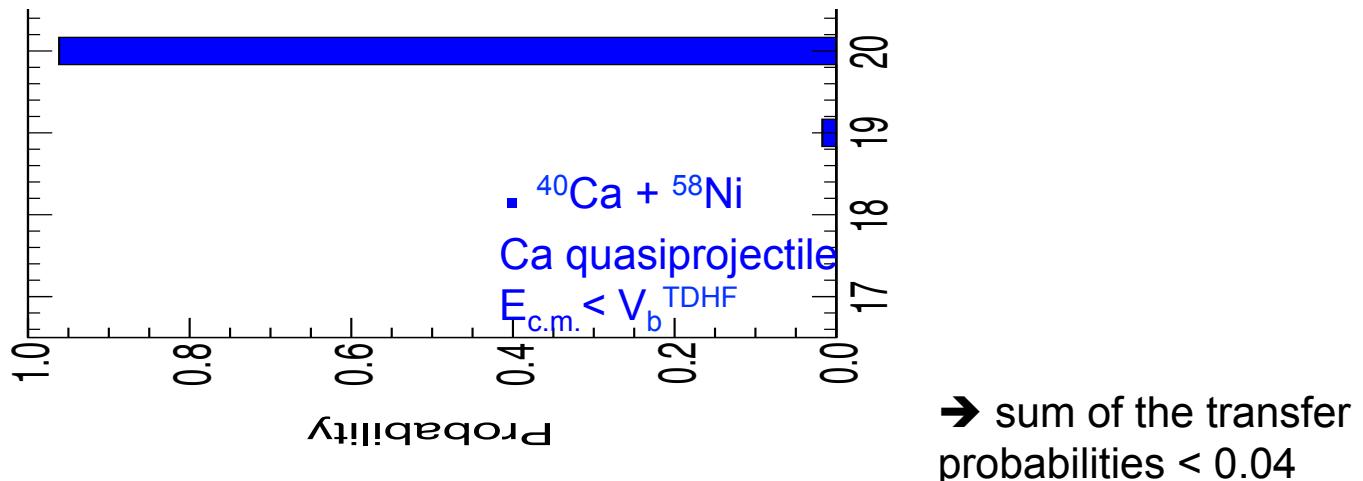
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TDHF calculations

Particle number projection technique

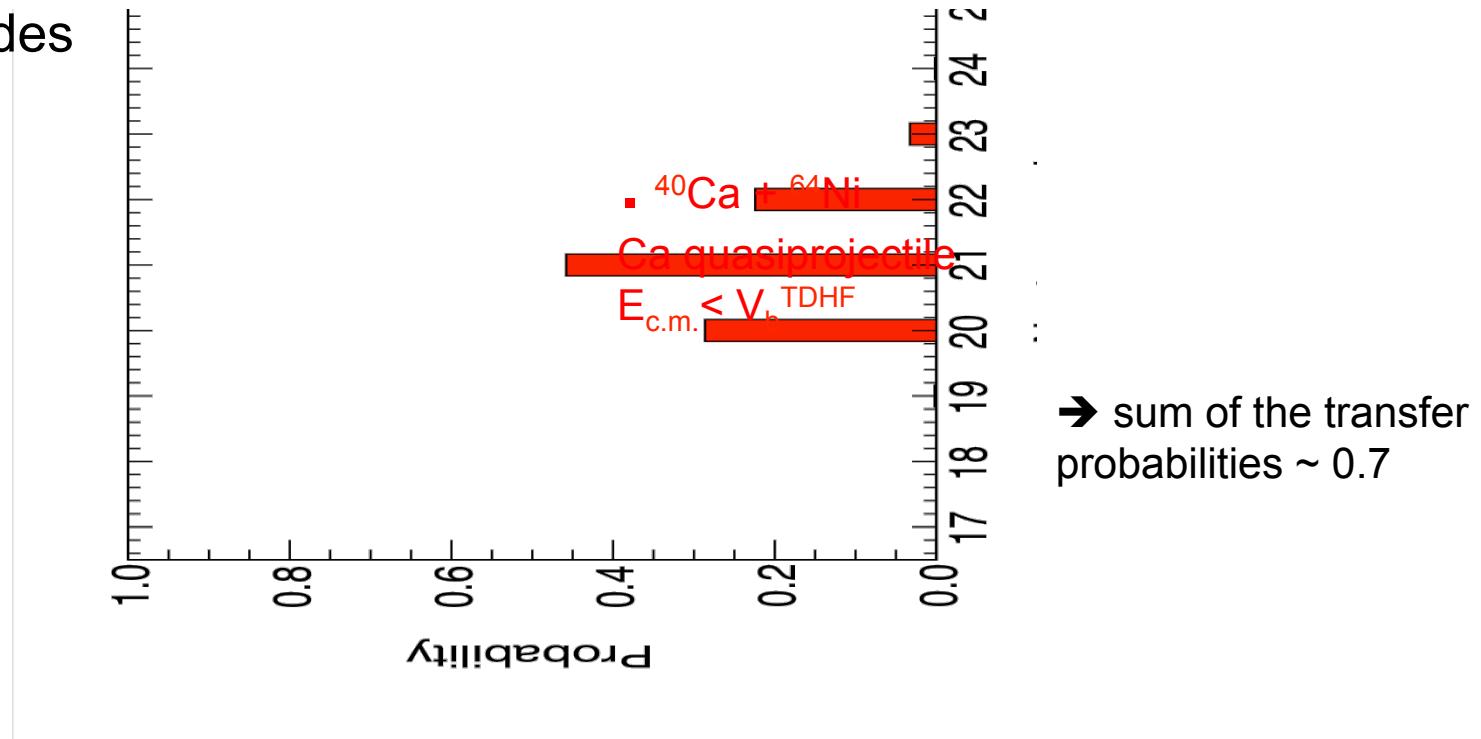
Time-Dependent Hartree-Fock + BCS calculations with the EV8 and TDHF3D codes



TDHF calculations

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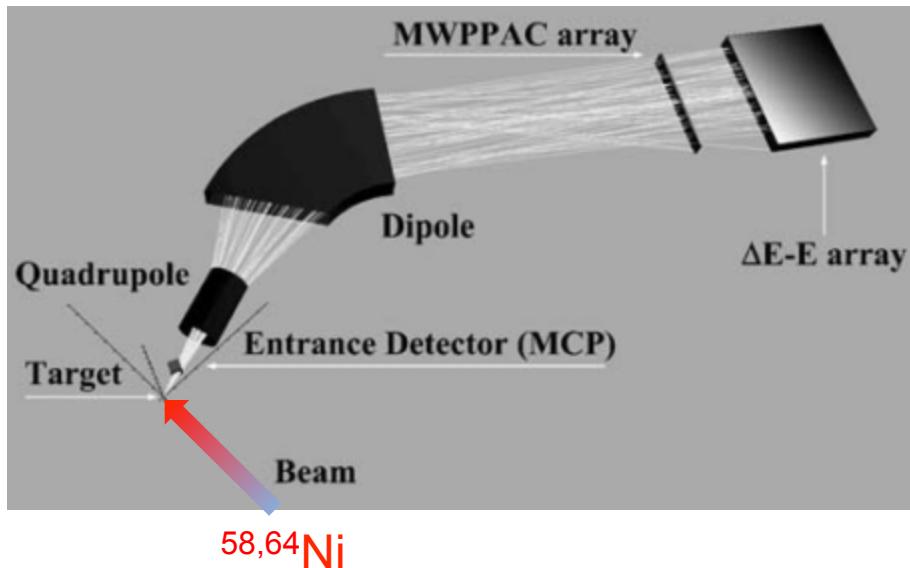
Time-Dependent Hartree-Fock + BCS calculations with the EV8 and TDHF3D codes



The transfer experiment

Nucleon transfer channels in $^{40}\text{Ca} + ^{58,64}\text{Ni}$

Transfer probability measurements from above to below the Coulomb barrier at INFN-LNL (Italy)



XTU Tandem accelerator

$^{58,64}\text{Ni}$ beams / 3 p nA intensity ($\approx 2 \times 10^{10} \text{ p s}^{-1}$)

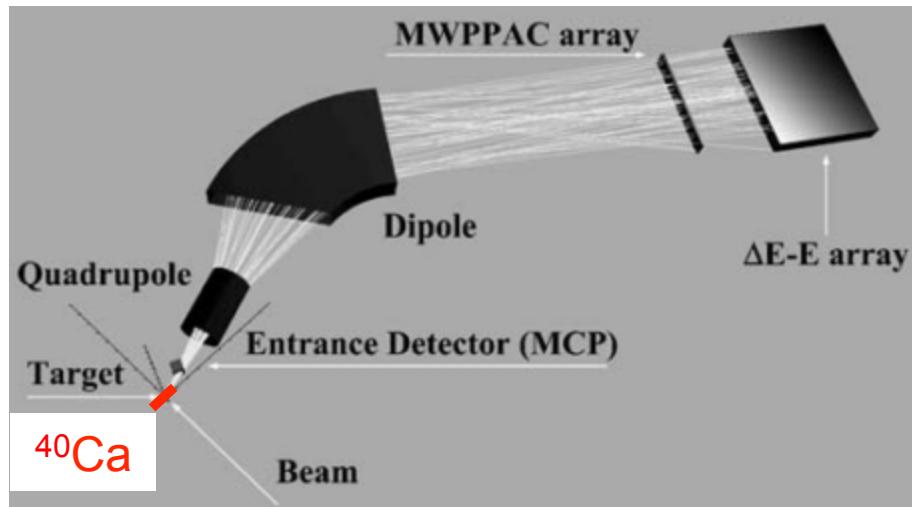


PRISMA magnetic spectrometer

The transfer experiment

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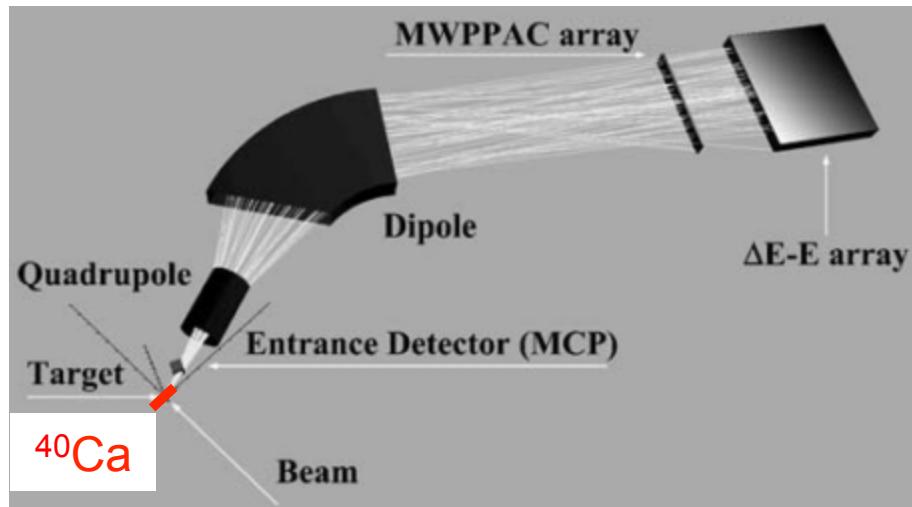


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reaction chamber

CaF_2 target of $100 \mu\text{g}/\text{cm}^2$
deposited on a $15 \mu\text{g}/\text{cm}^2$ ^{12}C backing

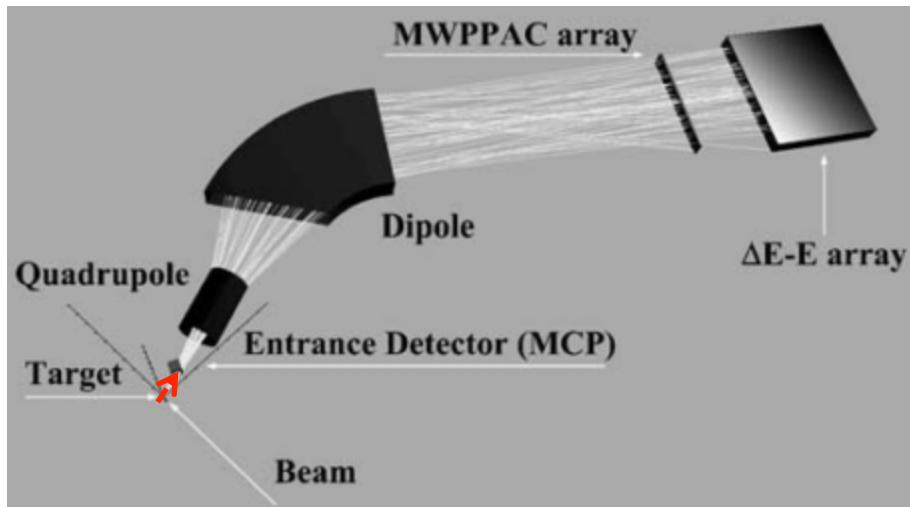


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MCP: t_i

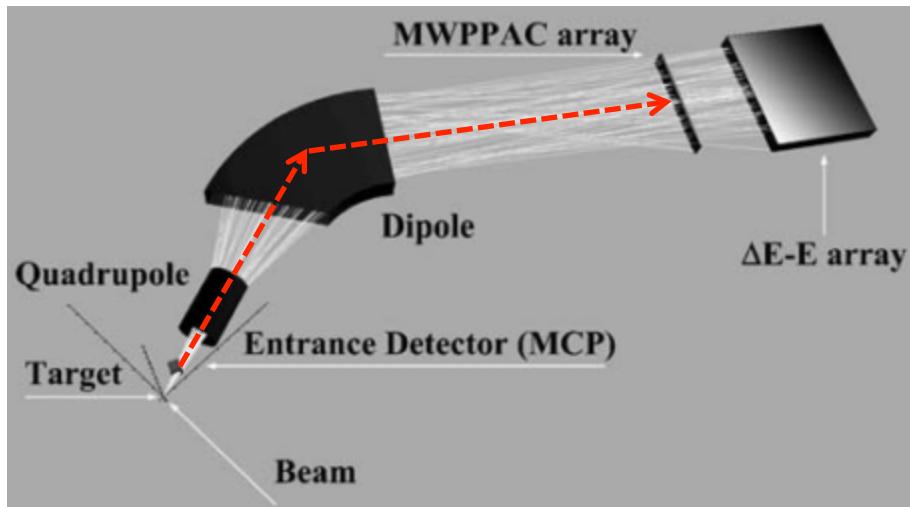


PRISMA magnetic spectrometer

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MWPPAC : t_f

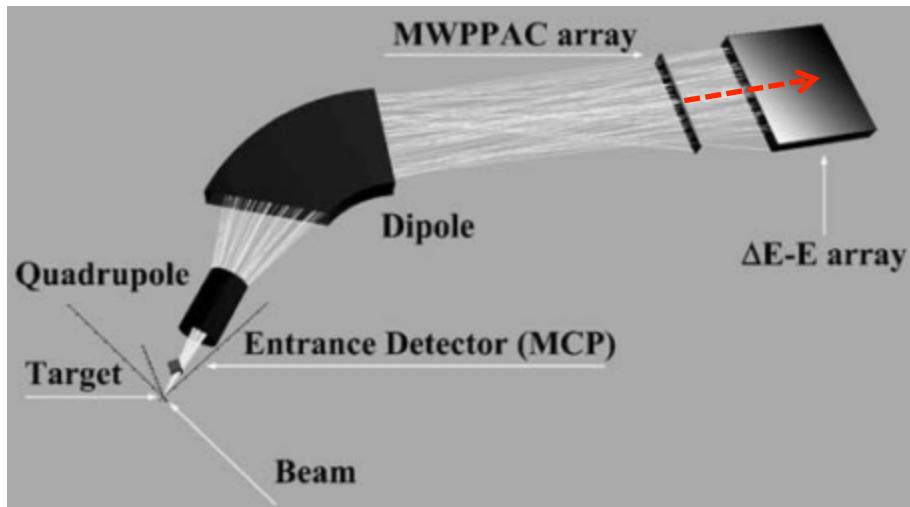
TOF = $t_f - t_i$

PRISMA magnetic spectrometer

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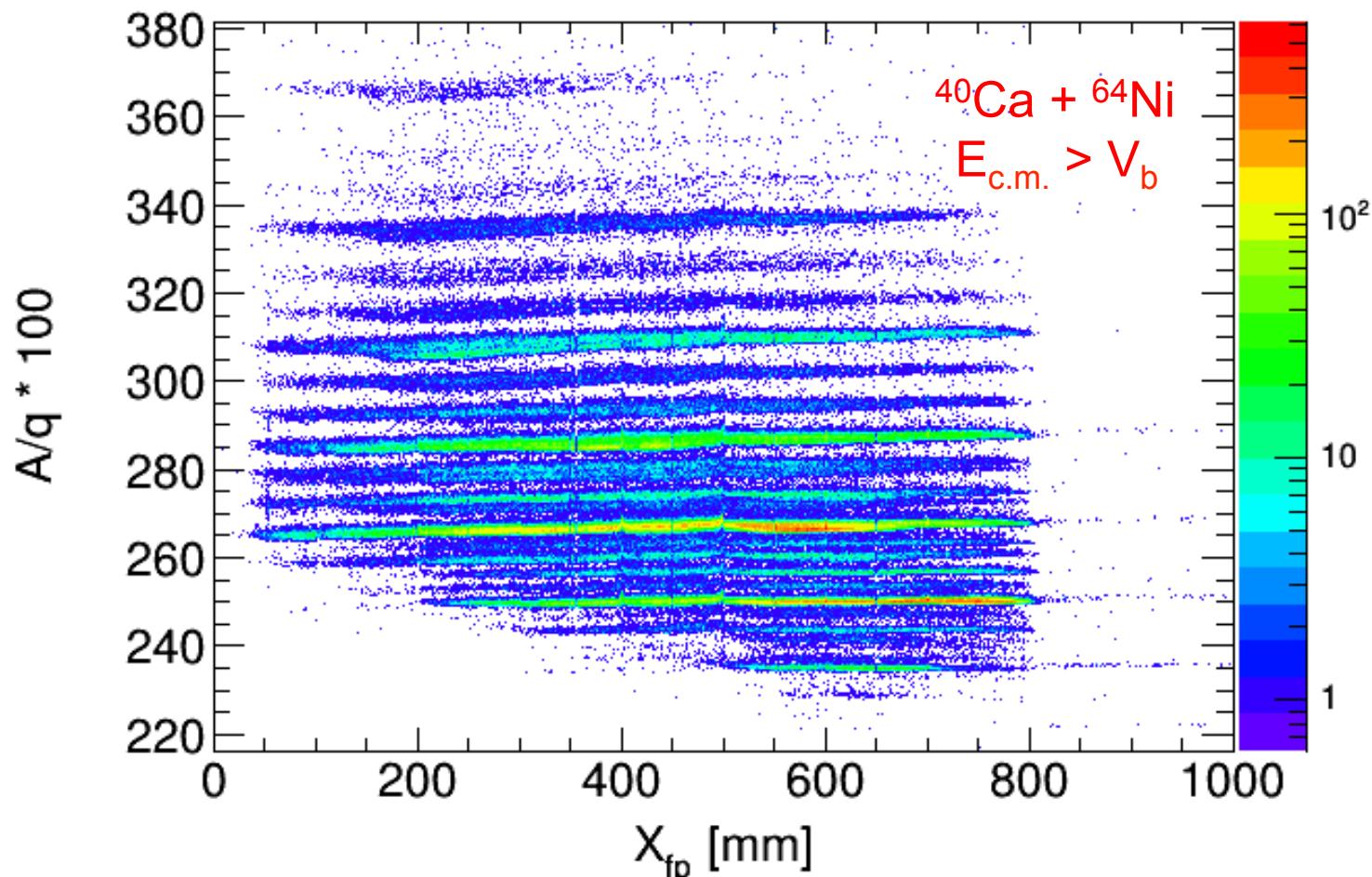
ionisation chamber: ΔE , E



PRISMA magnetic spectrometer

The transfer experiment

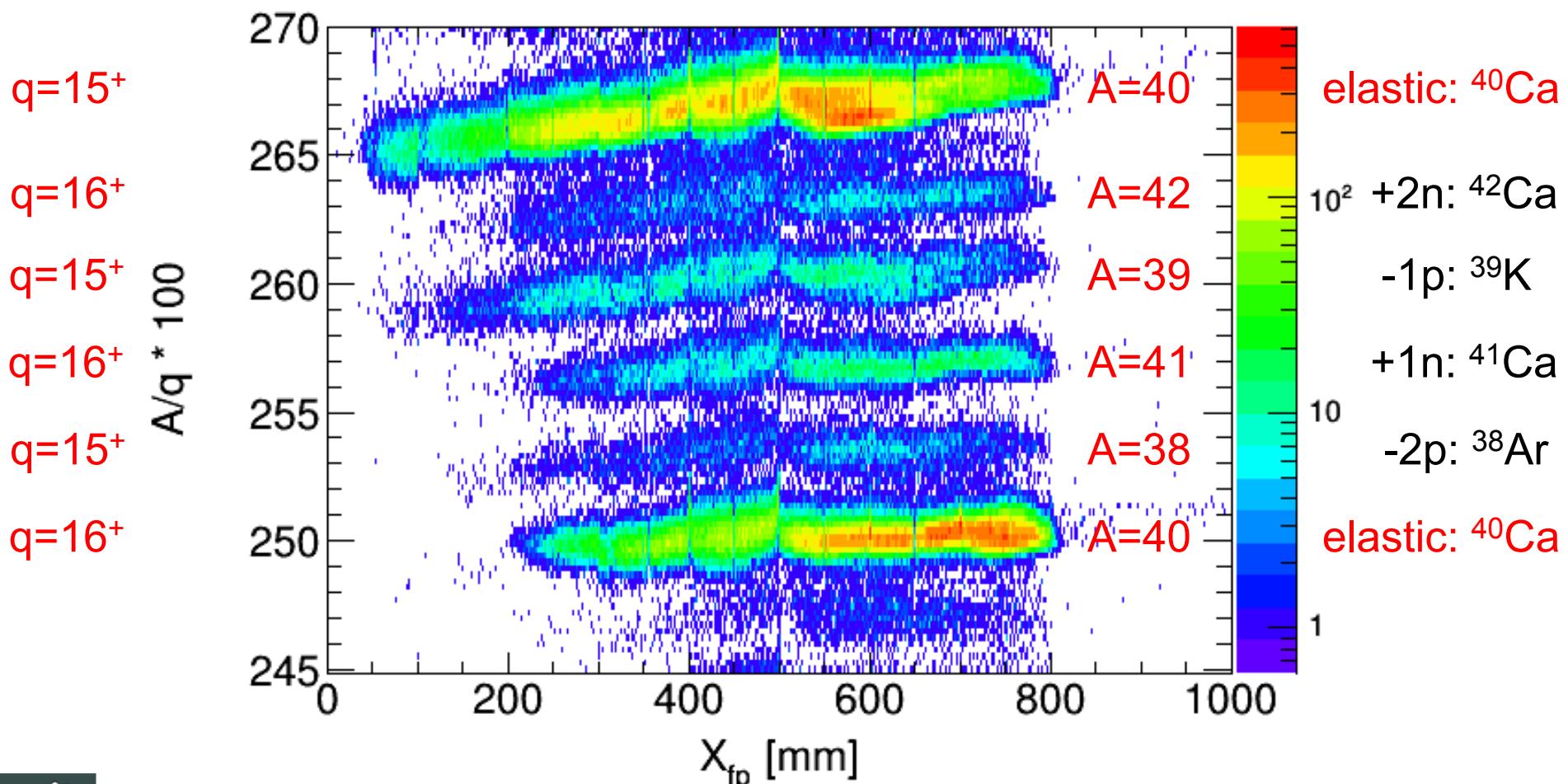
Spectrum of A/q vs X_{fp}



The transfer experiment

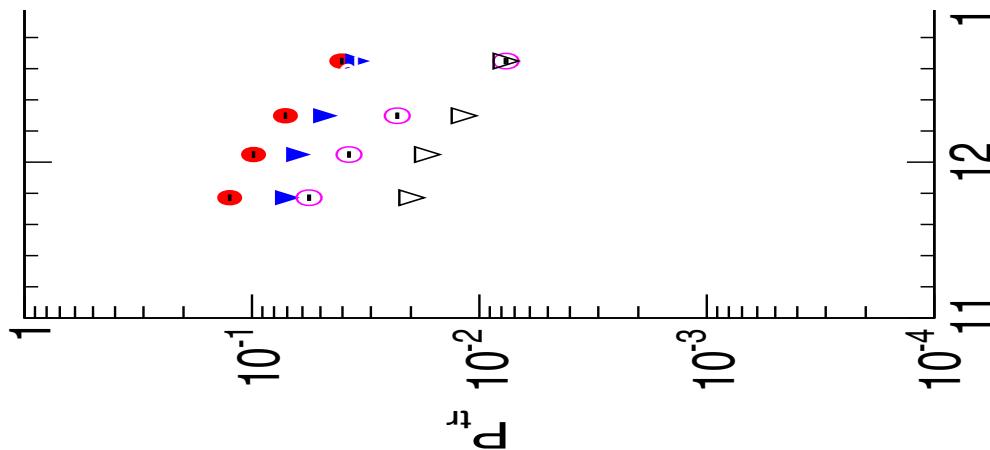
Spectrum of A/q vs X_{fp}

TDHF + BCS



The transfer experiment

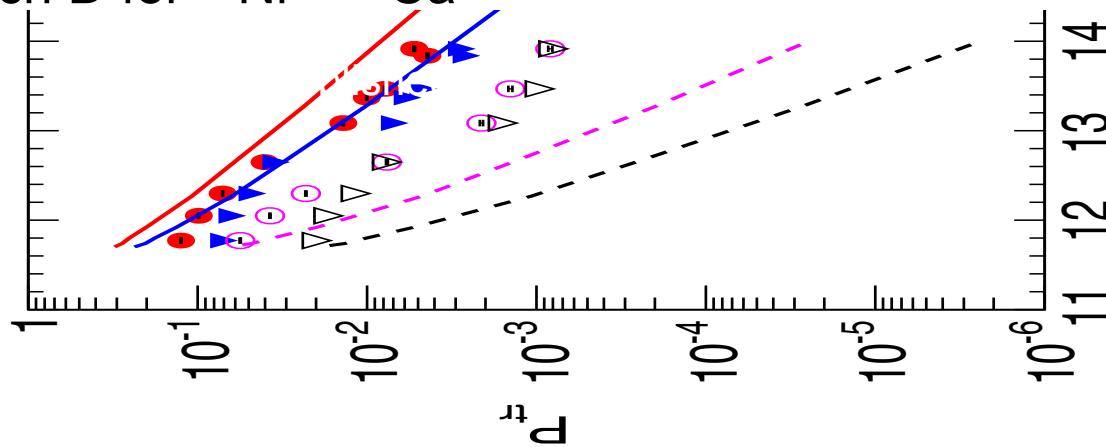
Nucleon transfer probabilities $P_{tr} = N_{tr} / N_{el+inel}$ vs distance of closest approach D for $^{64}\text{Ni} + ^{40}\text{Ca}$



$$D = \frac{Z_p Z_t e^2}{2E_{c.m.}} \left(1 + \frac{1}{\sin(\theta_{c.m.}/2)} \right)$$

The transfer experiment

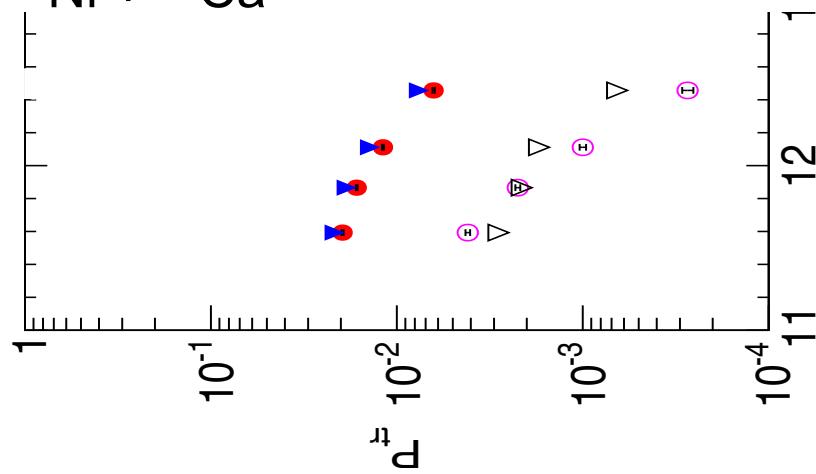
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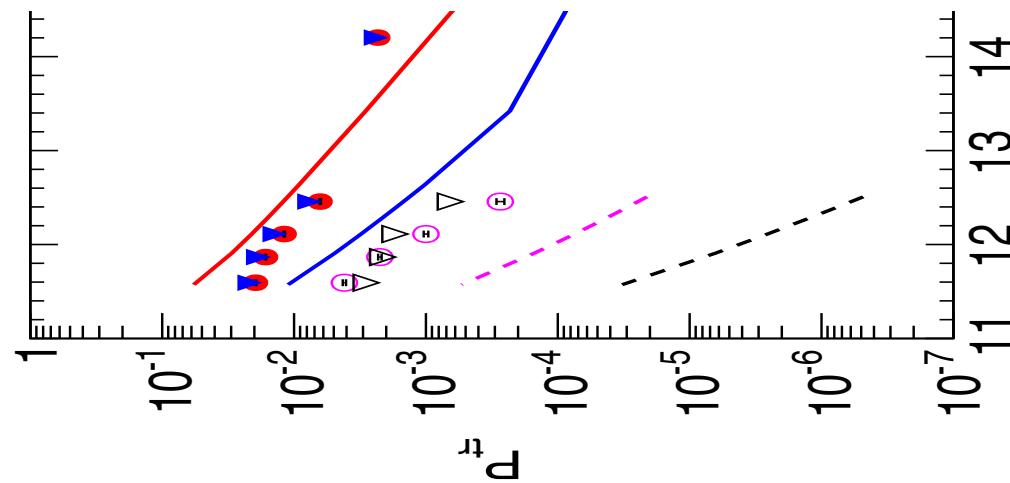
The transfer experiment

Nucleon transfer probabilities $P_{tr} = N_{tr} / N_{el+inel}$ vs distance of closest approach D for $^{58}\text{Ni} + ^{40}\text{Ca}$



The transfer experiment

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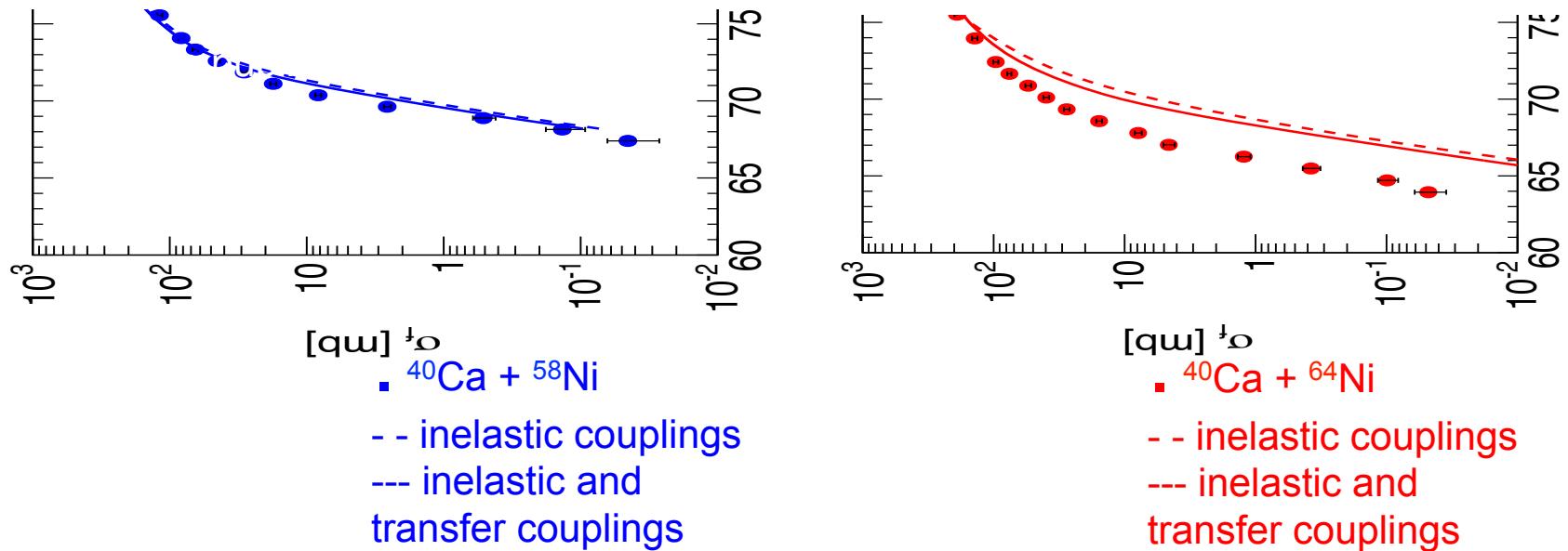
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Back to coupled channels

- the parameters for the transfer coupling form factors are extracted from the measured transfer probabilities
- then these parameters are used in the coupled-channels calculations of fusion cross sections

In collaboration with G. Scamps, Tohoku University, Japan

Back to coupled channels



- the direct two-neutron transfer scheme does not seem to explain the importance of nucleon transfer channels for $^{40}\text{Ca} + ^{64}\text{Ni}$ with $Q_{\text{tr}} > 0$
- underestimation of the sub-barrier fusion cross sections also observed for $^{40}\text{Ca} + ^{96}\text{Zr}$ with $Q_{\text{tr}} > 0$
[G. Scamps and K. Hagino, Phys. Rev. C **92**, 054614 (2015)]

Conclusions

- Study of $^{40}\text{Ca}+^{58}\text{Ni}$ and $^{40}\text{Ca}+^{64}\text{Ni}$ fusion reactions at energies above and below CB Nickel target nuclei : same structure features but different neutron numbers
- Influence of couplings to 2^+ , 3^- (^{40}Ca)
- Large influence of transfer channels in the $^{40}\text{Ca}+^{64}\text{Ni}$ system
- Transfer probabilities measured with the PRISMA spectrometer

... underestimated by CC calculations using form factors adjusted to transfer probabilities

- Challenges for the future
- Calculation including different parameters for the transfer channels
- complementary transfer probability measurements for $^{40}\text{Ca} + ^{58}\text{Ni}$ with $\text{Qtr} < 0$ around the Coulomb barrier
- New experimental setup for transfer measurements ?

... pave the way to exotic n-rich nuclei.

Collaboration

D. Bourgin, Florent Haas, G. Fruet, D. Montanari
IPHC and University of Strasbourg, France



A. Stefanini, G. Montagnoli, E. Fioretto, F. Galtarossa³, A. Goasduff,
L. Corradi, F. Galtarossa, A. Goasduff, T. Mijatovic⁴, F. Scarlassara,
G. Zhang

INFN-LNL, Legnaro, Italy



G. Montagnoli, F. Scarlassara, E. Strano,
University of Padova, Italy

D. Ackermann
GSI, Darmstadt Germany and GANIL, Caen, France



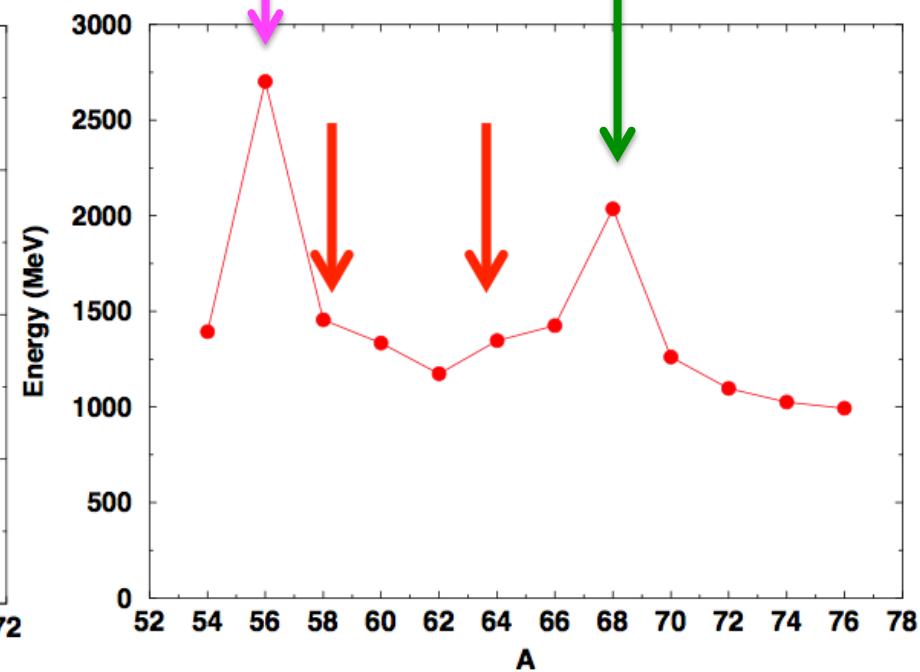
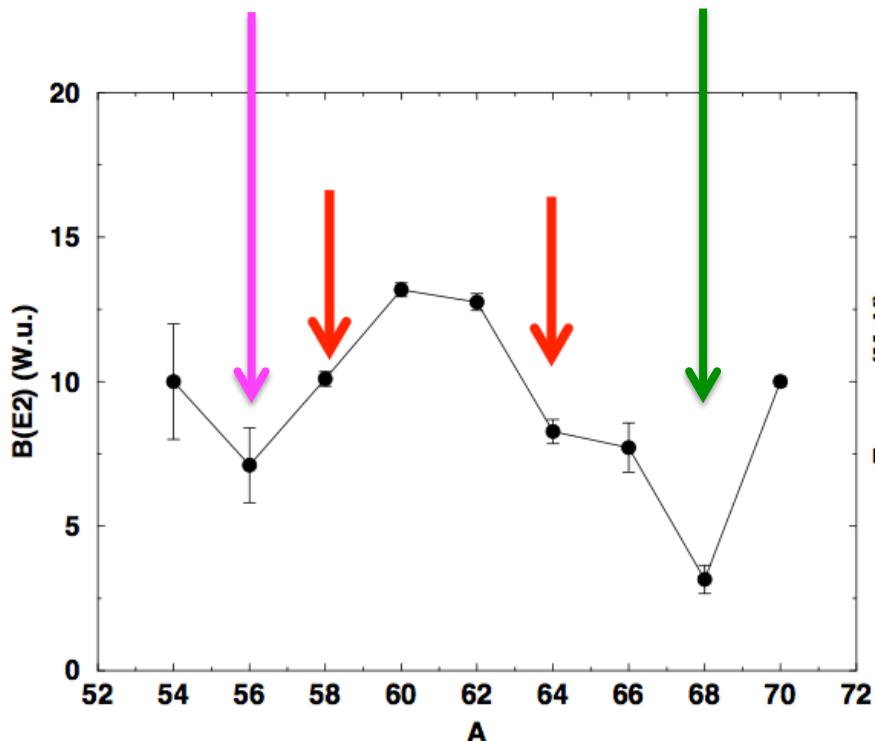
S. Szilner, T. Mijatovic, M. Varga Pajtler
RBI, Zagreb, Croatia



Ni + ^{40}Ca fusion reactions

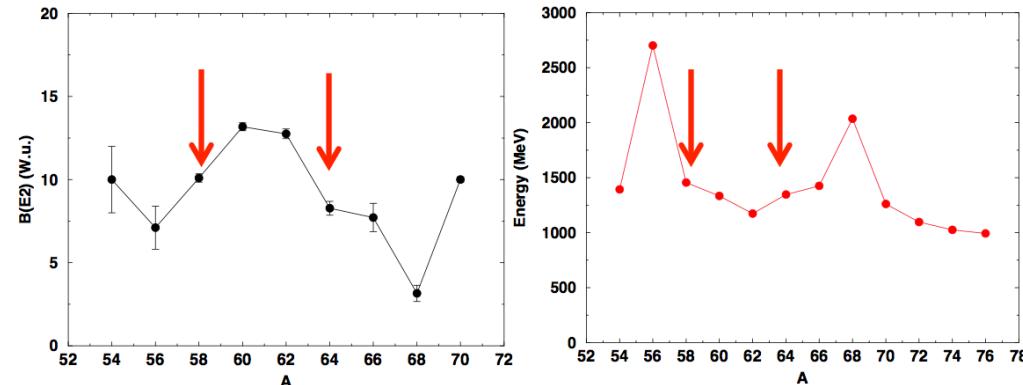
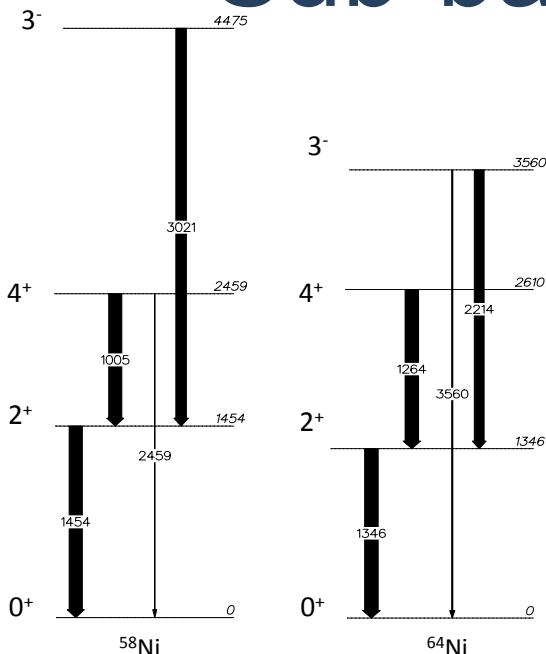
neutron-rich Ni isotope : ^{68}Ni

neutron-poor Ni isotope : ^{56}Ni



B. Pritychenko et al., Update of $B(E2)$ and $E(2^+)$ evaluation near $N \approx Z \approx 28$, At. Dat. Nucl. Dat. Tables (2012)

Sub-barrier fusion : Ca + Ni



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- Positive Q value for transfers for $^{40}\text{Ca} + ^{64}\text{Ni}$ (+2n to +6n and -2p), negative for all transfers in $^{40}\text{Ca} + ^{58}\text{Ni}$ (corrected for Coulomb, $Q_{\text{corr}} = Q_{\text{transfer}} + V_{\text{b-in}}^c - V_{\text{b-out}}^c$)

System	+1n	+2n	+3n	+4n	-1p	-2p	-3p	-4p
$^{40}\text{Ca} + ^{58}\text{Ni}$	-3.80	-2.52	-11.19	-14.21	-3.75	-3.60	-11.95	-15.97
$^{40}\text{Ca} + ^{64}\text{Ni}$	-1.23	3.47	0.86	4.22	0.26	4.19	0.88	1.81

Transfer coupling form factors

C. H. Dasso and A. Vitturi, Phys. Lett. B **179**, 337 (1986)

→ Q_{tr} and F_{tr} are adjusted to fit the measured fusion

$$F(r) = F_{tr} d \frac{V_N}{dr} \sim \frac{F_{tr} V_0}{a} e^{\frac{-(r-R_0)}{a}}$$
$$[F_{tr}] = fm, [V_0] = MeV, [a] = fm$$

G. Scamps and K. Hagino, Phys. Rev. C **92**, 054614 (2015)

$\beta_{nn'}$ and $\alpha_{nn'}$ are adjusted to fit the measured transfer probabilities to be used in the coupled-channels calculations of fusion cross sections

$$V_{nn'}(r) \sim \frac{\beta_{nn'}}{\sqrt{4\pi\alpha_{nn'}}} e^{\frac{-(r-r_p)}{\alpha_{nn'}}}$$
$$[\beta_{nn'}] = MeV \cdot fm, [\alpha_{nn'}] = fm$$