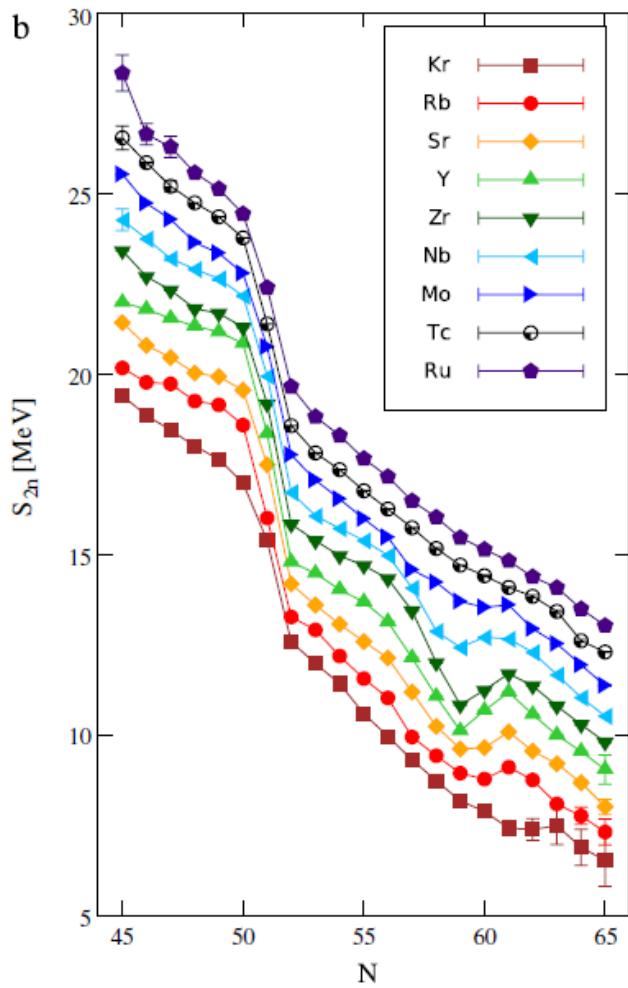


# *Spectroscopic Quadrupole Moment in $^{96,98}\text{Sr}$ : Shape coexistence at $N=60$*

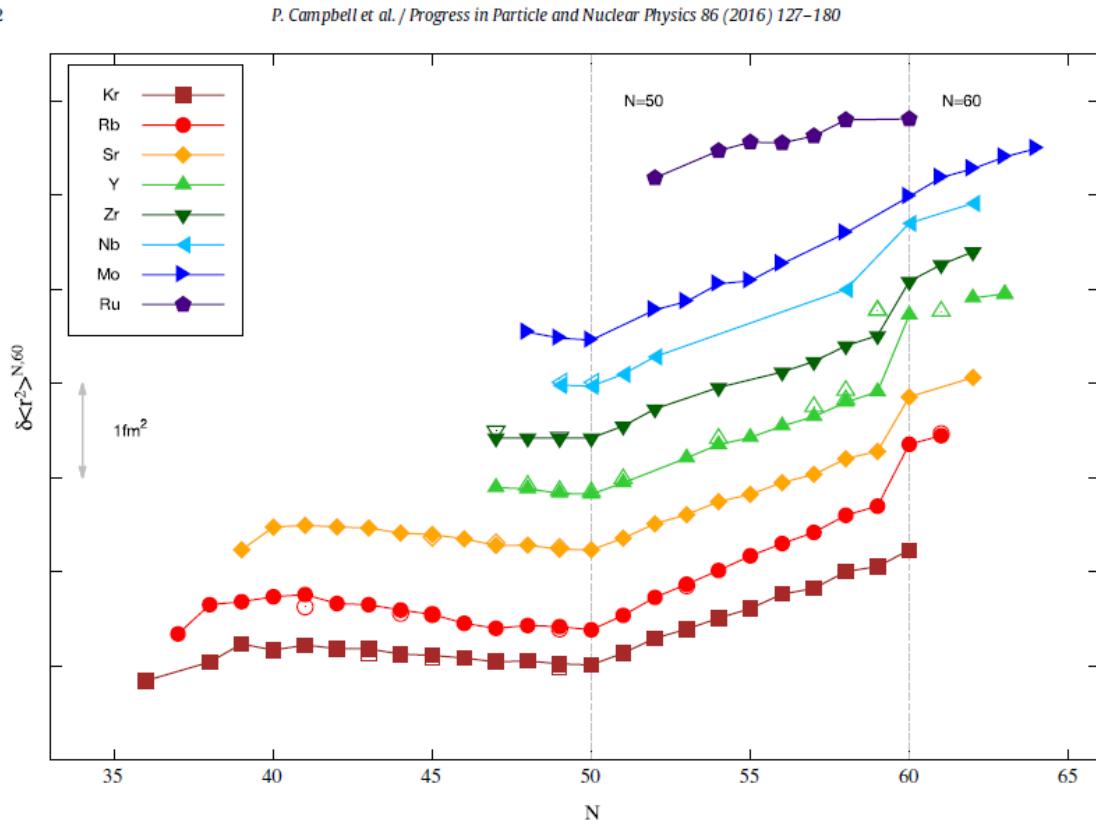
E.Clément-GANIL  
IS451 Collaboration

# Shape Transition at N=60

P. Campbell, I.D. Moore, M.R. Pearson  
Progress in Particle and Nuclear Physics 86  
(2016) 127–180

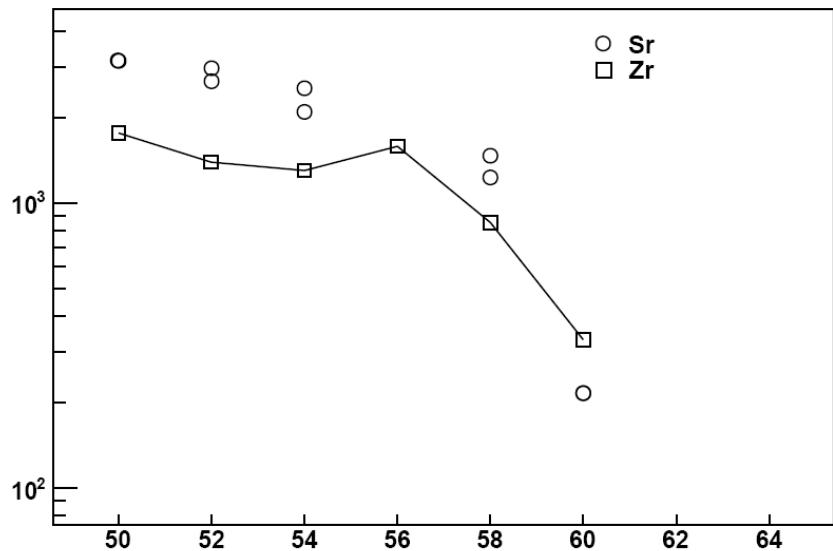
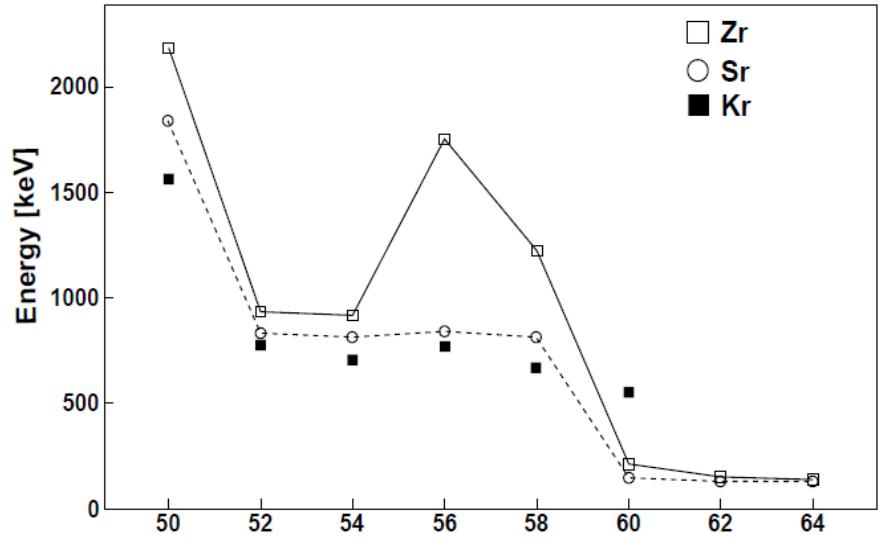


- The n-rich nuclei between Z=37 and Z=41 present at N=60 one of the most impressive deformation change in the nuclear chart
- Localized within the Z degree of freedom
  - Point to a specific  $\pi$ - $\nu$  interaction



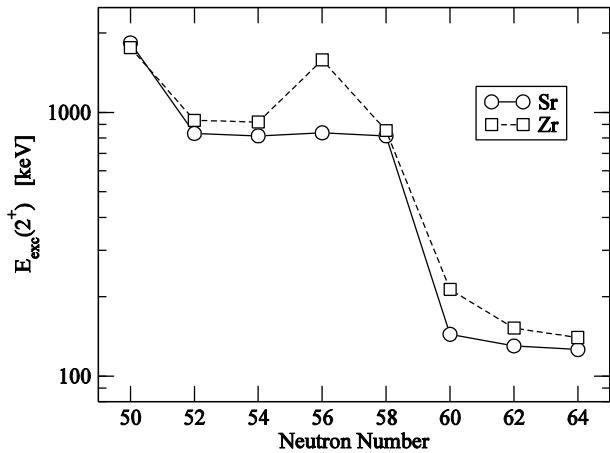
# Shape Transition at N=60

M. Albers *et al.*, *Phys. Rev. Lett.* 108, 062701 (2012)



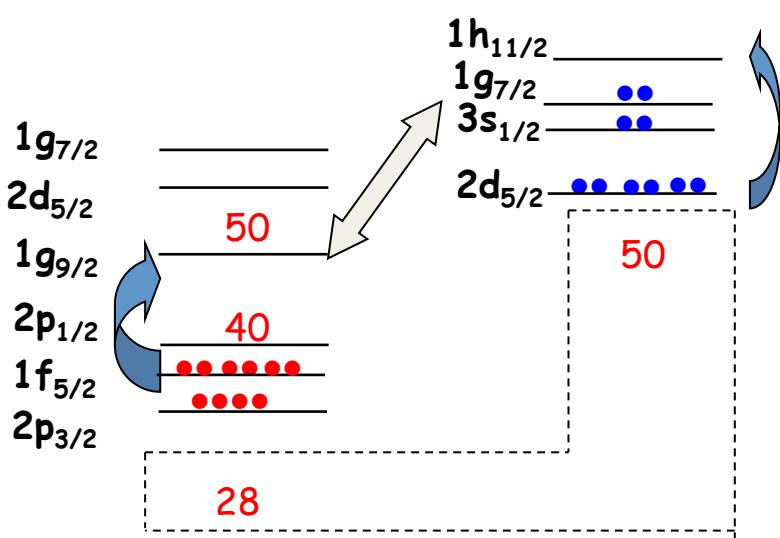
- ❖ First spectroscopy (GS and  $2^+_1$ ) indicated a shape change from  $\beta \sim 0.1$  to  $\beta \sim 0.4$
- ❖  $0^+_2$  states are indication of shape coexistence  
→ Shape inversion ?
- ❖ Kr isotopes behave differently : smooth  $2^+$  change, delayed  $S_{2n}$  increase, no low lying  $0^+_2$

# Shape Transition at N=60



The sharp transition and magnitude of the deformation remain still a challenge for theories (> 100 theoretical papers since the 70's)

- ✓ HFB + the generator coordinate method (GCM)
- ✓ the macroscopic-microscopic method
- ✓ the shell model
- ✓ the Monte Carlo shell model
- ✓ the interacting boson model (IBM) approximation
- ✓ the VAMPIR model
- ✓ covariant density functional (DF) theory (PC-PK1).



- ❑  $0^+_2$  state created by (2p-2h/4p-4h) excitation across  $Z=40$
- ❑ Beyond  $N=60$ ,  $g_{7/2}$  and  $h_{11/2}$  are populated, the  $\pi-\nu$  interaction and the participates to the lowering  $0^+_2$  state and to the high collectivity of  $2^+_1$  state.
- ❑ In BMF calculations, two minima appear in the PES

Mainly GS and level scheme are known and limit the comparison with theoretical models

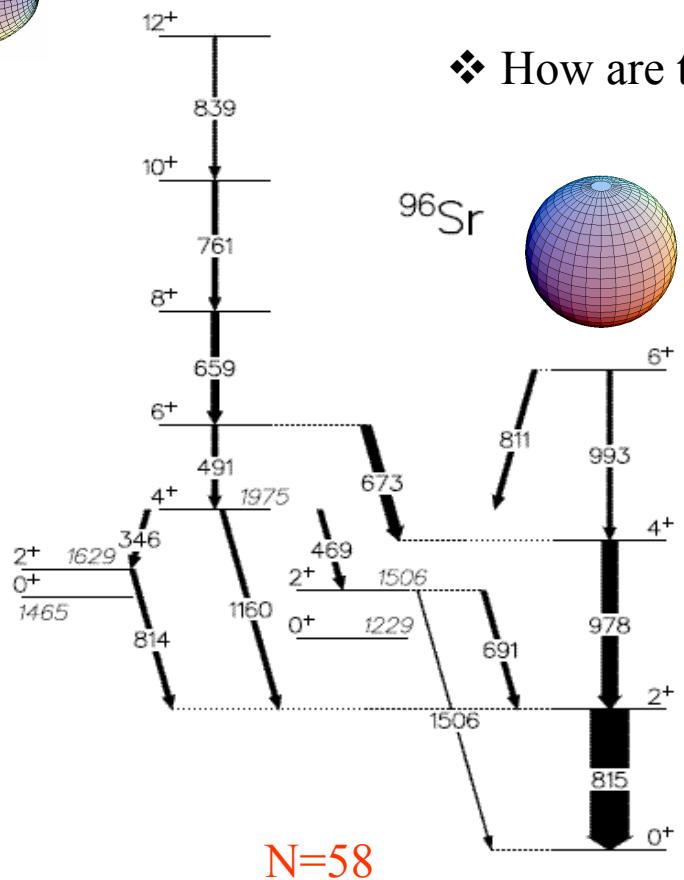
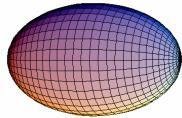
K. Sieja et al PRC 79, 064310 (2009)

A. Petrovici PRC 85, 034337 (2012)

T. Togashi et al, arXiv:1606.09056v1; T. Togashi et al, Accepted PRL (2016)

C. Kremer et al, arXiv:1606.09057v1 (2016)

# Shape Transition at N=60

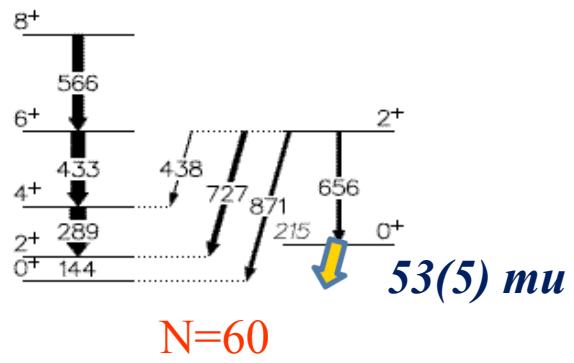


❖ What is the shape of the corresponding  $2^+$  states ?

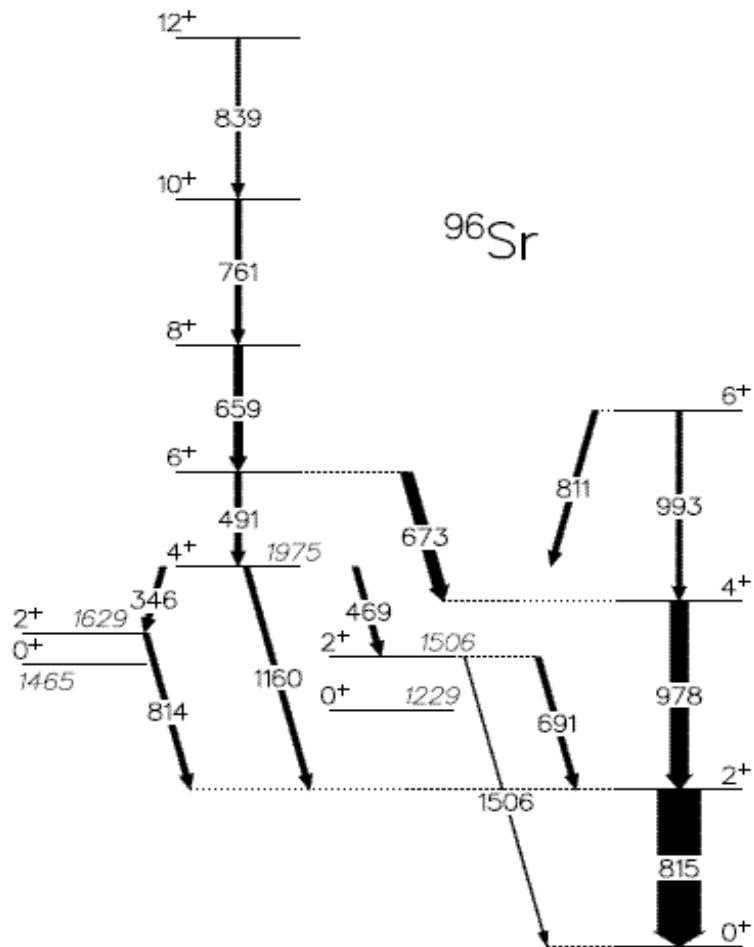
❖ How are the different configurations connected ?

→ Coulomb excitation of RIB

$^{98}\text{Sr}$

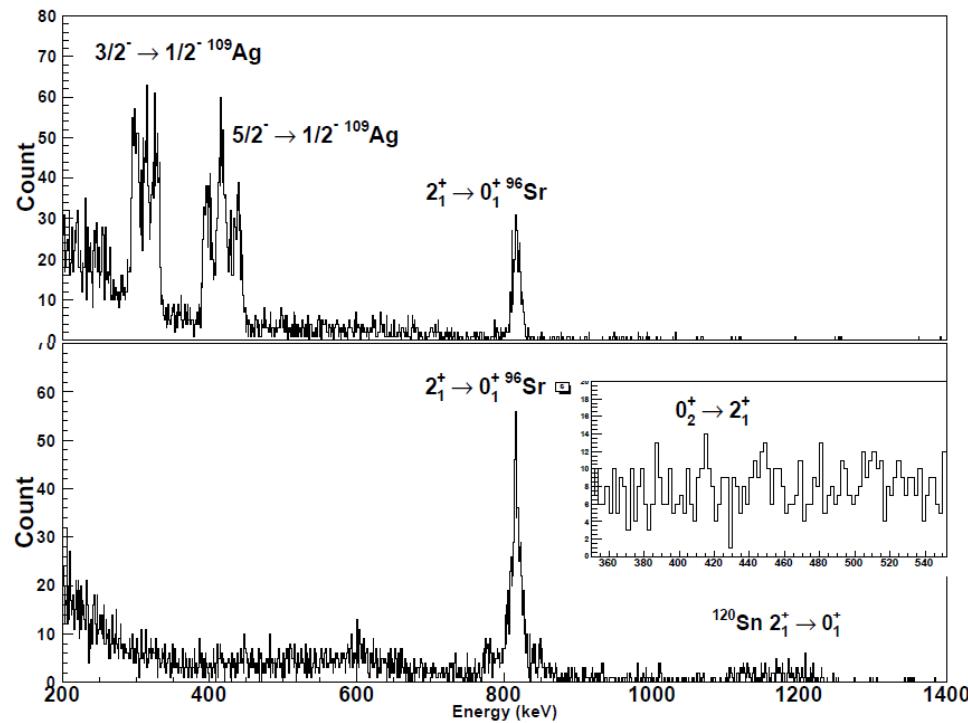


# Safe Coulomb excitation of $^{96,98}\text{Sr}$ beams at REX-ISOLDE using the MINIBALL array at CERN

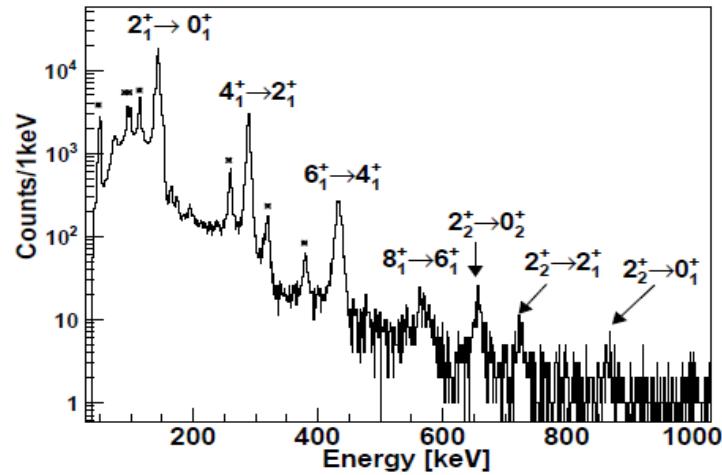
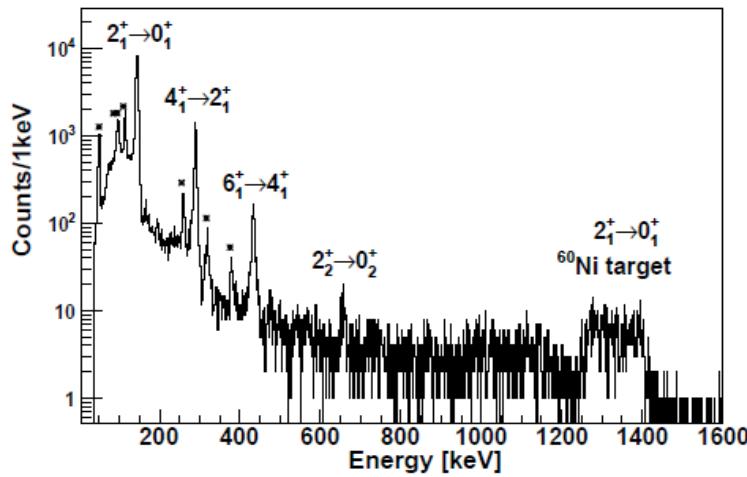


$^{96}\text{Sr} T_{1/2} = 1.07 \text{ sec. } 7000 \text{ pps at 275 MeV}$

$^{98}\text{Sr} T_{1/2} = 0.65 \text{ sec. } 60000 \text{ pps at 276 MeV}$



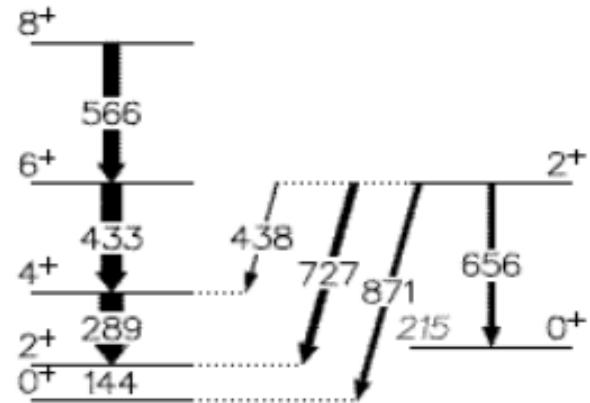
# Safe Coulomb excitation of $^{96,98}\text{Sr}$ beams at REX-ISOLDE using the MINIBALL array at CERN



$^{96}\text{Sr} T_{1/2} = 1.07$  sec. 7000 pps at 275 MeV  
 $^{98}\text{Sr} T_{1/2} = 0.65$  sec. 60000 pps at 276 MeV

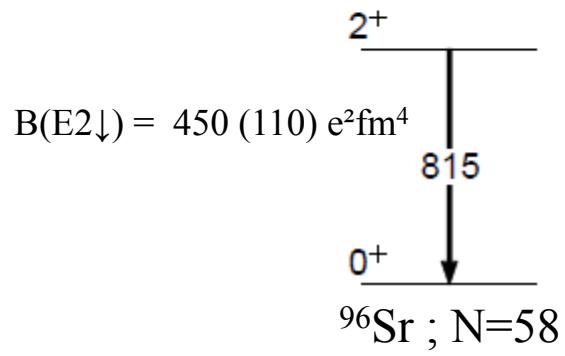
The Coulomb excitation cross section is analyzed using the least-squares fitting code GOSIA  
 T. Czosnyka, D. Cline, and C. Y. Wu, Bull. Am. Phys. Soc. **28**, 745 (1983).

$^{98}\text{Sr}$



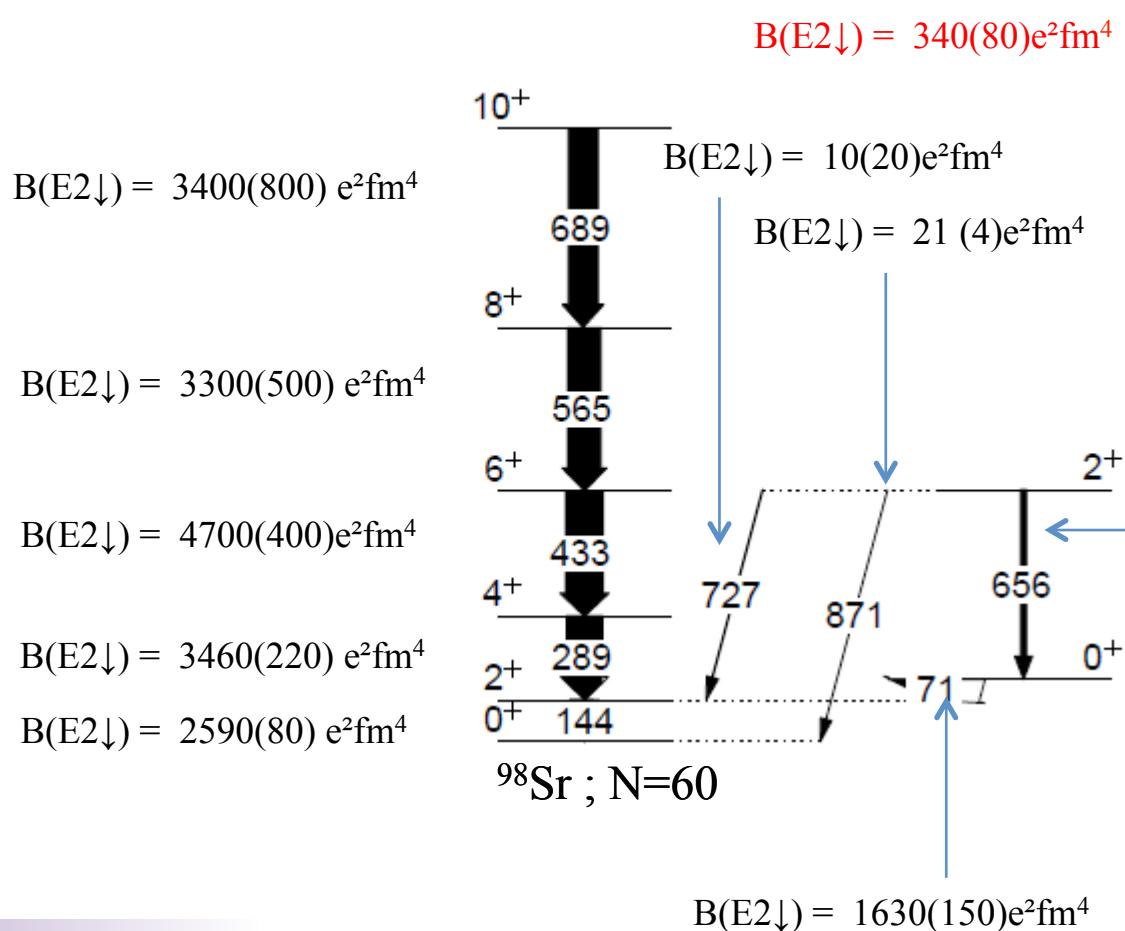
# Shape Coexistence in $^{96,98}\text{Sr}$

$$Q_s = -22(31) \text{ efm}^2$$



E. C. et al, Phys.Rev.Lett. 116, 022701 (2016)

E.Clément



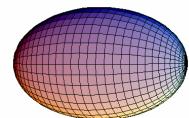
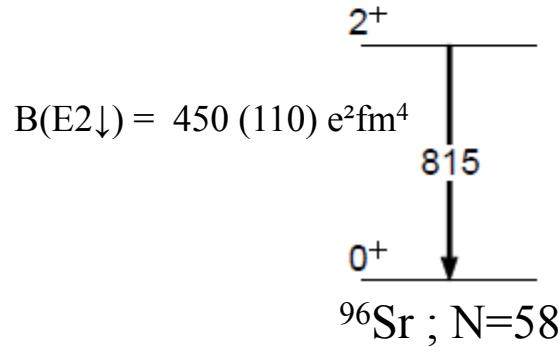
# Shape Coexistence in $^{96,98}\text{Sr}$

The  $2^+_1$  in  $^{96}\text{Sr}$  is weakly deformed

The ground state band in  $^{98}\text{Sr}$  has a large prolate deformation and the  $2^+_2$  is similar to the ground state in  $^{96}\text{Sr}$

- Shape coexistence in  $^{98}\text{Sr}$   
Shape inversion at N=60

$$Q_s = -22(31) \text{ efm}^2$$



$$\beta > 0.4$$

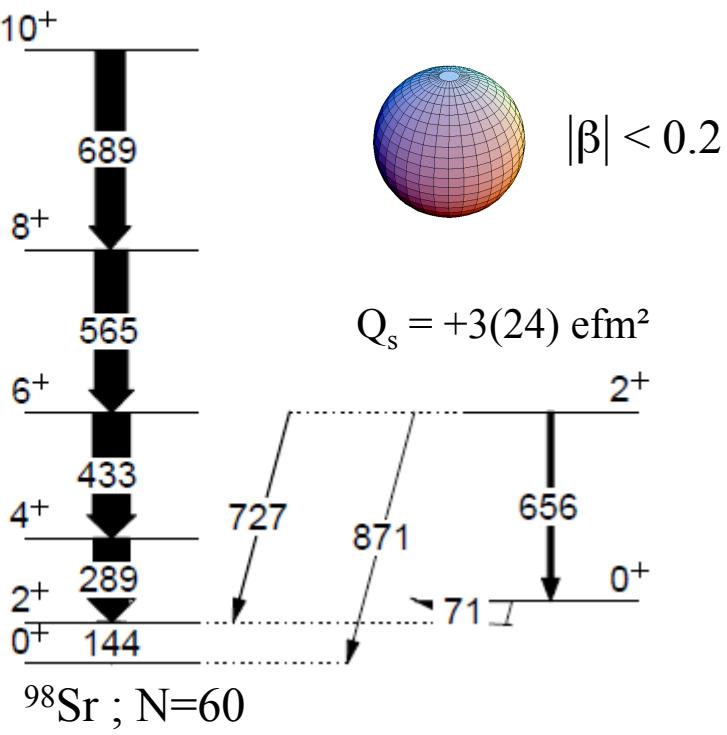
$$Q_s = -90(80) \text{ efm}^2$$

$$Q_s = -130(23) \text{ efm}^2$$

$$Q_s = -213(16) \text{ efm}^2$$

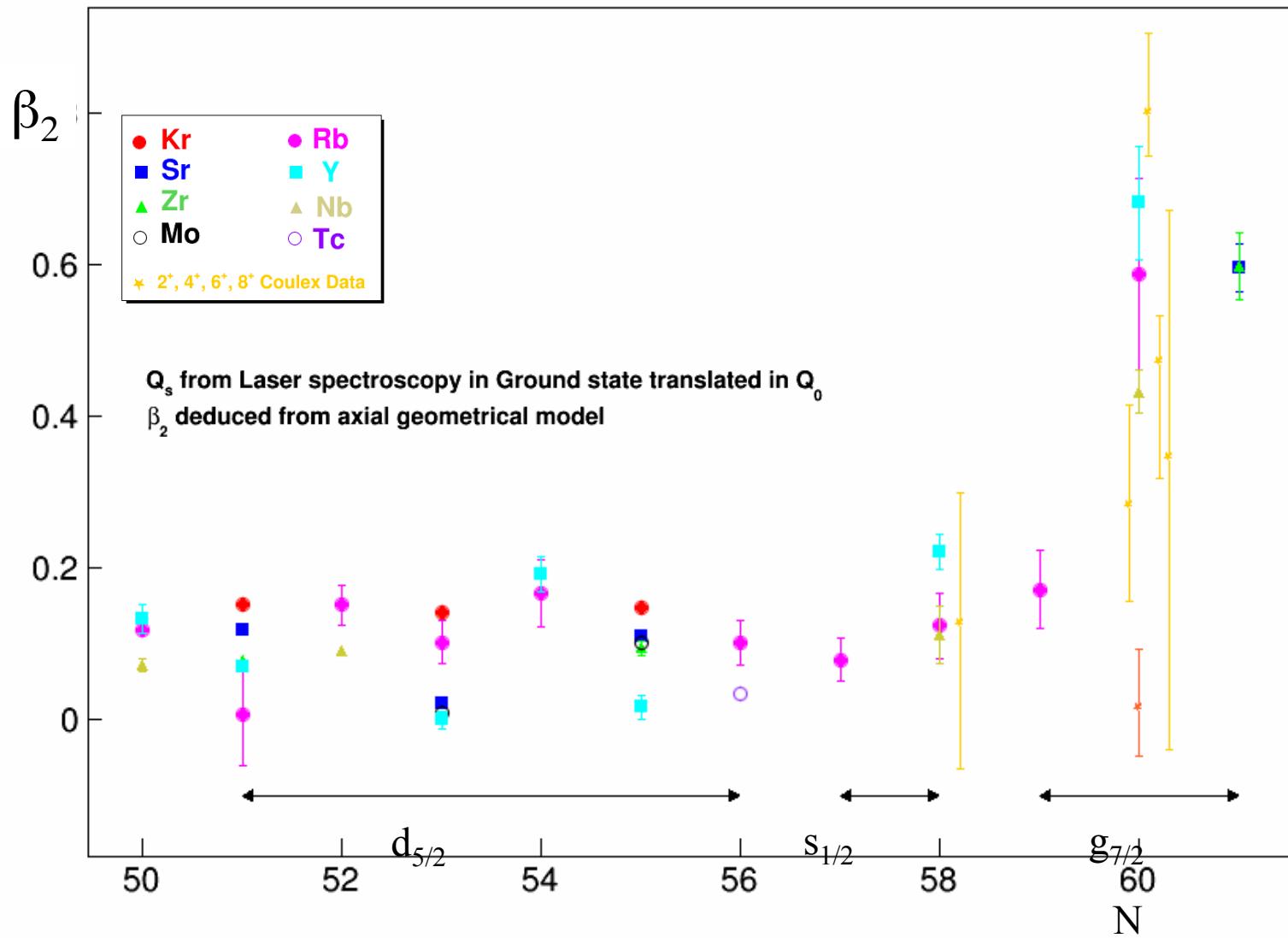
$$Q_s = -48(25) \text{ efm}^2$$

E. C. et al, Phys.Rev.Lett. 116, 022701 (2016)

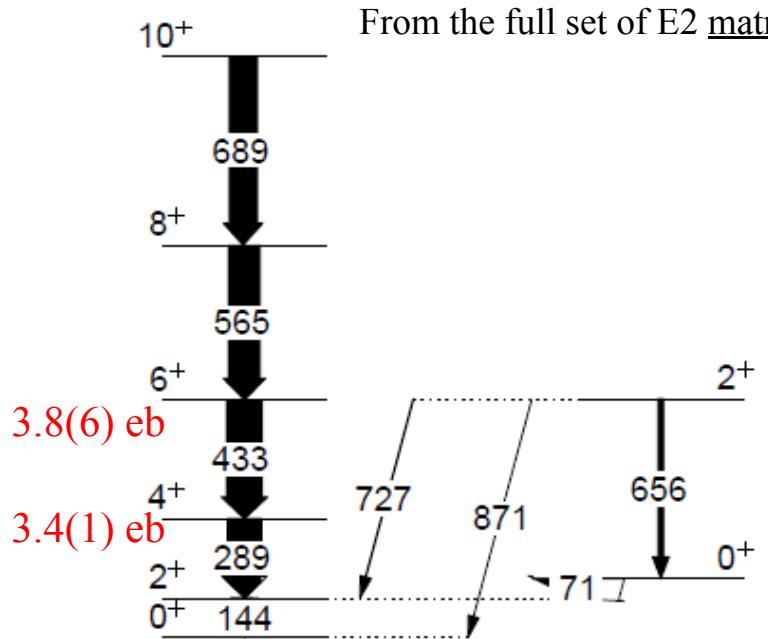


# Shape Coexistence at N=60

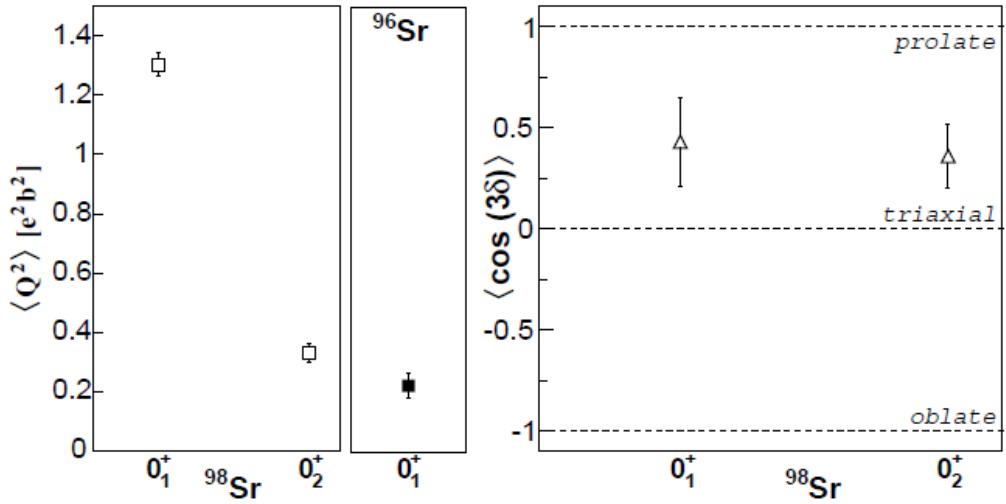
*Comparison between Ground and Excited state  
Quadrupole moments*



# Shape Coexistence in $^{96,98}\text{Sr}$



From the full set of E2 matrix elements,  $0^+$  states deformation can be probed using the QSR formalism



Shape coexistence in a two-state mixing model

$$\begin{aligned} |I_1\rangle &= + \cos \theta_I |I_{\text{pr}}\rangle + \sin \theta_I |I_{\text{ob}}\rangle \\ |I_2\rangle &= - \sin \theta_I |I_{\text{pr}}\rangle + \cos \theta_I |I_{\text{ob}}\rangle \end{aligned}$$

Perturbed states

Pure states

| Un-perturbated                         |                         |
|--|-------------------------|
| $\cos^2 \theta_0$                      | 0.87(1)                 |
| $\cos^2 \theta_2$                      | 0.99(1)                 |
| $Q_0^{\text{pr}}$                      | +3.85(6) eb             |
| $Q_0^{\text{sph}}$                     | -0.5(3) eb              |
| $\langle 2_p^+ \  E2 \  2_p^+ \rangle$ | -1.45(2) eb             |
| $\langle 2_s^+ \  E2 \  2_s^+ \rangle$ | +0.18(10) eb            |
|  | $-0.63^{+0.32}_{-0.28}$ |
|  | $+0.04^{+0.32}_{-0.20}$ |

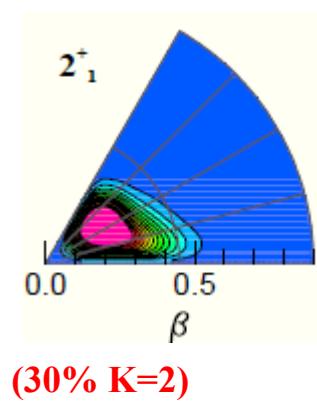
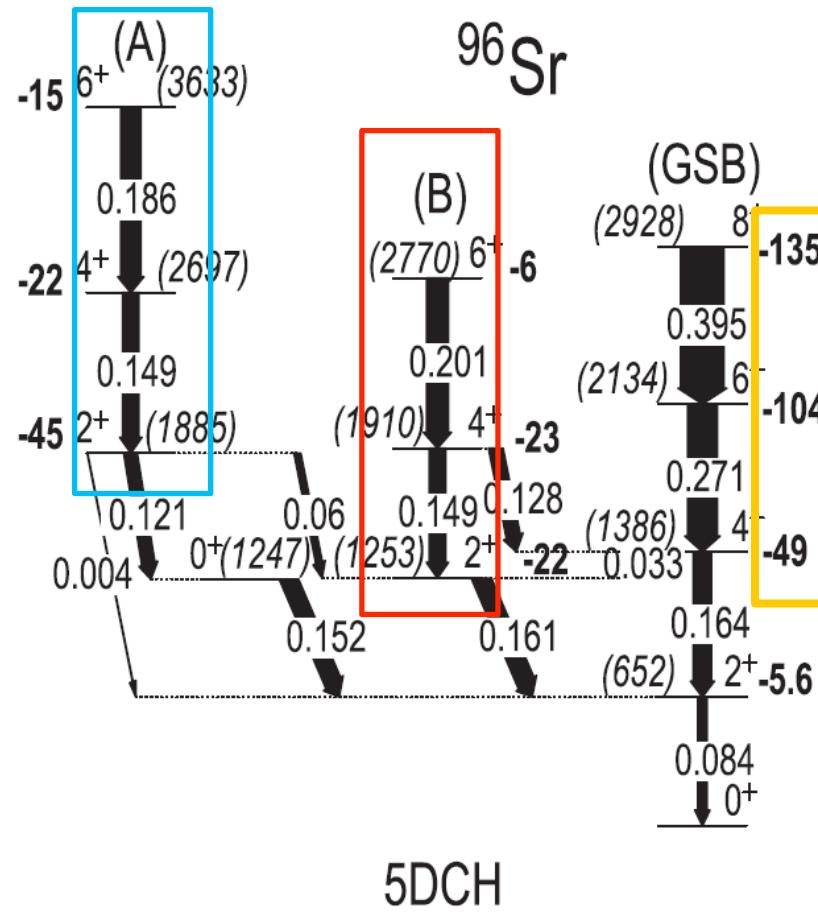
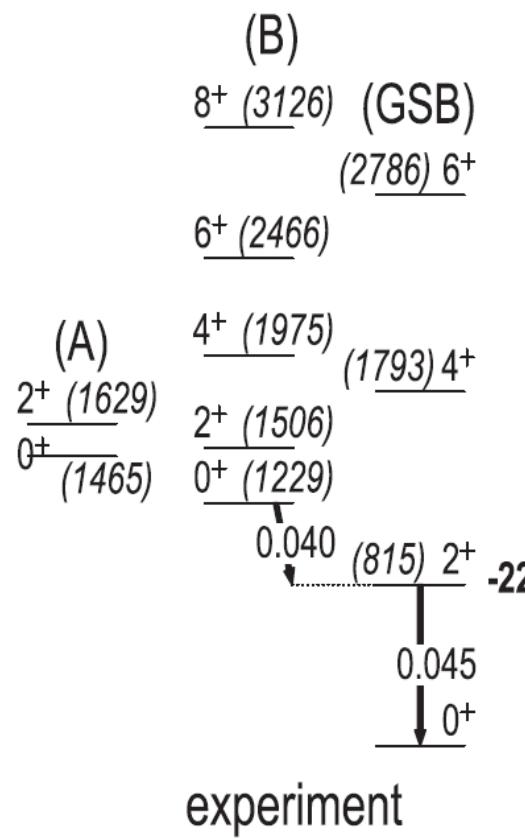
The sharp transition is related to the very weak mixing between competing configurations in contrast to the N~Z cases in Kr and Hg isotopes

# Collectivity around N=60

From a theoretical point of view

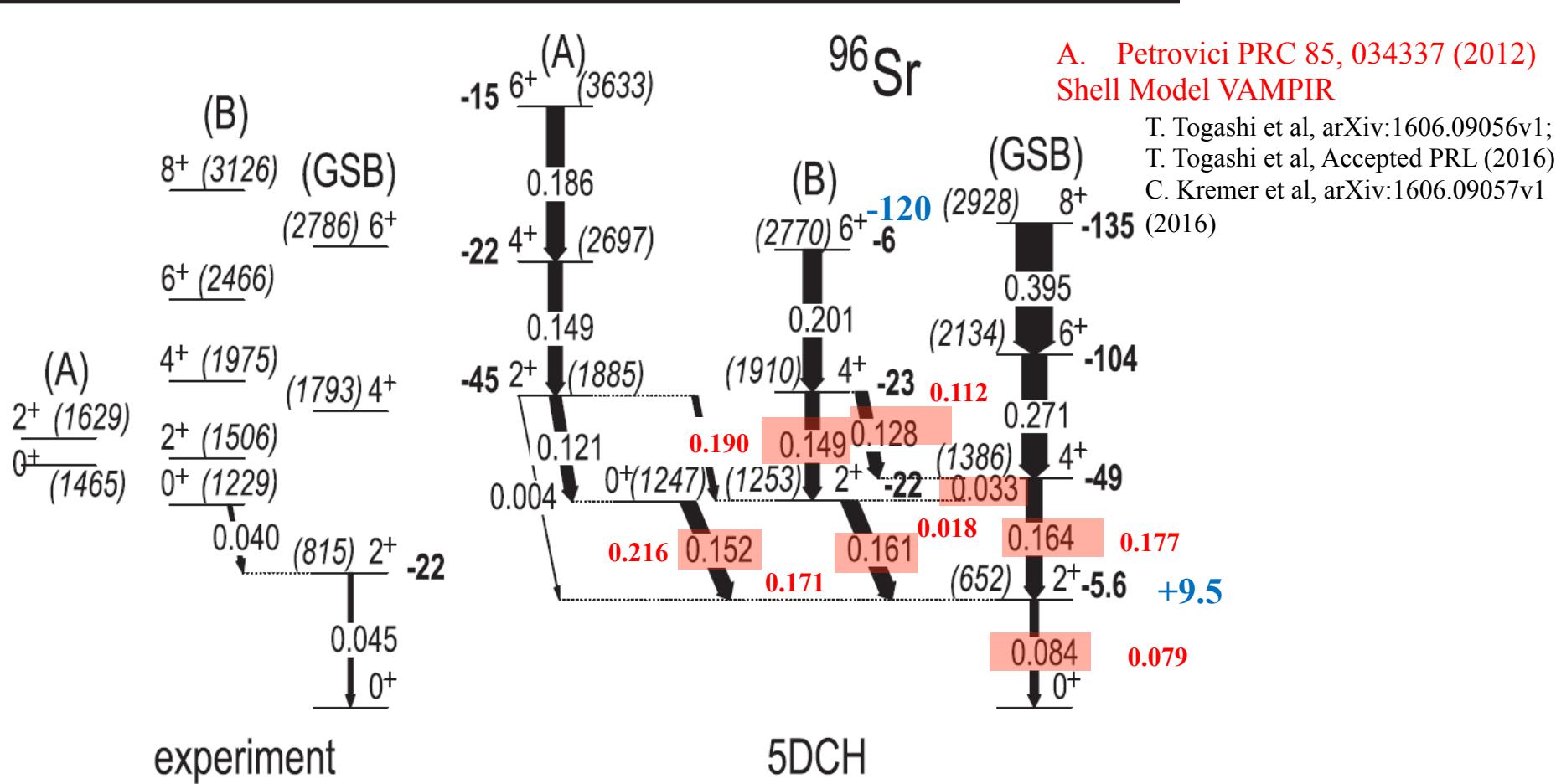
Large B(E2), higher Qs K=0 ~70%

Large B(E2), low Qs K=0 < 50%



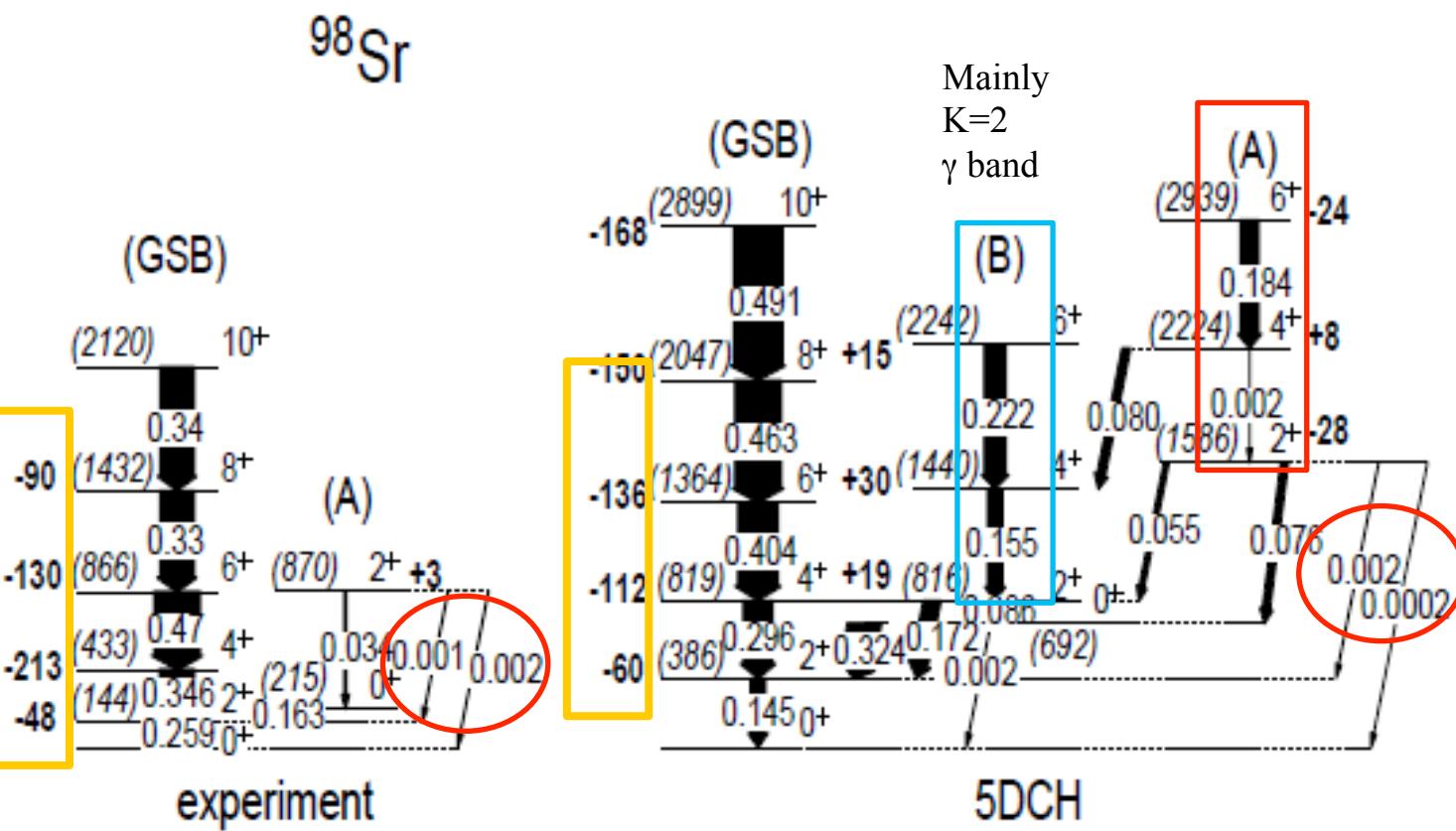
# Collectivity around N=60

From a theoretical point of view



# Collectivity around N=60

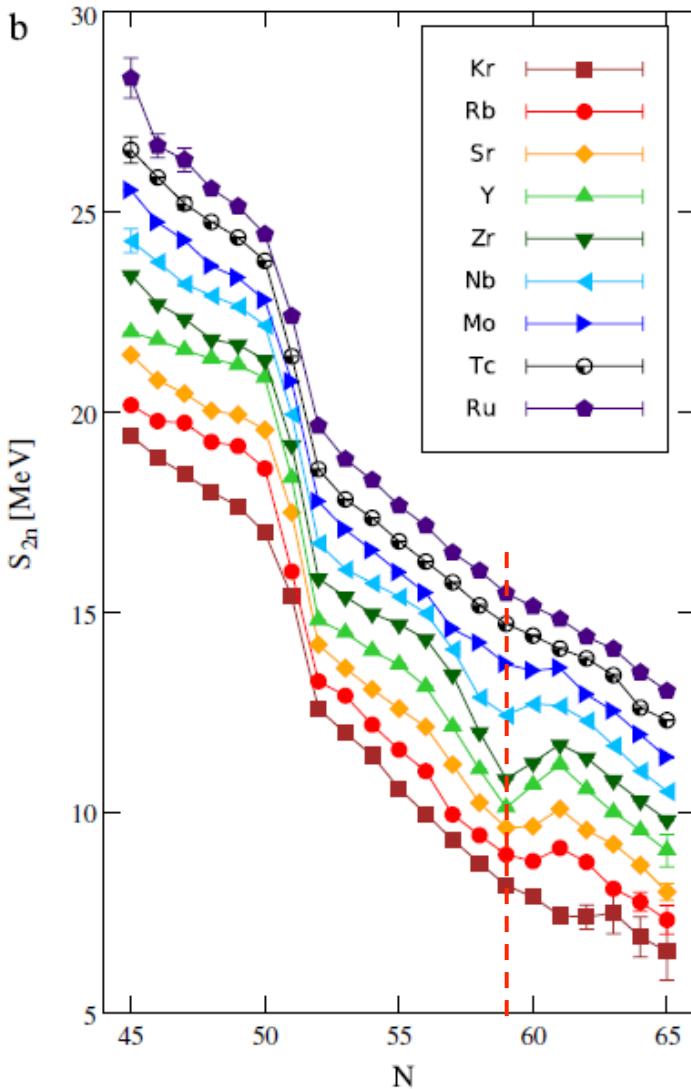
From a theoretical point of view



T. Togashi et al, arXiv:1606.09056v1;  
 T. Togashi et al, Accepted PRL (2016)  
 C. Kremer et al, arXiv:1606.09057v1 (2016)

J. Xiang et al . Phys. Rev. C 93, 054324 (2016)  
 E. Clément, et PRL. 116, 022701 (2016)

# Conclusions



- We investigated the collectivity and the deformation in  $^{96,98}\text{Sr}$  at the shape transition using RIB and the Coulomb excitation technique at REX-ISOLDE, CERN
- First levels in  $^{98}\text{Rb}$
- E2 matrix elements have been extracted and establish shape coexistence between small and large prolate deformations that do not mix and give rise to a sharp transition at N=60 where triaxiality plays a role
- *HFB+GCM Gogny force DIS* calculations reproduce the trend
- Large set of E0 transition strengths calculated
- Shell Model calculations (VAMPIR) show a nice agreement with BMF for  $\text{B}(\text{E}2)$  between low lying states
- The MCSM calculations are very promising

→ Why Kr behave differently ?

Fission runs at AGATA@GANIL (spectroscopy,  $\text{T}_{1/2}$ )

→ See J. Dudouet's talk on Thursday 16:35

ISOL facilities beams

→ Confusing predictions for  $^{96}\text{Sr}$  beyond the  $2^+_1$  ?

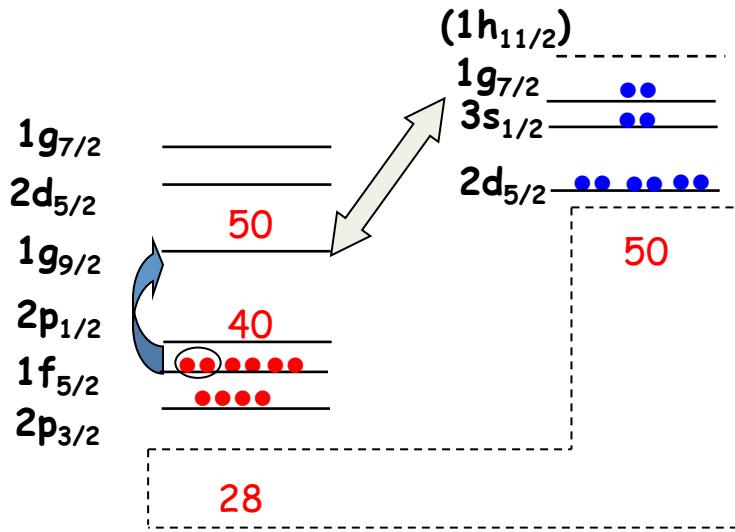
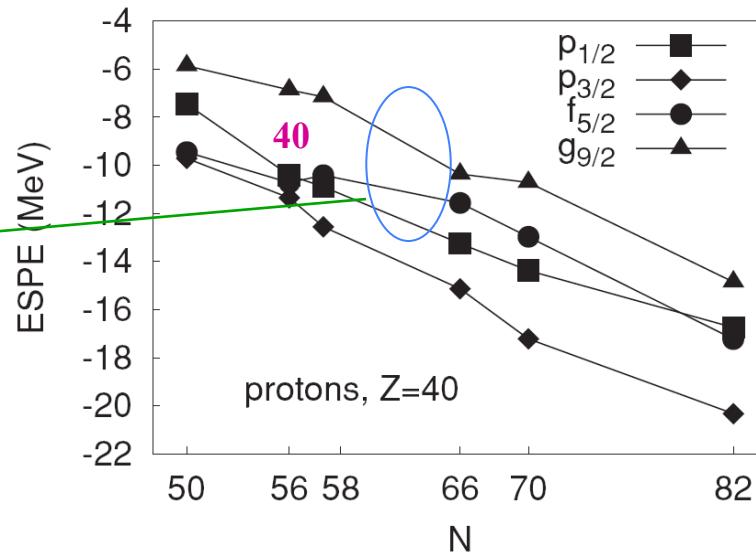
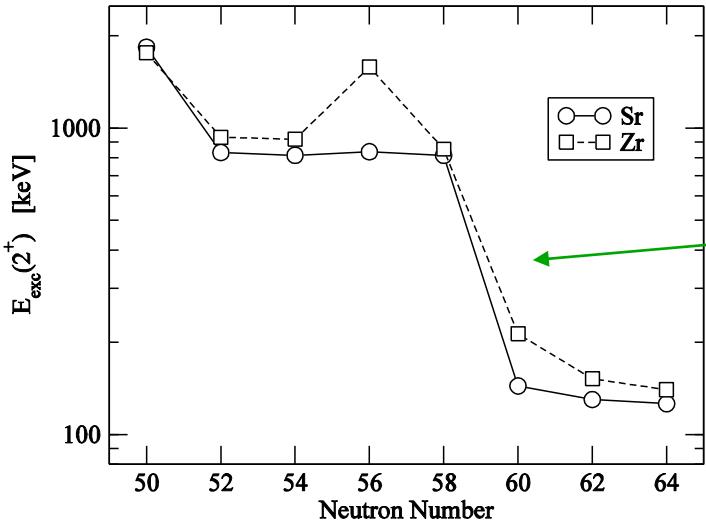
→ Pseudo and quasi -SU(3) approach is valid in this case, similarly to an island of inversion

## Spectroscopic Quadrupole Moments in $^{96,98}\text{Sr}$ : Evidence for Shape Coexistence in Neutron-Rich Strontium Isotopes at $N = 60$

E. Clément,<sup>1,2,\*</sup> M. Zielińska,<sup>3,4</sup> A. Görgen,<sup>5</sup> W. Korten,<sup>3</sup> S. Péru,<sup>6</sup> J. Libert,<sup>6</sup> H. Goutte,<sup>3</sup> S. Hilaire,<sup>6</sup> B. Bastin,<sup>1</sup> C. Bauer,<sup>7</sup> A. Blazhev,<sup>8</sup> N. Bree,<sup>9</sup> B. Bruyneel,<sup>8</sup> P. A. Butler,<sup>10</sup> J. Butterworth,<sup>11</sup> P. Delahaye,<sup>1,2</sup> A. Dijon,<sup>1</sup> D. T. Doherty,<sup>3</sup> A. Ekström,<sup>12</sup> C. Fitzpatrick,<sup>13</sup> C. Fransen,<sup>8</sup> G. Georgiev,<sup>14</sup> R. Gernhäuser,<sup>15</sup> H. Hess,<sup>8</sup> J. Iwanicki,<sup>4</sup> D. G. Jenkins,<sup>11</sup> A. C. Larsen,<sup>5</sup> J. Ljungvall,<sup>14</sup> R. Lutter,<sup>15</sup> P. Marley,<sup>11</sup> K. Moschner,<sup>8</sup> P. J. Napiorkowski,<sup>4</sup> J. Pakarinen,<sup>2</sup> A. Petts,<sup>10</sup> P. Reiter,<sup>8</sup> T. Renstrøm,<sup>5</sup> M. Seidlitz,<sup>8</sup> B. Siebeck,<sup>8</sup> S. Siem,<sup>5</sup> C. Sotty,<sup>14</sup> J. Srebrny,<sup>4</sup> I. Stefanescu,<sup>9</sup> G. M. Tveten,<sup>5,2</sup> J. Van de Walle,<sup>2</sup> M. Vermeulen,<sup>11</sup> D. Voulot,<sup>2</sup> N. Warr,<sup>8</sup> F. Wenander,<sup>2</sup> A. Wiens,<sup>8</sup> H. De Witte,<sup>9</sup> and K. Wrzosek-Lipska<sup>4</sup>

# Shape Transition at N=60

50 years later, where are we ?

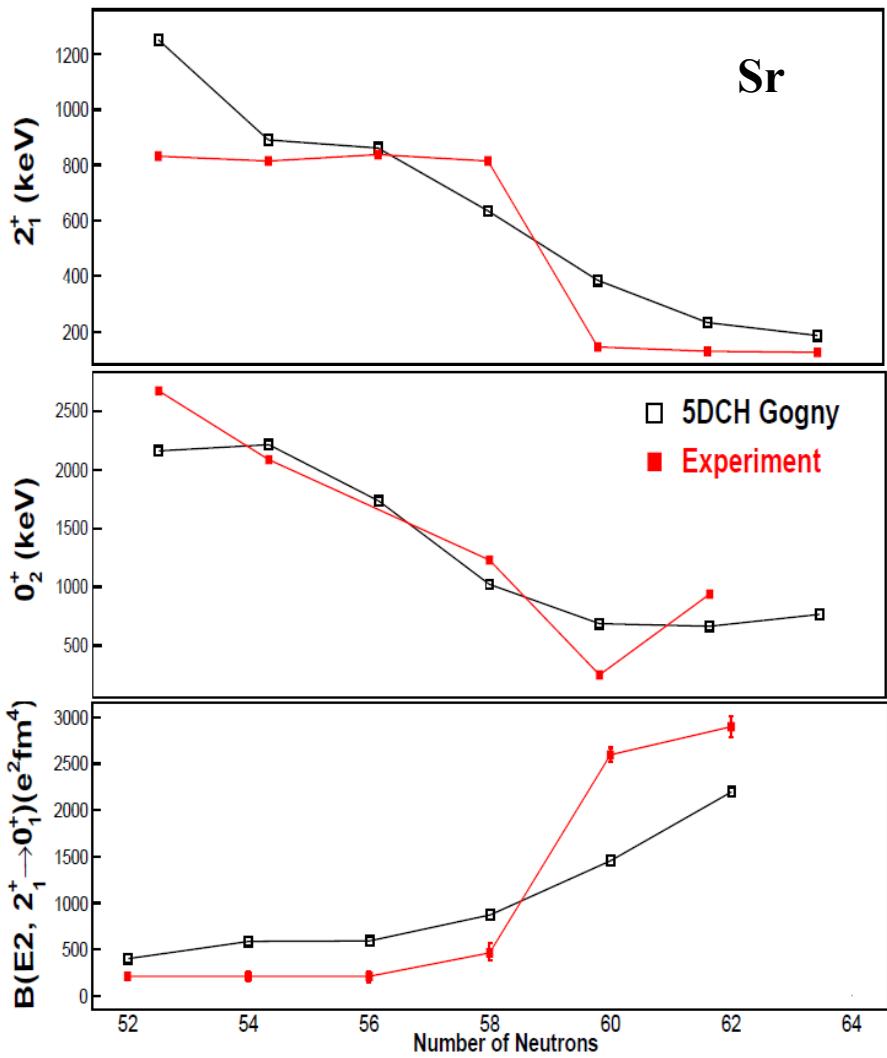


- $0^+_2$  state created by 2p-2h excitation across  $Z=40$
- Beyond  $N=60$ ,  $g_{7/2}$  is populated, the  $\pi-\nu$  interaction participates to the lowering  $0^+_2$  state and to the high collectivity of  $2^+_1$  state.
- In BMF calculations, two minima appear in the PES

# Collectivity around N=60

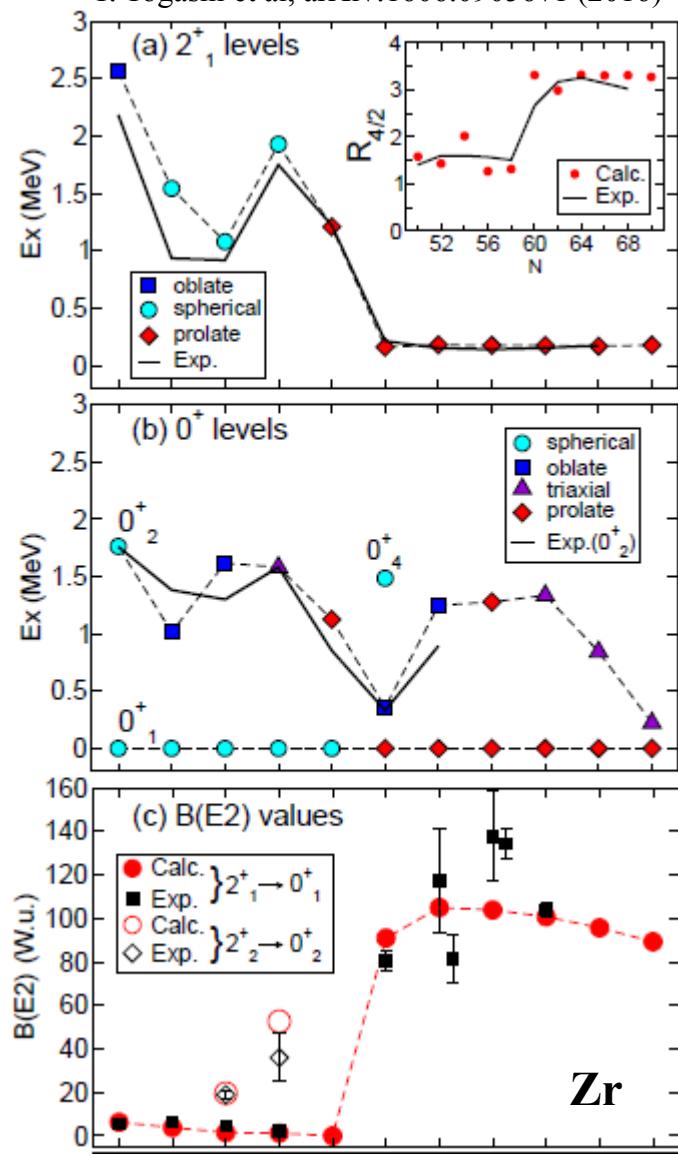
From a theoretical point of view

J. P. Delaroche et al., Phys. Rev. C 81, 014303 (2010).



E.Clément

T. Togashi et al, arXiv:1606.09056v1 (2016)

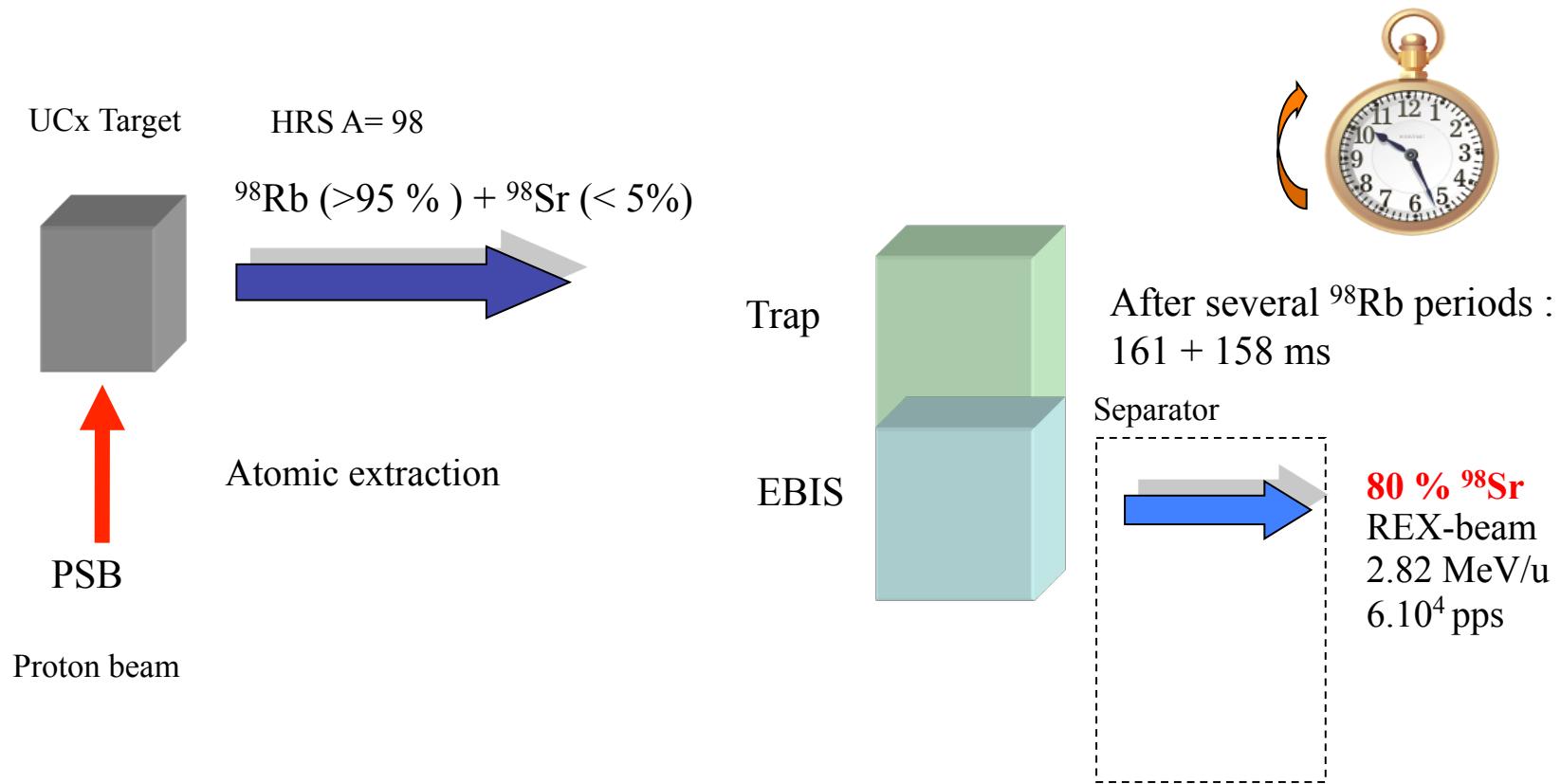


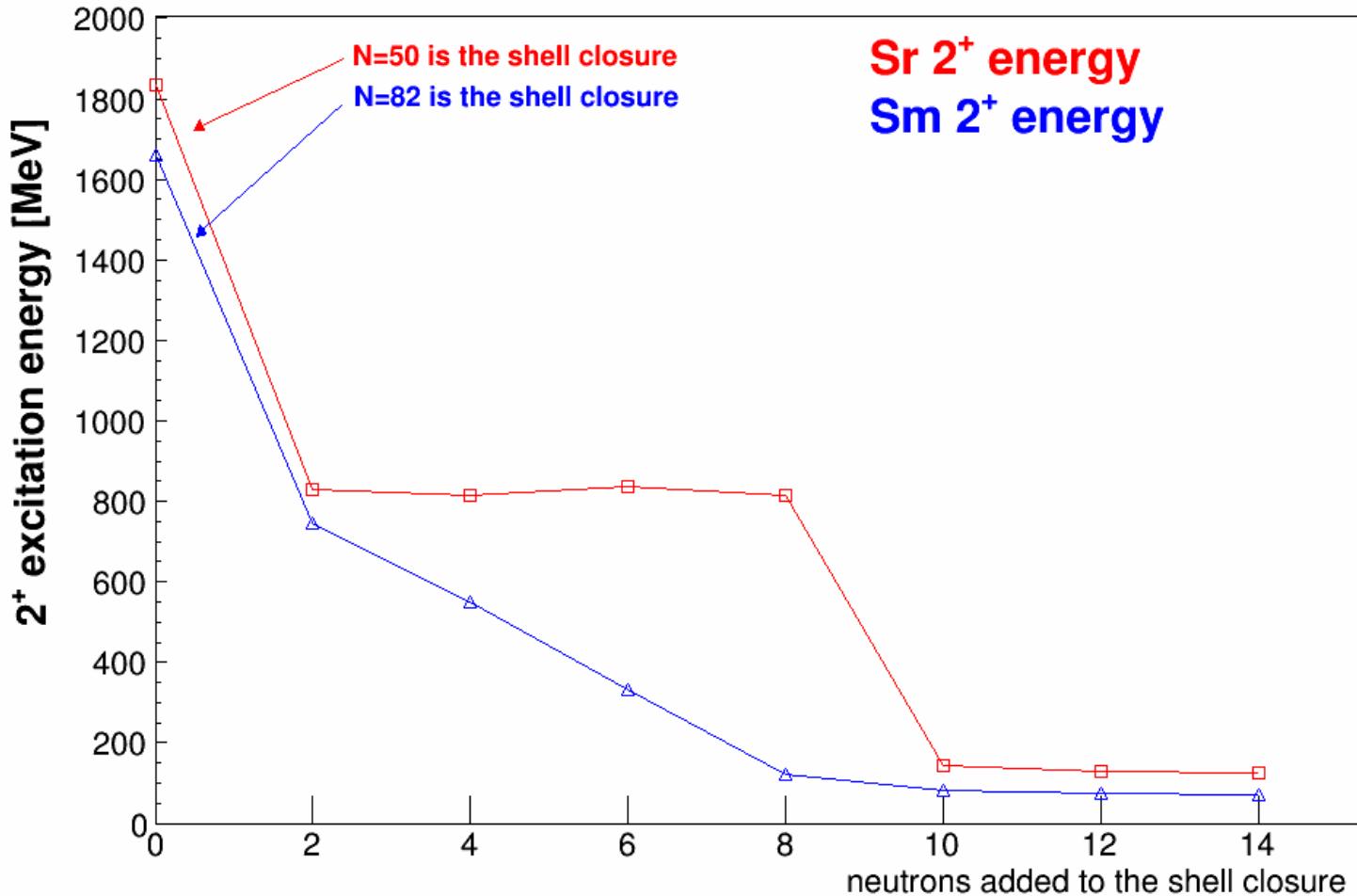
Zr

- ★ Post-accelerated radioactive  $^{96,98}\text{Sr}$  beam at REX-ISOLDE (2.8 MeV/A)  $^{96}\text{Sr}$   $T_{1/2} = 1\text{s}$ ,  $^{98}\text{Sr}$   $T_{1/2} = 0.6\text{s}$
- ★ Safe Coulomb excitation
- ★  $B(E2)$ 's and  $Q_0$  extracted from the Coulomb excitation cross section

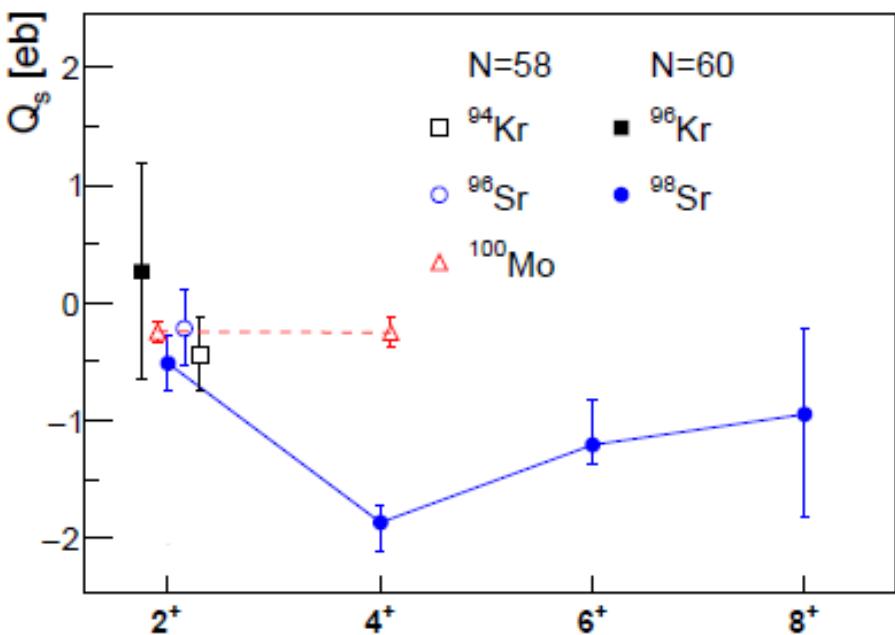
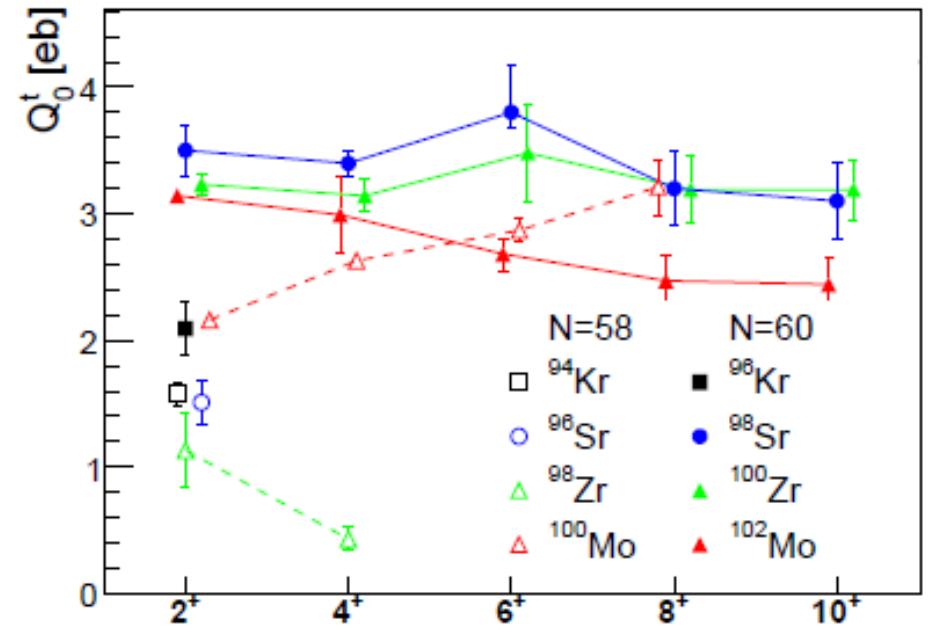
re  $^{96}\text{Sr}^{23+}$  REX-  
am  
37 MeV/u  
to  $0.5 \sim 10^4$  pps

- ★ Post-accelerated radioactive  $^{96,98}\text{Sr}$  beam at REX-ISOLDE (2.8 MeV/A)
- ★ Safe Coulomb excitation
- ★  $B(E2)$ 's and  $Q_0$  extracted from the Coulomb excitation cross section

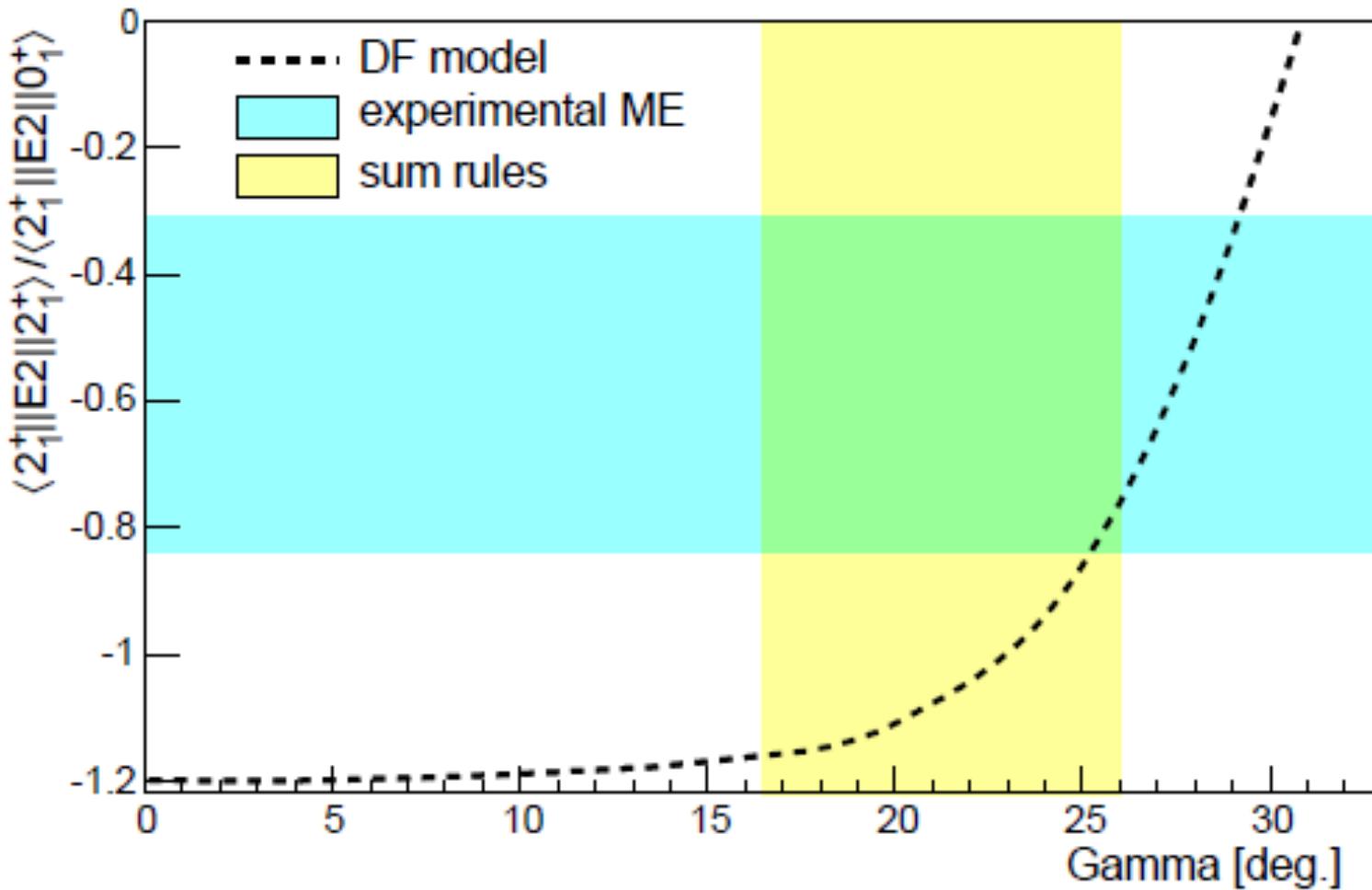




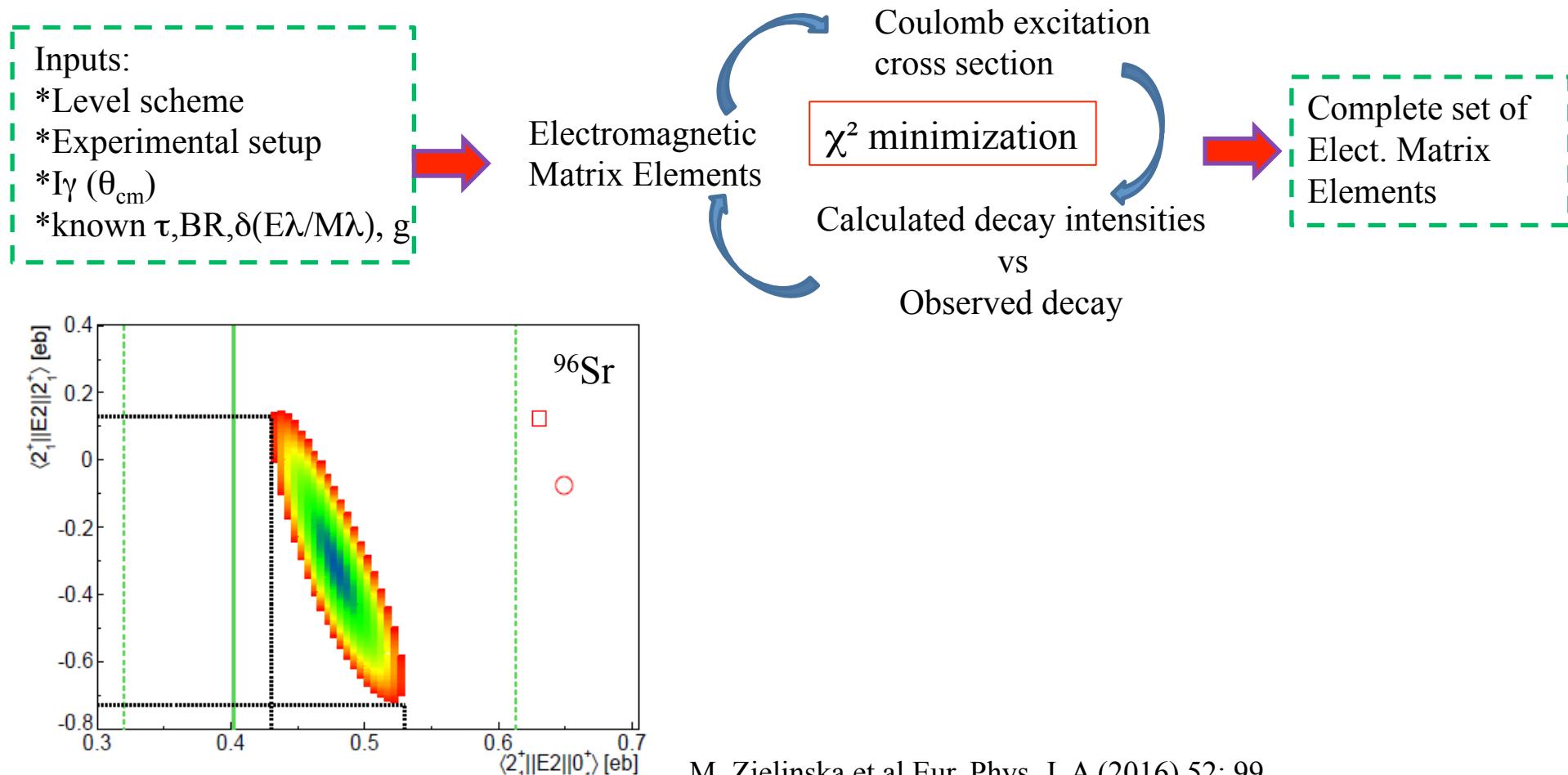
# Collectivity around N=60

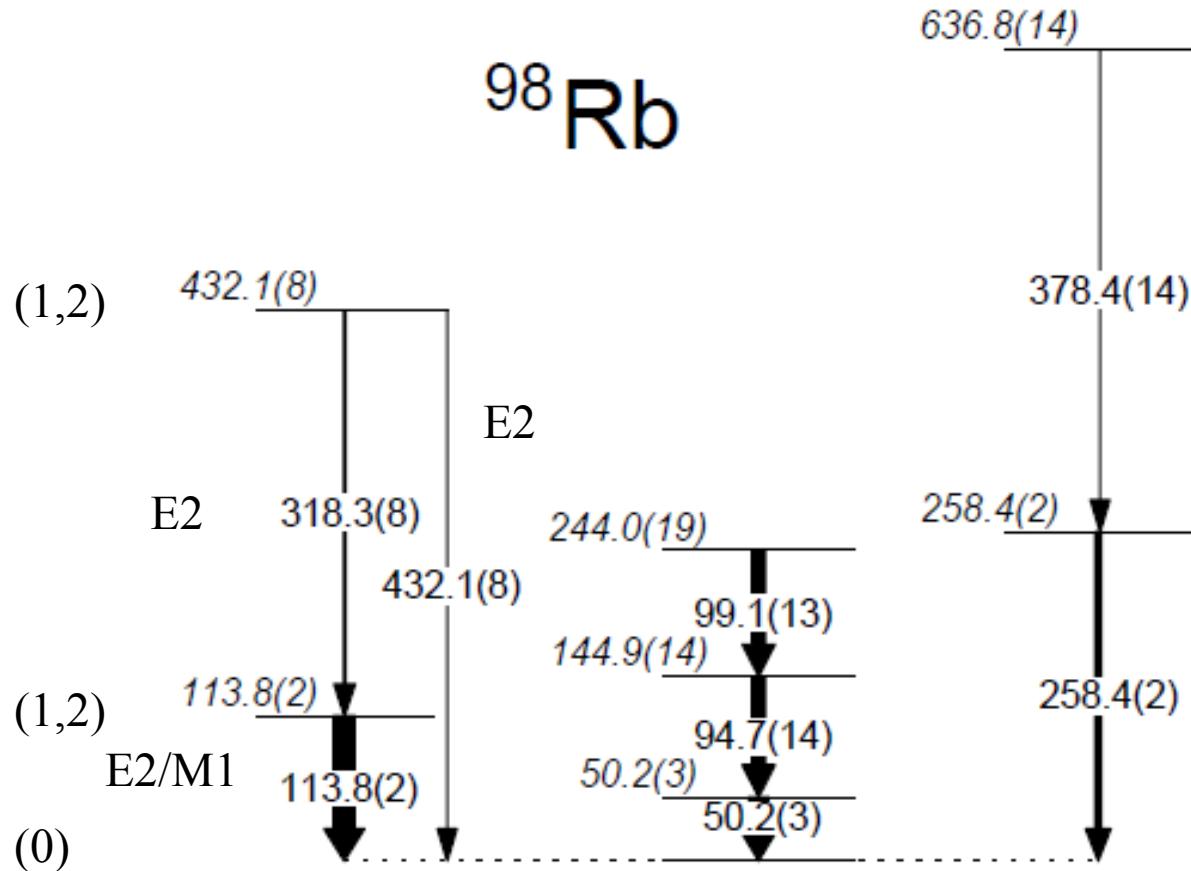


## Davydov-Filippov model



# Experimental results 3/3





$^{96}\text{Sr}$ 

| $I_1^\pi$              | $I_2^\pi$ | B( $E2, I_1 \rightarrow I_2$ ) (W.u.) |              |                |
|------------------------|-----------|---------------------------------------|--------------|----------------|
|                        |           | experiment                            | 5DCH (Gogny) | Excited VAMPIR |
| $2_1^+$                | $0_1^+$   | $17.3_{-3.2}^{+4.0}$                  | 32           | 30             |
| $4_1^+$                | $2_1^+$   |                                       | 63           | 68             |
| $0_2^+$                | $2_1^+$   | 15.3(16) [10]                         | 58           | 83             |
| $0_3^+$                | $2_1^+$   | 0.028(11) [11]                        |              |                |
| $2_2^+$                | $2_1^+$   | > 8.9 [10]                            | 62           | 65             |
| $4_1^+$                | $2_2^+$   |                                       | 13           | 7              |
| $4_2^+$                | $2_2^+$   |                                       | 57           | 73             |
| $4_2^+$                | $4_1^+$   |                                       | 49           | 47             |
| $\rho^2(E0) (10^{-3})$ |           |                                       |              |                |
| $0_2^+$                | $0_1^+$   |                                       | 106          | 66             |
| $0_3^+$                | $0_1^+$   |                                       | 22           |                |
| $0_3^+$                | $0_2^+$   | 185(50)[13]                           | 95           | 9              |

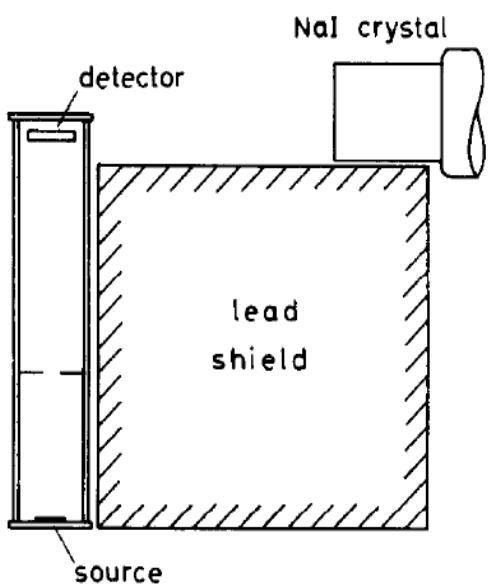
 $^{98}\text{Sr}$ 

| $I_1^\pi$              | $I_2^\pi$ | B( $E2, I_1 \rightarrow I_2$ ) (W.u.) |              |                  |
|------------------------|-----------|---------------------------------------|--------------|------------------|
|                        |           | experiment                            | 5DCH (Gogny) | 5DCH (PC-PK1)    |
| $2_1^+$                | $0_1^+$   | 96 (3)                                | 54           | 73.5             |
| $4_1^+$                | $2_1^+$   | $129_{-7}^{+8}$                       | 110          | 162              |
| $6_1^+$                | $4_1^+$   | $175_{-14}^{+17}$                     | 150          | 196              |
| $8_1^+$                | $6_1^+$   | $123_{-14}^{+19}$                     | 173          | 211              |
| $2_2^+$                | $0_2^+$   | 13 (2)                                | 28           | 39.2             |
| $0_2^+$                | $2_1^+$   | 61 (5)                                | 120          | 195 <sup>a</sup> |
| $2_2^+$                | $0_1^+$   | 0.77 (13)                             | 0.07         |                  |
| $2_2^+$                | $2_1^+$   | $0.61_{-0.30}^{+0.22}$                | 0.78         |                  |
| $2_2^+$                | $4_1^+$   | $4_{-2}^{+4}$                         | 19.4         |                  |
| $\rho^2(E0) (10^{-3})$ |           |                                       |              |                  |
| $0_2^+$                | $0_1^+$   | 53(5)[21]                             | 179          | 117              |
| $0_3^+$                | $0_1^+$   |                                       | 40           |                  |
| $0_3^+$                | $0_2^+$   |                                       | 75           |                  |

| $^{96}\text{Sr}, \rho^2(E0) (10^{-3})$ |         |         |         |         |         |         |         |
|--|---------|---------|---------|---------|---------|---------|---------|
| $0_1^+$                                | $0_2^+$ | $2_1^+$ | $2_2^+$ | $4_1^+$ | $4_2^+$ | $6_1^+$ | $6_2^+$ |
| $0_2^+$                                | 106     | -       | $2_2^+$ | 28      | -       | $4_2^+$ | 83      |
| $0_3^+$                                | 22      | 95      | $2_3^+$ | 117     | 65      | $4_3^+$ | 113     |
|  |         |         |         |         |         | $6_3^+$ | 89      |
|  |         |         |         |         |         | $6_3^+$ | 32      |
| $^{98}\text{Sr}, \rho^2(E0) (10^{-3})$ |         |         |         |         |         |         |         |
| $0_1^+$                                | $0_2^+$ | $2_1^+$ | $2_2^+$ | $4_1^+$ | $4_2^+$ | $6_1^+$ | $6_2^+$ |
| $0_2^+$                                | 179     | -       | $2_2^+$ | 81      | -       | $4_2^+$ | 43      |
| $0_3^+$                                | 40      | 75      | $2_3^+$ | 120     | 1       | $4_3^+$ | 0       |
|  |         |         |         |         |         | $6_3^+$ | 27      |
|  |         |         |         |         |         | $8_3^+$ | 2       |
|  |         |         |         |         |         | $8_3^+$ | 32      |

# Shape Transition at N=60

It has been established in the 60's that elements with  $A \sim 110$  belong to a new island of stable deformation similar to the rare earth region



S. A. E. Johansson, Nucl. Phys. **64** (1965) 147

