

Exploring Nuclear Shell Evolution with Nucleon Transfer Reactions

W.N. Catford¹, A. Matta¹, N.A. Orr², A.J. Knapton¹, I.C. Celik¹, G.L. Wilson¹, G. Lotay¹, B. Fernández Domínguez³, C. Aa. Diget⁴, G. Hackman⁵

and the TIARA and SHARC/TIGRESS collaborations

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WILTON CATFORD

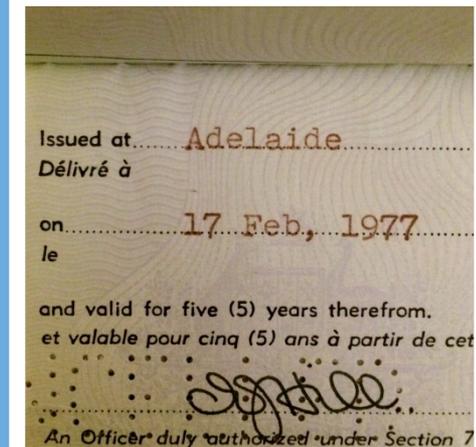
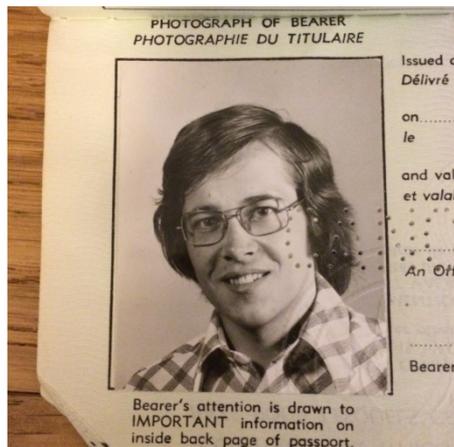
University of Surrey, UK

Experiments performed at TRIUMF
and at Texas A&M University, USA

Exploring Nuclear Shell Evolution with Nucleon Transfer Reactions

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Adelaide, 1977

WILTON CATFORD

University of Surrey, UK

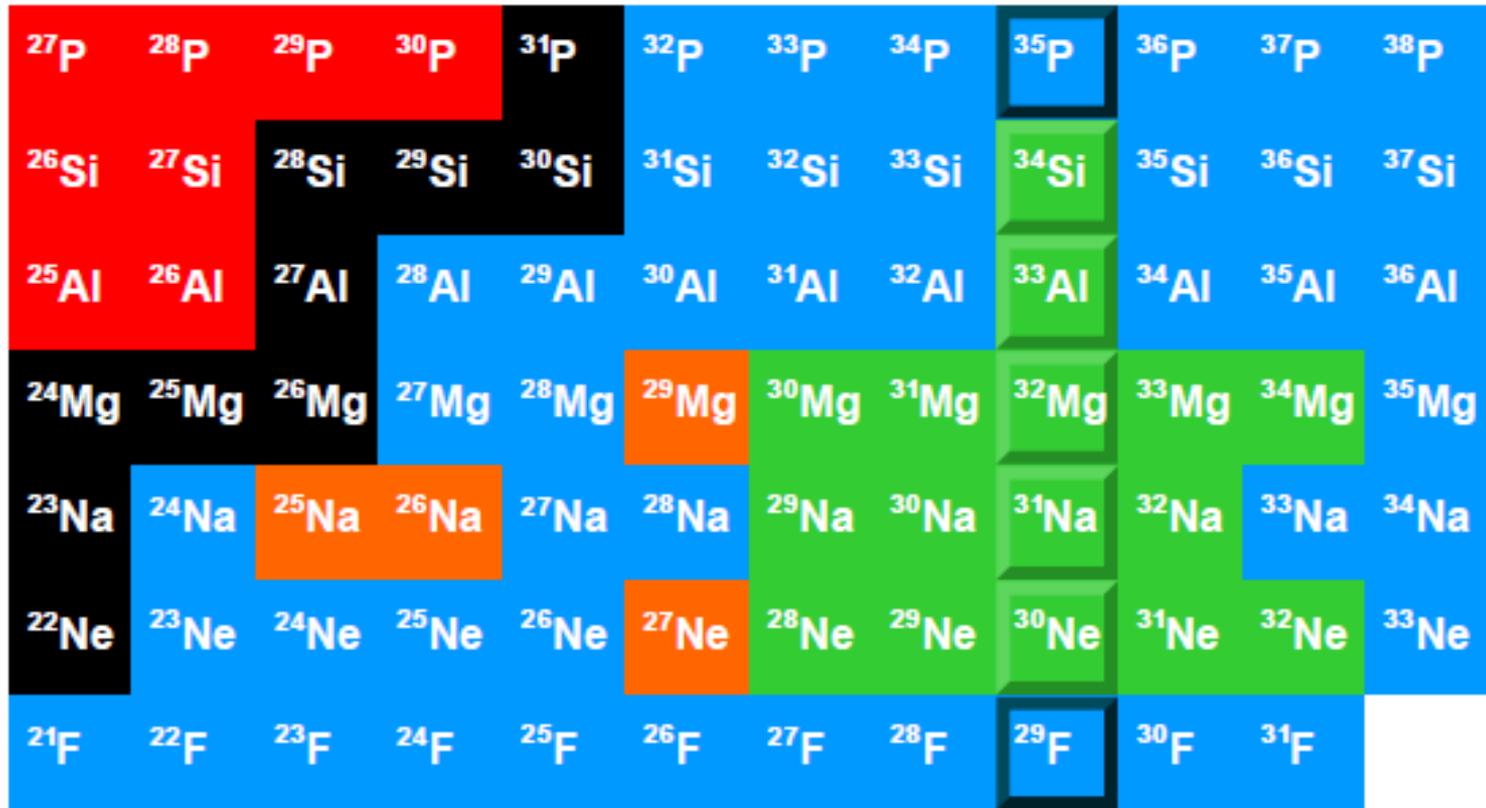
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EXPLORING SHELL EVOLUTION

with nucleon transfer reactions
specifically, via $(d,p\gamma)$ neutron transfer

- (a) motivation: changing shell structure
- (b) experiments: SHARC + TIGRESS + trifoil
- (c) update on recent PLB $^{25}\text{Na},p\gamma)^{26}\text{Na}$
- (d) new results from $d(^{24}\text{Na},p\gamma)^{25}\text{Na}$
- (e) new results from $d(^{28}\text{Mg},p\gamma)^{29}\text{Mg}$
- (f) perspectives: T-Rex at Texas A&M

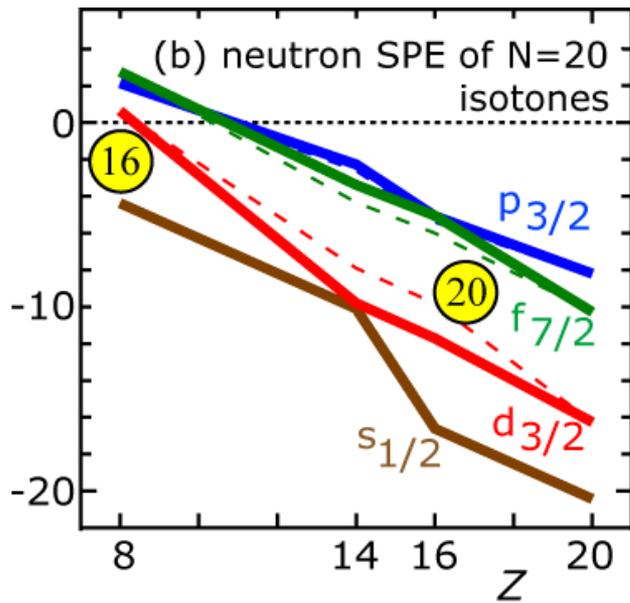
Region of Interest – Approaching the Island of Inversion



orange – nuclei studied
by us, using (d,p)

green – (a) N=20,
(b) island of inversion
(intruder structure dominates
ground state structure)

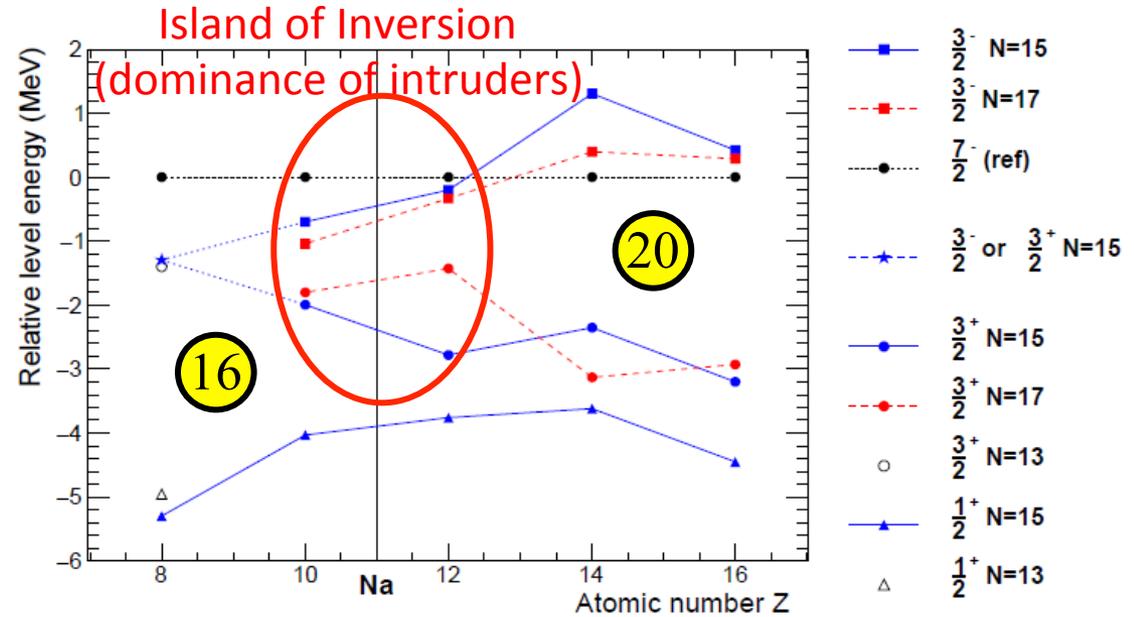
Theory: effective spe's



PRL 104, 012501 (2010)

Otsuka et al.

Experiment: energies of just the lowest levels



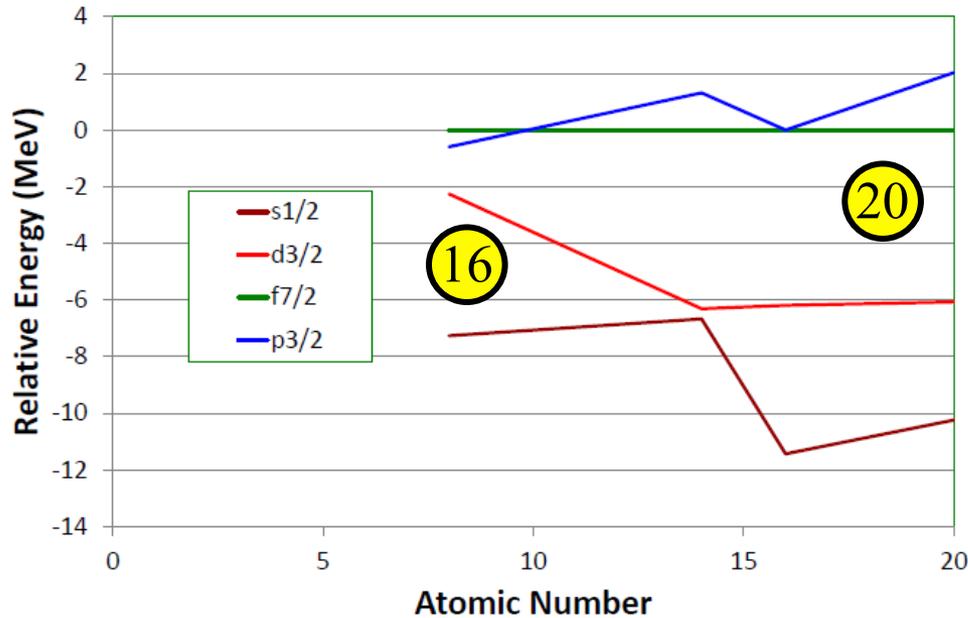
PLB (2016)

N=15 and 17 isotones

<http://dx.doi.org/10.1016/j.physletb.2016.05.093>

G.L. Wilson et al.

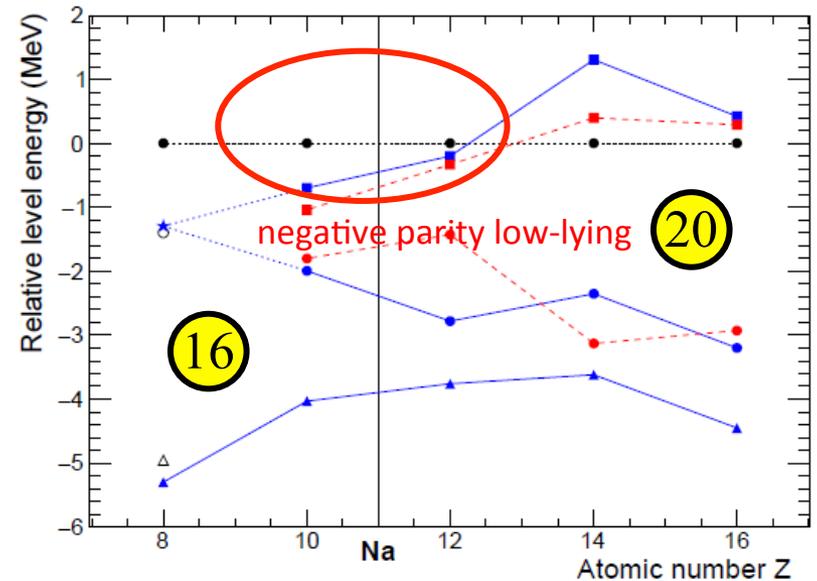
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N=15 and 17 isotones

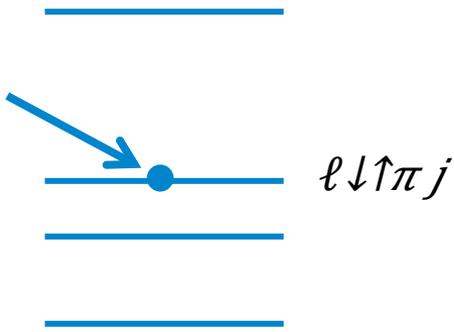
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G.L. Wilson et al.

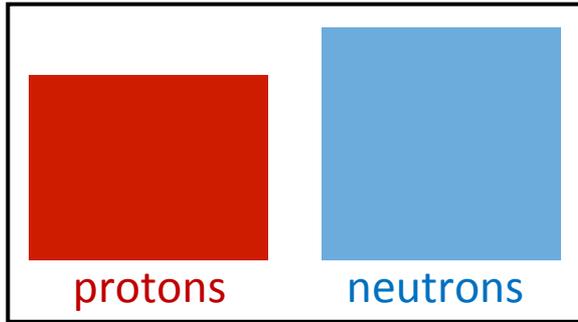
- Our aim is to identify single-particle-like levels and determine their spin/parity
- We use the selective nature of (d,p) neutron transfer (with radioactive beams)
- We aim to track the evolution of these levels and compare to the shell model

(d,p) adds a neutron

$J\uparrow\pi$

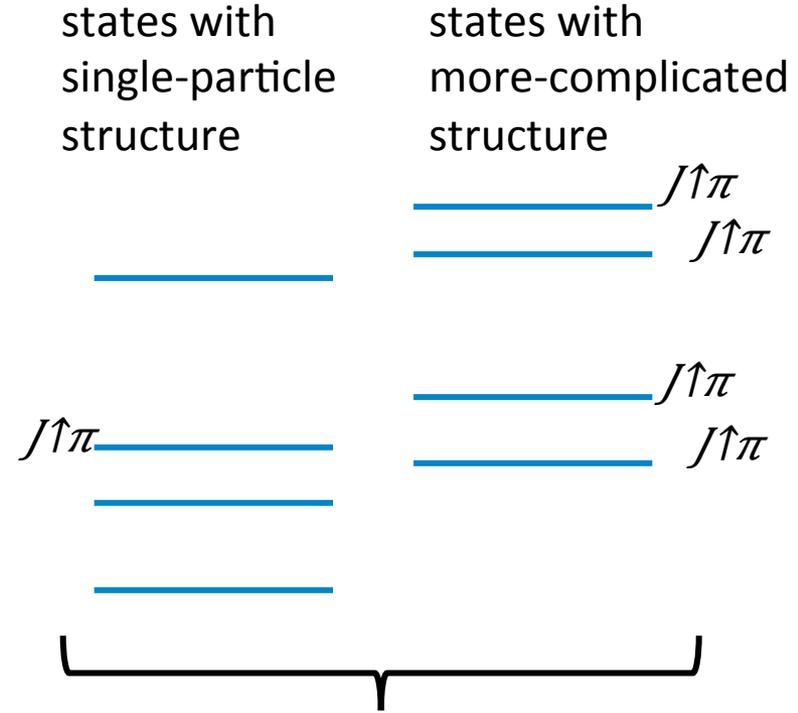


$l\downarrow\uparrow\pi j$



single-particle state,
unperturbed core
(idealized situation)

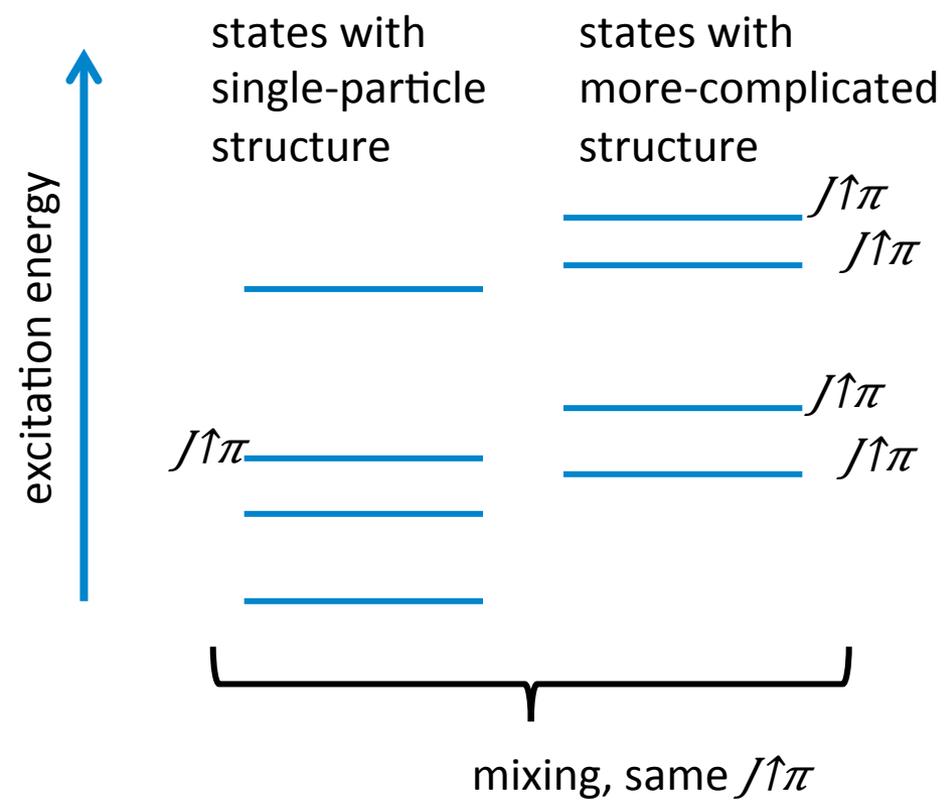
excitation energy ↑



$$|J\downarrow i\uparrow\pi\rangle = \sqrt{S} |J\downarrow SP\uparrow\pi\rangle + \sum_k \alpha_k |J\downarrow k\uparrow\pi\rangle$$

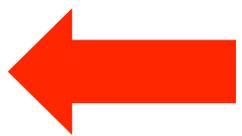
$$S = |\langle J\downarrow SP\uparrow\pi | J\downarrow i\uparrow\pi \rangle|^2$$

spectroscopic factor
= overlap with pure SP state



$$|J \downarrow i \uparrow \pi\rangle = \sqrt{S} |J \downarrow SP \uparrow \pi\rangle + \sum_k \alpha_k |J \downarrow k \uparrow \pi\rangle$$

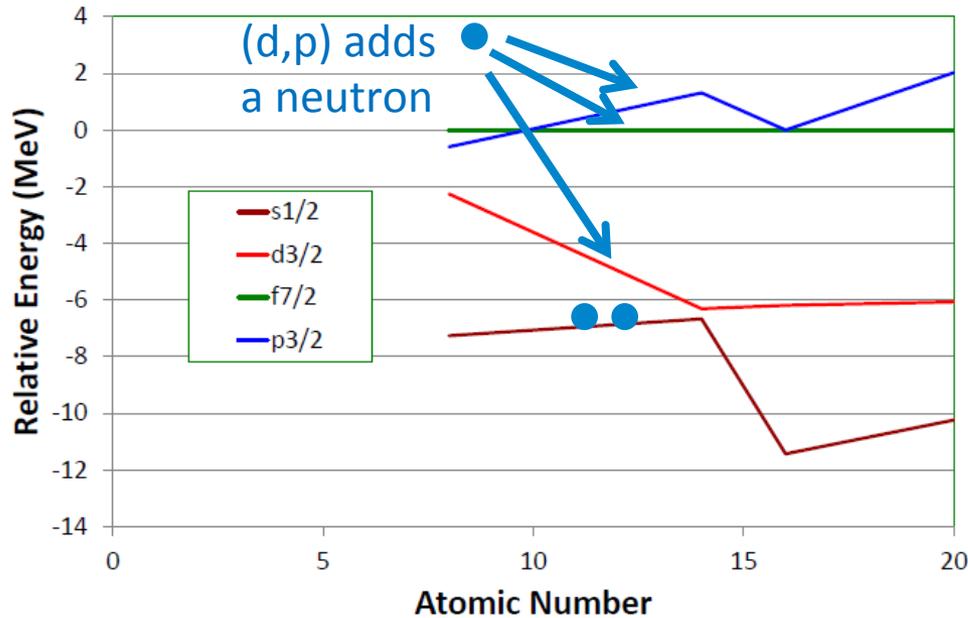
- we measure transferred $\ell \downarrow n$
- we measure gamma-decays
- we aim to identify J and π
- we deduce S



$$S = | \langle J \downarrow SP \uparrow \pi | J \downarrow i \uparrow \pi \rangle |^2$$

spectroscopic factor
= overlap with pure SP state

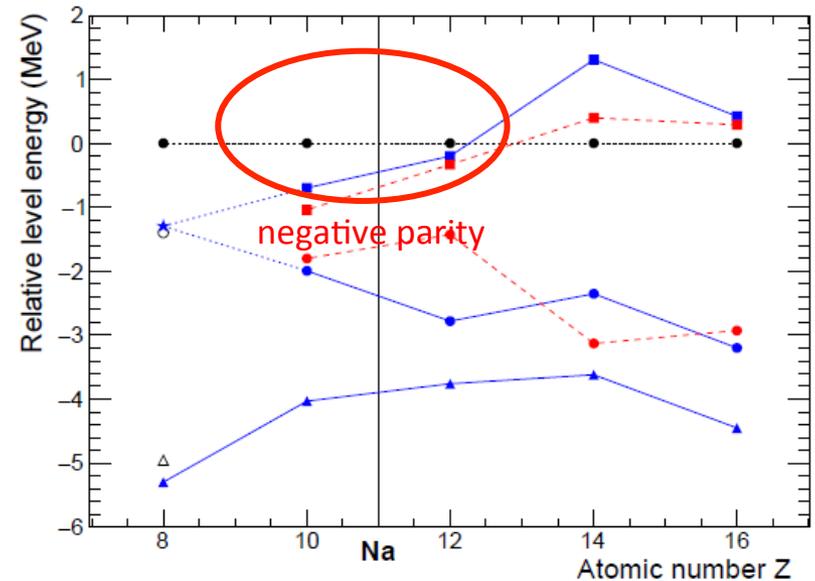
Theory: effective spe's



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Experiment: energies of just the lowest levels



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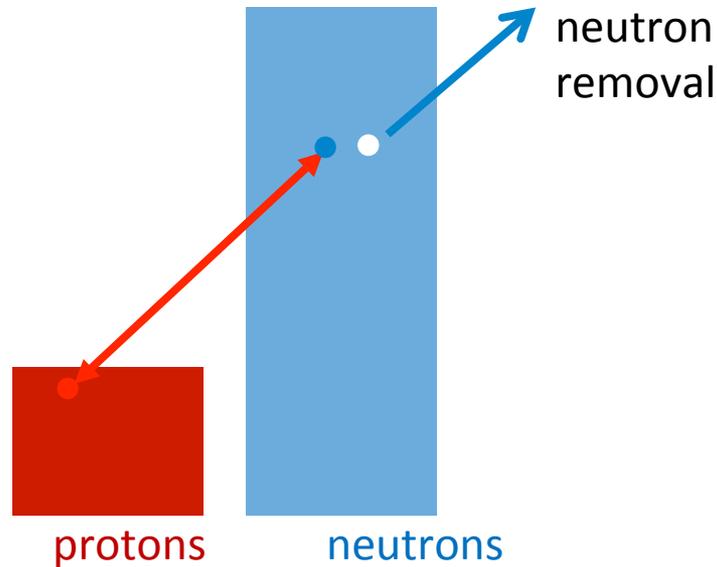
N=15 and 17 isotones

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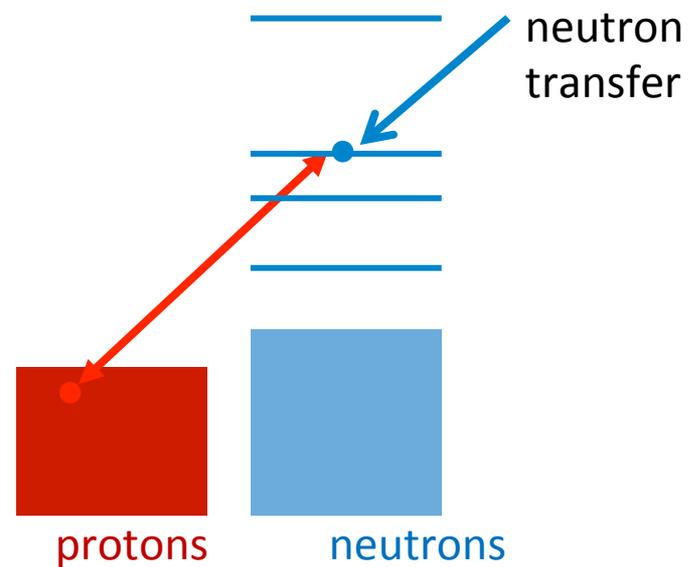
G.L. Wilson et al.

- Our aim is to identify single-particle-like levels and determine their spin/parity
- We use the selective nature of (d,p) neutron transfer (with radioactive beams)
- We aim to track the evolution of these levels and compare to the shell model
- We use the large SF for theory/experimental states to associate them with each other
- Details of the precise numerical value of the SF don't affect this process
- Results will be shown here for Z=11,12 for N=14,15,17, **probing higher orbitals**

KNOCKOUT



WHY TRANSFER IS SUCH A GOOD CHOICE

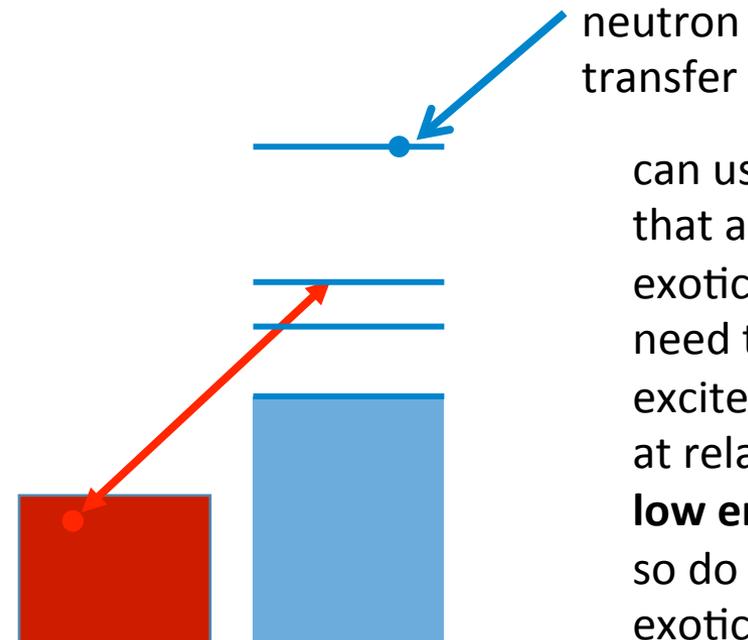


can make beams of VERY exotic nuclei
and learn properties by removing neutrons

OR

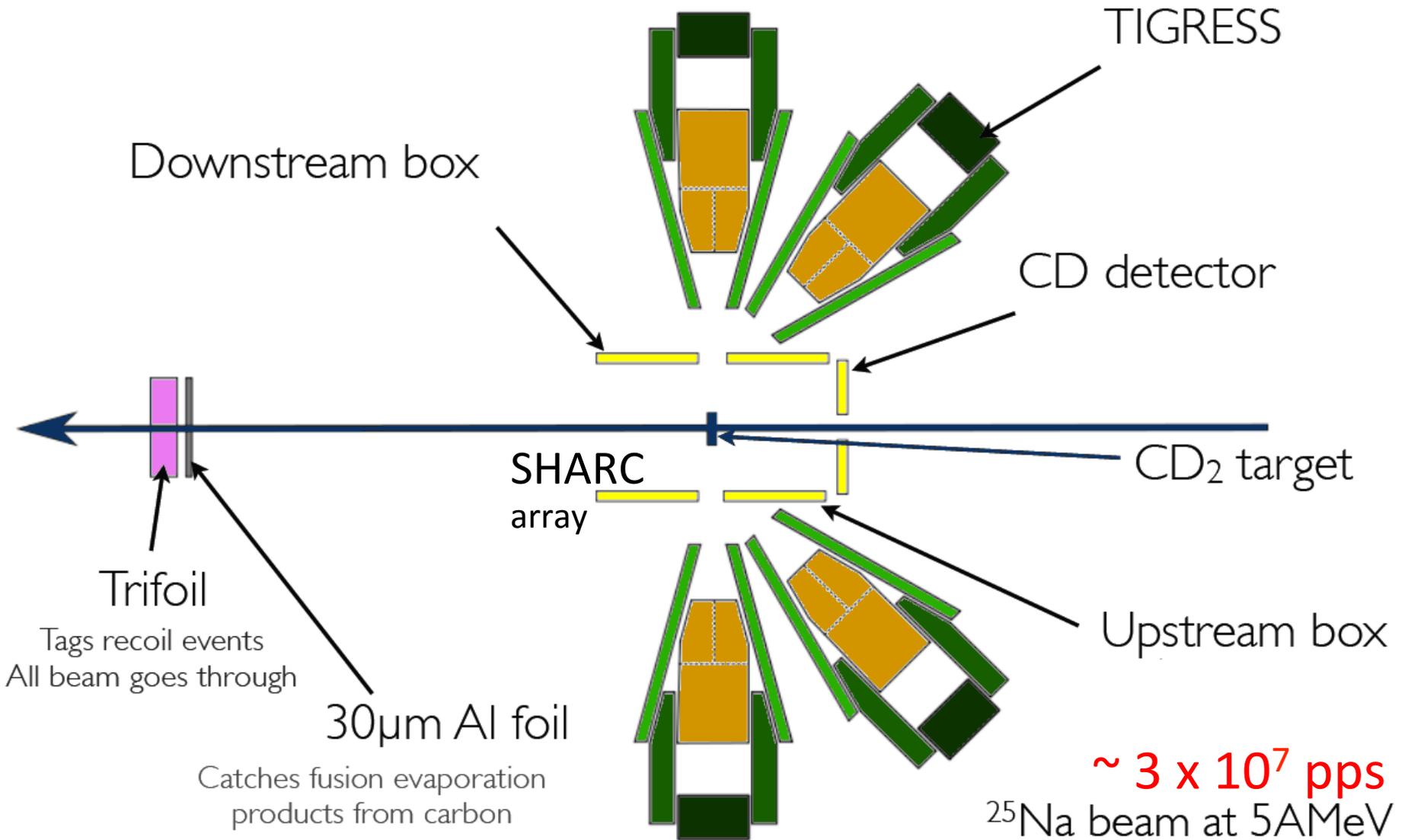
can learn the important interactions that
explain the structure by isolating p-n
interactions, using a **single nucleon** to probe
the additional orbitals one at a time

thus **transfer** is an excellent way to isolate the
separate interactions



can use beams
that are less
exotic, but do
need to keep
excited states
at relatively
low energies,
so do need
exotic beams

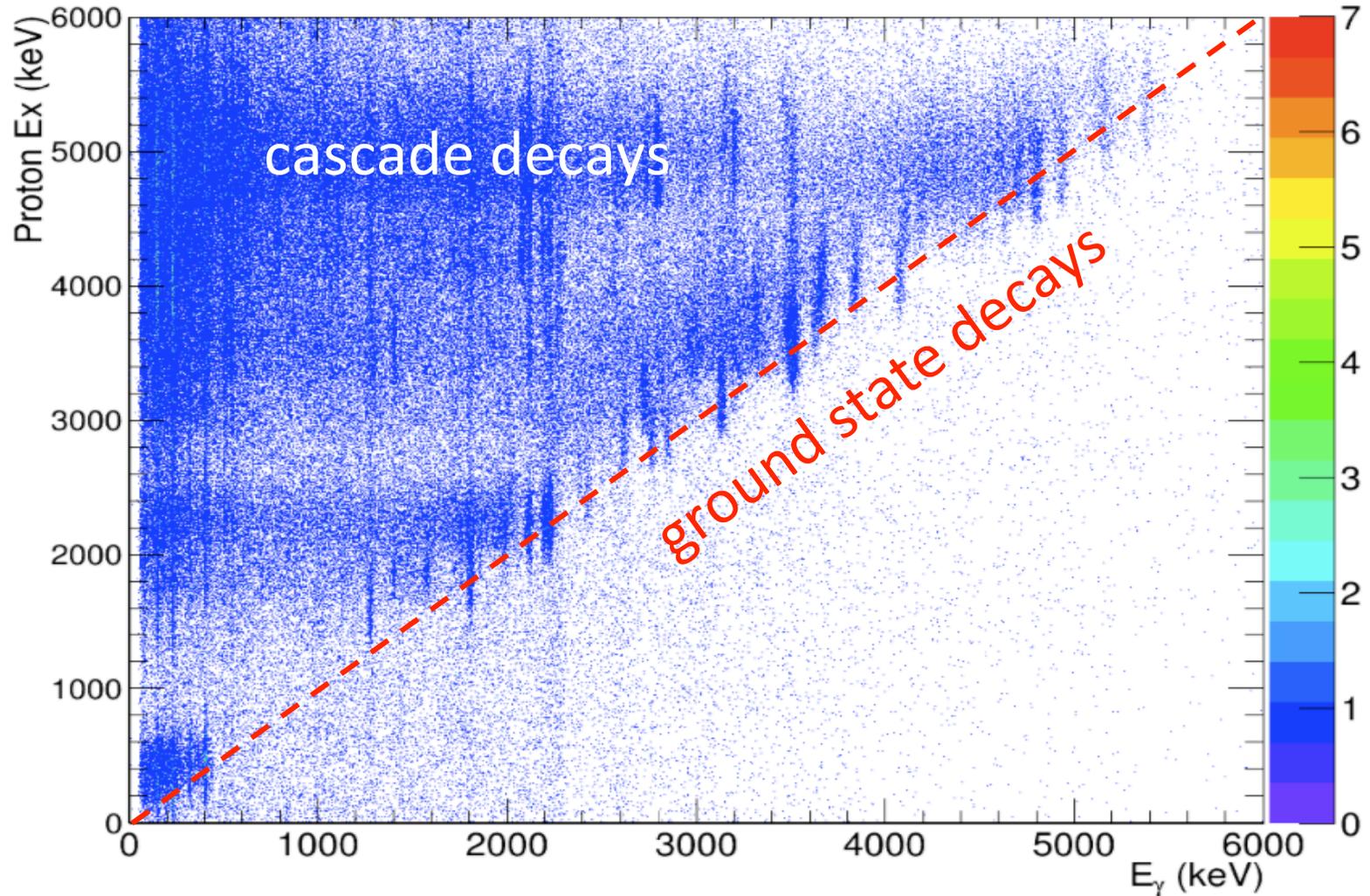
Experimental Setup to Measure $d(^{25}\text{Na},p)^{26}\text{Na}$ at TRIUMF



Data from $d(^{25}\text{Na},p)^{26}\text{Na}$ at 5 MeV/A using SHARC at ISAC2 at TRIUMF

Gemma Wilson, Surrey

Excitation energy deduced from proton energy and angle



Doppler corrected ($\beta=0.10$) gamma ray energy measured in TIGRESS

Experimental Results from studying $d(^{25}\text{Na},p)^{26}\text{Na}$ at TRIUMF

Negative parity states

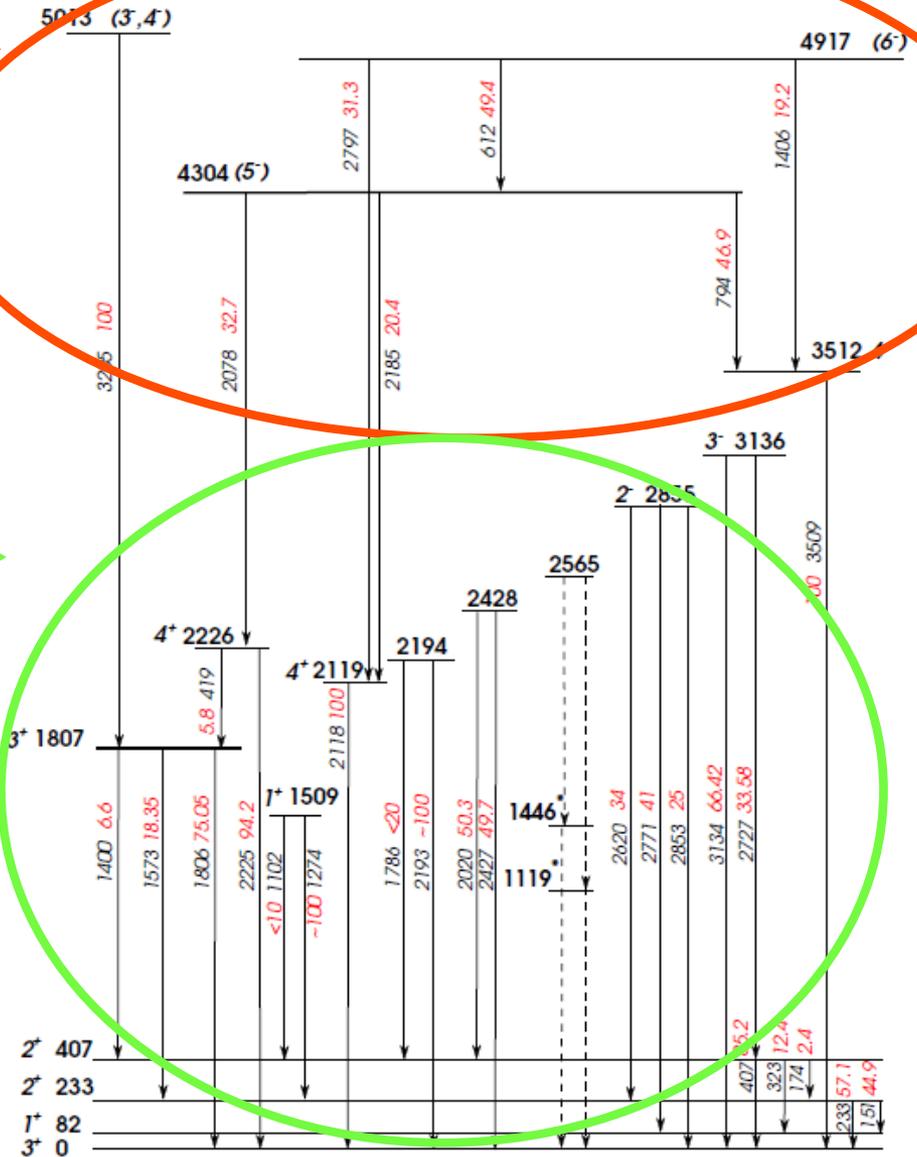
Levels never seen before,
selected by (d,p)

Gamma-ray decay scheme
Gamma-ray branching ratios

Positive parity states

GATE on the gamma rays,
take advantage of 30 keV
energy resolution

CHECK that this does not
bias the proton distribution
(*gamma angular efficiency*)

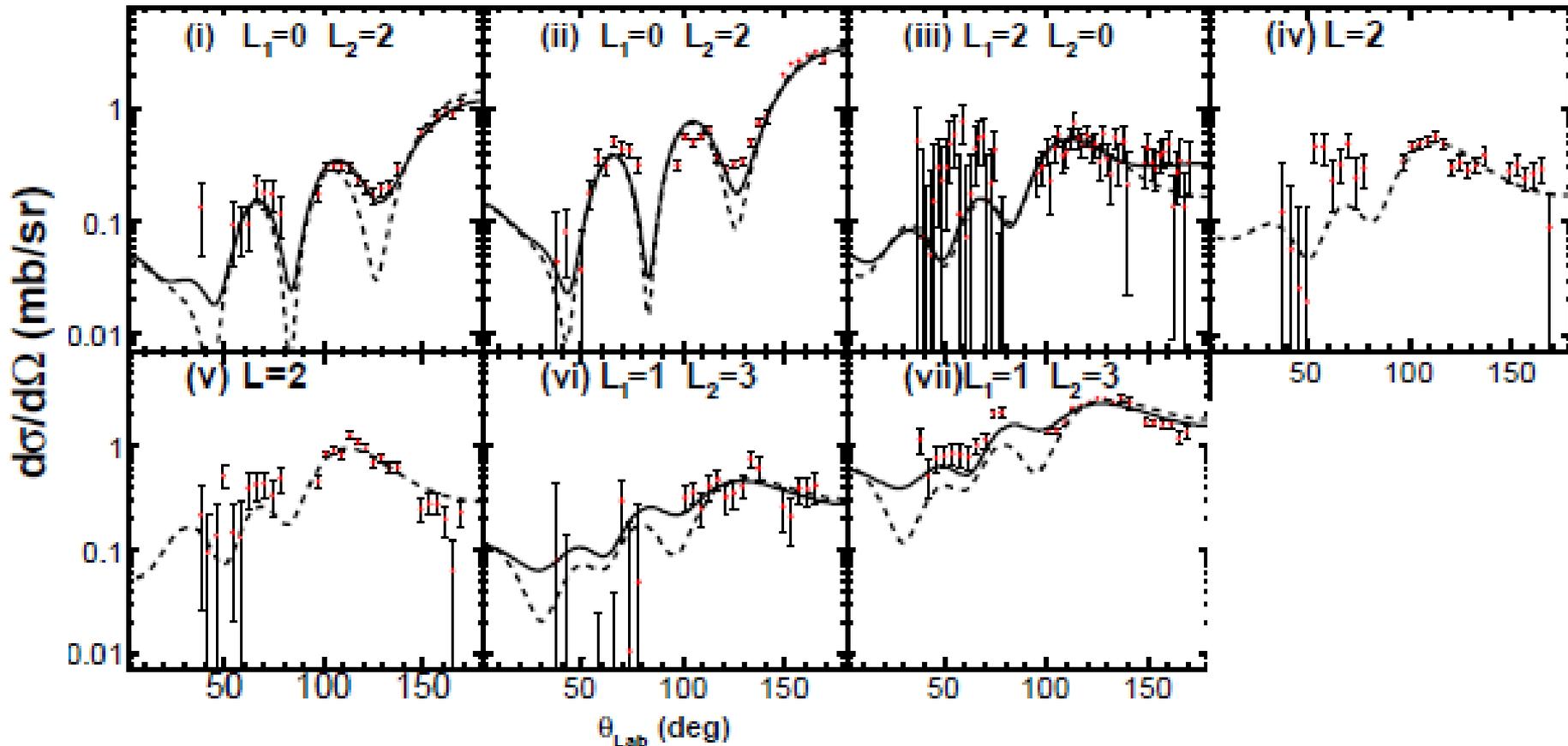


Differential cross sections and spectroscopic factors

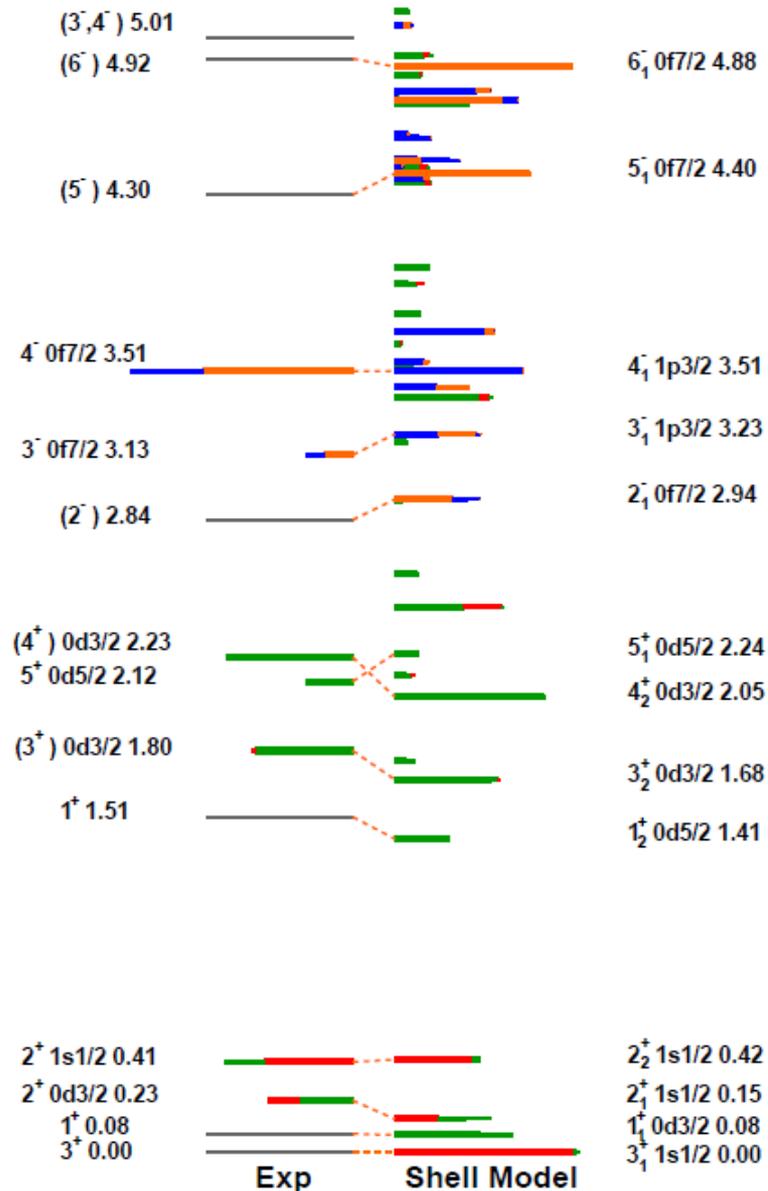
First analysis of this type:

Each of these distributions is:

- (a) gated on a gamma-ray peak
- (b) background-subtracted
- (c) corrected for gamma ray efficiency
- (d) corrected for gamma ray branching ratio



Experimental Results from studying $d(^{25}\text{Na},p)^{26}\text{Na}$ at TRIUMF



comparison between revised shell model energies and SFs

the results are somewhat subtle

evidence for stronger influence of the 1p3/2 orbital in the low-lying negative parity states, compared to the less exotic isotone ^{28}Al

this is evidence for the 1p3/2 orbital becoming lower, relative to the 0f7/2 orbital which is clear, in ^{27}Ne and ^{29}Mg

the shell model works surprisingly well
wbc spsdpf 0+1ħω

Experimental Results from studying $d(^{25}\text{Na},p)^{26}\text{Na}$ at TRIUMF

No.	E_x^a	$E_x^{SM\ b}$	$J^\pi\ c)$	J_{SM}^π	single L analysis			two L analysis (where applicable)								
					L	nlj	S	S^{SM}	L_1	$n_1l_1j_1$	S_1	S_1^{SM}	L_2	$n_2l_2j_2$	S_2	S_2^{SM}
	0	0	3^+	3_1^+	*	$1s_{1/2}$		0.61	*	$1s_{1/2}$		0.61	*	$0d_{3/2}$		0.01
														$0d_{5/2}$		0.01
	0.082 ^{d)}	0.077	1^+	1_1^+	*	$0d_{3/2}$		0.29								
						$0d_{5/2}$		0.11								
	0.232	0.149	2^+	2_1^+	0	$1s_{1/2}$	0.13	0.15	0	$1s_{1/2}$	0.10	0.15	2	$0d_{3/2}$	0.19†	0.10
														$0d_{5/2}$		0.09
	0.405	0.416	2^+	2_2^+	0	$1s_{1/2}$	0.33	0.27	0	$1s_{1/2}$	0.30	0.27	2	$0d_{5/2}$	0.13†	0.03
														$0d_{3/2}$		0.03
	1.507	1.409	1^+	1_2^+	2	$0d_{3/2}$	0.39	0.09								
						$0d_{5/2}$		0.10								
	1.805	1.676	(3^+)	3_2^+	2	$0d_{3/2}$	0.37	0.33	2	$0d_{3/2}$	0.33†	0.33	0	$1s_{1/2}$	0.01‡	0.00
						$0d_{5/2}$		0.02	2	$0d_{5/2}$		0.02				
	1.992	1.758	4^+	4_1^+	2	$0d_{3/2}$	0.07	0.07								
	2.116	2.241	5^+	5_1^+	2	$0d_{5/2}$	0.16	0.08								
	2.195	2.142	2^+	2_3^+	2	$0d_{3/2}$	0.49	0.06								
	2.225	2.048	(4^+)	4_2^+	2	$0d_{3/2}$	0.43	0.51								
						$0d_{5/2}$		0.01								
	2.423	2.452	2^+	2_4^+					0	$1s_{1/2}$	0.00	0.13	2	$0d_{3/2}$	0.14	0.23
	2.843	2.936	(2^-)	2_1^-	3	$1p_{3/2}$		0.20	3	$0f_{7/2}$	1.10	0.20	1	$1p_{3/2}$	0.10	0.05
						$0f_{5/2}$		0.00		$0f_{5/2}$		0.00		$1p_{1/2}$		0.04
	3.135	3.228	3^-	3_1^-	1	$1p_{3/2}$	0.07†	0.15	1	$1p_{3/2}$	0.06†	0.15	3	$0f_{7/2}$	0.10‡	0.13
						$1p_{1/2}$		0.02		$1p_{1/2}$		0.02		$0f_{5/2}$		0.00
	3.511	3.513	4^-	4_1^-	1	$1p_{3/2}$	0.30	0.44	1	$1p_{3/2}$	0.25	0.44	3	$0f_{7/2}$	0.51†	0.00
														$0f_{5/2}$		0.00
	4.087	3.690	2^-	2_2^-	3				1	$1p_{3/2}$	0.34	0.31	3	$0f_{7/2}$	0.78	0.03
	4.239	3.975	4^+	4_5^+	2	$0d_{3/2}$	0.12	0.12								
	4.305	4.401	(5^-)	5_1^-	3				1	$1p_{3/2}$	0.01	0.00	3	$0f_{7/2}$	0.25	0.46
	4.597	4.460	3^-	3_2^-	3	$0f_{7/2}$			1	$1p_{3/2}$	0.02	0.10	3	$0f_{7/2}$	0.76	0.10
	4.800	4.730	4^-	4_2^-	3	$0f_{7/2}$			1	$1p_{3/2}$	0.00	0.05	3	$0f_{7/2}$	0.62	0.37
	4.917	4.881	(6^-)	6_1^-	3	$0f_{7/2}$	0.51	0.61								
	4.932	4.770	3^-	3_4^-	3	$0f_{7/2}$			1	$1p_{3/2}$	0.00	0.28	3	$0f_{7/2}$	0.63	0.05
	5.009		$(3^-, 4^-)$		*											

UPDATE

8 new states

plus

4 new ℓ values

IMPROVED

background

subtraction

NEW

gamma-ray

angular

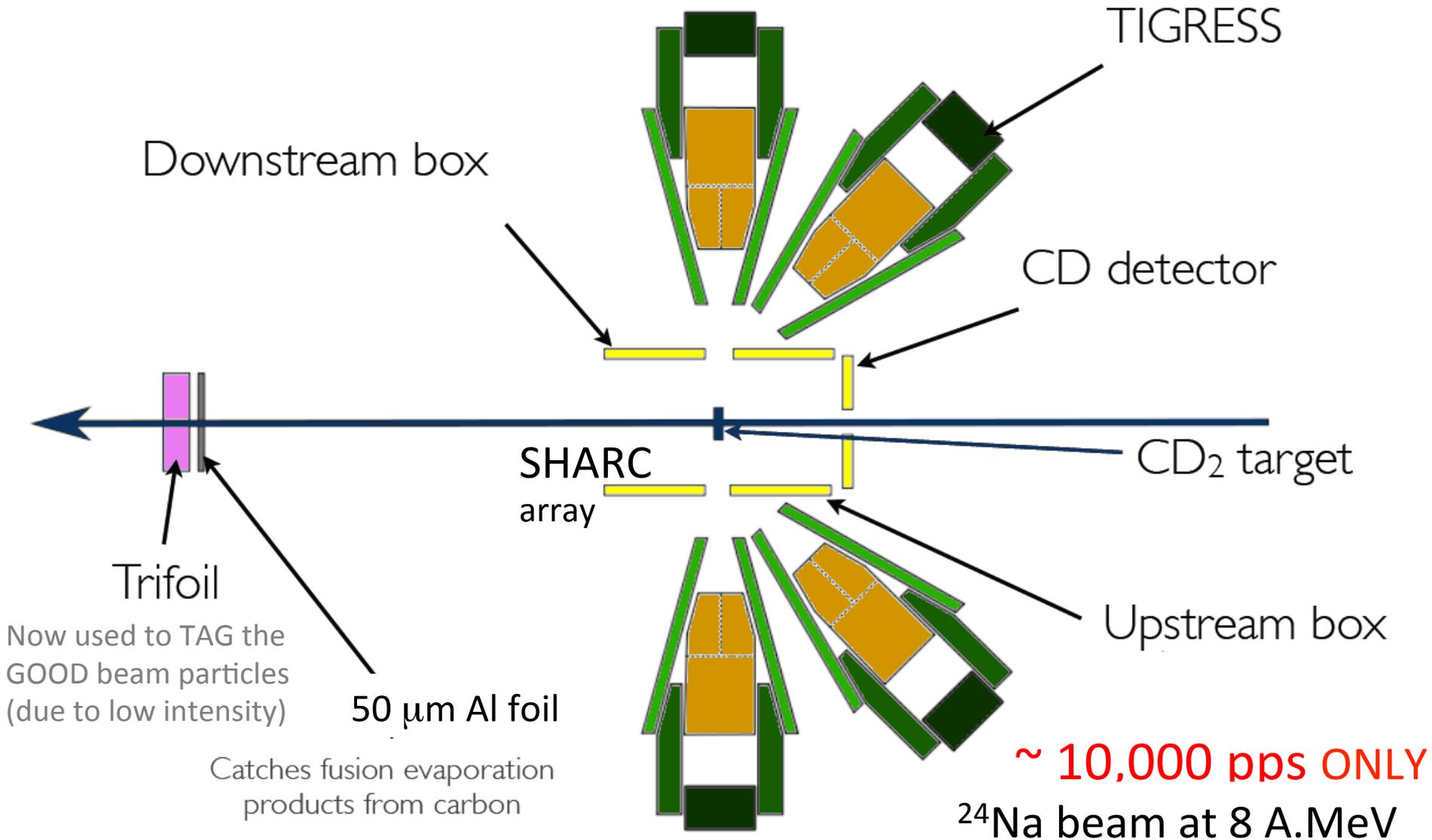
correlations

I.C. Celik

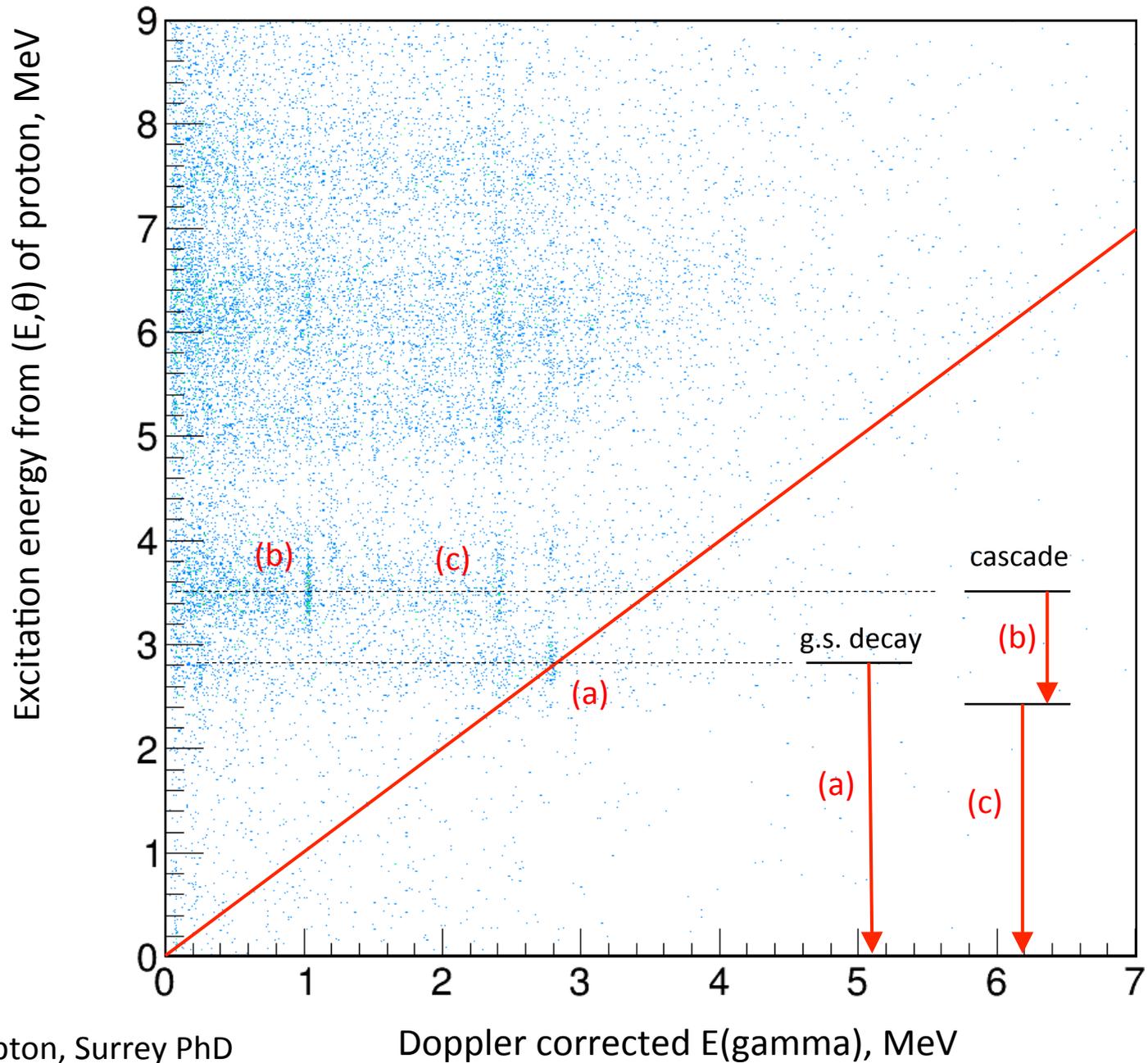
PhD thesis

Surrey 2015

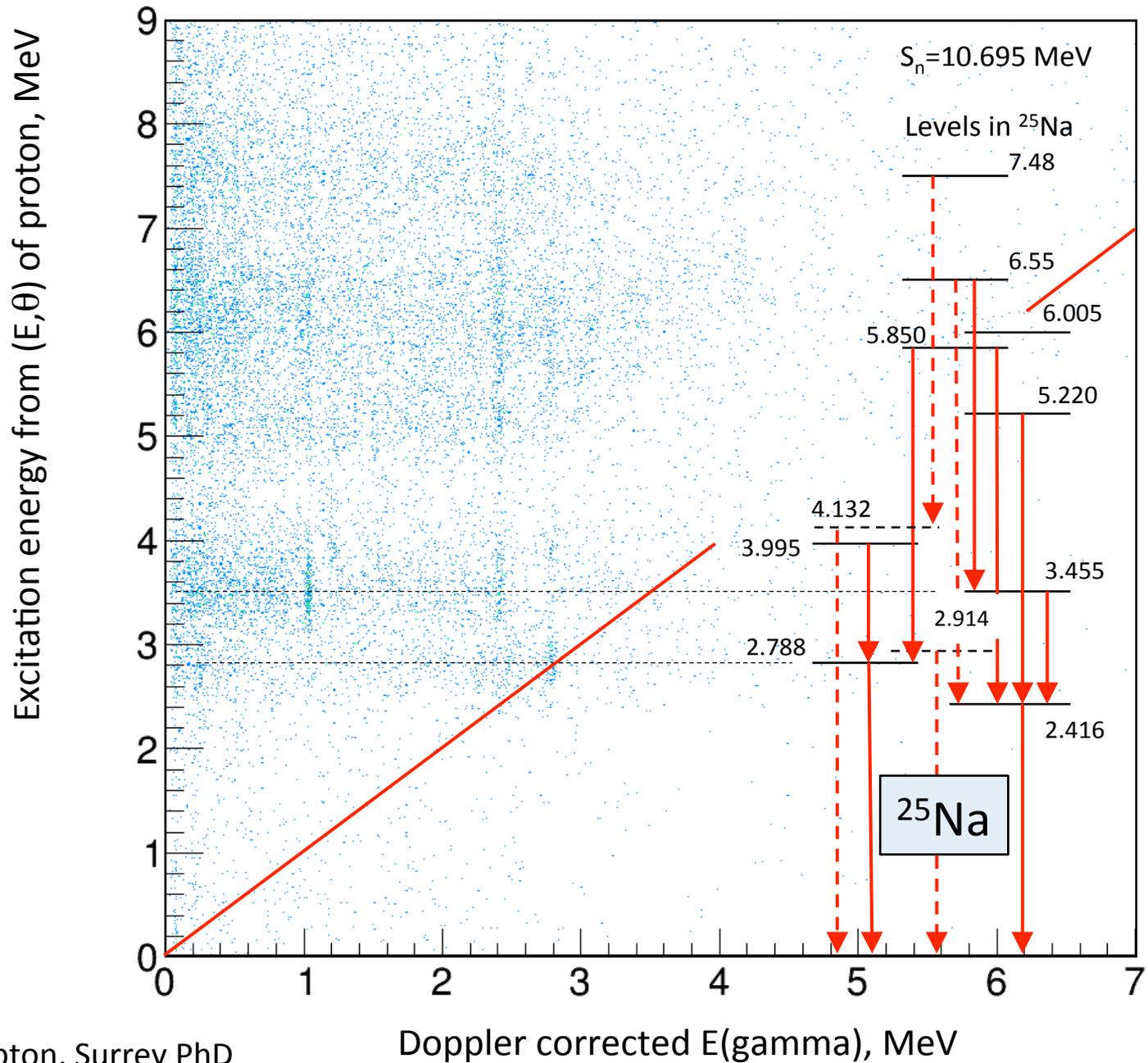
Experimental Setup to Measure $d(^{24}\text{Na},p)^{25}\text{Na}$ at TRIUMF



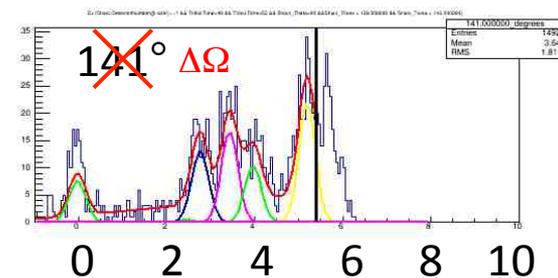
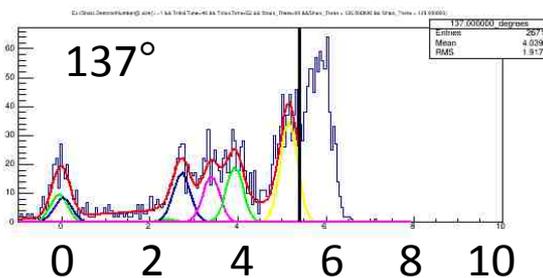
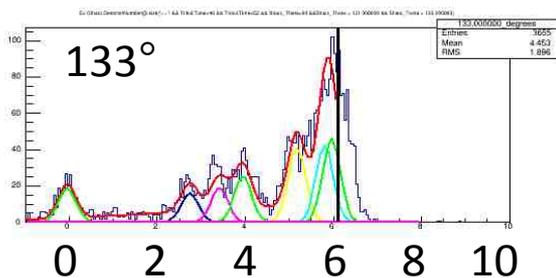
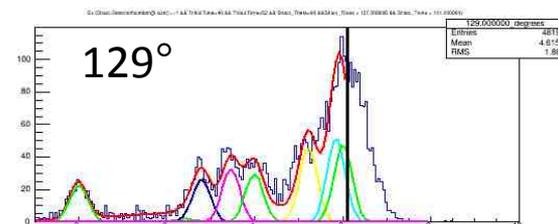
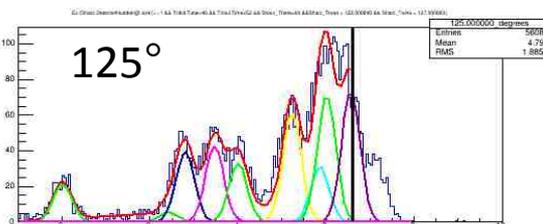
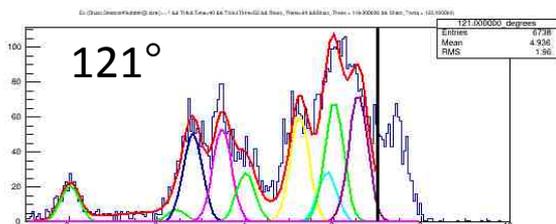
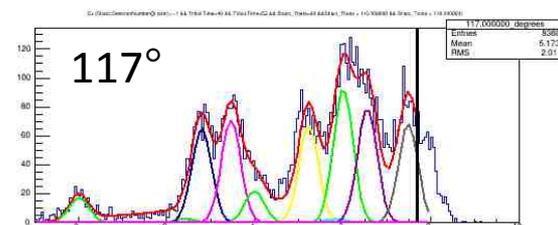
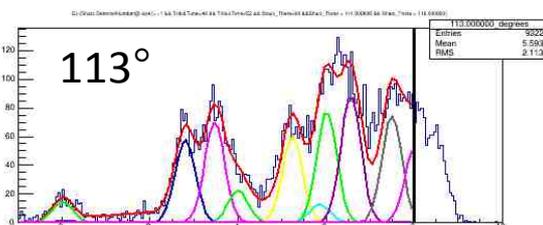
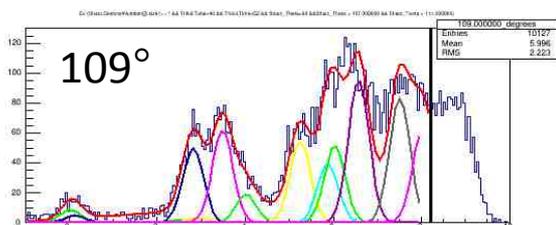
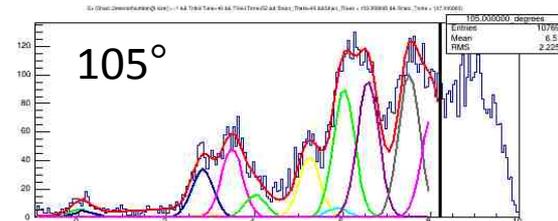
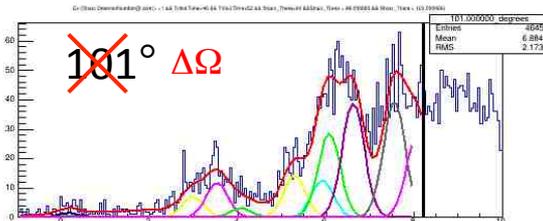
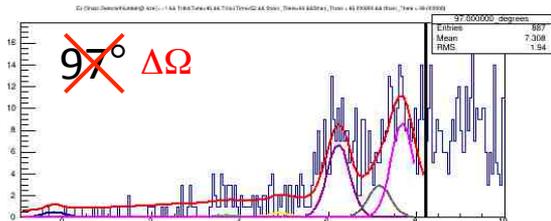
$d(^{24}\text{Na}, p)^{25}\text{Na}$ at 8.0 MeV/u with 10,000 pps



$d(^{24}\text{Na},p)^{25}\text{Na}$ at 8.0 MeV/u with 10,000 pps



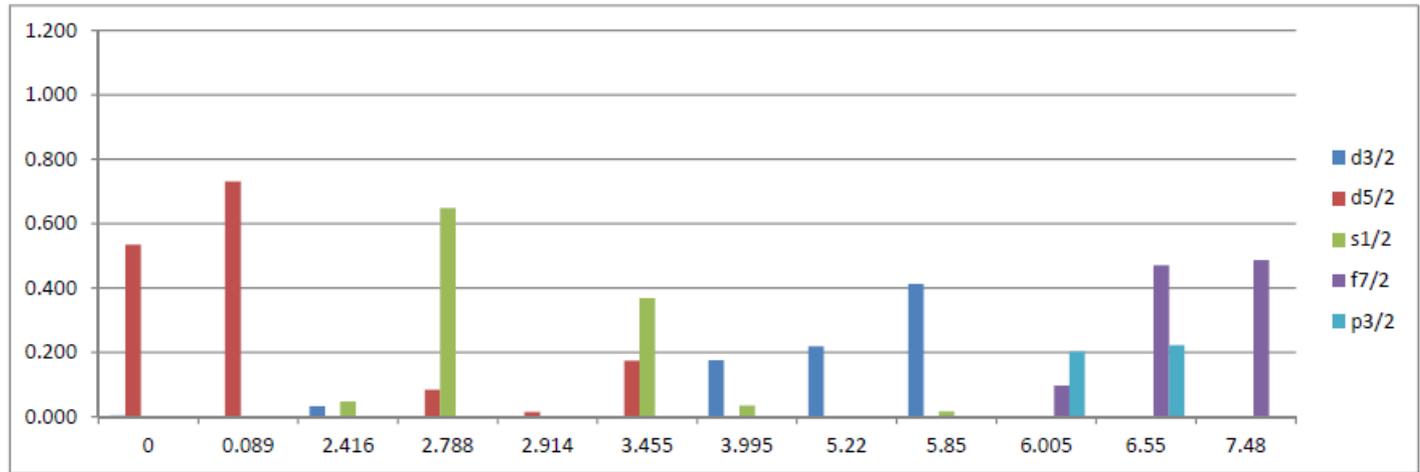
$d(^{24}\text{Na}, p)^{25}\text{Na}$ – fits to excitation energy spectrum at each angle



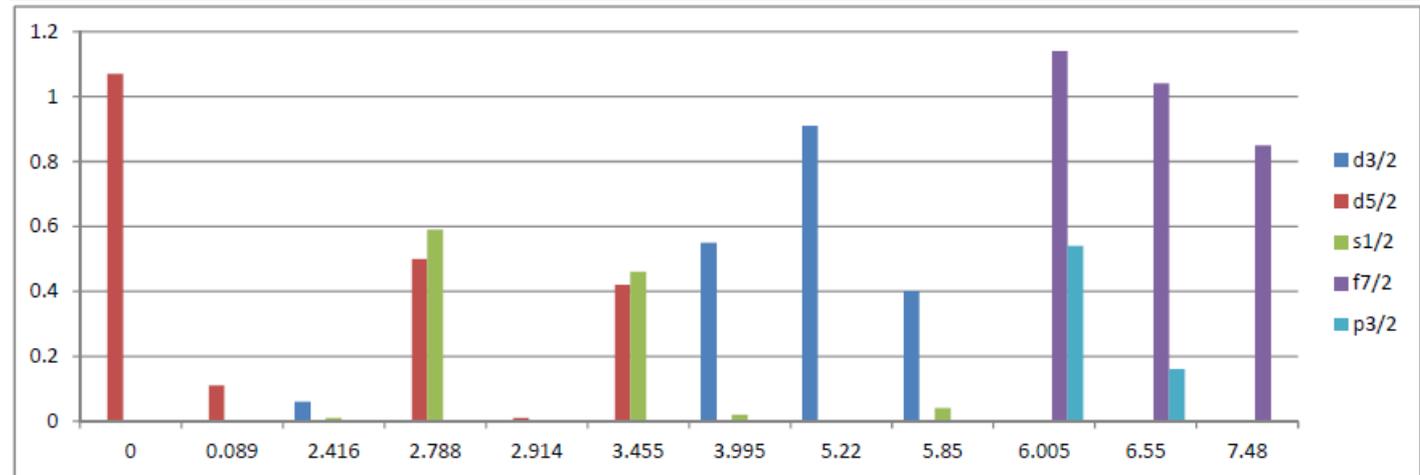
Excitation Energy in ^{25}Na (MeV)

$d(^{24}\text{Na},p)^{25}\text{Na}$ – spectroscopic factors in ^{25}Na compared to theory

wbc
nushellx
(0+1) $\hbar\omega$



this work
ADWA
std geom

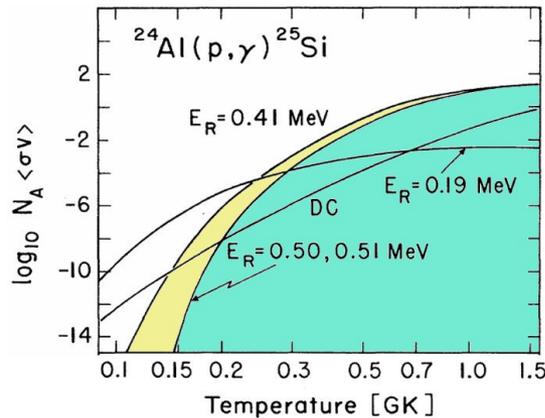


Excitation Energy in ^{25}Na (MeV)

present work	5/2+	3/2+	9/2+	7/2+	5/2+	9/2+	9/2+	11/2+	7/2+	7/2-	11/2-	13/2-
literature	5/2+	3/2+	?	3/2	5/2+	3/2+?	1/2-	?	?	(1/2, 3/2)-	?	?

BIG IMPROVEMENTS IN LEVEL IDENTIFICATIONS

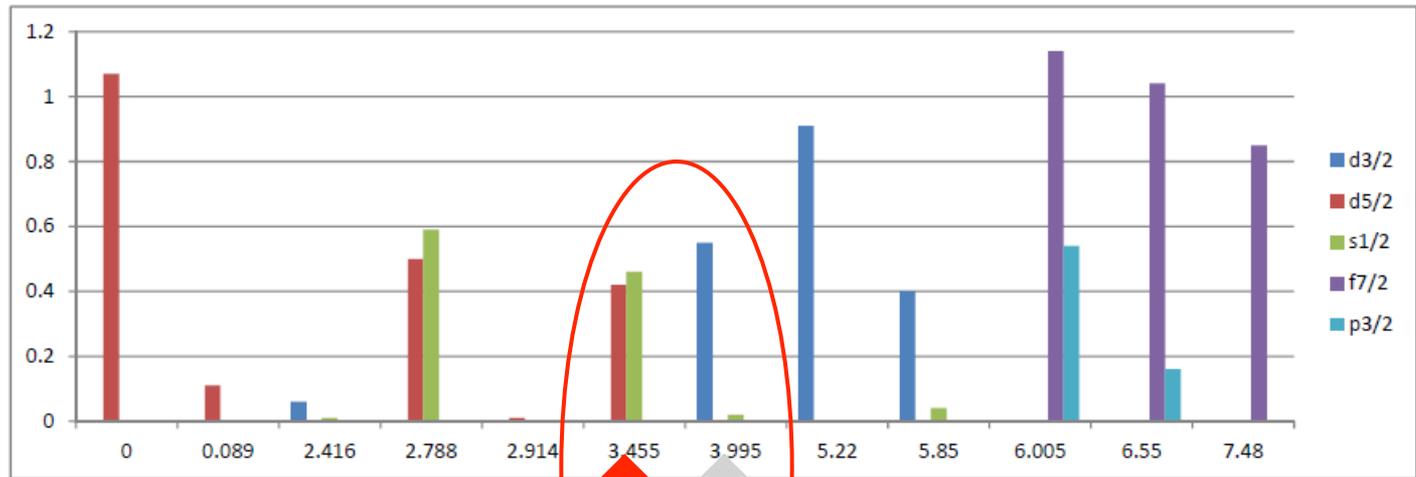
Using the ^{25}Na SFs to calculate $^{24}\text{Al}(p,\gamma)^{25}\text{Si}$ widths and $\omega\gamma$'s for novae



Wiescher, Brown PRC52, 1078 (1995)
revised the rate for $^{24}\text{Al}(p,\gamma)$ upwards $\times 100$

\longrightarrow 0.41 = 3.995 in ^{25}Na
resonance states in ^{25}Si
↖
 \longrightarrow 0.02 = 3.455 in ^{25}Na
 (not considered important before,
 due to misidentification)

this work
ADWA
std geom



Excitation Energy in ^{25}Na (MeV)

present work	5/2+	3/2+	9/2+	7/2+	5/2+	9/2+	9/2+	11/2+	7/2+	7/2-	11/2-	13/2-
literature	5/2+	3/2+	?	3/2	5/2+	3/2+?	1/2-	?	?	(1/2, 3/2)-	?	?

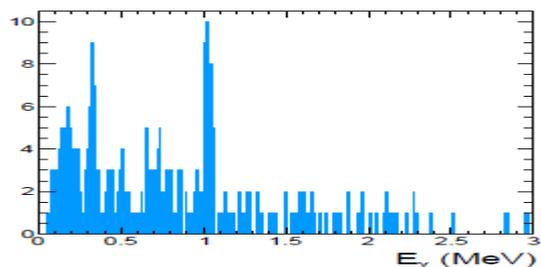
bound states in mirror ^{25}Na

$d(^{28}\text{Mg},p)^{25}\text{Na}$ at 8.0 MeV/u with 3,000 pps

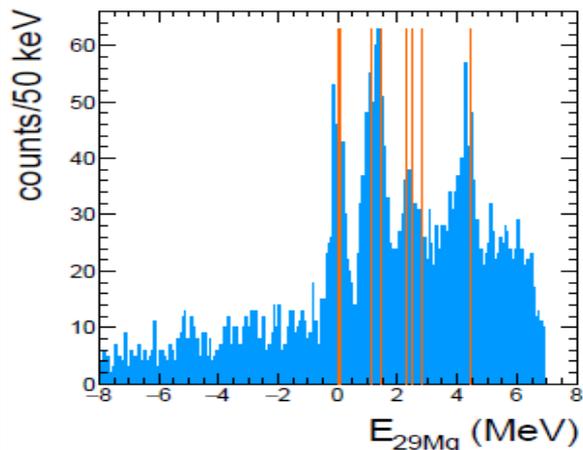
Secondary Beam

- ^{28}Mg beam 3000 pps at 8 AMeV
- With strong contamination
- ^{28}Si cont. ($3 \cdot 10^5$ pps)
- ^{28}Al cont. (300 pps)

Gated E_γ

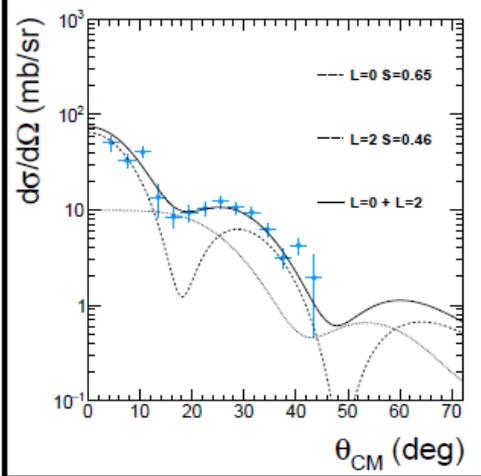


Gated Excitation Energy

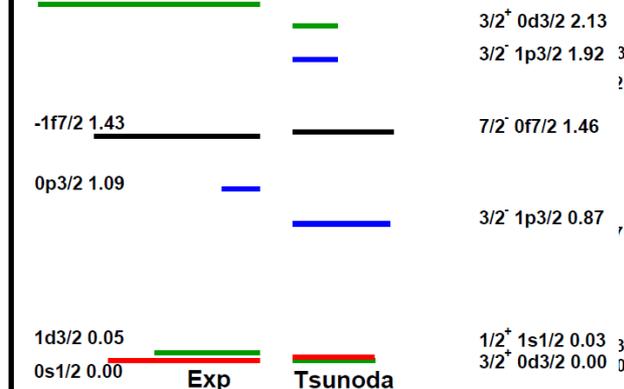


Experiment – SHARC and TIGRESS at TRIUMF

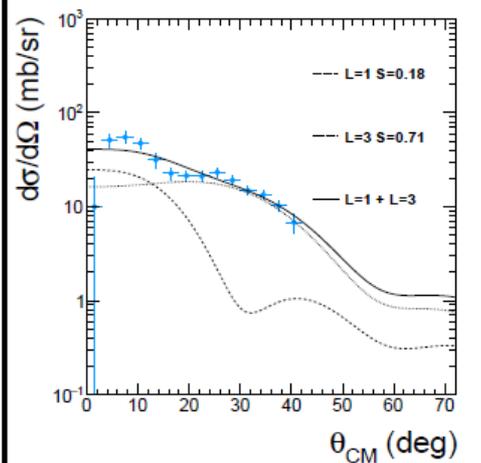
Ground State Doublet



Microscopic Shell Model



1 MeV Doublet



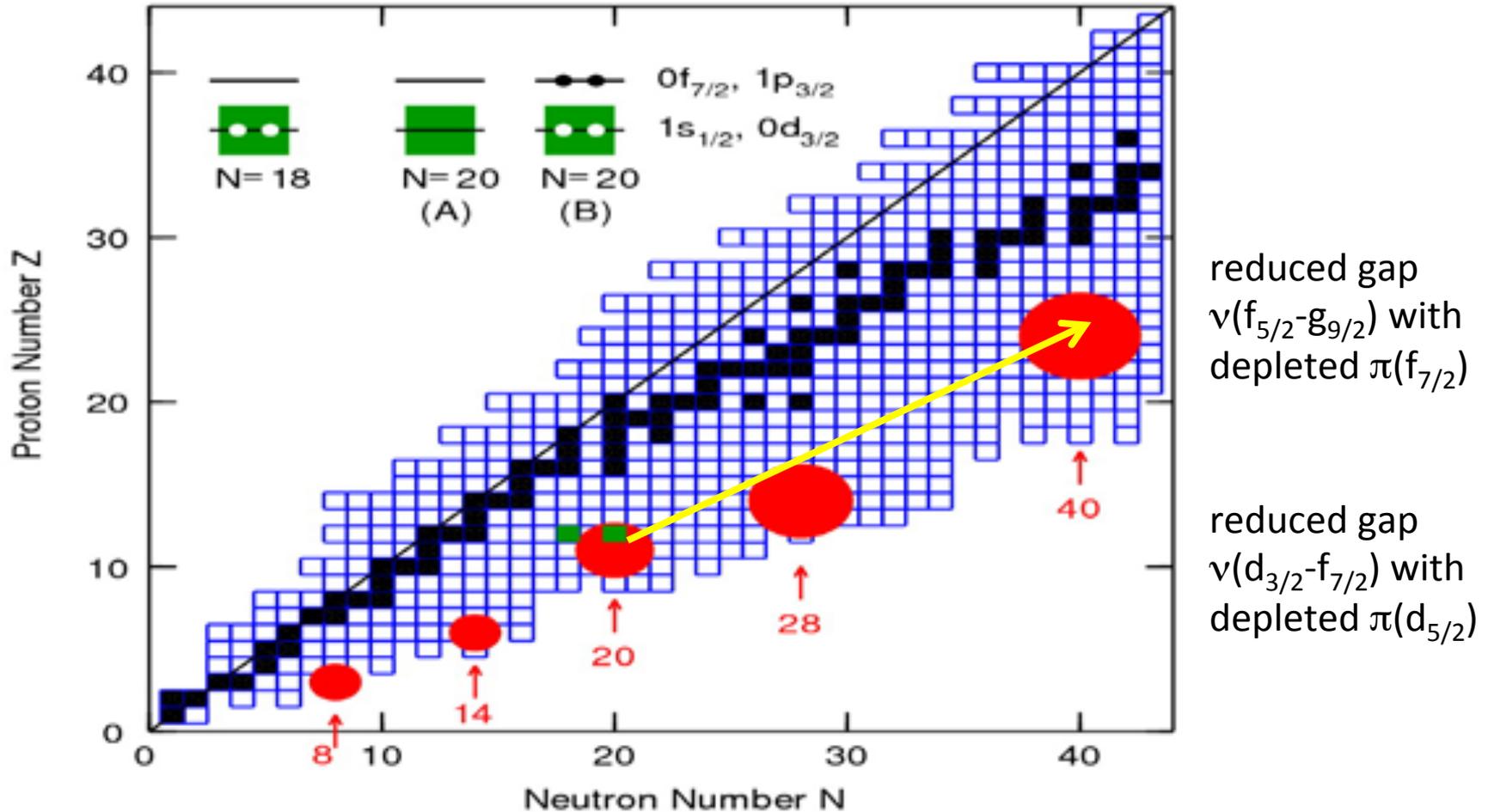
We have preliminary results from this experiment using a heavily contaminated beam.

New shell model calculations with realistic interactions and expanded sd-pf model space...
Tsunoda, Otsuka EEdf1 (EKK)

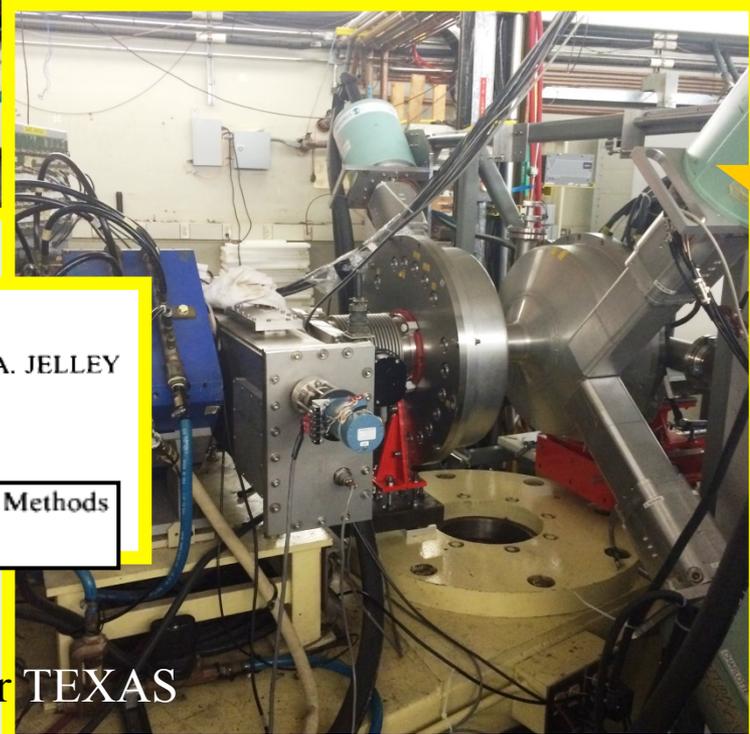
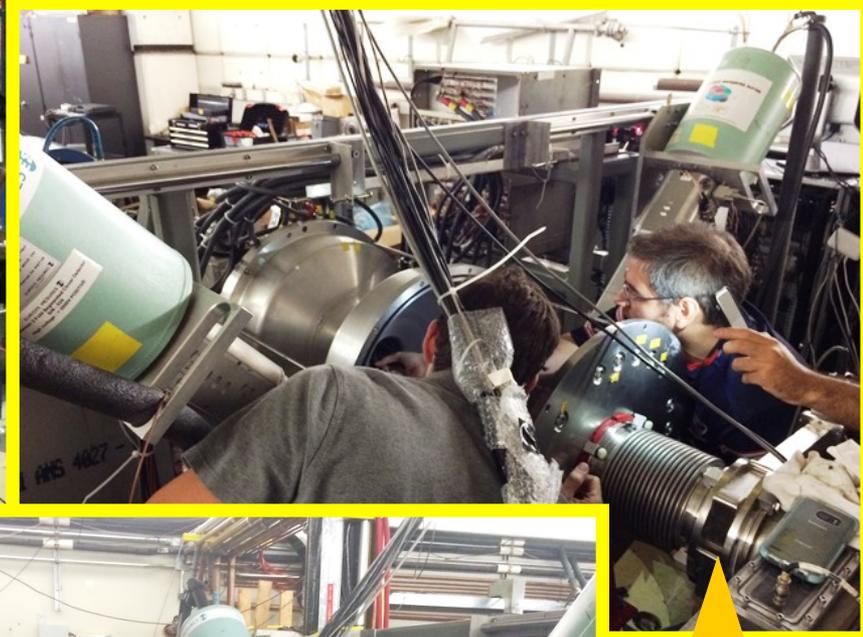
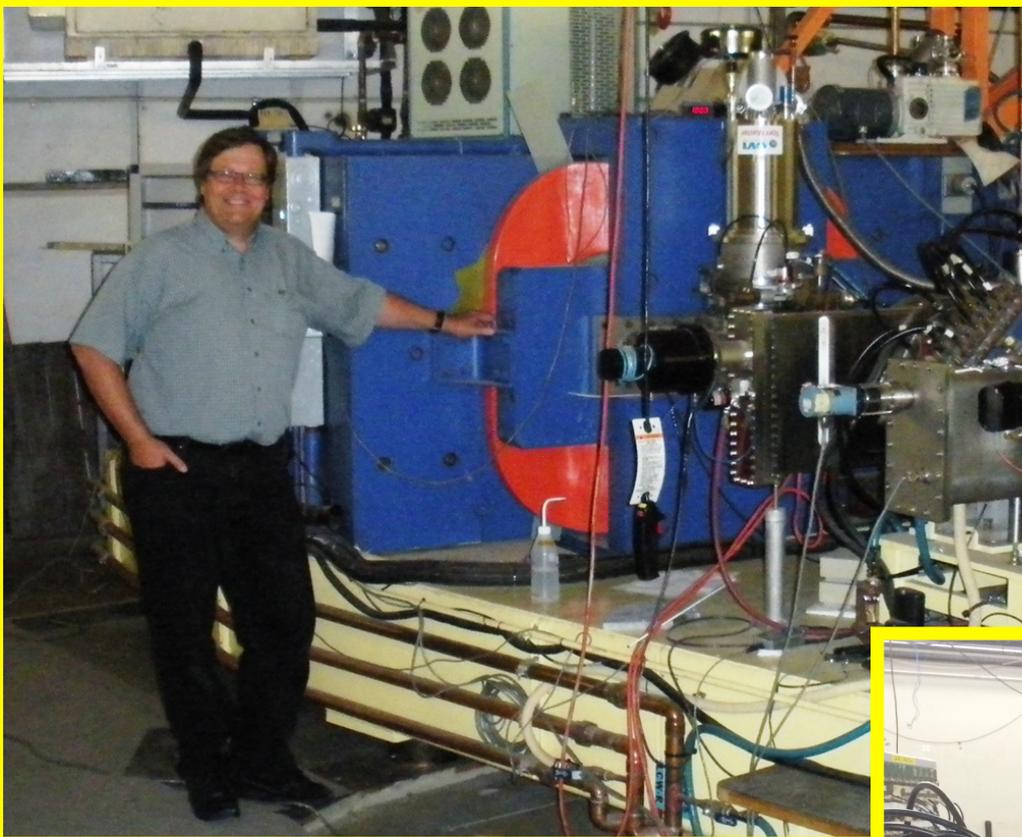
Too early to judge agreement.

Future plans – $d(^{60}\text{Cr}, p)^{61}\text{Cr}$ at 10.0 MeV/u

We have plans to move towards studying the second island of inversion e.g. via $^{60}\text{Cr}(d, p)$ at Texas A&M...



Texas A&M– radioactive beams using gas catcher and cyclotron reacceleration



zero-degree detection using Oxford MDM

THE OXFORD MDM-2 MAGNETIC SPECTROMETER

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**Nuclear Instruments and Methods
A245 (1986) 230**

installed,
first run
Aug 2016



TIARA  for TEXAS

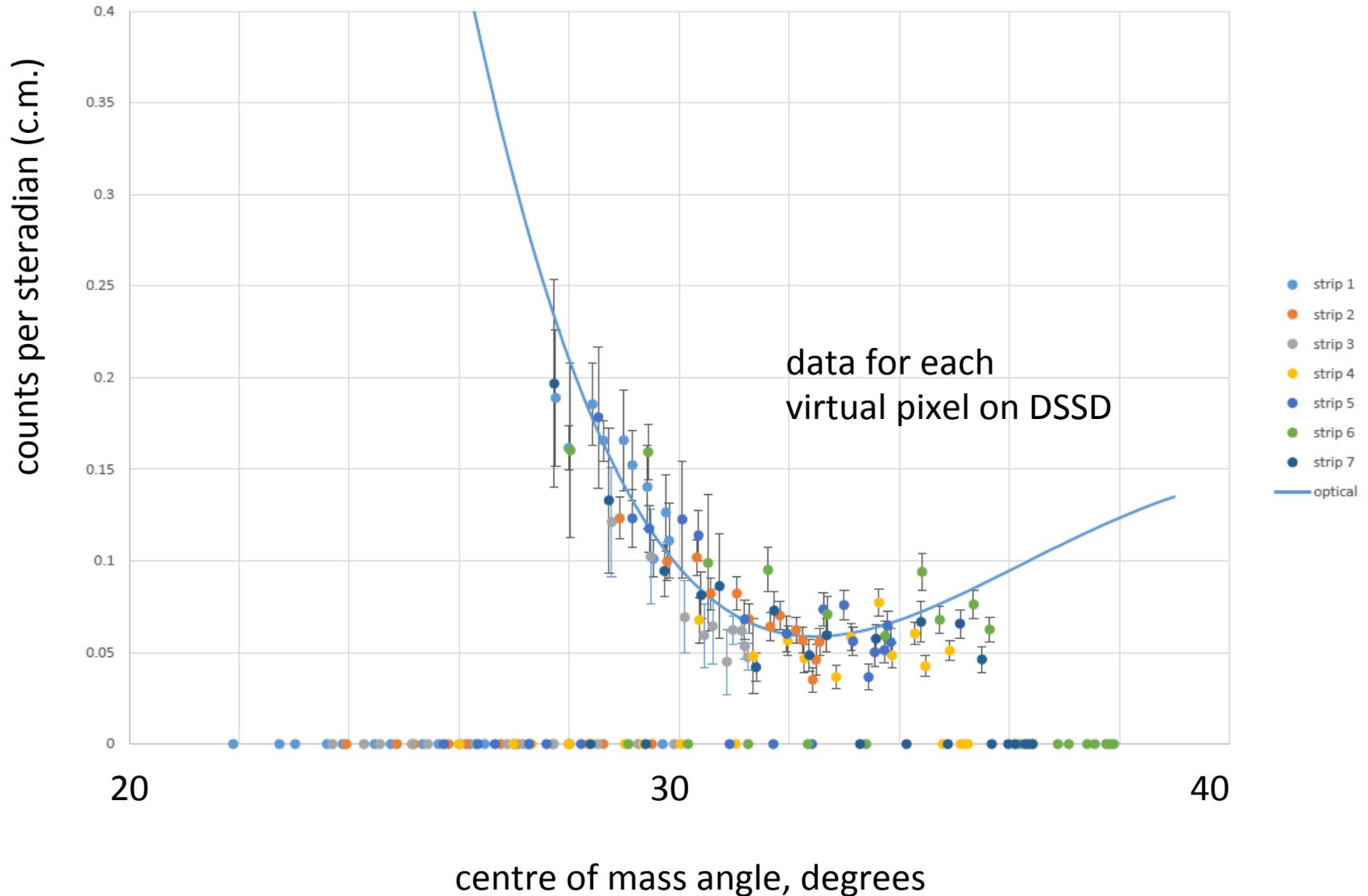
Summary

- We found that just outside the borders of the island of inversion, the shell model that was adapted for the island (i.e. USD-A, wbc) seems to work reasonably well – we have very useful discussions with those developing the new EEdf1 interaction
- Even in some less exotic nuclei, the selectivity of (d,p) has been shown to be hugely powerful in identifying the most interesting states (for the first time) e.g. ^{25}Na , and WE STUDY THE SAME orbitals and physics as in much more exotic nuclei.
- The new technique of gating on the coincident gamma rays to separate states that are not otherwise resolved has worked well
- We are edging closer towards the island of inversion to test the shell model further and improve it, and have plans to move attention to the second island of inversion
- We are preparing for new availability of beams at Texas A&M (also HIE-ISOLDE and MUGAST at GANIL)

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In-built normalisation from $d(^{24}\text{Na},d)^{24}\text{Na}$ near 70° (lab)



AIM:

Perform fits to spectra of E_x for each of a number of angle bins

Constraints in fitting:

- Excitation energy scale calibration checked using states of known E_x e.g. 3.455 MeV
- Allow for slight shift from angle to angle, in case corrections are imperfect
- Constrain energies of peaks using evidence from E_x spectra and supporting gamma rays
- Constrain the widths guided by simulations (observe little E_x change, but angular dependence)

