

# Diquark-antidiquark with open charm in QCD sum rules

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# New scalar charmed mesons

BABAR @ SLAC: (PRL90  
(2003) 242001)

very narrow ( $\Gamma < 5 \text{ MeV}$ )

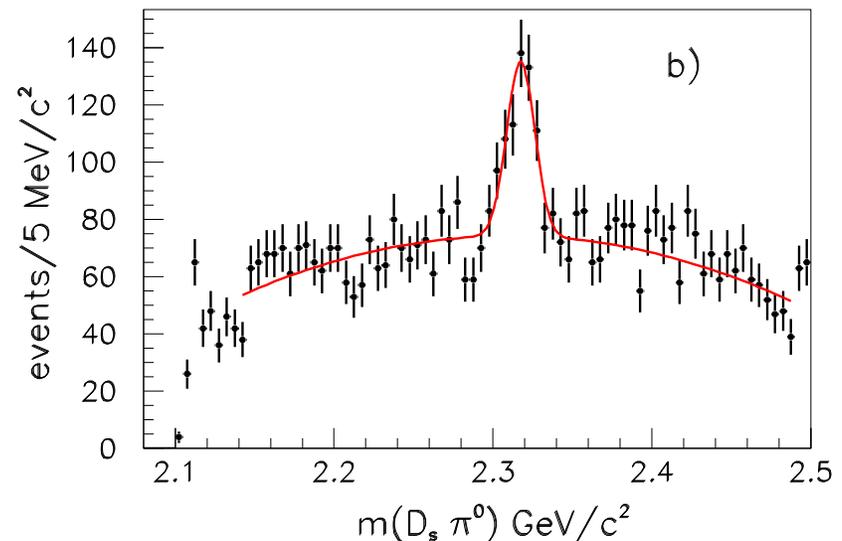
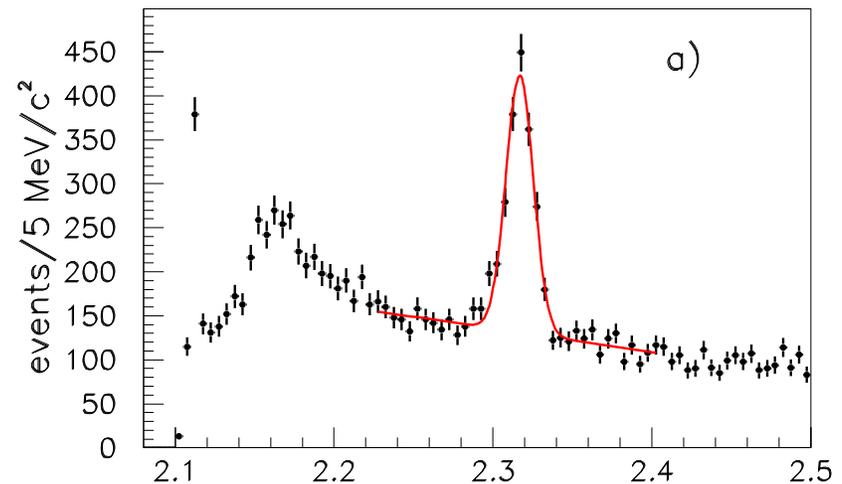
meson  $\rightarrow D_s^+ \pi^0$

$Q = 1, C = 1, S = 1 \Rightarrow$

minimum quark content:  $c\bar{s}$

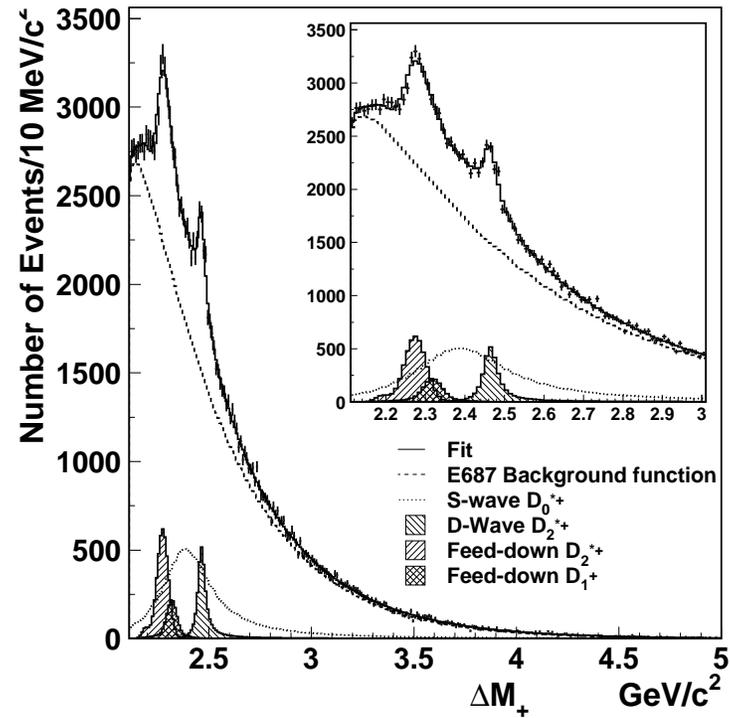
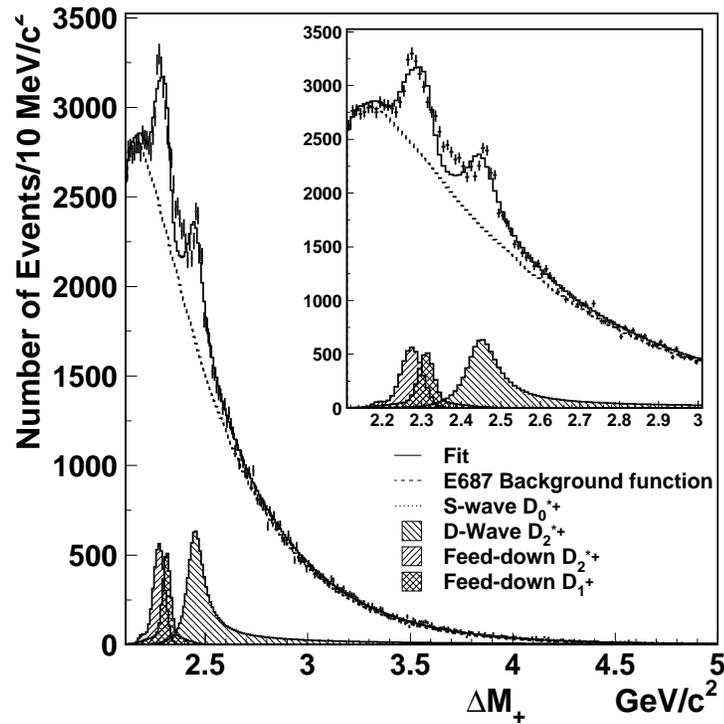
$D_{sJ}^+(2317), J^P = 0^+$

confirmed by CLEO, Belle,  
FOCUS



# FOCUS @ Fermilab (PLB586 (2004) 11):

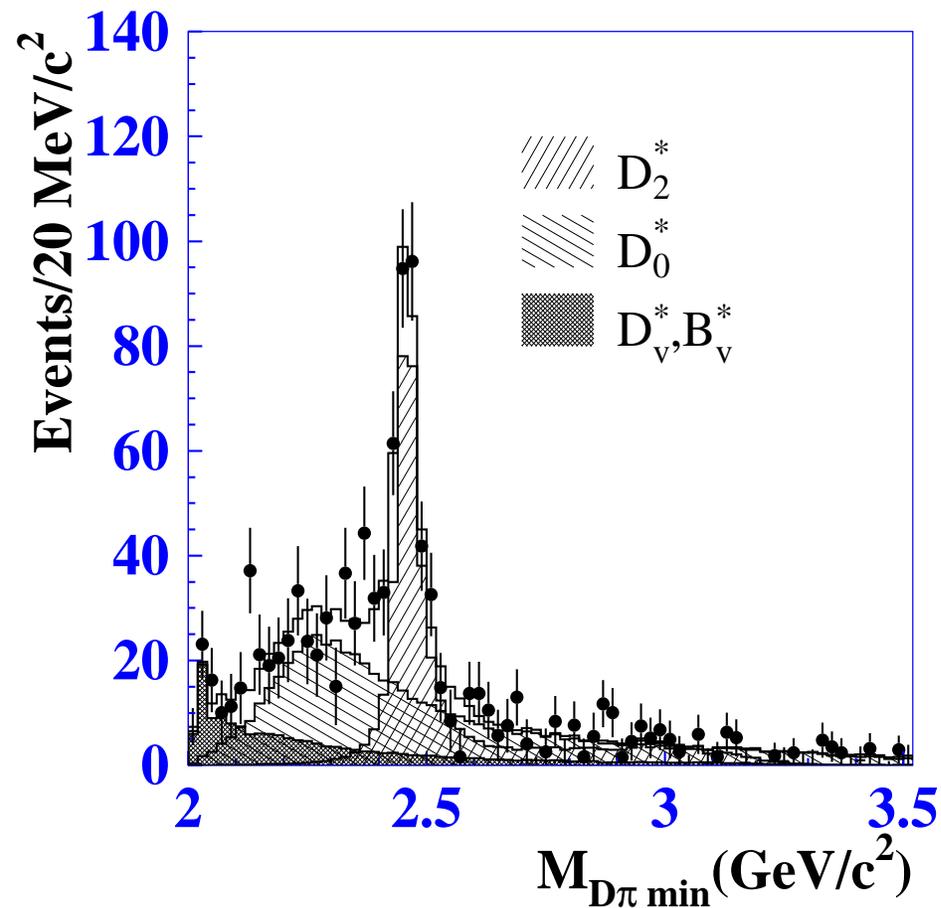
Evidence for broad scalar states ( $\Gamma \sim 250$  MeV)  $\rightarrow D_0^{*0}(2407) \rightarrow D^+ \pi^-$   
 $\rightarrow D_0^{*+}(2403) \rightarrow D^0 \pi^-$



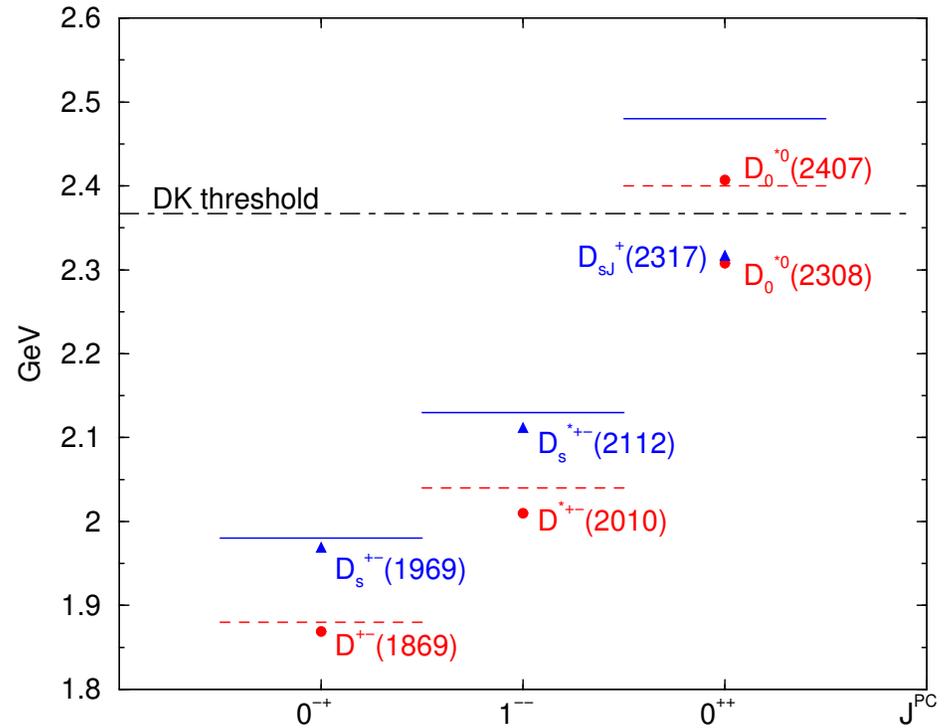
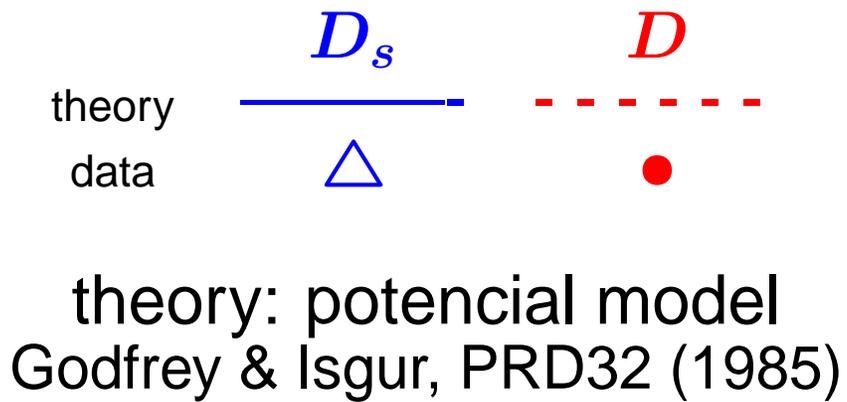
Belle @ KEK (PRD69 (2004) 112002):

Observation of a broad scalar state:  $D_0^{*0}(2308) \rightarrow D^+ \pi^-$

$\Gamma \sim 270 \text{ MeV}$

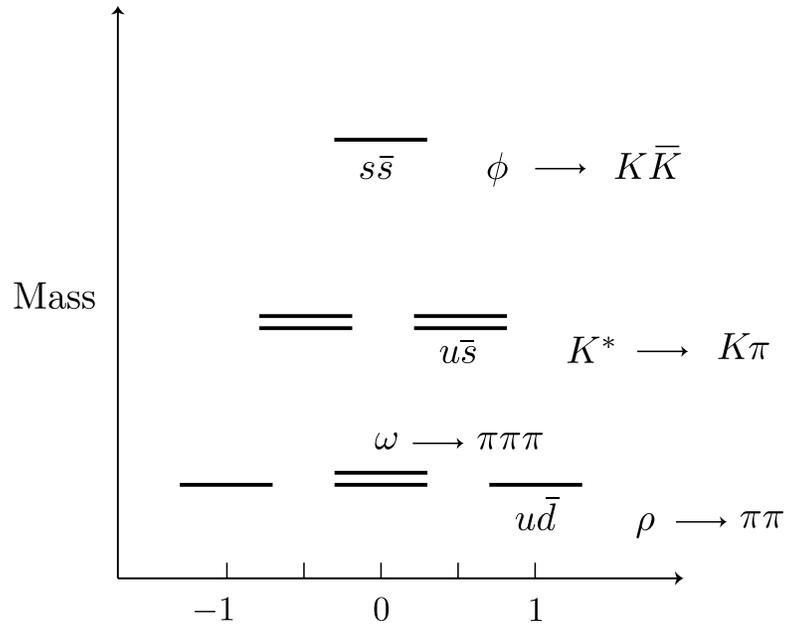


# Meson $D$ spectroscopy



# Light Sector

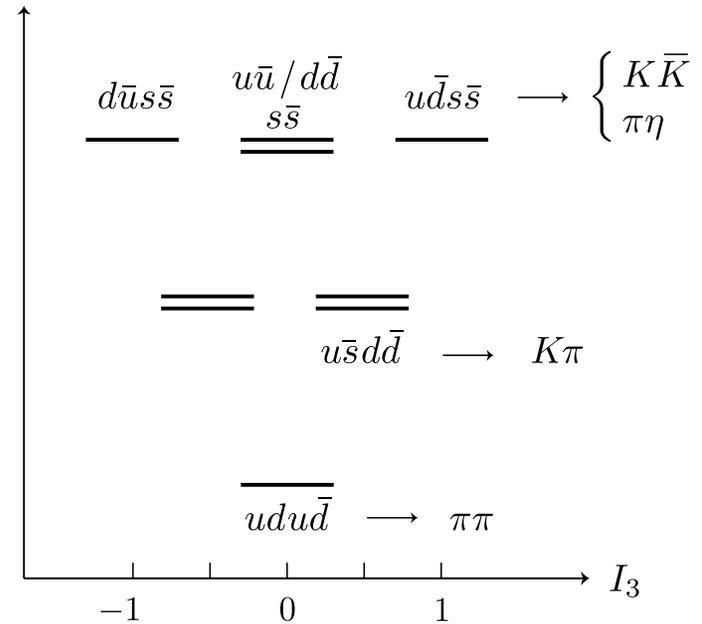
## Vector Mesons



1(a)

$\phi(1020)$   
 $K^*(890)$   
 $\rho(770), \omega(780)$

## Scalar Mesons



1(b)

$f_0(980), a_0(980)$   
 $\kappa(800)$   
 $\sigma(480)$

$\kappa(800), \sigma(480) \Rightarrow$  E791 Coll.  $D \rightarrow \kappa\pi, D \rightarrow \sigma\pi$

E791 Coll. P.R.L. **86** (2001) 765, 770; P.R.L. **89** (2002) 121801

$$D_{sJ}^+(2317) \left\{ \begin{array}{l} \text{pure } c\bar{s} \text{ state} \\ c\bar{q}q\bar{s} \text{ four-quark state} \\ \text{two-meson molecular state} \\ \text{mixing: two-meson and four-quark states} \end{array} \right.$$

$$\text{QCD Sum Rules} \left\{ \begin{array}{l} D_{sJ}^+(2317), D_0^{*0}(2308) \text{ [Belle]} \\ \text{as four-quark states} \\ \text{diquark antidiquark structure} \end{array} \right.$$

$$\Pi(q) = i \int d^4x \langle 0 | \mathbf{T} [j_S(x) j_S^\dagger(0)] | 0 \rangle e^{iq \cdot x}$$

$$j_S \left\{ \begin{array}{l} j_0 = \epsilon_{abc} \epsilon_{dec} (d_a^T C \gamma_5 c_b) (\bar{u}_d \gamma_5 C \bar{d}_e^T) \\ j_s = \frac{\epsilon_{abc} \epsilon_{dec}}{\sqrt{2}} [(u_a^T C \gamma_5 c_b) (\bar{u}_d \gamma_5 C \bar{s}_e^T) + u \leftrightarrow d] \\ j_{ss} = \epsilon_{abc} \epsilon_{dec} (s_a^T C \gamma_5 c_b) (\bar{u}_d \gamma_5 C \bar{s}_e^T) \end{array} \right.$$

# QCD Sum Rule

**Fundamental Assumption: Principle of Duality**

Theoretical side



quark level  
quark and gluon  
degrees of freedom



Wilson OPE

Phenomenological side



hadron level  
hadron parameters  
(masses, couplings,  
form-factors,...)



dispersion relation

**To improve the matching  $\Rightarrow$  Borel transform**

# Phenomenological side

$$\Pi^{phen} = \langle 0 | j_S | S \rangle \frac{1}{m_S^2 - q^2} \langle S | j_S | 0 \rangle + \text{Continuum}$$

$$\langle 0 | j_S | S \rangle = \sqrt{2} f_S m_S^4$$

## Theoretical Side

$$\Pi^{OPE}(q^2) = \int_{m_c^2}^{\infty} ds \frac{\rho(s)}{s - q^2}, \quad \rho(s) = \frac{1}{\pi} \text{Im}[\Pi^{OPE}]$$

condensates up to dimension 6

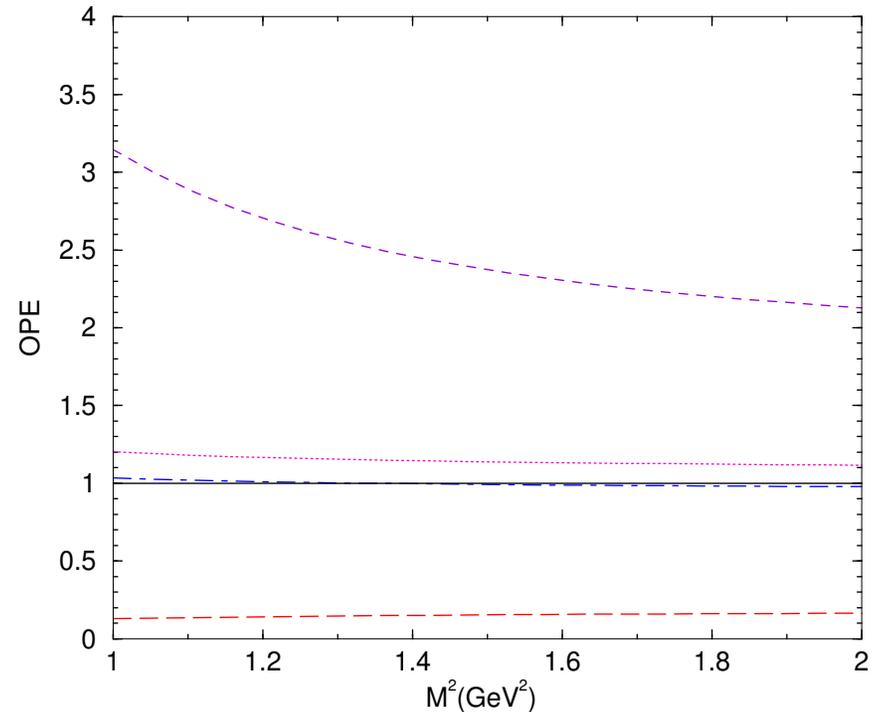
- quark condensate
- gluon condensate
- mixed condensate
- four-quark condensate

up to order  $m_s$  with  $m_c$  finite

# Sum Rule

$$2f_S^2 m_S^8 e^{-m_S^2/M^2} = \int_{m_c^2}^{s_0} ds e^{-s/M^2} \rho_S(s)$$

$$\begin{aligned}
 m_s &= (0.13 \pm 0.02) \text{ GeV} \\
 m_c &= (1.3 \pm 0.2) \text{ GeV} \\
 \langle \bar{q}q \rangle &= -(0.23)^3 \text{ GeV}^3 \\
 \langle \bar{s}s \rangle &= 0.8 \langle \bar{q}q \rangle \\
 \langle \bar{q}g\sigma \cdot Gq \rangle &= 0.8 \langle \bar{q}q \rangle \\
 \langle g^2 G^2 \rangle &= 0.5 \text{ GeV}^4 \\
 \sqrt{s_0} &= (2.7 \pm 0.1) \text{ GeV}
 \end{aligned}$$

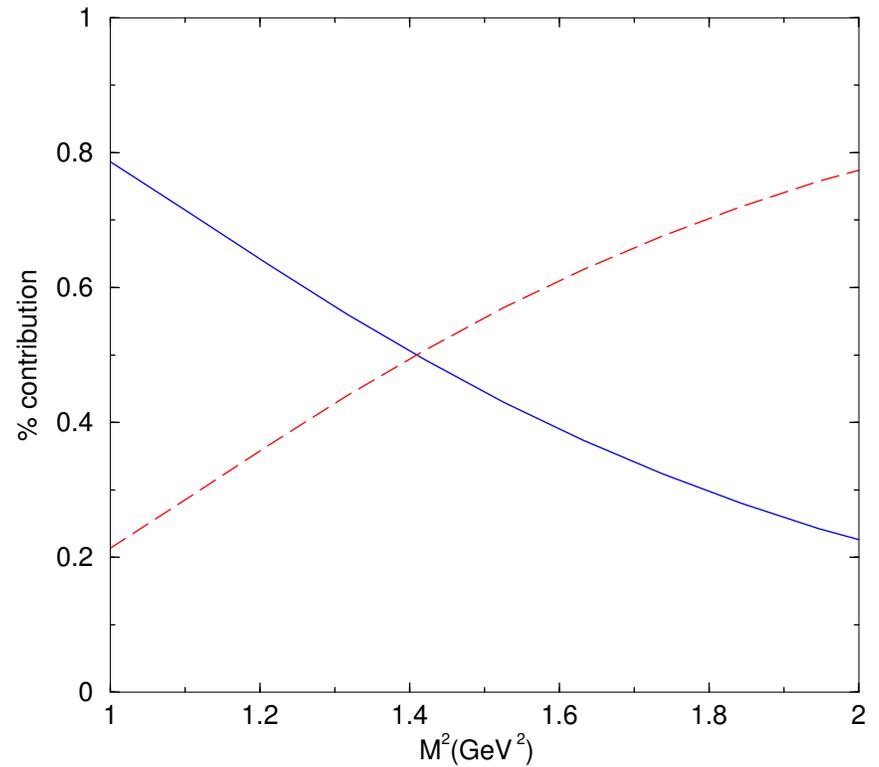


- perturbative
- . - . - . + quark condensate
- ..... + gluon condensate
- + four-quark condensate
- total

# Continuum Contribution

OPE side = pole + continuum contribution

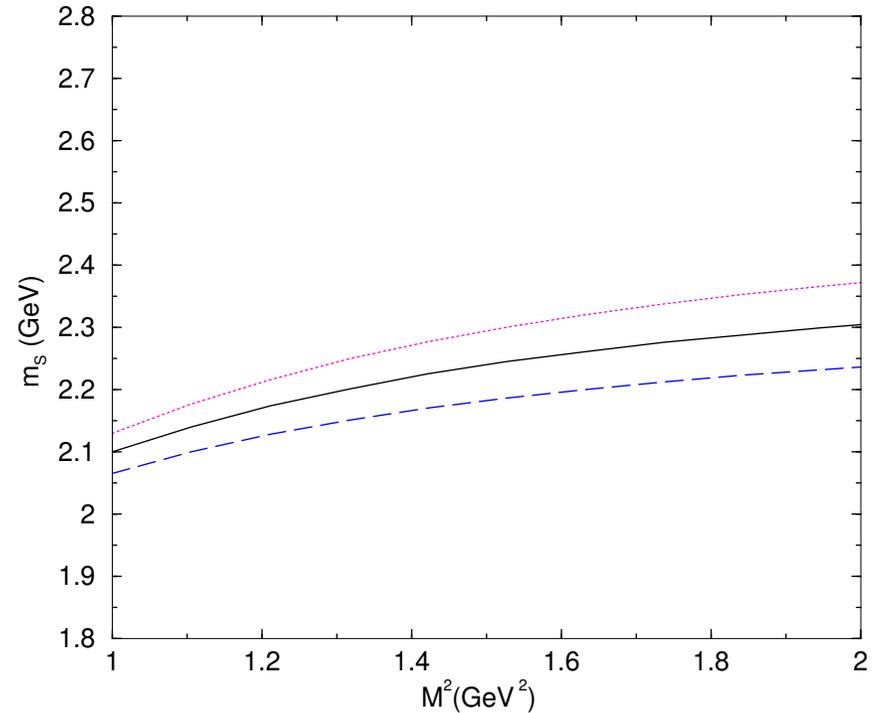
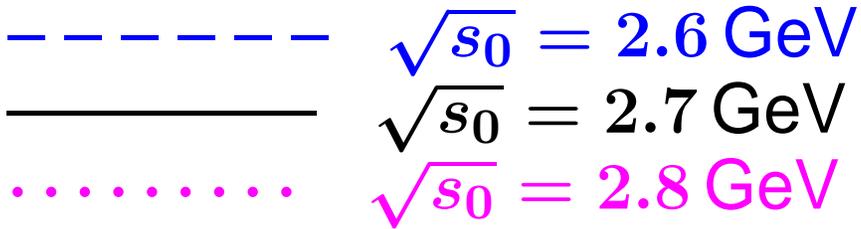
----- continuum cont.  
———— pole cont.



# Masses

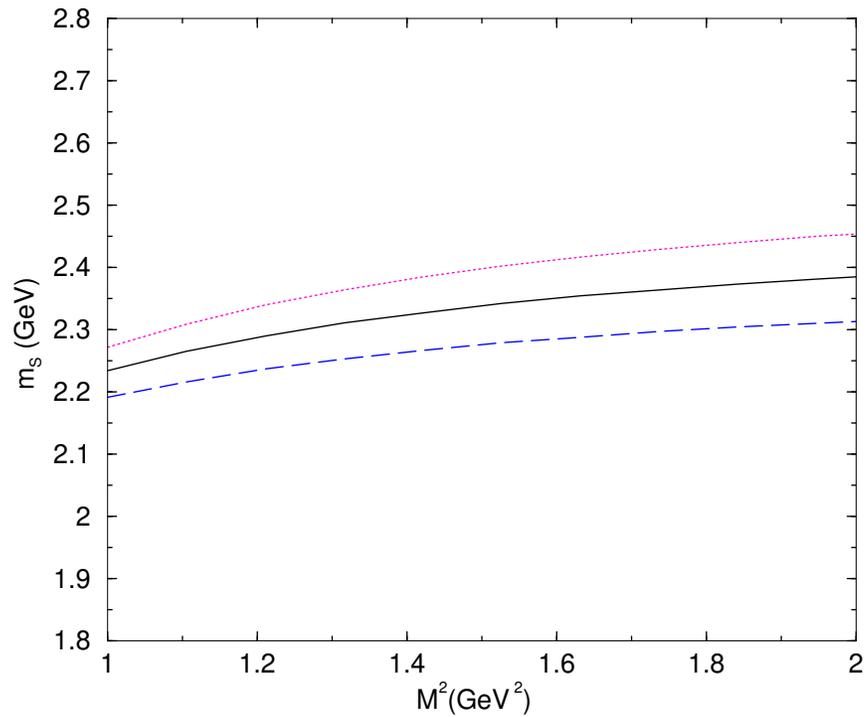
$$m_S^2 = \frac{\int_{m_c^2}^{s_0} ds e^{-s/M^2} s \rho_S(s)}{\int_{m_c^2}^{s_0} ds e^{-s/M^2} \rho_S(s)}$$

$$j_S = j_0$$



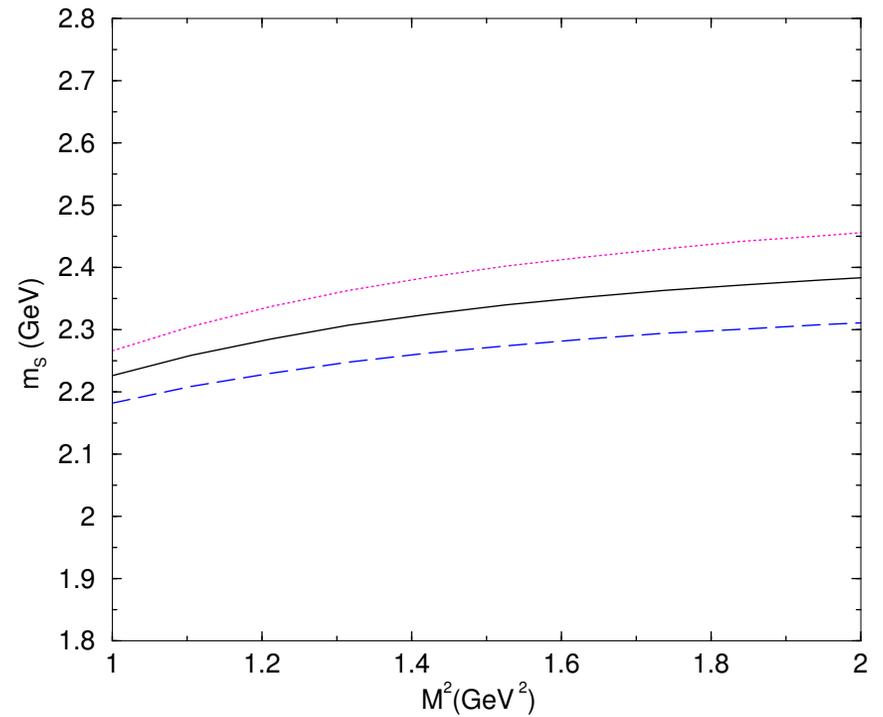
$$m_{0s} = (2.22 \pm 0.20) \text{ GeV}$$

$$j_S = j_s$$



$$m_{1s} = (2.32 \pm 0.20) \text{ GeV}$$

$$j_S = j_{ss}$$



$$m_{2s} = (2.31 \pm 0.20) \text{ GeV}$$

resonance	$D_0^{(0s)}$	$D_0^{(1s)}$	$D_0^{(2s)}$
mass (GeV)	$2.22 \pm 0.20$	$2.32 \pm 0.20$	$2.31 \pm 0.20$

to be seen

$D_{sJ}^+(2317)$

$D_0^{*0}(2308)$

Width  $\rightarrow D_{sJ}^+(2317) \rightarrow D_s^+ \pi^0 \Rightarrow \Gamma < 5 \text{ MeV}$

$\rightarrow (\text{Belle}) D_0^{*0}(2308) \rightarrow D^+ \pi^- \Rightarrow \Gamma \sim 270 \text{ MeV}$

$$\Pi^{phen}(M^2) = 2f_S^2 m_S^8 \int_{(m_\pi + m_D)^2}^{s_0} ds e^{-s/M^2} \rho_{BW}(s)$$

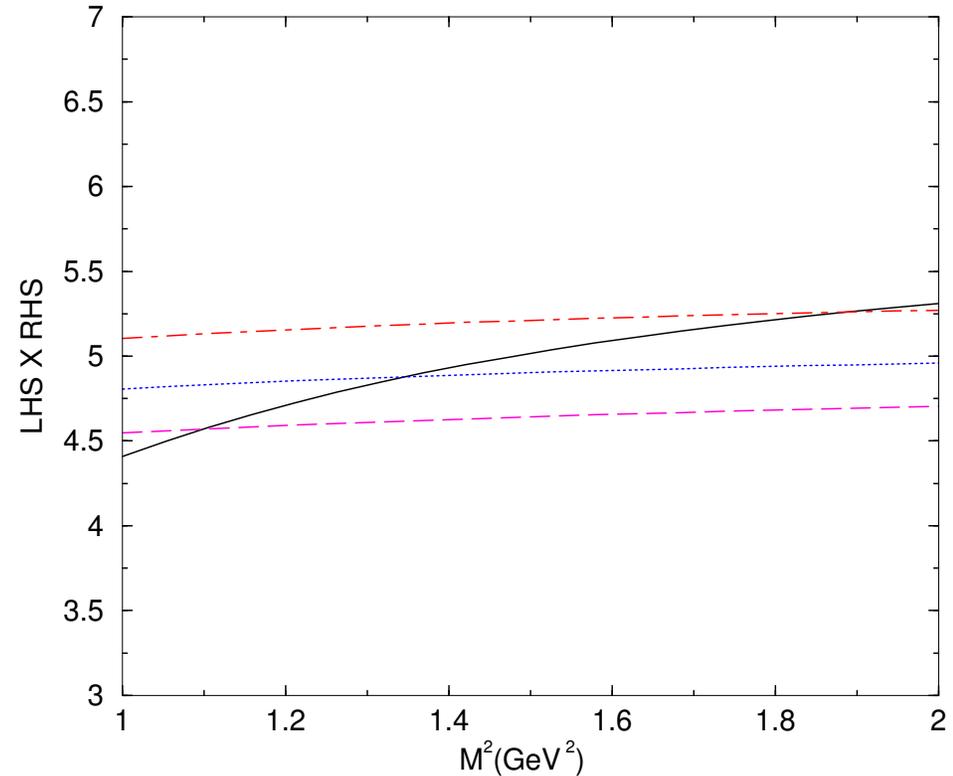
$$\rho_{BW}(s) = \frac{1}{\pi} \frac{\Gamma(s) m_S}{(s - m_S^2)^2 + m_S^2 \Gamma(s)^2}, \quad \Gamma(s) = \Gamma_0 \sqrt{\frac{\lambda(s, m_D^2, m_\pi^2)}{\lambda(m_S, m_D^2, m_\pi^2)}} \frac{m_S^2}{s}$$

$$\lambda(x, y, z) = x^2 + y^2 + z^2 - 2xy - 2xz - 2yz$$

$$\frac{\int_{(m_\pi+m_D)^2}^{s_0} ds e^{-s/M^2} s \rho_{BW}(s)}{\int_{(m_\pi+m_D)^2}^{s_0} ds e^{-s/M^2} \rho_{BW}(s)} = \frac{\int_{m_c^2}^{s_0} ds e^{-s/M^2} s \rho_S(s)}{\int_{m_c^2}^{s_0} ds e^{-s/M^2} \rho_S(s)} .$$

mass is a parameter

- - - - -  $m_S = 2.2 \text{ GeV}$   
 .....  $m_S = 2.3 \text{ GeV}$   
 - . - .  $m_S = 2.4 \text{ GeV}$   
 \_\_\_\_\_ RHS

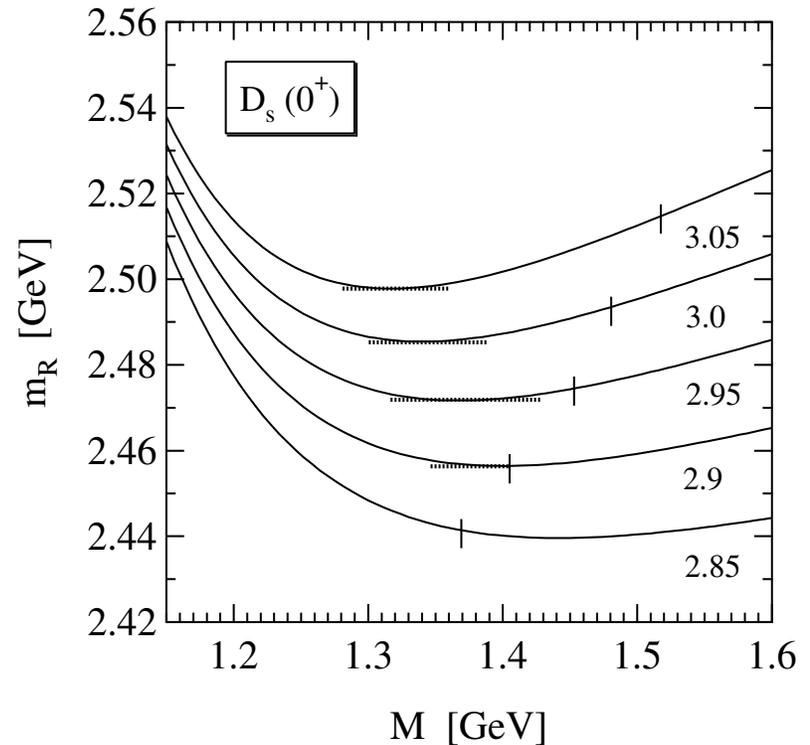
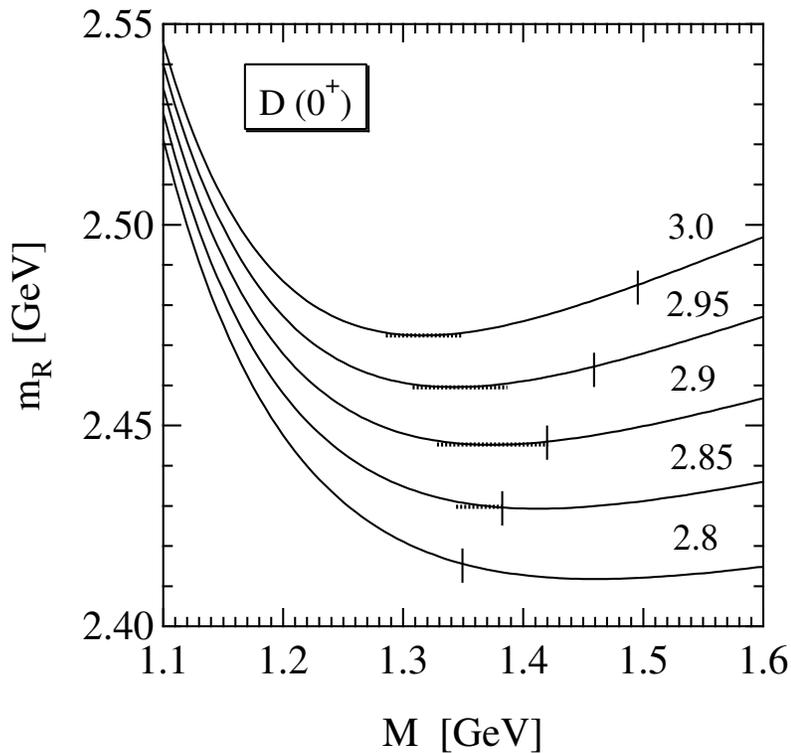


$m_S$  compatible with 2.3 GeV

# Two-quark states

Hayashigaki & Terasaki (hep-ph/0411285)

resonance	$c\bar{q}$	$c\bar{s}$
mass (GeV)	$2.45 \pm 0.03$	$2.48 \pm 0.03$
mass <sup>exp</sup> (GeV)	2.308 (Belle), 2.405 (FOCUS)	2.317



pseudoscalar and vector mesons compatible with experiment

# Light Scalars

Decay width (diquark-antidiquark states)  $\left\{ \begin{array}{l} \sigma \rightarrow \pi^+ \pi^- \\ \kappa \rightarrow K^+ \pi^- \\ f_0 \rightarrow K^+ K^- \\ f_0 \rightarrow \pi^+ \pi^- \end{array} \right.$

$$T_{\mu\nu}(p, p', q) = \int d^4x d^4y e^{i \cdot p' \cdot x} e^{iq \cdot y} \langle 0 | T \{ j_{5\mu}^{P_1}(x) j_{5\nu}^{P_2}(y) j_S^\dagger(0) \} \rangle$$

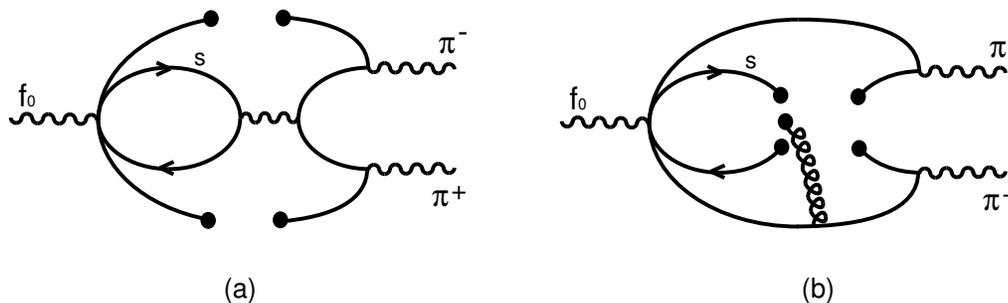
$$T_{\mu\nu}^{phen} = \frac{\sqrt{2} F_{P_1} F_{P_2} m_S^4 f_S}{(m_S^2 - p^2)(m_{P_1}^2 - p'^2)(m_{P_2}^2 - q^2)} g_{SP_1P_2} p'_\mu q_\nu + \dots$$

$$\Gamma(S \rightarrow P_1 P_2) = \frac{1}{16\pi m_S^3} (g_{SP_1P_2})^2 \sqrt{\lambda(m_S^2, m_{P_1}^2, m_{P_2}^2)}$$

vertex	$\sigma \pi^+ \pi^-$	$\kappa K^+ \pi^-$	$f_0 K^+ K^-$	$f_0 \pi^+ \pi^-$
$g$ (GeV)	$3.1 \pm 0.5$	$3.6 \pm 0.3$	$1.6 \pm 0.1$	$0.47 \pm 0.05$
$g^{exp}$ (GeV)	$2.6 \pm 0.2$	$4.5 \pm 0.4$		$1.6 \pm 0.8$

PLB 608 (2005) 69

$f_0 \rightarrow \pi^+ \pi^-$  mediated by one gluon exchange



needs  $\alpha_s$  corr.

QCD sum rule calculation:

$$\Gamma_{D_{sJ}^+ (2317) \rightarrow D_s^+ \pi^0} \propto (\langle \bar{u}u \rangle - \langle \bar{d}d \rangle)^2 \Rightarrow \text{very small}$$

preliminary calculation:  $g_{D_{sJ} D_s \pi} \sim 0.06 \text{ GeV} \Rightarrow \Gamma \sim 8 \text{ KeV}$

isovector state:  $\Gamma \sim 260 \text{ MeV}$

# Conclusions

We have evaluated the masses of the four-quark states:  
 $(cd)(\bar{u}\bar{d})$ ,  $(cu)(\bar{d}\bar{s})$  and  $(cs)(\bar{u}\bar{s})$

resonance	$D_0^{(0s)}$	$D_0^{(1s)}$	$D_0^{(2s)}$
mass (GeV)	$2.22 \pm 0.20$	$2.32 \pm 0.20$	$2.31 \pm 0.20$

The masses of BABAR,  $D_{sJ}^+$  (2317), and Belle,  $D_0^{*0}$  (2308), resonances can be reproduced by the four-quark states  $D_0^{(1s)}$  and  $D_0^{(2s)}$ , although the OPE convergence is not good

The observation of a new scalar charmed meson, with mass  $\sim 2.2$  GeV, would confirm the existence of four-quark states

We interpret the FOCUS,  $D_0^{*(0+)}$  (2405), resonance as a normal two-quark  $(c\bar{q})$  state