

Measurement of the photon Light-Cone wave function by diffractive dissociation

Outline

Wave Functions, Structure Functions and Form Factors

Comments on Measurement of the Pion Valence LCWF

Measurement of the EM component of the Photon LCWF

Measurement of the hadronic component of the Photon LCWF

LCWF of the proton

Summary

Light-Cone Wave Functions:

Solutions of LC Hamiltonian: $H_{LC}^{QCD} |\psi_h\rangle = M_h^2 |\psi_h\rangle$

$$H_{LC}^{QCD} = P^+ P^- - P_\perp^2$$

Fock States Expansion for the Pion:

$$\begin{aligned} |\psi_{\pi^-} \rangle &= \sum_n \langle n | \pi^- \rangle |n \rangle \\ &= \psi_{d\bar{u}/\pi}^{(\Lambda)}(u_i, \vec{k}_{\perp i}, \lambda_i) |\bar{u}d \rangle \\ &\quad + \psi_{d\bar{u}g/\pi}^{(\Lambda)}(u_i, \vec{k}_{\perp i}, \lambda_i) |\bar{u}dg \rangle + \dots \end{aligned}$$

$$u_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{p^0 + p^z}, \quad \sum_{i=1}^n u_i = 1, \quad \sum_{i=1}^n \vec{k}_{\perp i} = \vec{0}_\perp.$$

$k_\perp$ is the quark (antiquark) transverse momentum.

ANY parton with fractional momentum x :

$$G_{a/h}(x, Q) = \sum_n \int d[\mu_n] \left| \Psi_{n/h}^{(Q)}(u_i, \vec{k}_{\perp i}, \lambda_i) \right|^2 \sum_i \delta(x - u_i)$$

Parton Distribution Functions Derived from *inclusive* DIS cross sections.

VALENCE QUARK with fractional momentum u :

$$\phi_{q\bar{q}}(u) \sim \int_0^{Q^2} \psi_{q\bar{q}}(u, k_{\perp}) dk_{\perp}^2 \quad Q^2 = \frac{k_{\perp}^2}{u(1-u)}$$

For not too small Q^2 :

$$\psi(u, k_{\perp}) \sim \frac{\phi(u)}{k_{\perp}^2}$$

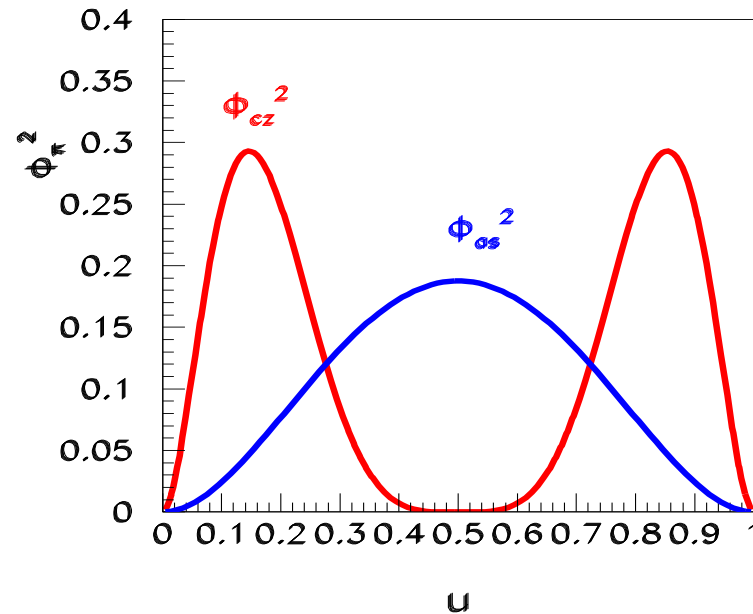
Distribution Amplitude $\phi(u)$, an *exclusive* quantity.

PION DISTRIBUTION AMPLITUDES

$$\phi_\pi(u, \mu^2) = u(1-u) \sum_{n \geq 0} a_n C_n^{3/2}(2u-1) \left(\ln \frac{\mu^2}{\Lambda^2}\right)^{-\gamma_n/2\beta_2}$$

1. The Asymptotic Function: $a_2 = 0, a_4 = 0$
 pQCD; for $Q^2 \rightarrow \infty$: $\phi_{Asy}(u) = \sqrt{3}f_\pi u(1-u)$

2. The Chernyak-Zhitnitsky Function: $a_2 = 0.4, a_4 = 0$
 QCD sum rules; for low Q^2 : $\phi_{cz}(u) = 5\sqrt{3}f_\pi u(1-u)(1-2u)^2$



(1) G.P. Lepage, S.J. Brodsky, Phys. Lett.B87, 359 (1979)

A.V. Efremov, A.V. Radyushkin, Theor. Math. Phys. 42, 97 (1980).

(2) V.L. Chernyak and A.R. Zhitnitski, Phys. Rep. 112,173 (1984).

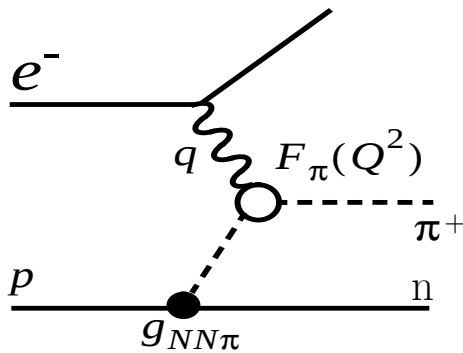
THE PION FORM FACTOR and WAVE FUNCTION

Space-Like Form Factor Measurements:

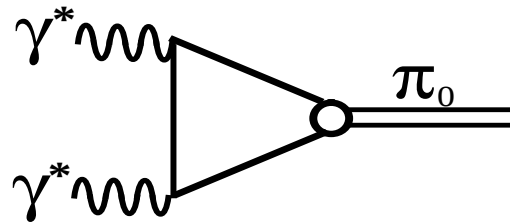
- $\pi e \rightarrow \pi e$: Very low Q^2

- $p(e, e' \pi^+) n$

$$e^+ + e^- \rightarrow \pi^0$$



(a)

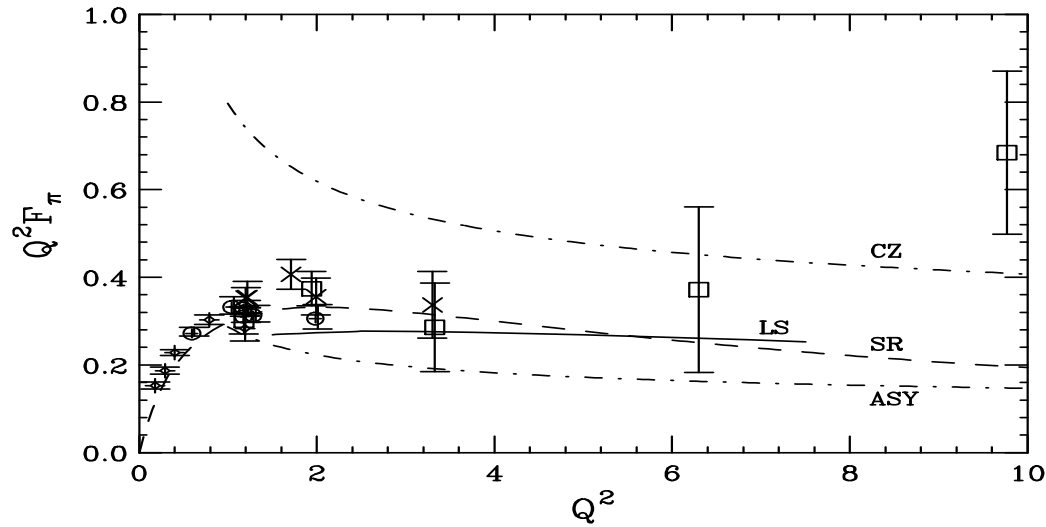


(b)

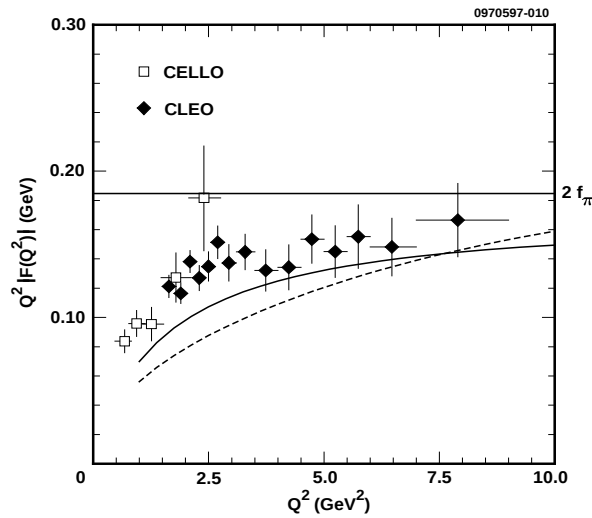
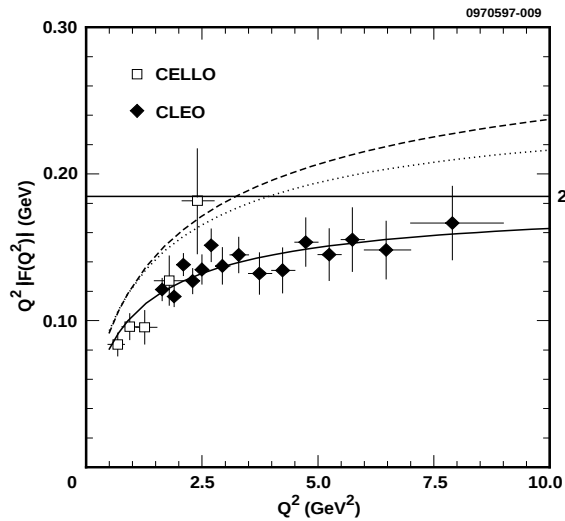
$$\sigma_L \sim -\frac{t g_{\pi NN}^2(t)}{(t - m_\pi^2)^2} F_\pi^2(Q^2)$$

$$F_\pi(Q^2) = \int_0^1 dx dy \left[\phi_\pi(y, \mu^2) \right] T(y, x, Q^2, \mu^2) \left[\phi_\pi(x, \mu^2) \right], \quad x, y = \frac{p_{quark}}{p_\pi}$$

Space-Like π^+ Form Factors (G. Stermann, P. Stoler, A.R.N.P.S. 43, 193 (1997))



π^0 Transition Form Factor CLEO Col. Phys. Rev. D57, 33 (1998)

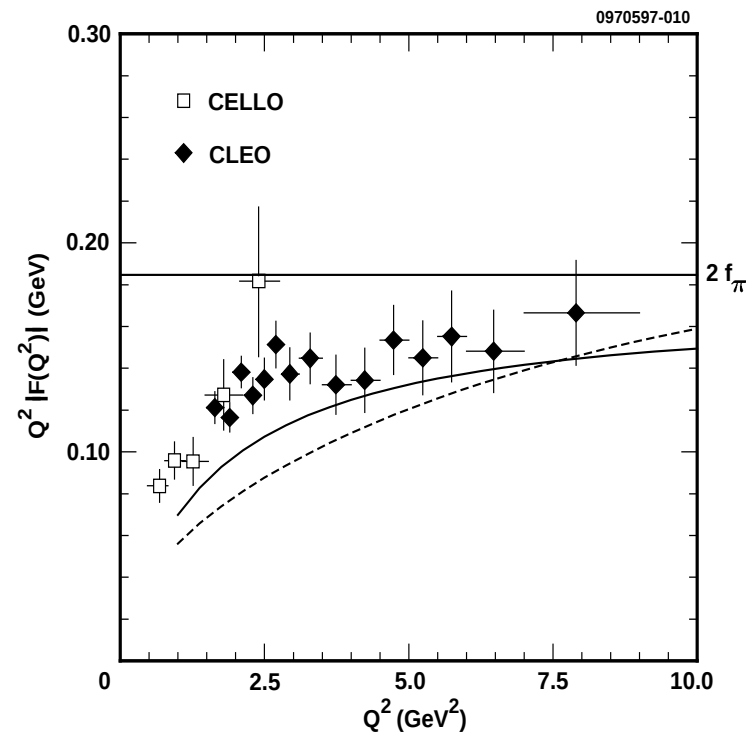
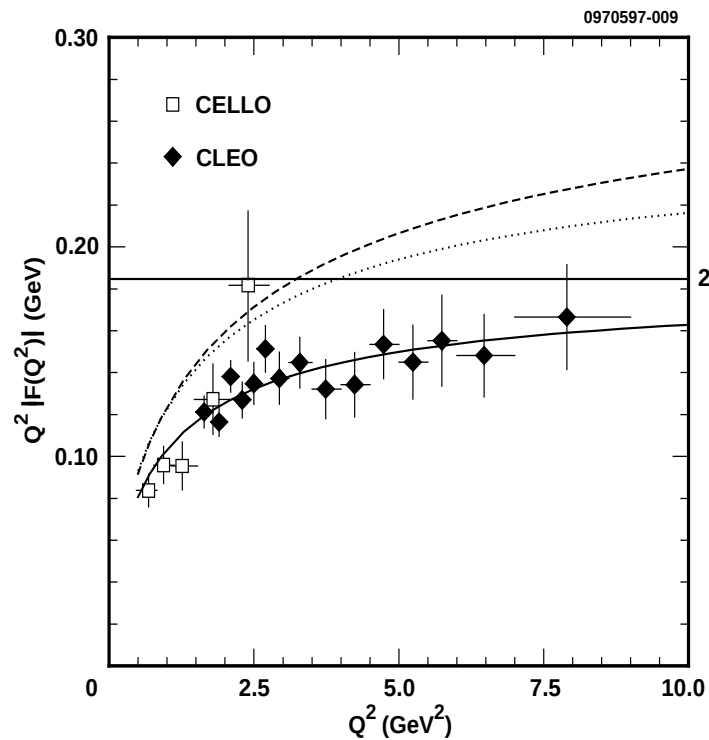


π^0 Transition Form Factor

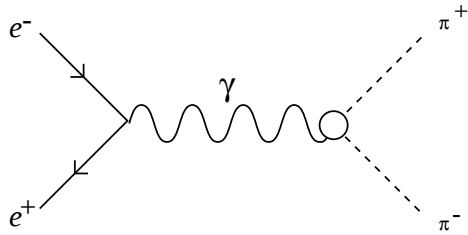
CLEO Col. Phys. Rev. **D57**, 33 (1998)

Asymptotic Wave Function (solid lines), CZ Wave Function (dashed lines)

R. Jakob *et al.* J. Phys. G22, 45 (1996) F.-G. Cao *et al.* Phys. Rev D53, 6582 (1996)



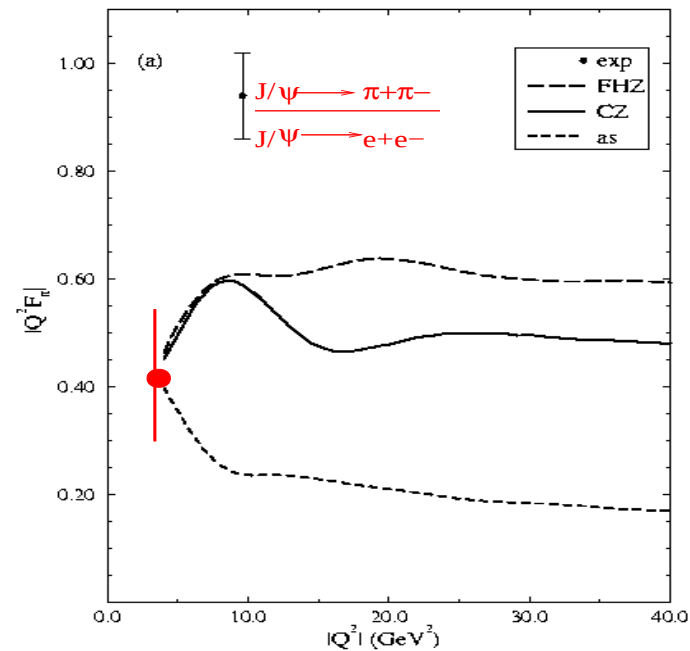
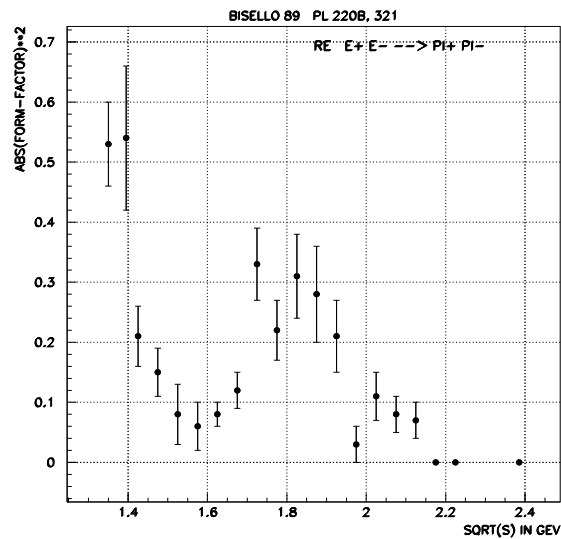
Time-Like Form Factor ($q^2 > 0$)

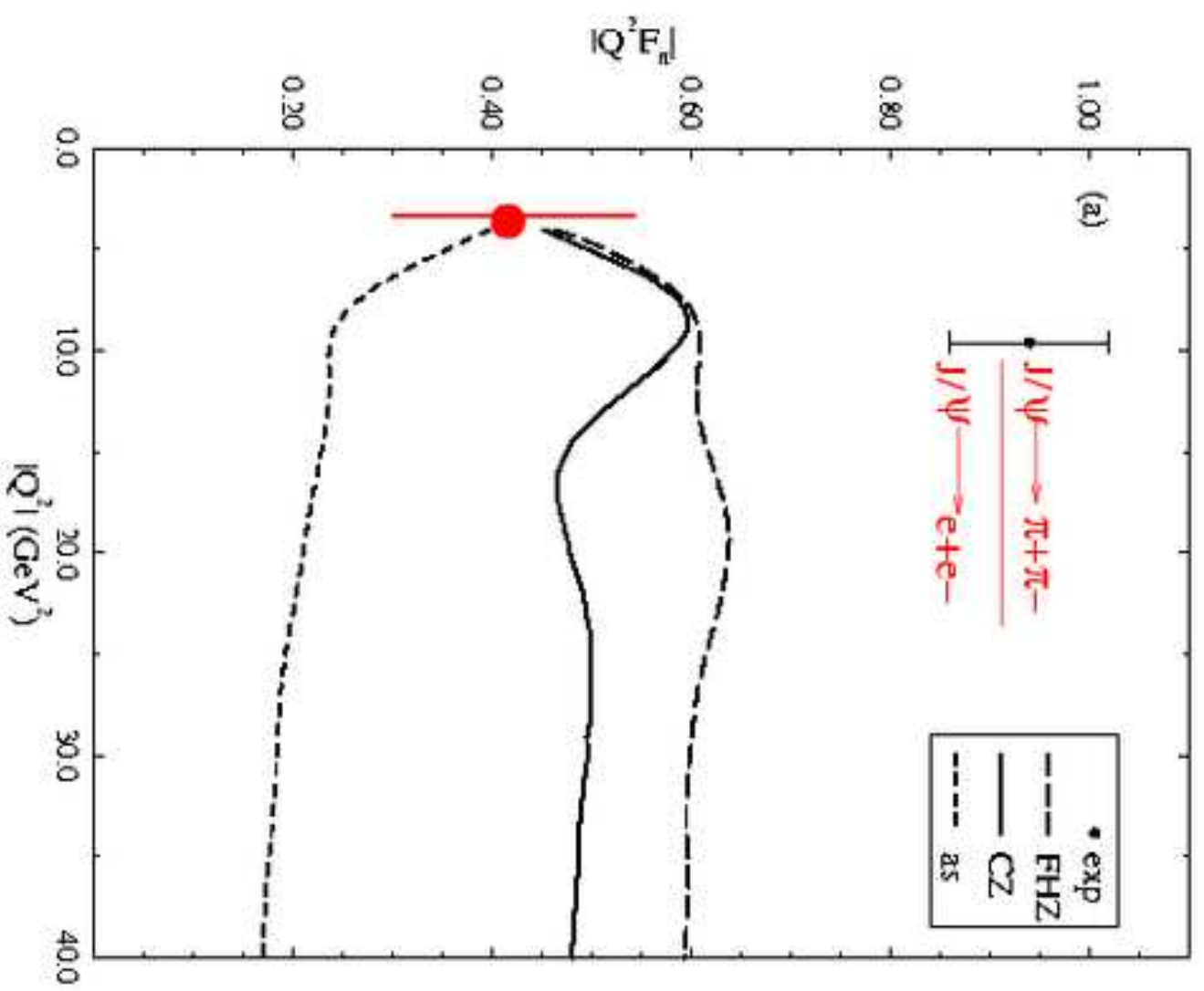


$$\sigma = \sigma(e^+e^- \rightarrow q\bar{q})|F_\pi(s)|^2 = \frac{\alpha^2\pi}{3} \frac{(s - 4m_\pi^2)^{3/2}}{s^{5/2}} |F_\pi(s)|^2.$$

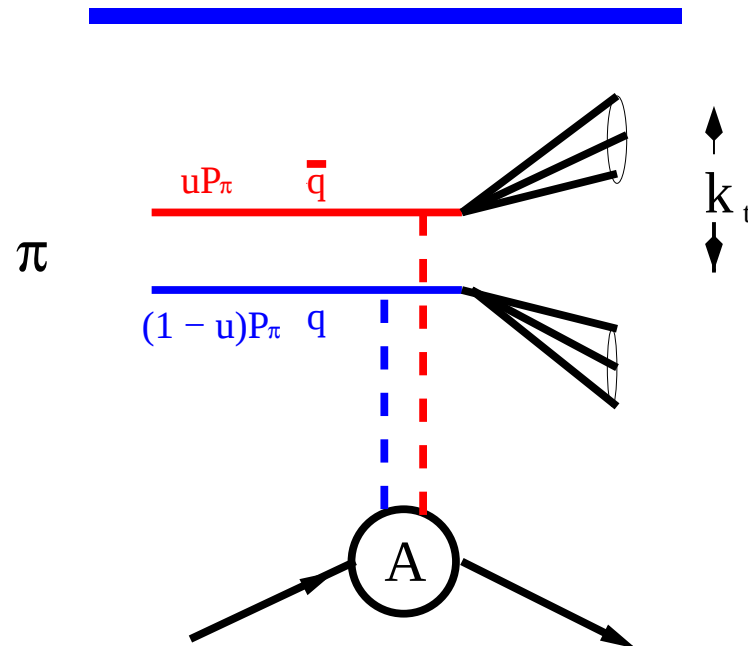
DM2 Coll. Phys. Lett. **B220**, 321 (1989)

Gousset and Pire, Phys. Rev. **D51**, 15 (1995)





Differential Measurement of the Pion Wave Function



In the diffractive dissociation of the $|q\bar{q}\rangle$ configuration into DJ, u can be measured by the momentum ratio of the two jets:

$$u_{\text{measured}} = \frac{p_{\text{jet1}}}{p_{\text{jet1}} + p_{\text{jet2}}}, \quad Q_{DJ}^2 = \frac{k_t^2}{u(1-u)}$$

L. Frankfurt, G.A. Miller and M. Strikman,
P.L. B304(1993)1

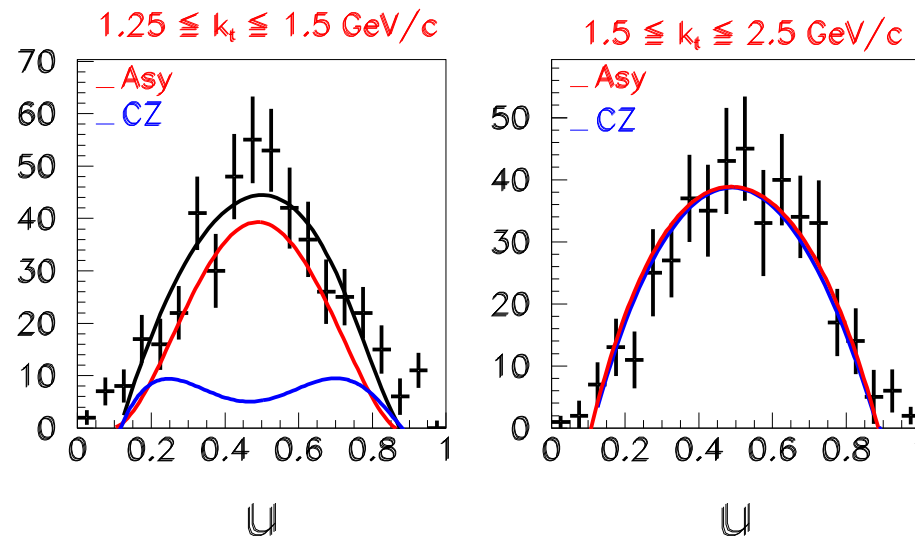
6. Cross-section Estimate

$$\frac{d^4\sigma_N}{dudM_J^2 \cdot d^2P_{N_t}} = 2.6 \text{ GeV}^{-6} \left(\frac{\text{GeV}}{\kappa_t} \right)^8 \phi^2(u), \quad (9)$$

“ with $g = 2$ and $L = 1\text{GeV}$. For $\kappa_t = 2 \text{ GeV}$ and at the maxima of $\phi(u)$ we find $\frac{d^3\sigma_N}{dx dM_T^2 d^2P_{N_t}} = 1.8(3.0) \times 10^{-3} \text{ GeV}^{-6}$ where the larger (smaller) value is obtained **using** ϕ_{cz} (ϕ_{as}) ”.

THE $q\bar{q}$ MOMENTUM WAVE FUNCTION MEASURED BY DI-JETS

Fermilab E791 Collaboration, PRL 86, 4768 (2001)



$$\underline{1.5 \text{ GeV}/c \leq k_t \leq 2.5 \text{ GeV}/c; \quad Q^2 \sim 16 \text{ (GeV}/c)^2 : \quad \phi^2 > 0.9 \phi_{Asy}^2}$$

$$\underline{1.25 \text{ GeV}/c \leq k_t \leq 1.5 \text{ GeV}/c; \quad Q^2 \sim 8 \text{ (GeV}/c)^2 :}$$

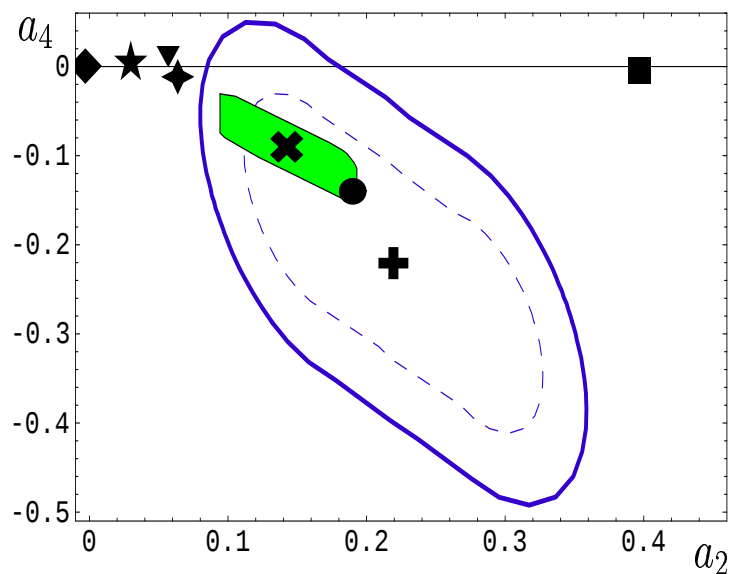
ϕ^2 contains contributions from CZ or other non-perturbative wave functions

CLEO and E791 data: A smoking gun for the pion distribution amplitude?

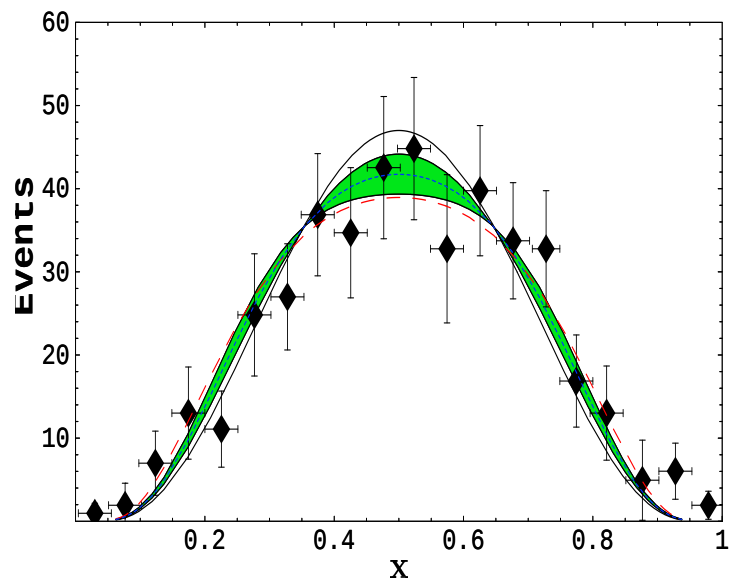
Alexander P. Bakulev, S. V. Mikhailov and N. G. Stefanis

$$\varphi_{\pi}^{BMS}(u) = \varphi_{\pi}^{as}(u) [1 + a_2^{opt} \cdot C_2^{3/2}(2u - 1) + a_4^{opt} \cdot C_4^{3/2}(2u - 1)],$$

CLEO



E791 high k_t



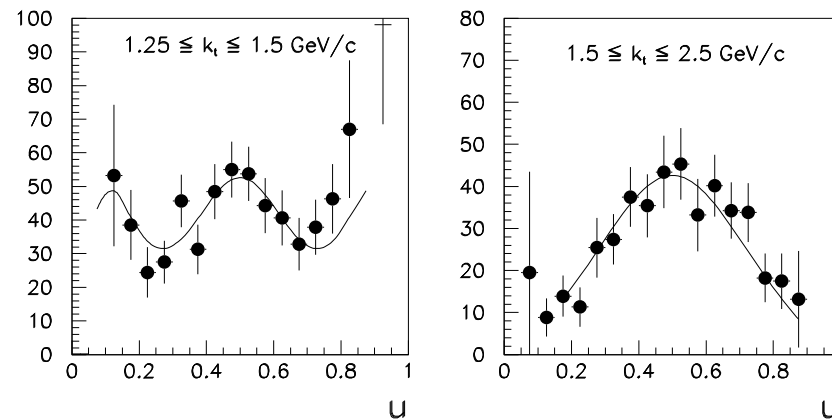
Fit to Gegenbauer Polynomials

Generate **Acceptance-Corrected** Momentum distributions

Assume $\frac{d\sigma}{du} \propto \phi_\pi^2(u, Q^2)$ in both $k_\perp$ regions

Fit distributions to:

$$\frac{d\sigma}{du} \propto \phi_\pi^2(u, Q^2) = 36u^2(1-u)^2 \left(1.0 + a_2 C_2^{3/2}(2u-1) + a_4 C_4^{3/2}(2u-1) \right)^2$$



For low k_t : $a_2 = 0.30 \pm 0.05$, $a_4 = (0.5 \pm 0.1) \cdot 10^{-2}$

For high k_t : $a_2 = a_4 = 0 \rightarrow$ **Asymptotic**

THE k_t DEPENDENCE OF DI-JETS YIELD

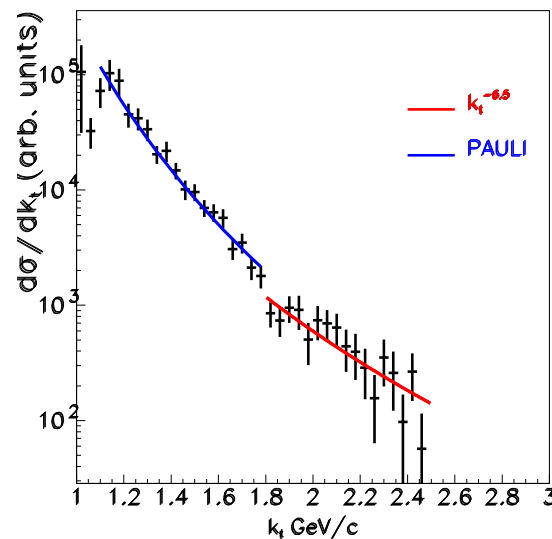
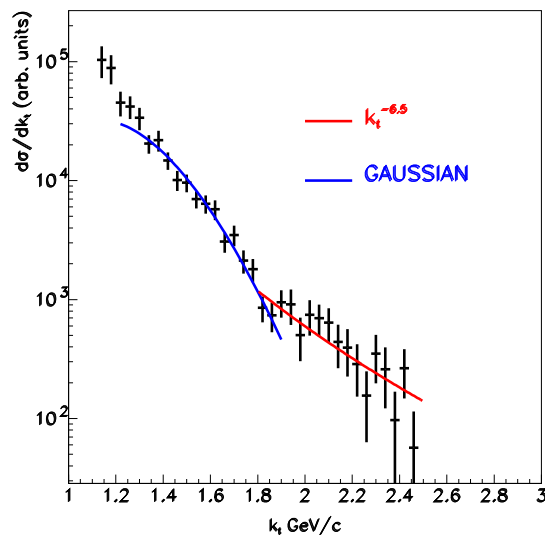
$$\frac{d\sigma}{dk_t^2} \propto \left| \alpha_s(k_t^2) G(x, k_t^2) \right|^2 \left| \frac{\partial^2}{\partial k_t^2} \psi(u, k_t) \right|^2$$

With $\psi \sim \frac{\phi}{k_t^2}$, weak $\phi(k_t^2)$ and $\alpha_s(k_t^2)$ dependences and $G(x, k_t^2) \sim k_t^{1/2}$: $\frac{d\sigma}{dk_t} \sim k_t^{-6}$

For low k_t :

Gaussian: $\psi \sim e^{-\beta k_t^2}$ (Jakob and Kroll)

Coulomb: $\psi(p) = \left(\frac{1}{1+p^2/p_a^2} \right)^2$ (Pauli)



Is $\sigma \propto \phi^2$??

hep-ph/0103275

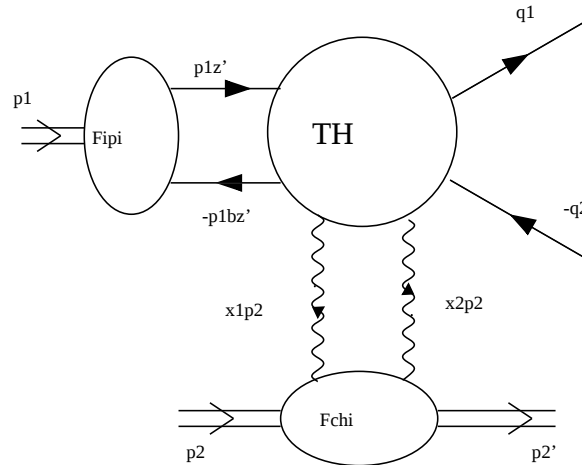
QCD factorization for the pion diffractive dissociation to two jets

V.M. BRAUN¹, D.YU. IVANOV^{1,2} A. SCHÄFER¹ and L. SZYMANOWSKI^{1,3}

hep-ph/0103295

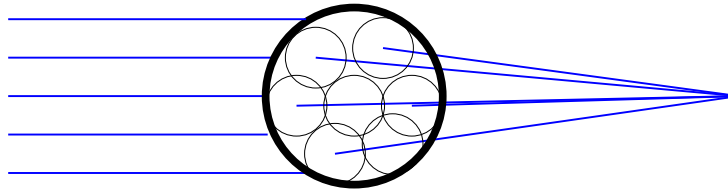
Has the E791 experiment measured
the pion wave function profile ?

Victor Chernyak



When measured in a heavy nucleus $\sigma \propto \phi^2$ (Brodsky, Frankfurt, Nikolaev, Braun...)

EXPECTED A-DEPENDENCE
FOR COLOR TRANSPARENCY



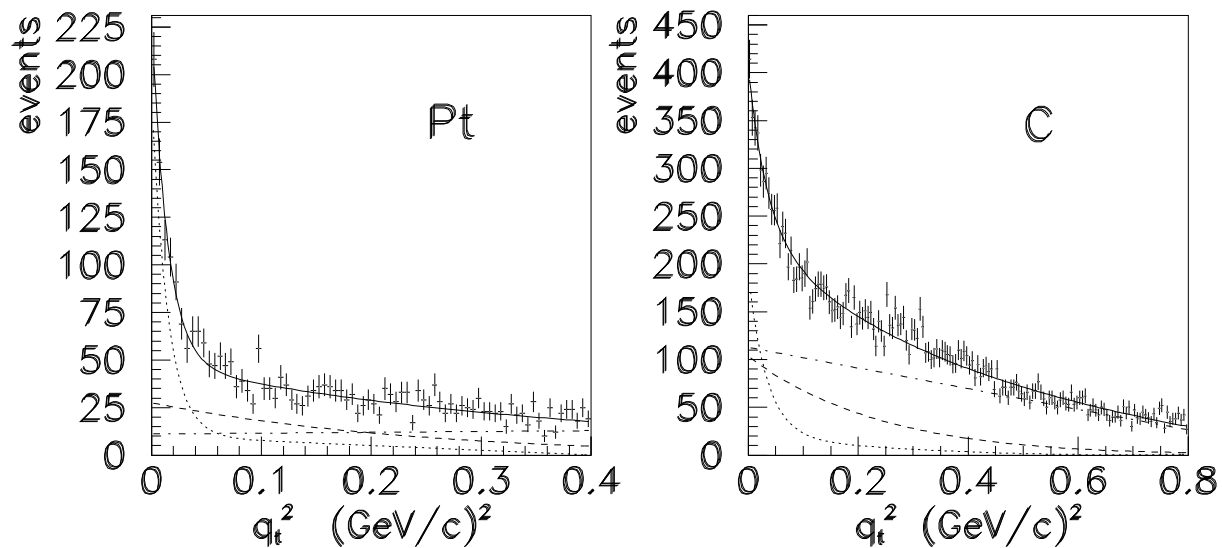
- Fully coherent interactions between pion and nucleons.
- Emerging Di-Jets do not interact with nucleus.

$$\mathcal{M}(\mathcal{A}) = \mathcal{A} \cdot \mathcal{M}(\mathcal{N})$$

$$\frac{d\sigma}{dq_t^2} \propto A^2 \quad q_t^2 \sim 0$$

$$\underline{\sigma \propto A^{4/3}}$$

E791 Collaboration, E. Aitala *et al.*, Phys. Rev. Lett. 86, 4773 (2001)



A-Dependence results: $\sigma \propto A^\alpha$

<u>k_t range (GeV/c)</u>	<u>α</u>	<u>α (CT)</u>
$1.25 < k_t < 1.5$	$1.64 +0.06 -0.12$	1.25
$1.5 < k_t < 2.0$	1.52 ± 0.12	1.45
$2.0 < k_t < 2.5$	1.55 ± 0.16	1.60

α (Incoh.) = 0.70 ± 0.1

Measurements of the photon light-cone wave function

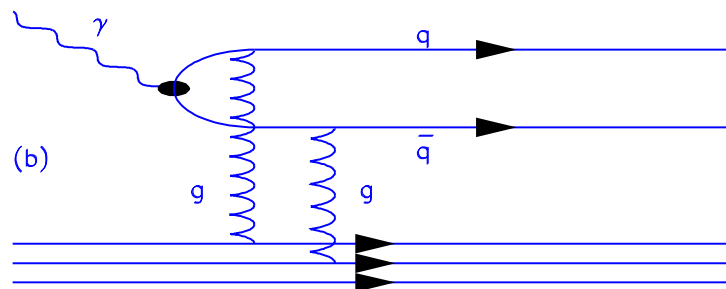
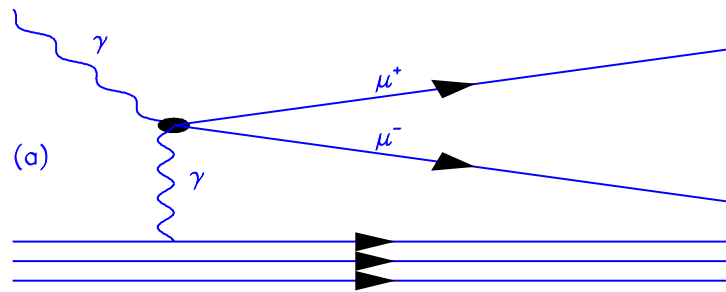
Fock state decomposition:

$$\begin{aligned}\psi_\gamma = & a|\gamma_p\rangle + b|l^+l^-\rangle + c|l^+l^-\gamma\rangle + (\textit{other e.m.}) + d|q\bar{q}\rangle + e|q\bar{q}g\rangle \\ & + (\textit{other had.}) + \dots\end{aligned}$$

Electromagnetic and Hadronic components

Real and Virtual Photons

Transverse and Longitudinal polarizations



The electromagnetic $|l^+l^- \rangle$ component of the photon

The wave function of the first component of a photon with virtuality Q^2 is¹:

$$\psi_{\lambda_1\lambda_2}^\lambda(k_\perp, u) = -ee_l \frac{\bar{l}_{\lambda_1}(k)\lambda \cdot \epsilon^\lambda l_{\lambda_2}(q-k)}{\sqrt{u(1-u)} \left(Q^2 + \frac{k_\perp^2 + m^2}{u(1-u)}\right)}$$

The distribution amplitude (squared) for transversely polarized photons:

$$\Phi_{\bar{l}l/\gamma_T^*}^2(u, k_\perp) \sim \sum_{\mu=1}^2 \frac{1}{4} \text{Tr} \psi_{\gamma^*}^2 = \frac{m_l^2 + k_\perp^2 [u^2 + (1-u)^2]}{[k_\perp^2 + a_l^2]^2}, \quad a_l^2 = m_l^2 + Q^2 u(1-u).$$

For longitudinally polarized photons:

$$\Phi_{\bar{l}l/\gamma_L^*}^2 \sim \frac{Q^2 [u^2(1-u)^2]}{[k_\perp^2 + a^2]^2}$$

(1)S. J. Brodsky, L. Frankfurt, J. F. Gunion, A. H. Mueller and M. Strikman, Phys. Rev. D50, 3134 (1994)

The hadronic $|q\bar{q}\rangle$ component of the photon

For $k_{\perp}^2 \gg \Lambda_{QCD}^2$ the wave function of the $|q\bar{q}\rangle$ component of a photon with virtuality Q^2 is the same as for the $|l^+l^-\rangle$ component.

The distribution for massive quarks and transversely polarized photons:

$$\Phi_{q\bar{q}/\gamma_T^*}^2(u, k_{\perp}) \sim \frac{m_q^2 + k_{\perp}^2[u^2 + (1-u)^2]}{[k_{\perp}^2 + a_q^2]^2}$$

where:

$$a_q^2 = m_q^2 + Q^2 u(1-u).$$

For low $k_{\perp}^2$ other predictions:

1. Instanton models
(1999)

Petrov *et al.*, Phys.Rev. D59, 11401

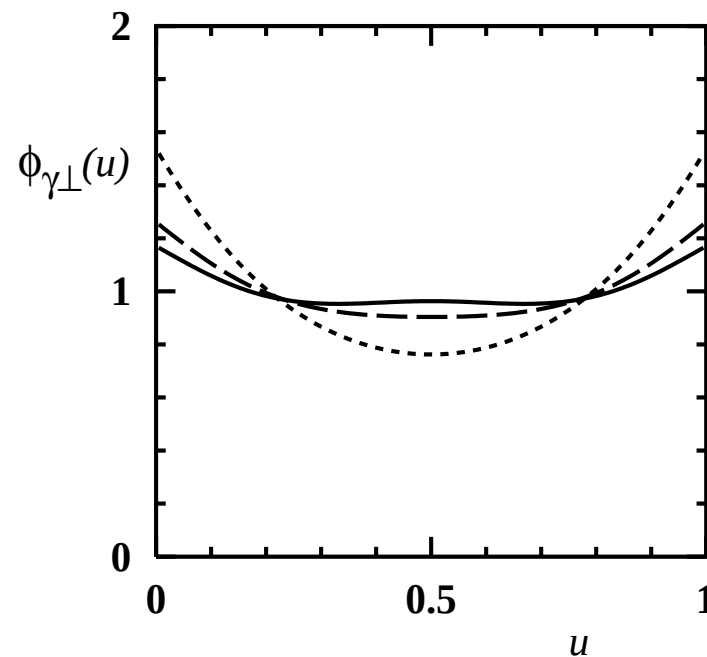
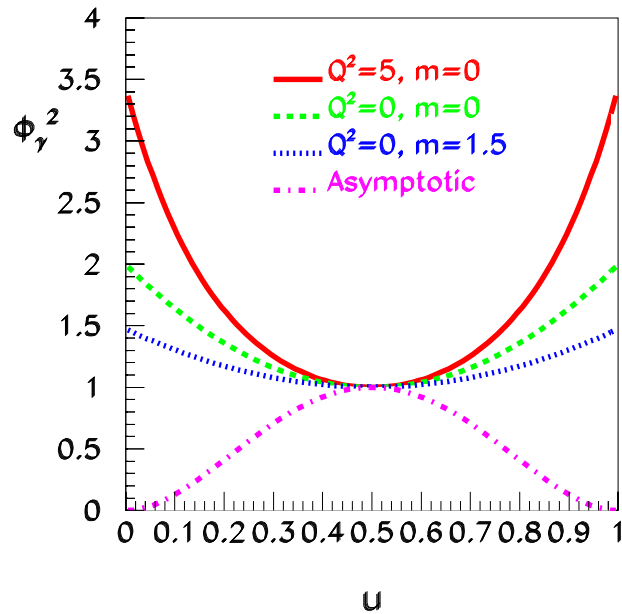
2. Asymptotic distribution: $\Phi_{q\bar{q}/\gamma}^2 \sim u^2(1-u)^2$ Balitsky *et al.*, Nucl. Phy. B312, 509 (1989)

Φ Distributions of $|l^+l^- \rangle, |q\bar{q} \rangle$ components of the photon

Instanton Wave Functions, real photons (solid line), virtual

Perturbative Wave functions

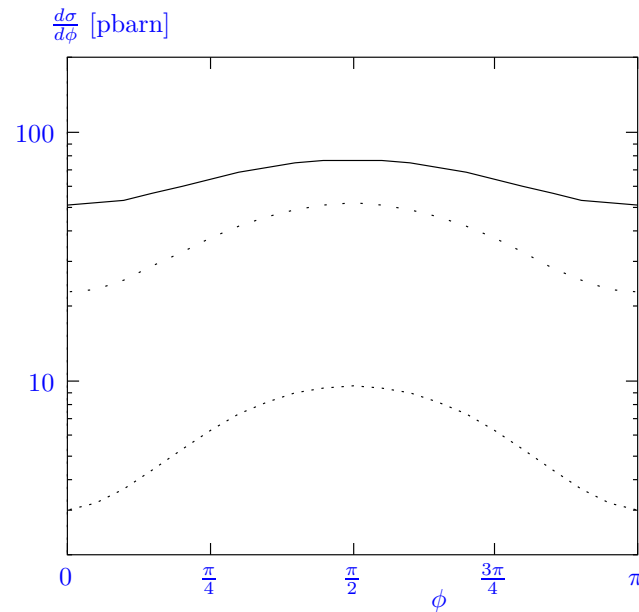
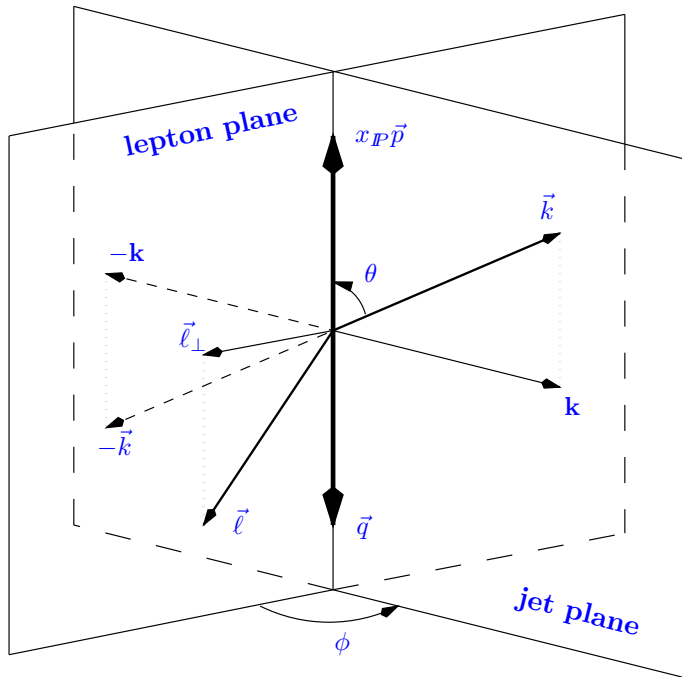
$Q^2 = 250 \text{ MeV}^2$ (dashed line), $Q^2 = 500 \text{ MeV}^2$ (dotted line).



ϕ Distribution for $q\bar{q}$ Diffractive Dissociation to Dijets

J. Bartels *et al.*, Phys. Lett. **B386**, 389 (1996)

$$d\sigma_D^{e^-p} = \frac{\alpha_{em}}{yQ^2\pi} \left[\frac{1 + (1-y)^2}{2} d\sigma_{D,T}^{\gamma^*p} - 2(1-y) \frac{\frac{k_t^2}{M^2}}{1 - 2\frac{k_t^2}{M^2}} \cos 2\phi d\sigma_{D,T}^{\gamma^*p} \right. \\ \left. + (1-y) d\sigma_{D,L}^{\gamma^*p} + (2-y) \sqrt{(1-y)} \cos \phi d\sigma_{D,I}^{\gamma^*p} \right]$$



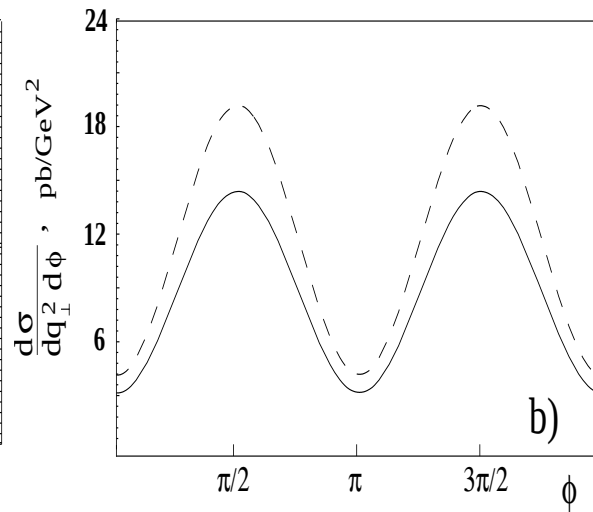
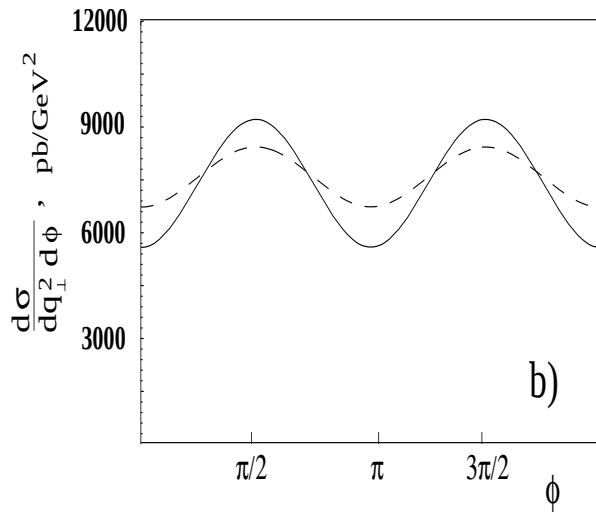
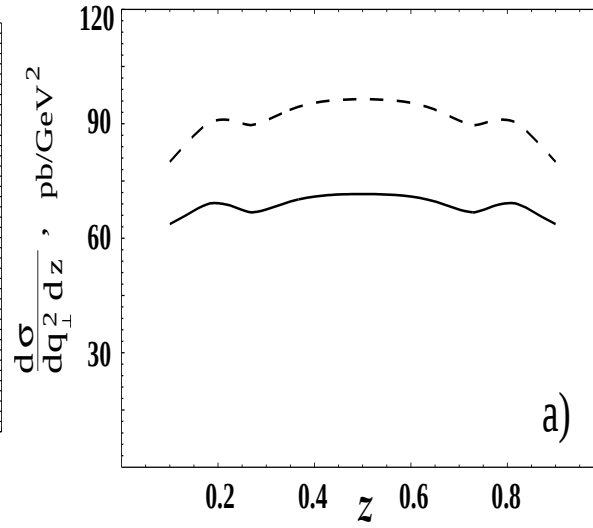
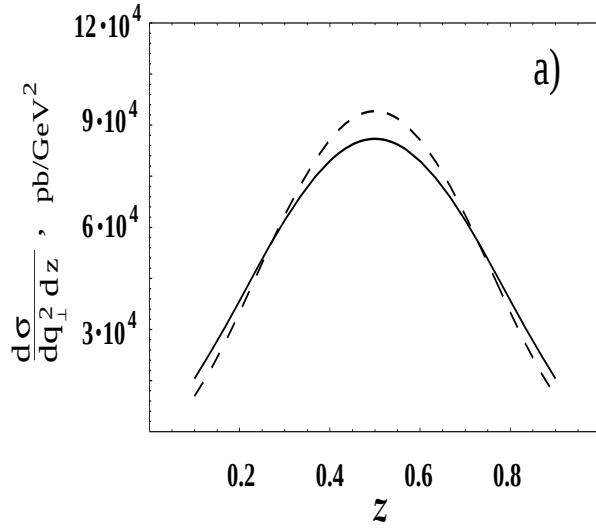
Photoproduction: V.M. Braun *et al.* PRL 89 (2002) 172001

$k_{\perp} = 2\text{GeV}/c$, chiral-odd

$\uparrow\uparrow, L_z = 0$

$k_{\perp} = 5\text{GeV}/c$, chiral-even

$\uparrow\downarrow, L_z = 1$



Measurements of the photon light-cone wave function ZEUS/HERA/DESY

Channels:

$$\gamma p \rightarrow \mu^+ \mu^- p$$

$$\gamma^* p \rightarrow 2J p$$

$$\gamma^* p \rightarrow \pi^+ \pi^- p$$

Janusz Szuba, UMM Cracow

Iuliana Cohen, TAU

Eyal Nevo, TAU

Justyna Ukleja, Warsaw U.

Janusz Szuba, UMM Cracow

Justyna Ukleja, Warsaw U.

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....

Electromagnetic component of LCWF:

Photoproduction of DiMuons (Bethe-Heitler)

$$\left. \frac{d\sigma_T}{dt \, du \, dk_t^2} \right|_{t=0} \propto \text{Tr} \left| \frac{\partial}{\partial k_\mu} \psi_\mu^T \right|^2$$

$$\frac{d\sigma_T}{dt \, du \, dk_t^2} \propto \frac{4m_l^2 k_t^2 + 2(k_t^4 + a^4)[u^2 + (1-u)^2]}{(a^2 + k_t^2)^4}$$

$$a^2 = Q^2 u(1-u) + m_l^2.$$

For real photons and using $m_l = 0 \rightarrow a = 0$:

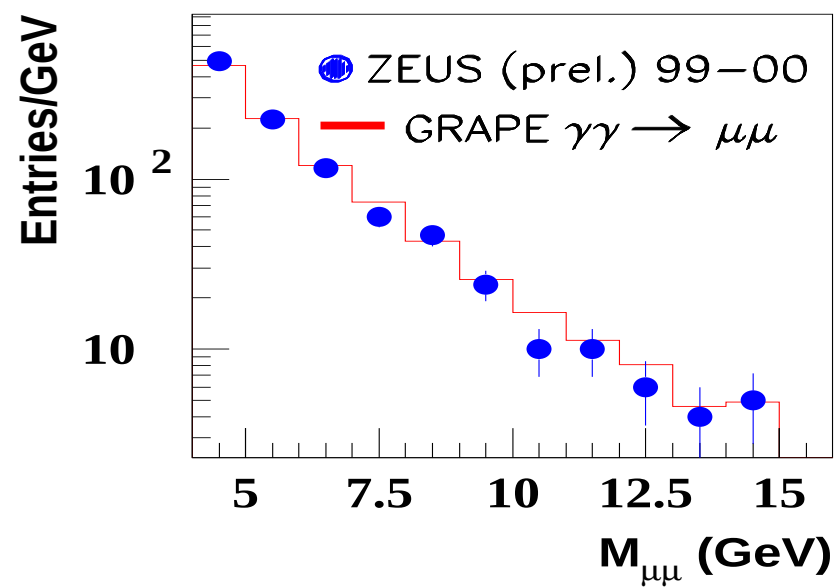
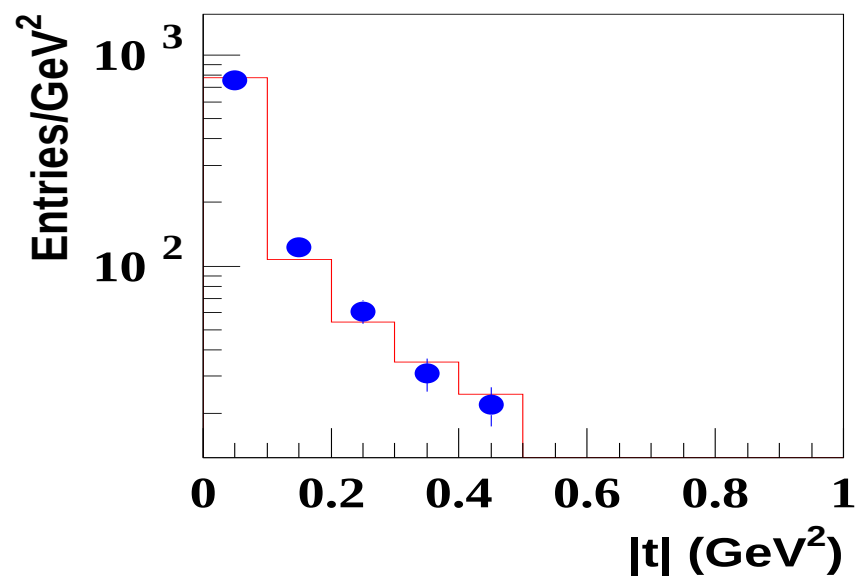
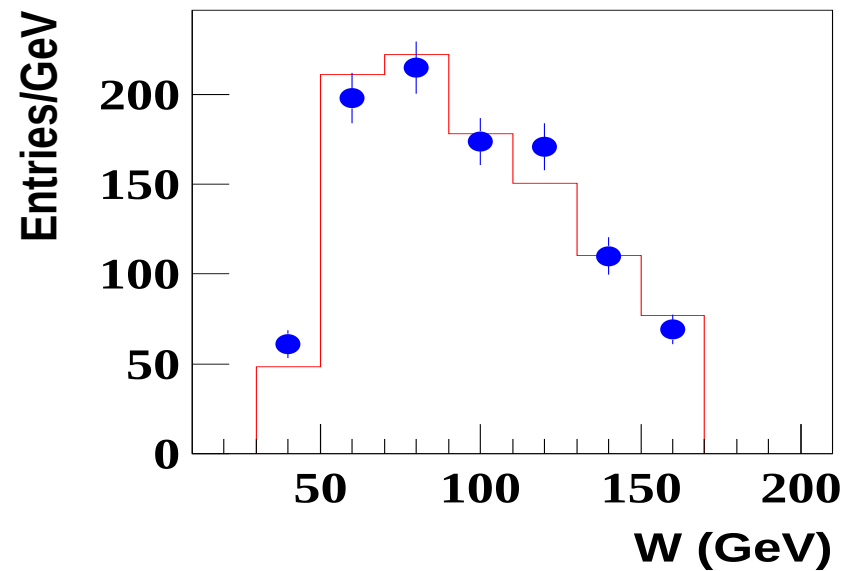
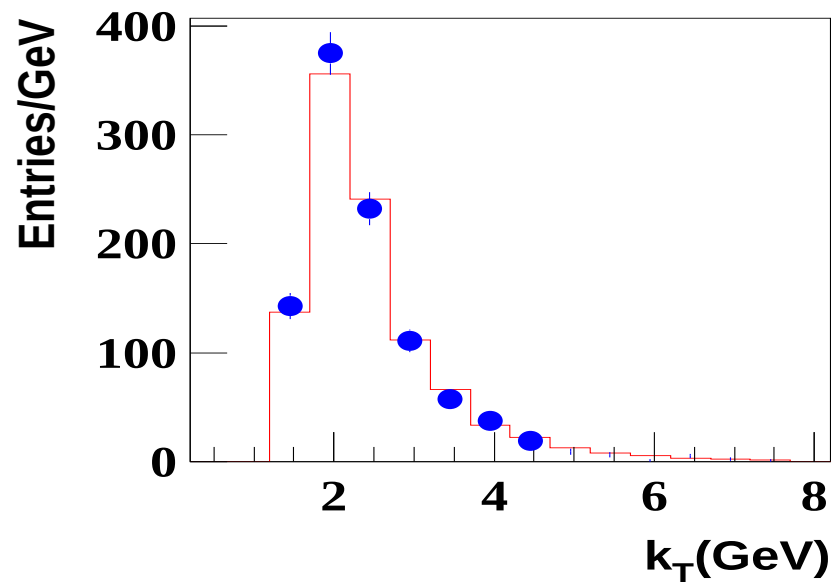
$$\frac{d\sigma_T}{dt \, du \, dk_t^2} \propto \frac{2[u^2 + (1-u)^2]}{k_t^4} \sim \frac{\Phi^2}{k_t^2}.$$



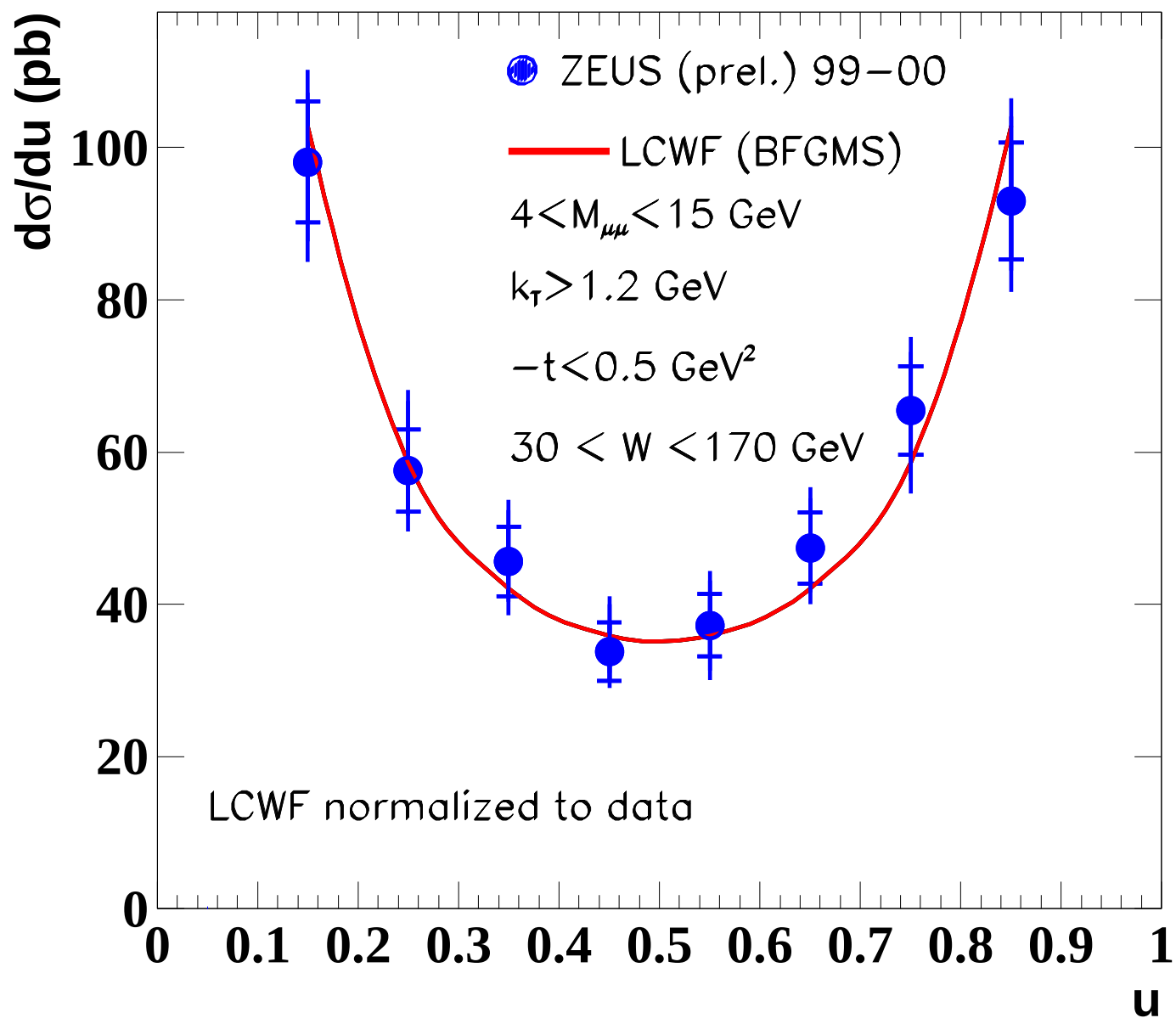
Event Selection for $\gamma p \rightarrow \mu^+ \mu^- p$

- μ Trigger
- Proton did not disintegrate
- Elasticity (only 2μ in event)
- Diffractive (small t)
- $4 \leq M_{\mu^+\mu^-} \leq 15\text{GeV}$ (avoid resonances)
- Various cleaning cuts

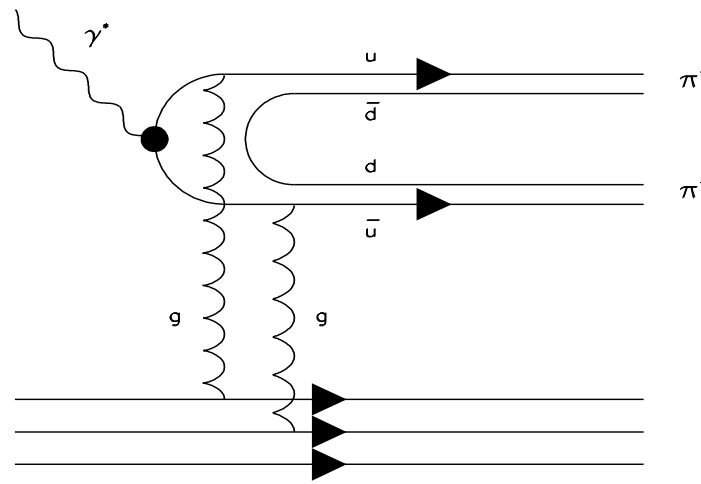
ZEUS



ZEUS



Hadronic component - special case: $\gamma^* p \rightarrow \pi^+ \pi^- p$



Relation to pion Time-Like form factor ?

$$\frac{\sigma(\gamma^* + p \rightarrow 2\pi + p)}{\sigma(\gamma^* + p \rightarrow X + p)} \propto |F_\pi|^2$$

Pion quantum numbers ? Longitudinal/Transverse ?

Pomeron - Odderon interference

The Odderon: $3g$ color singlet, Charge-parity $C = -1$

$C(\pi^+\pi^-) = (-)^\ell$: produced by both Pomeron and Odderon.

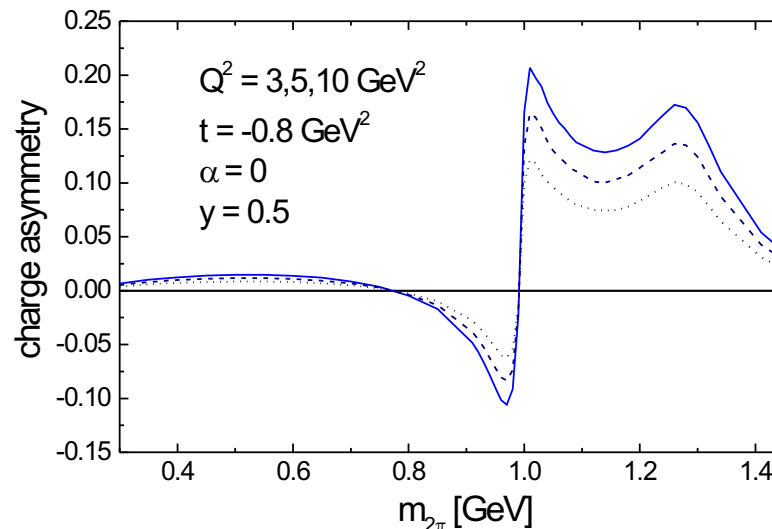
Pomeron-Odderon Interference:

Brodsky, Rathsman and Merino, Phys. Lett. B461, 114 (1999)

Results in charge asymmetry:

$$A = \frac{u(\pi^+) - u(\pi^-)}{u(\pi^+) + u(\pi^-)}$$

Hagler, Szymanowski and Teryaev Phys. Lett. B535, 117 (2002):

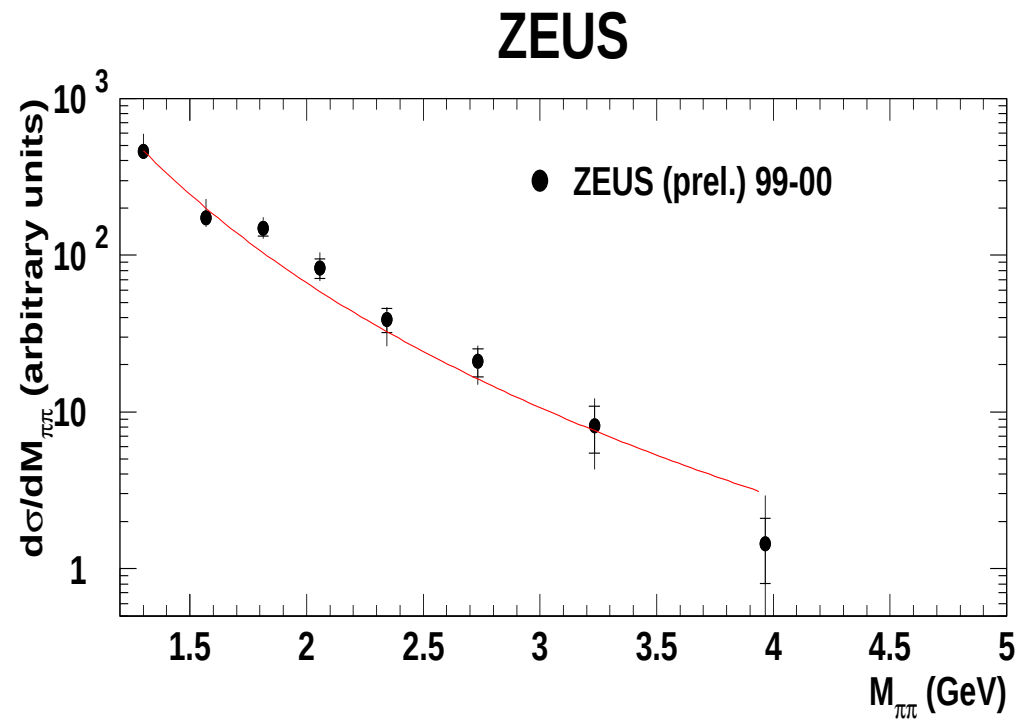


Event Selection for $\gamma^* p \rightarrow \pi^+ \pi^- p$

- $E_{e'} > 10 \text{ GeV}$
- Proton did not disintegrate
- Pion identification by Neural Net
- Elasticity (only 2π in event)
- Various cleaning cuts
- Diffractive (small t)
- $1.2 \leq M_{\pi^+\pi^-} \leq 5 \text{ GeV}$
- $2 < Q^2 < 20 \text{ GeV}^2$
- $40 < W < 120 \text{ GeV}$

$$\beta = \frac{Q^2}{Q^2 + M_X^2}$$

Mass Dependence

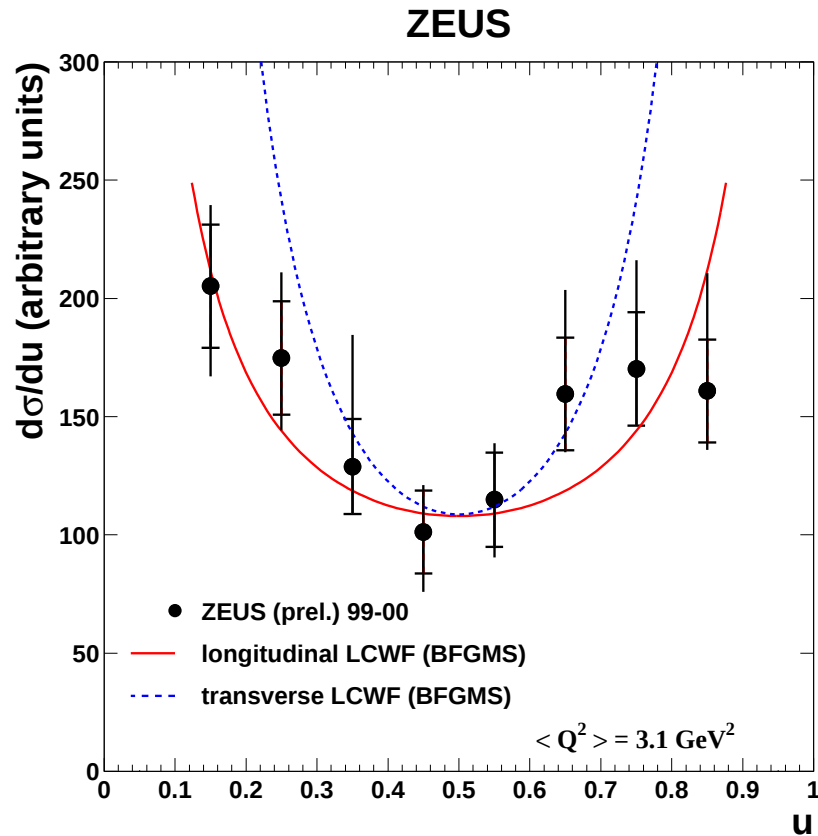


Fit : $M_{\pi\pi}^{-4.5}$

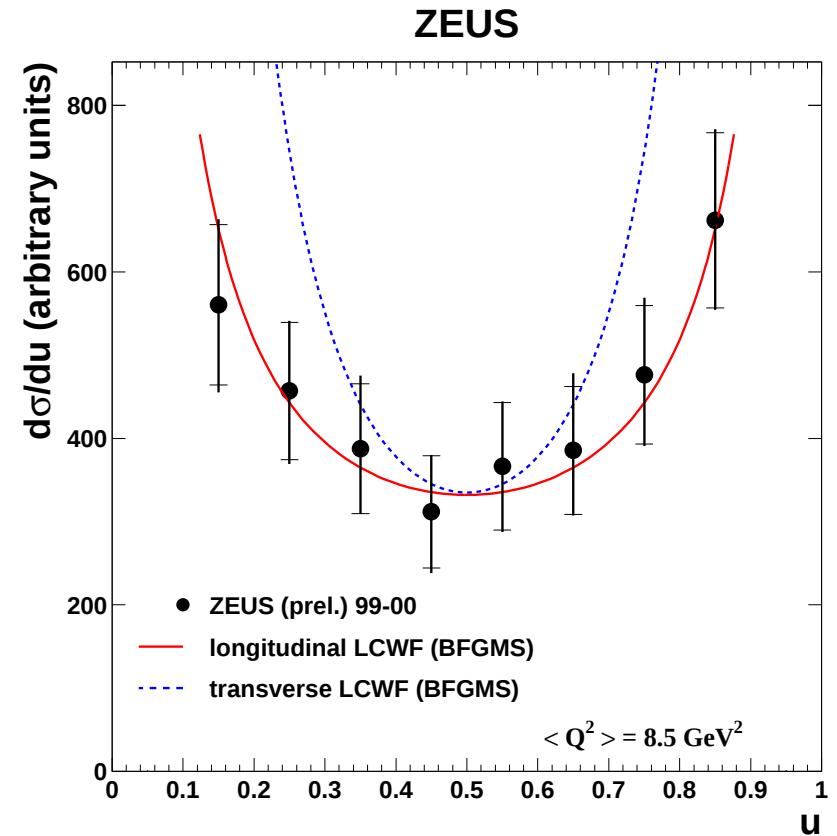
Future derivation of Time-Like $|F_{\pi}|^2$

u Dependence

D. Ashery
Tel Aviv University



$$\langle \beta \rangle = 0.52$$



$$\langle \beta \rangle = 0.75$$

Longitudinal photon fluctuating to $q\bar{q}$.

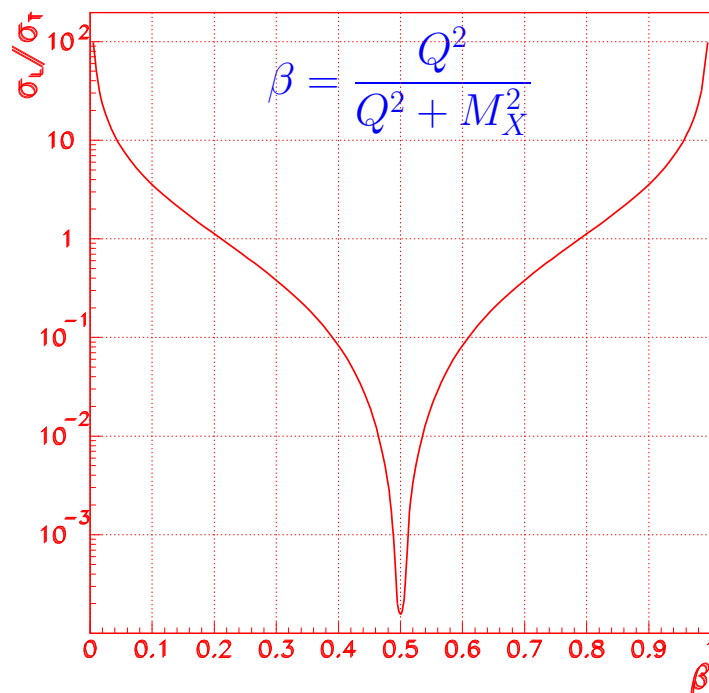
Cross section for diffractive dissociation to $q\bar{q}$:

$$\left. \frac{d\sigma}{dt \, du \, dk_t^2} \right|_{t=0} \propto |Tr \Delta \psi|^2. \quad \text{For } m_q = 0 :$$

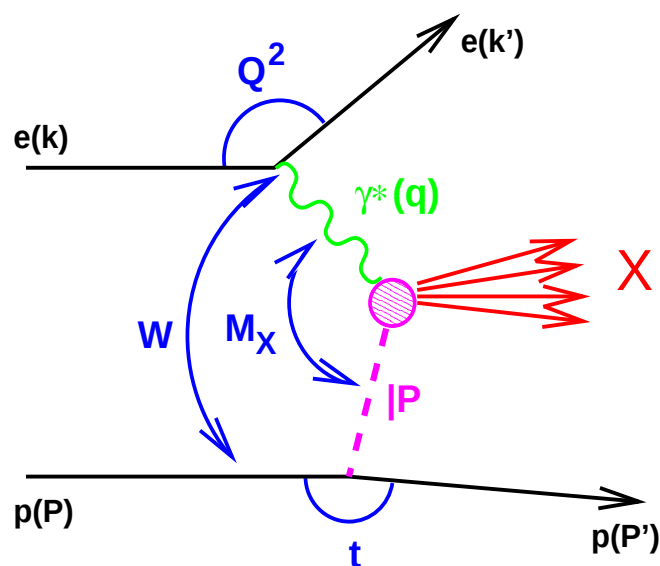
$$\frac{d\sigma_L}{dt \, du \, dM^2} = \frac{\pi \alpha_s^2}{9} e^2 Q^2 \sum e_q^2 (xg)^2 \cdot \frac{(Q^2 - M^2)^2}{(Q^2 + M^2)^6} \cdot \frac{1}{u(1-u)}$$

$$\frac{d\sigma_T}{dt \, du \, dM^2} = \frac{\pi \alpha_s^2}{18} e^2 \sum e_q^2 (xg)^2 \cdot \frac{8Q^4 M^2 [u^2 + (1-u)^2]}{(Q^2 + M^2)^6 u^2 (1-u)^2}.$$

$u = 0.5$:



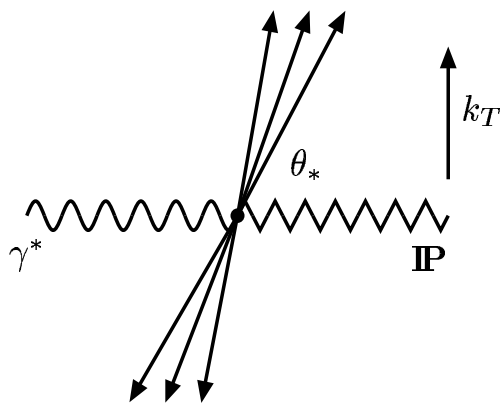
Kinematics of diffractive DIS



M_X : mass of the diffractive system

$x_{\text{IP}} = \frac{M_X^2 + Q^2}{W^2 + Q^2}$: fraction of proton momentum carried by IP

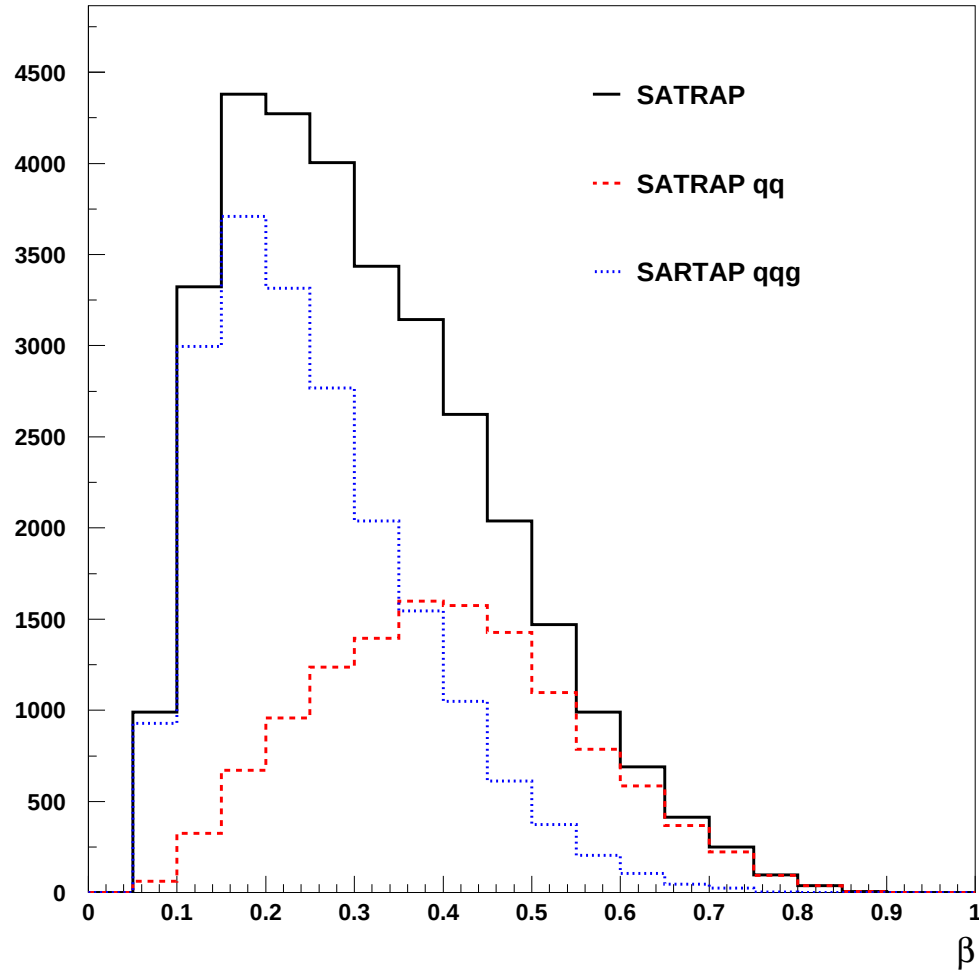
$\beta = \frac{Q^2}{M_X^2 + Q^2}$: fraction of IP momentum which enters the interaction



$u = \frac{1 + \cos \theta^*}{2}$: Longitudinal momentum fraction

k_t : transverse momentum of jets in γ^* -IP CM frame

Selection of $q\bar{q}$ dijets using β :



For $\beta > 0.45$, 23% $q\bar{q}g$ background

Event Selection for $\gamma^* p \rightarrow DJ$

- $E_{e'} > 10 \text{ GeV}$
- Proton did not disintegrate
- Jet identification with clustering algorithm
- Elasticity (only 2 jets in event)
- Various cleaning cuts
- Diffractive (small t)
- $5 \leq M_{DJ} \leq 30 \text{ GeV}$
- $10 < Q^2 < 500 \text{ GeV}^2$
- $100 < W < 200 \text{ GeV}$
- $0.01 < y < 0.9$
- $k_t > 1.25 \text{ GeV}$
- $\beta > 0.45$, Test by ϕ Angular Distribution
- $0.1 < u < 0.9$
- $0.00001 < x_P < 0.015$

For experimental results....

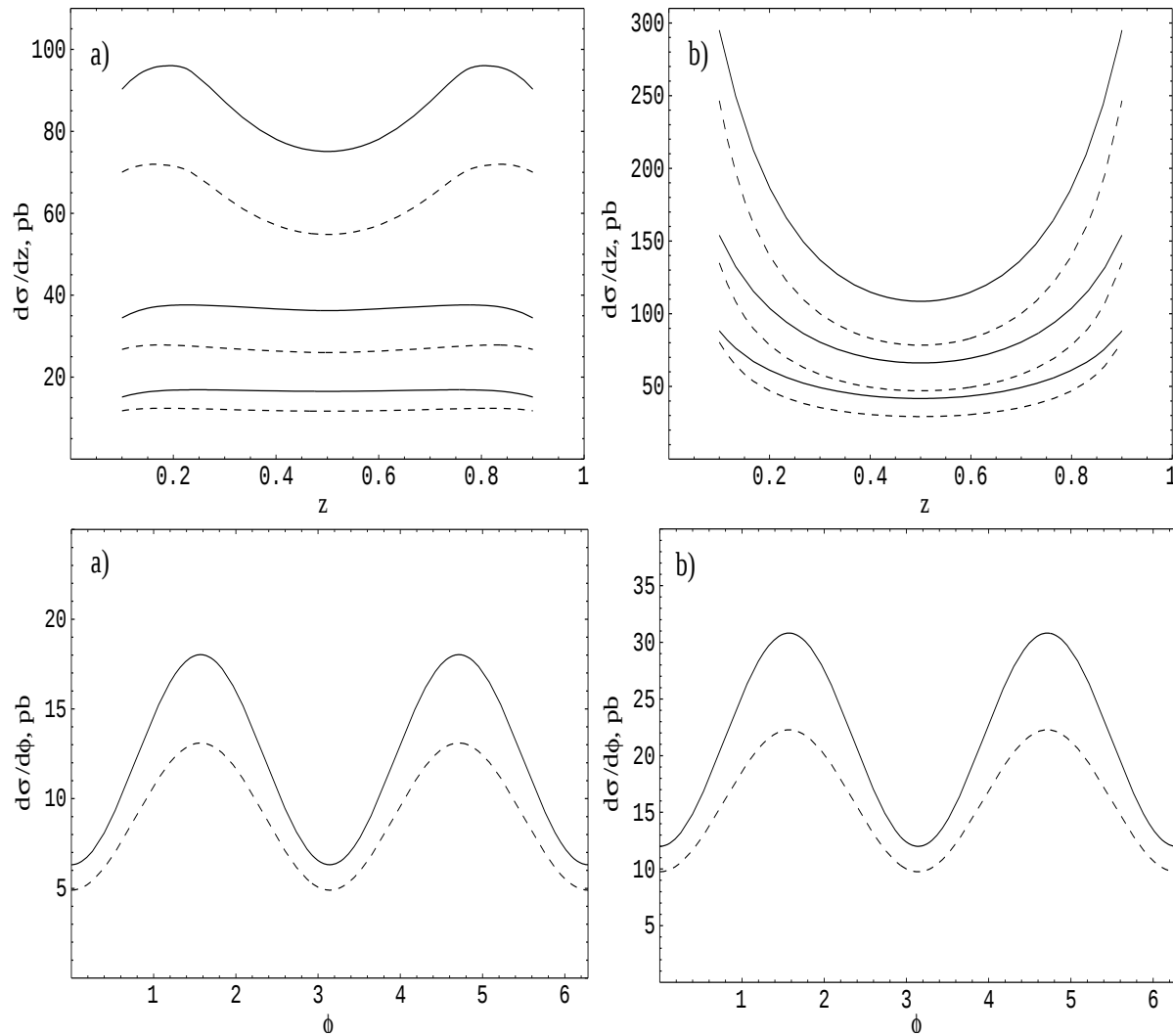
stay tuned

Electroproduction: V.M. Braun and D.Yu. Ivanov, hep-ph/0505263

$k_{\perp}=1.25, 1.5, 1.75 \text{ GeV}/c$; Solid: CTEQ6L, dashed: MRST2001LO

$\beta > 0.5$

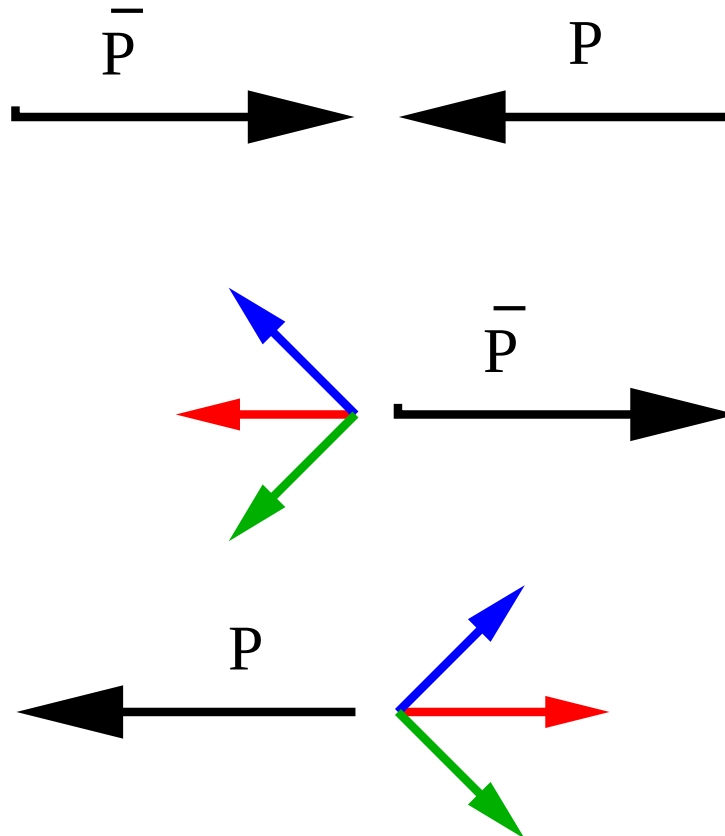
$\beta > 0$



The Proton Light-Cone Wave Function

1. HERA: $p e \rightarrow 3J e'$

2. Fermilab Collider: $p \bar{p} \rightarrow 3J p$, use Roman Pots.



Summary

- Diffractive dissociation of hadrons and photons can be used to study their internal quark structure.
- The momentum wave function of the $|q\bar{q}\rangle$ in the pion is described well at $Q^2 > 10 \text{ GeV}^2$ by the Asymptotic wave function.
- For lower Q^2 values the momentum wave function of the $|q\bar{q}\rangle$ in the pion contains 2^{nd} and 4^{th} Gegenbauer Polynomials with coefficients: $a_2 = 0.30 \pm 0.05$, $a_4 = (0.5 \pm 0.1) \cdot 10^{-2}$.

- Measurements of the photon **electromagnetic** light-cone wave functions are completed and the results are in agreement with QED.
- This provides the first proof that diffractive dissociation of particles can be reliably used to measure their light cone wave functions.

- Measurements of the photon **hadronic** light-cone wave functions are in progress.
- Photon dissociation $\gamma^* p \rightarrow \pi^+ \pi^- p$ is dominated by **Longitudinal** photons fluctuating to $q\bar{q}$. Charge asymmetry as signal of the Odderon being studied.
- Photon dissociation $\gamma^* p \rightarrow J J p$ is dominated by **Transverse** photons fluctuating to $q\bar{q}$ as observed in the azimuthal angular distribution.