

The structure of a bound nucleon

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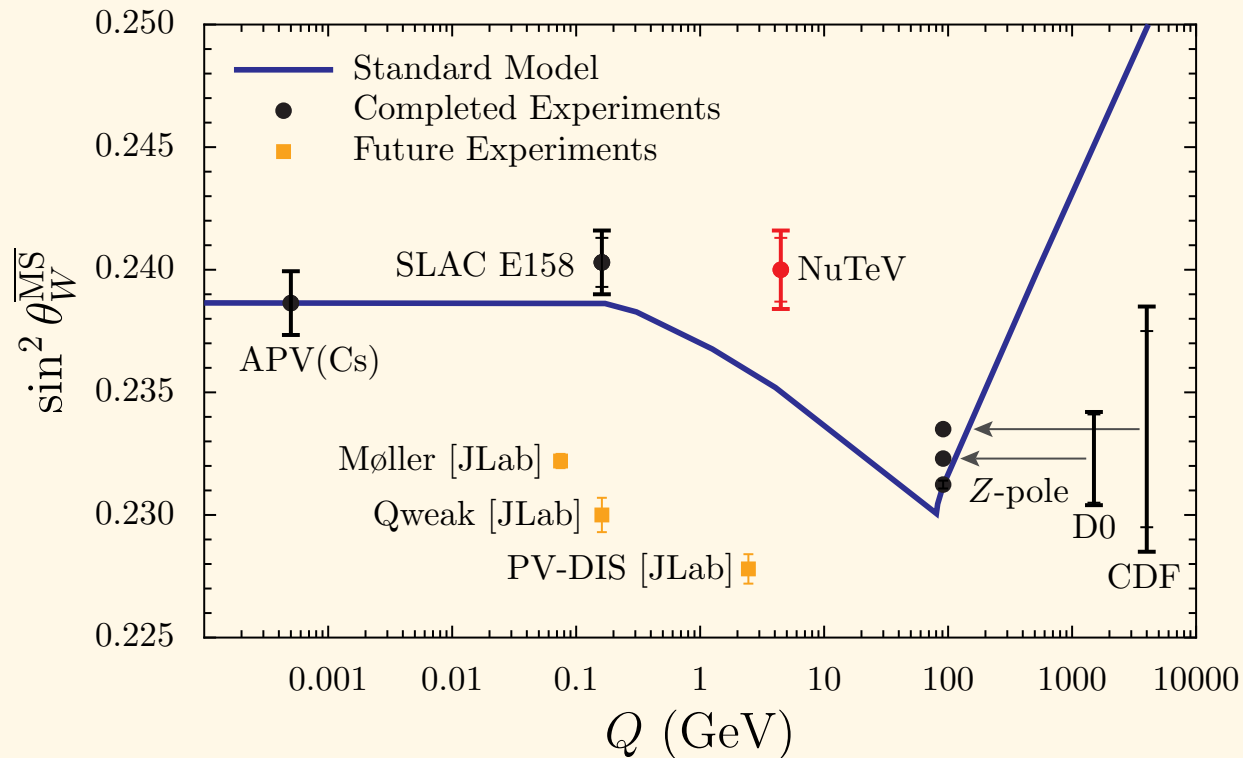
Tony's 60–Fest

15 – 19 February 2010

Theme

- Gain insights into nuclear structure from a QCD viewpoint
- Highlight opportunities provided by nuclear systems to study QCD
- Present complementary approach to traditional nuclear physics
 - ❖ formulated as a covariant quark theory
 - ❖ grounded in good description of mesons and baryons
 - ❖ at finite density self-consistent mean-field approach
- Fundamental difference
 - ❖ bound nucleons differ from free nucleons
 - ❖ **medium modification** – effects typically $\sim 10\text{--}20\%$
- Possible answers to many long standing questions: we address
 - ❖ **the EMC effect** [European Muon Collaboration]
 - ❖ **the NuTeV anomaly** [Neutrinos at the Tevatron]

Weak mixing angle and the NuTeV anomaly

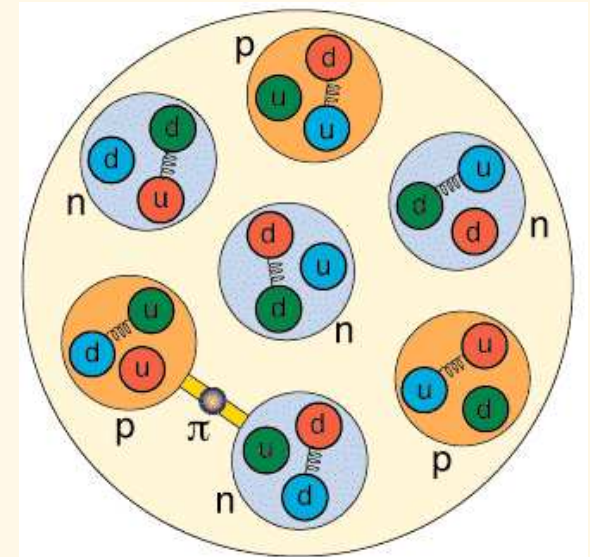
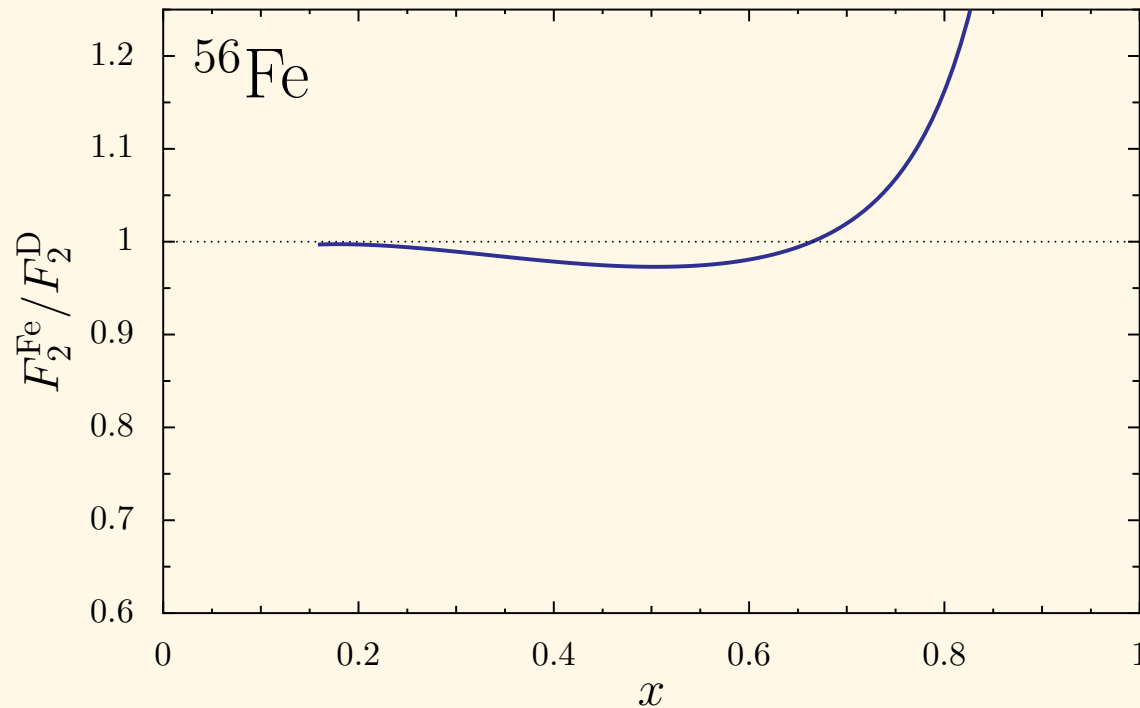


- NuTeV: $\sin^2 \theta_W = 0.2277 \pm 0.0013(\text{stat}) \pm 0.0009(\text{syst})$

❖ G. P. Zeller *et al.* Phys. Rev. Lett. **88**, 091802 (2002)

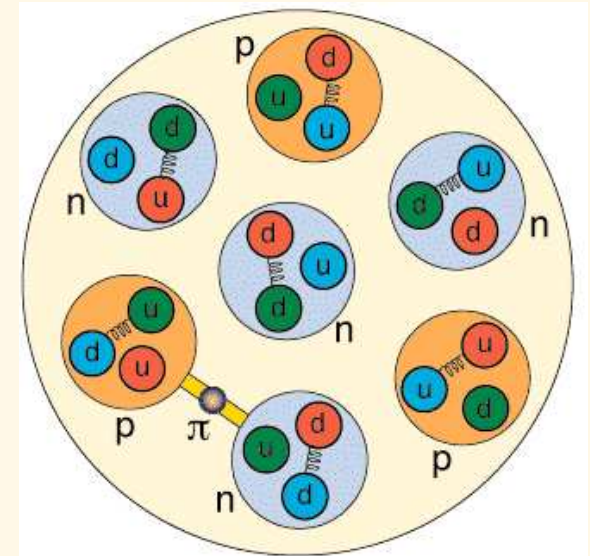
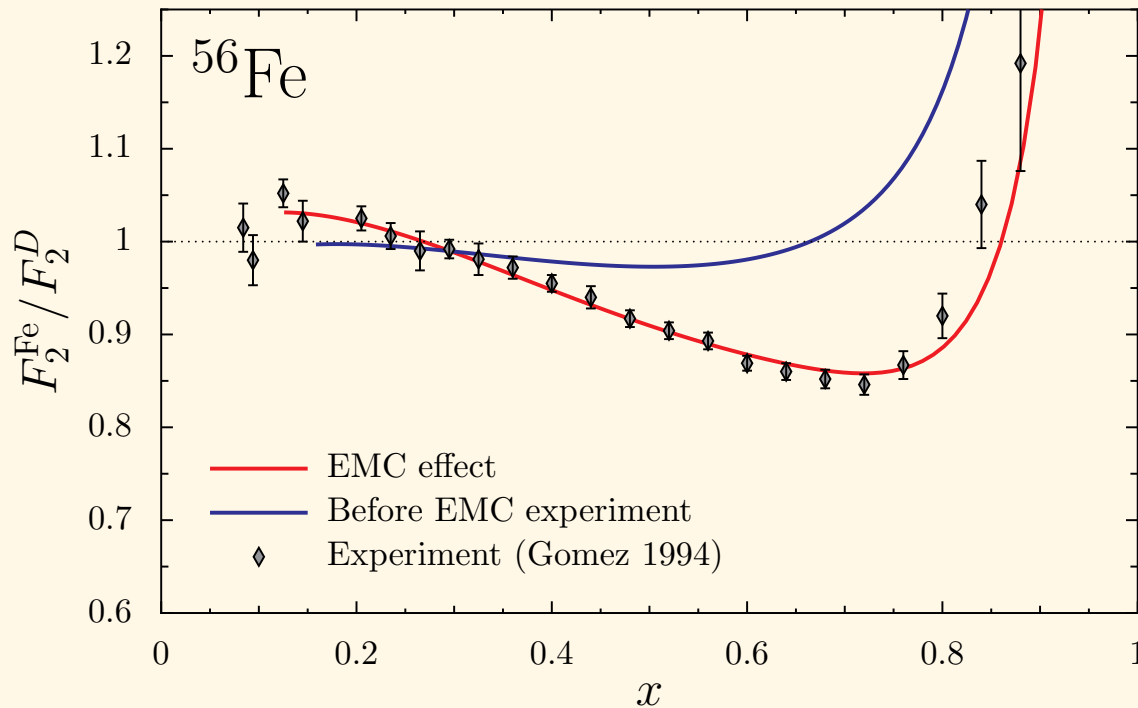
- World average $\sin^2 \theta_W = 0.2227 \pm 0.0004$: $3 \sigma \implies$ “NuTeV anomaly”
- Huge amount of experimental & theoretical interest [over 400 citations]
- No universally accepted complete explanation

EMC Effect



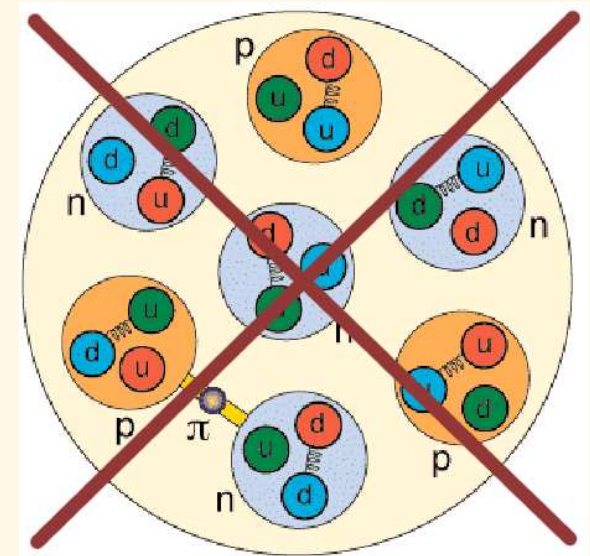
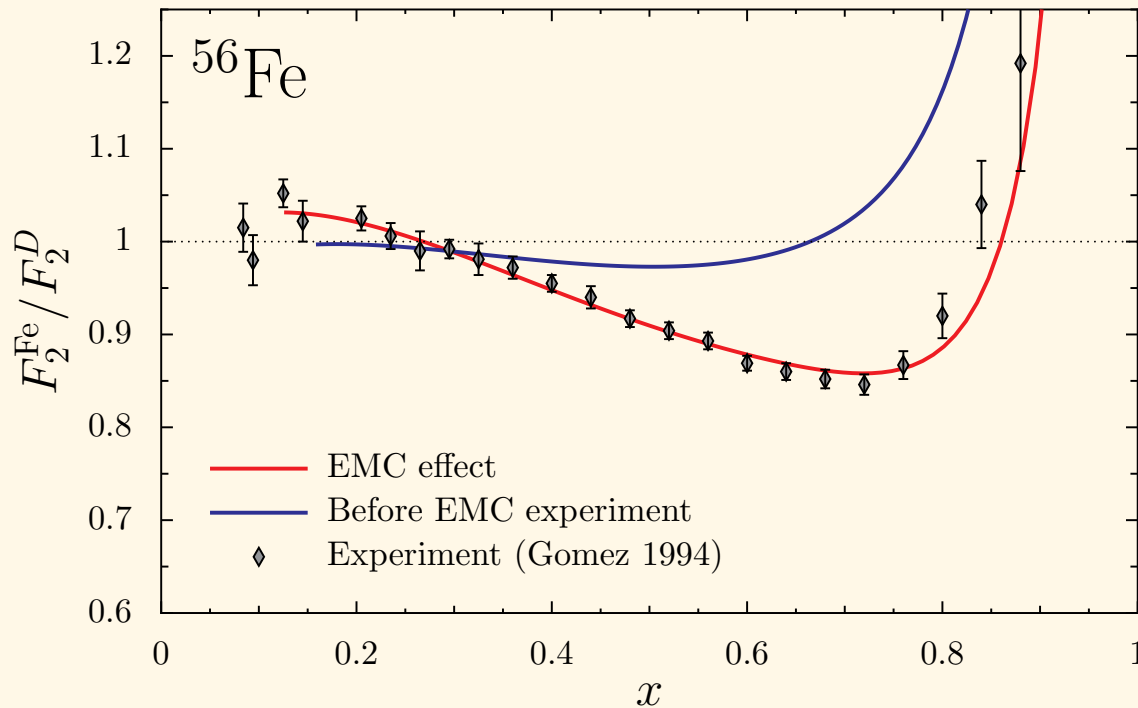
- Pre-1983: before the EMC experiment
- Nucleon quark distributions unchanged in medium
- Long distance nuclear effects not expected to influence “short distance” quark physics
- Fermi motion of nucleons dominate at large x

EMC Effect



- J. J. Aubert *et al.* [European Muon Collaboration], *Phys. Lett. B* **123**, 275 (1983).
- Immediate parton model interpretation:
 - ❖ valence quarks in nucleus carry less momentum than in nucleon
- Nuclear effects do influence quark physics
- What is the mechanism? After 25 years no consensus
- EMC \iff medium modification \iff NuTeV anomaly?

EMC Effect



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- EMC \iff medium modification \iff NuTeV anomaly?

Medium Modification

- What does this mean?
- 50 years of traditional nuclear physics tells us that the nucleus is composed of nucleon-like objects
- However if a nucleon property is not protected by a symmetry its value may change in medium e.g.
 - ❖ mass, magnetic moments, radii
 - ❖ quark distributions, form factors, GPDs, etc
- There must be medium modification:
 - ❖ nucleon propagator is changed in medium
 - ❖ off-shell effects: in-medium nucleon has 12 form factors
 - consequently for example $F_{1p}(Q^2 = 0) \neq 1$
- Need to understand these effects as first step toward QCD based understanding of nuclei

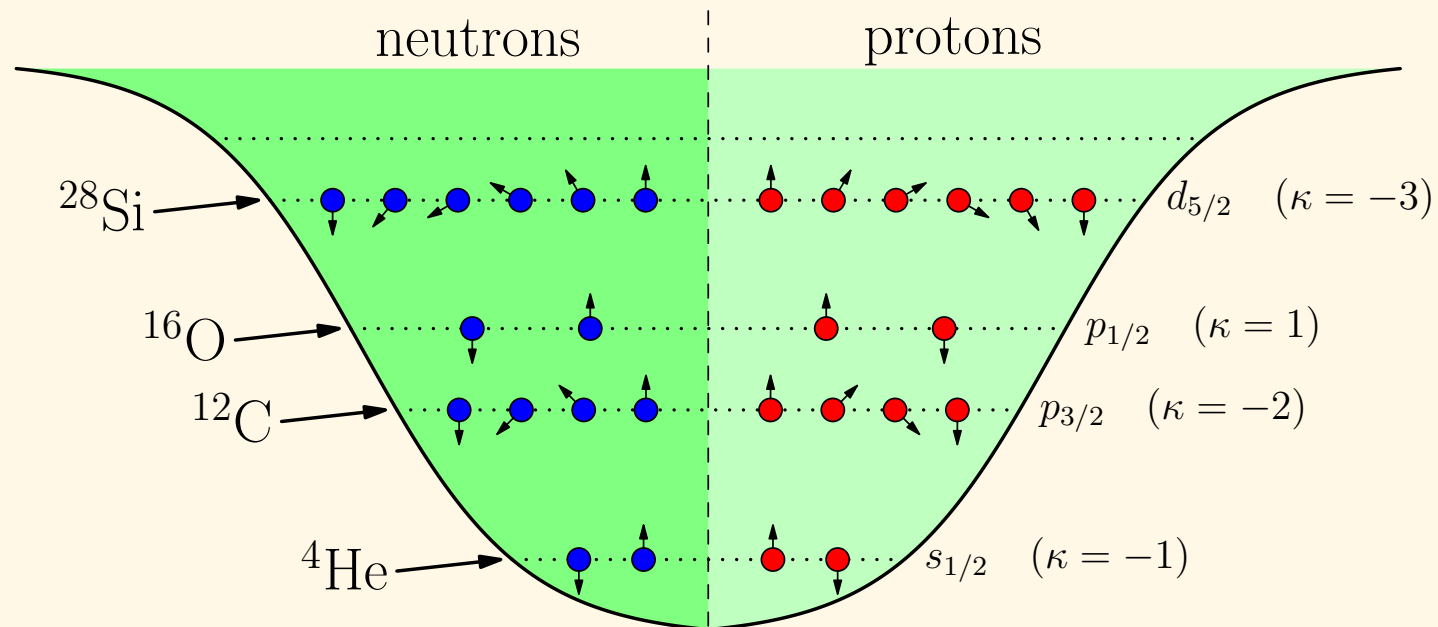
Finite Nuclei quark distributions

- Definition of finite nuclei quark distributions

$$q_A(x_A) = \frac{P^+}{A} \int \frac{d\xi^-}{2\pi} e^{\frac{iP^+ x_A \xi^-}{A}} \langle A, P | \bar{\psi}_q(0) \gamma^+ \psi_q(\xi^-) | A, P \rangle$$

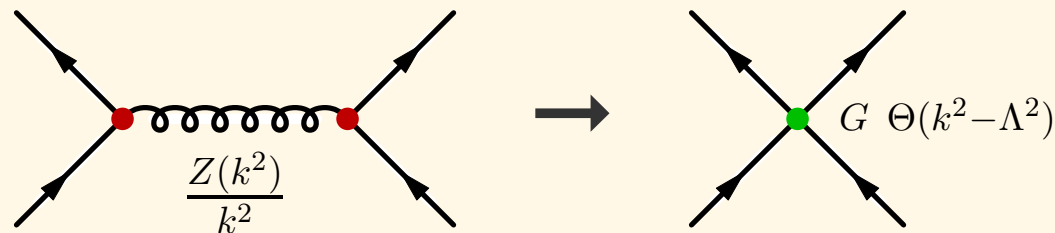
- Approximate using a modified convolution formalism

$$q_A(x_A) = \sum_{\alpha, \kappa, m} \int dy_A \int dx \delta(x_A - y_A x) f_{\alpha, \kappa, m}(y_A) q_{\alpha, \kappa}(x)$$

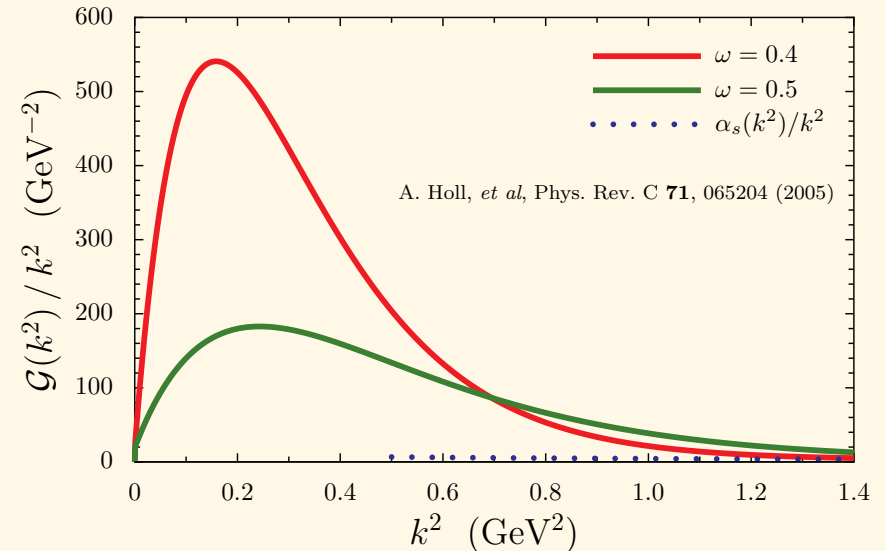


Nambu–Jona-Lasinio Model

- Interpreted as low energy chiral effective theory of QCD



- Can be motivated by infrared enhancement of gluon propagator e.g. DSEs and Lattice QCD

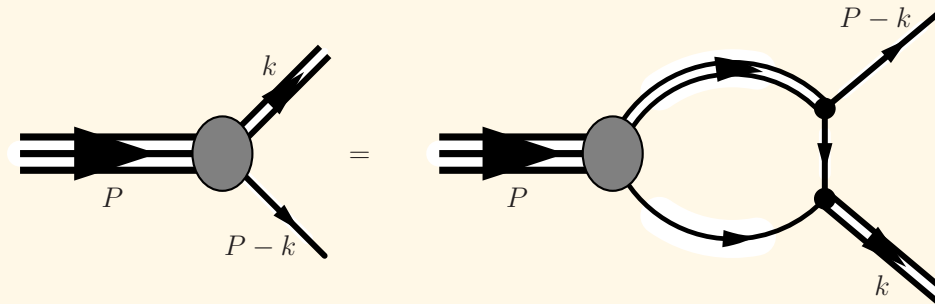


- Investigate the role of quark degrees of freedom.
- NJL has same symmetries as QCD
- Lagrangian:

$$\mathcal{L}_{NJL} = \bar{\psi} (i\cancel{D} - m) \psi + G (\bar{\psi} \Gamma \psi)^2$$

Nucleon in the NJL model

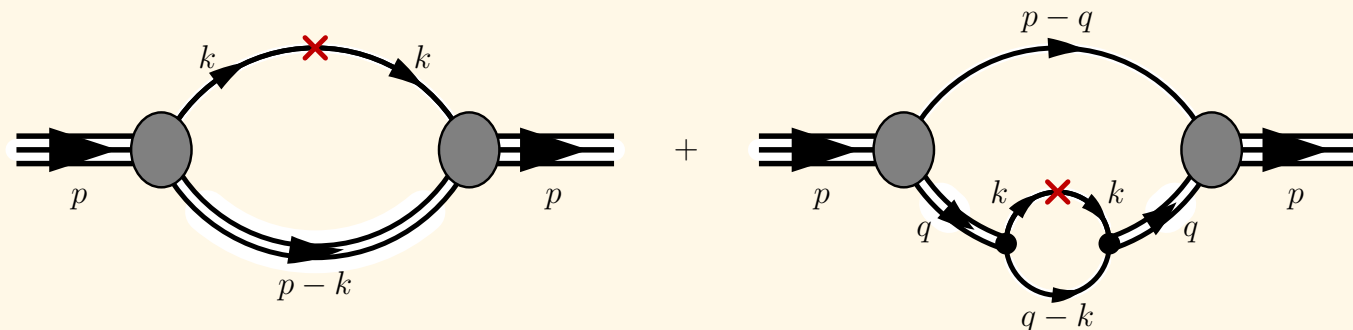
- Nucleon approximated as quark-diquark bound state.
- Use relativistic Faddeev approach:



- Nucleon quark distributions

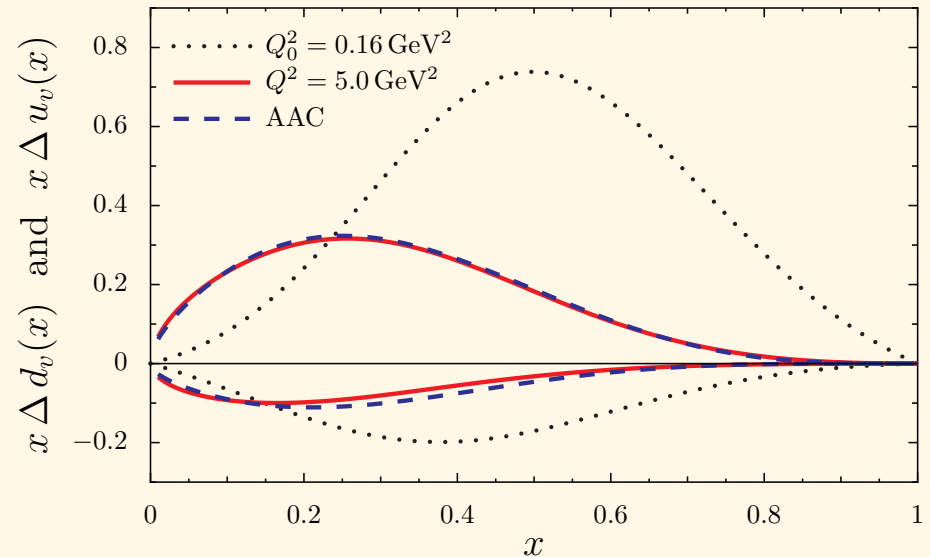
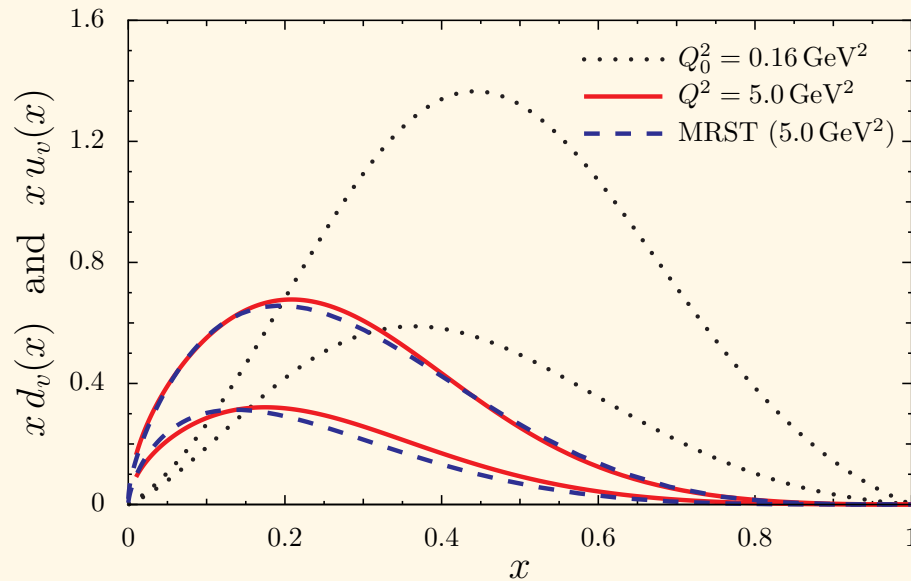
$$q(x) = p^+ \int \frac{d\xi^-}{2\pi} e^{i x p^+ \xi^-} \langle p, s | \bar{\psi}_q(0) \gamma^+ \psi_q(\xi^-) | p, s \rangle_c, \quad \Delta q(x) = \langle \gamma^+ \gamma_5 \rangle$$

- Associated with a Feynman diagram calculation



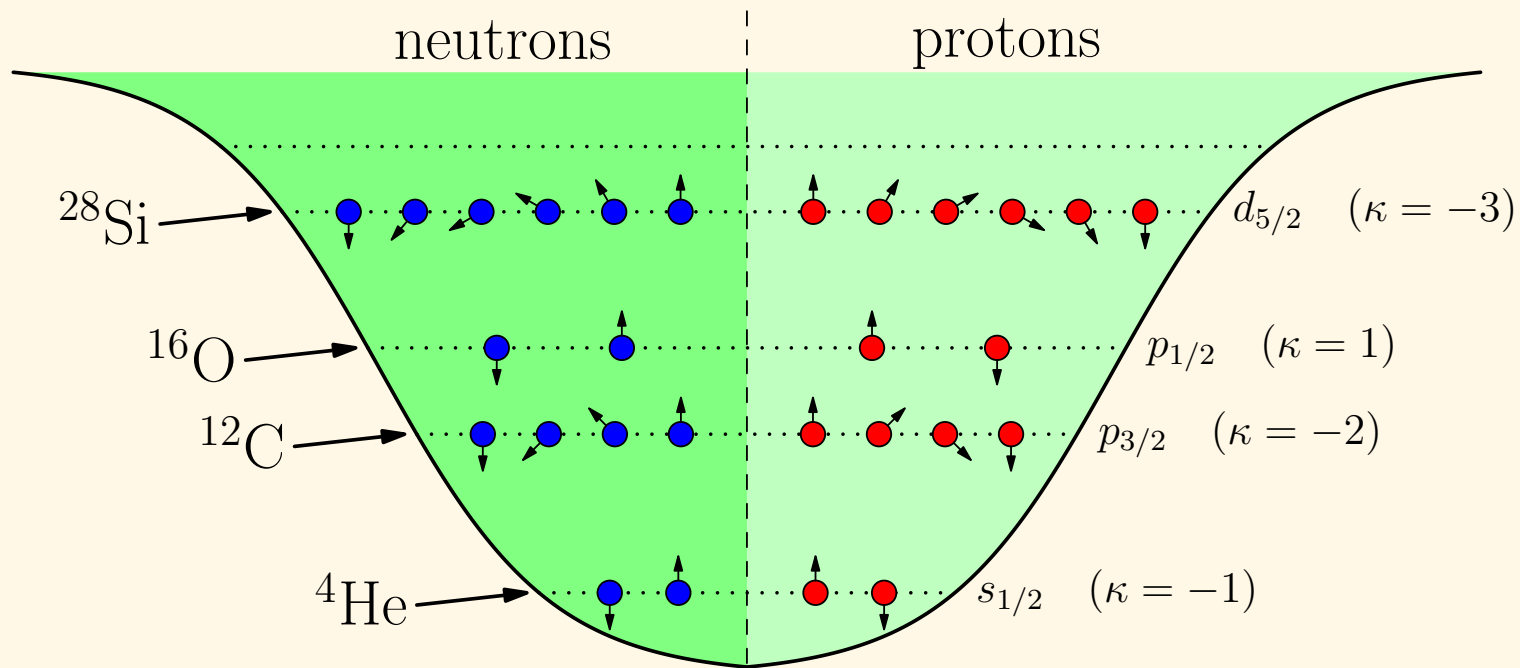
$$\blacklozenge [q(x), \Delta q(x), \Delta_T q(x)] \rightarrow \mathbf{X} = \delta \left(x - \frac{k^+}{p^+} \right) [\gamma^+, \gamma^+ \gamma_5, \gamma^+ \gamma^1 \gamma_5]$$

Results: proton quark distributions



- Empirical spin-independent distributions:
 - ◆ Martin, Roberts, Stirling and Thorne, Phys. Lett. B **531**, 216 (2002).
- Empirical helicity:
 - ◆ M. Hirai, S. Kumano and N. Saito, Phys. Rev. D **69**, 054021 (2004).
- Dotted line \implies model result, Solid line \implies evolved model result
Dashed line \implies empirical result
- Approach is covariant, satisfies all sum rules & positivity constraints

Recall: Shell Model Picture



$$q_A(x_A) = \sum_{\alpha, \kappa, m} \int dy_A \int dx \delta(x_A - y_A x) f_{\alpha, \kappa, m}(y_A) q_{\alpha, \kappa}(x)$$

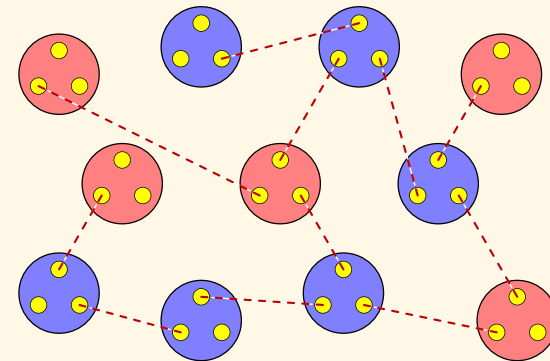
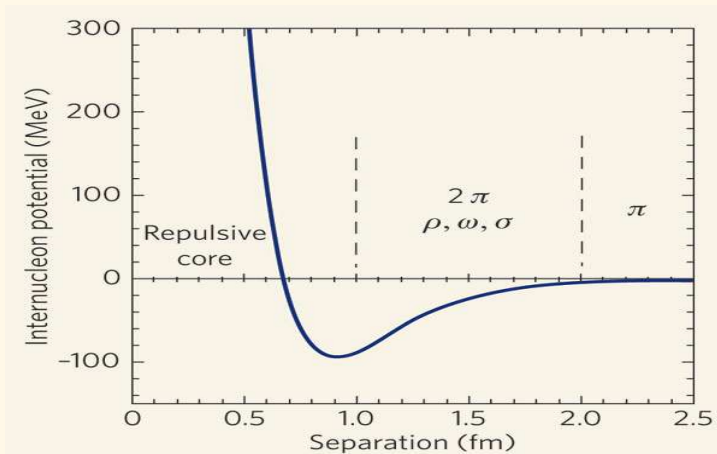
- We now discuss κ or density dependence
- For nuclear matter $f_{\alpha, \kappa, m}(y_A)$ & hence $\sum_{\alpha, \kappa, m}$ greatly simplify

Asymmetric Nuclear Matter: Lagrangian

- Finite Density Lagrangian: σ , ω , ρ mean fields

$$\mathcal{L} = \bar{\psi} (i \not{\partial} - M^* - \mathcal{V}) \psi + \mathcal{L}'_I$$

- σ : isoscalar-scalar – attractive
- ω : isoscalar-vector – repulsive
- ρ : isovector-vector – attractive/repulsive
- **Fundamental physics**: mean fields couple to the quarks in nucleons



- Finite density quark propagator

$$S(k)^{-1} = \not{k} - M - i\varepsilon \quad \rightarrow \quad S_q(k)^{-1} = \not{k} - M^* - \mathcal{V}_q - i\varepsilon$$

Effective Potential

- Hadronization → Effective potential

$$\mathcal{E} = \mathcal{E}_V - \frac{\omega_0^2}{4 G_\omega} - \frac{\rho_0^2}{4 G_\rho} + \mathcal{E}_p + \mathcal{E}_n$$

- ❖ \mathcal{E}_V : vacuum energy
 $\mathcal{E}_{p(n)}$: energy of nucleons moving in σ, ω, ρ fields

- Effective potential provides

$$\omega_0 = 6 G_\omega (\rho_p + \rho_n), \quad \rho_0 = 2 G_\rho (\rho_p - \rho_n), \quad \frac{\partial \mathcal{E}}{\partial M^*} = 0$$

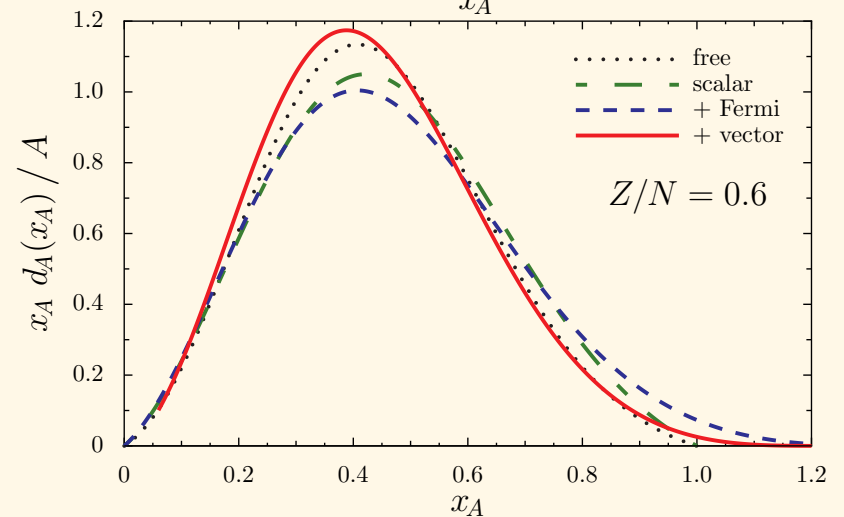
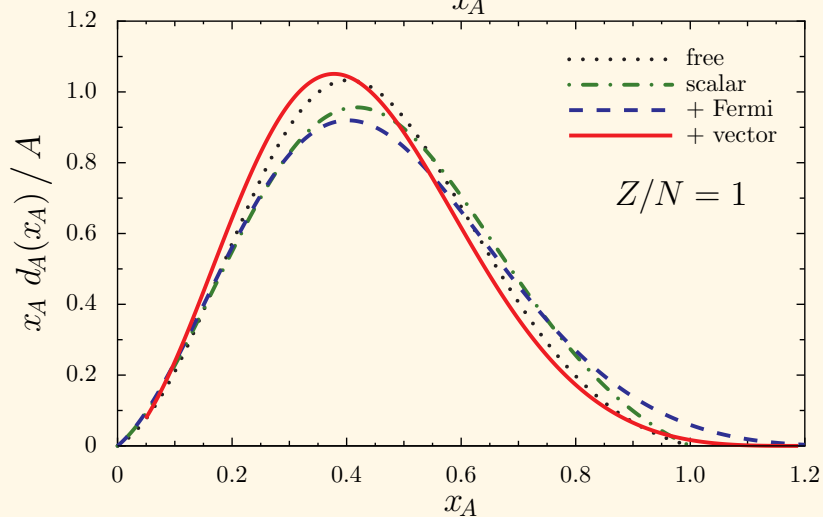
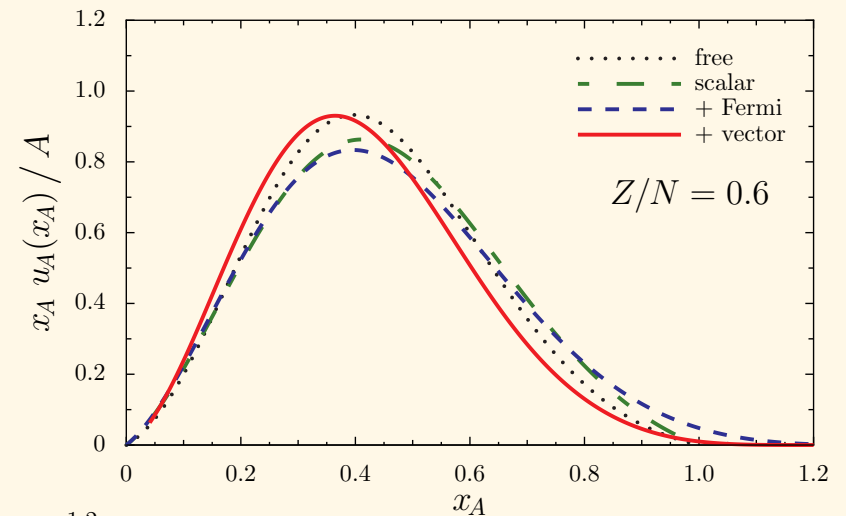
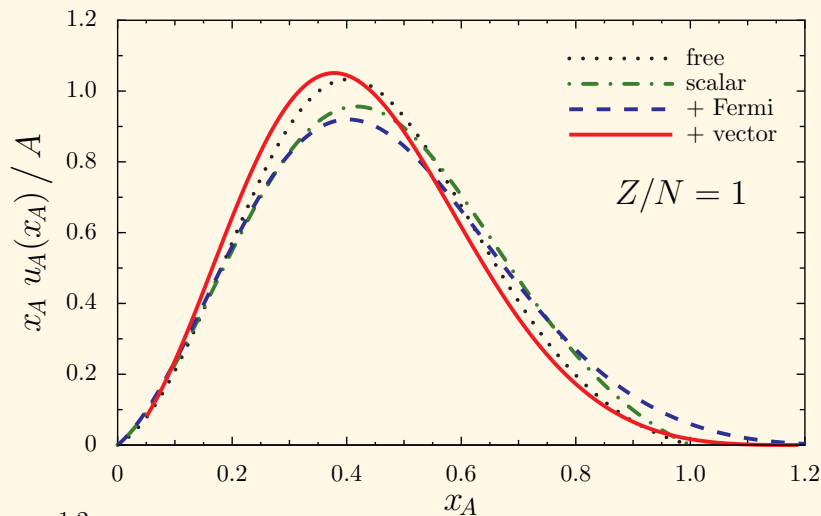
- ❖ $G_\omega \Leftrightarrow Z = N$ saturation & $G_\rho \Leftrightarrow$ symmetry energy

- Vector potentials:

$$V_{u(d)} = \omega_0 \pm \rho_0 \quad V_{p(n)} = 3\omega_0 \pm \rho_0$$

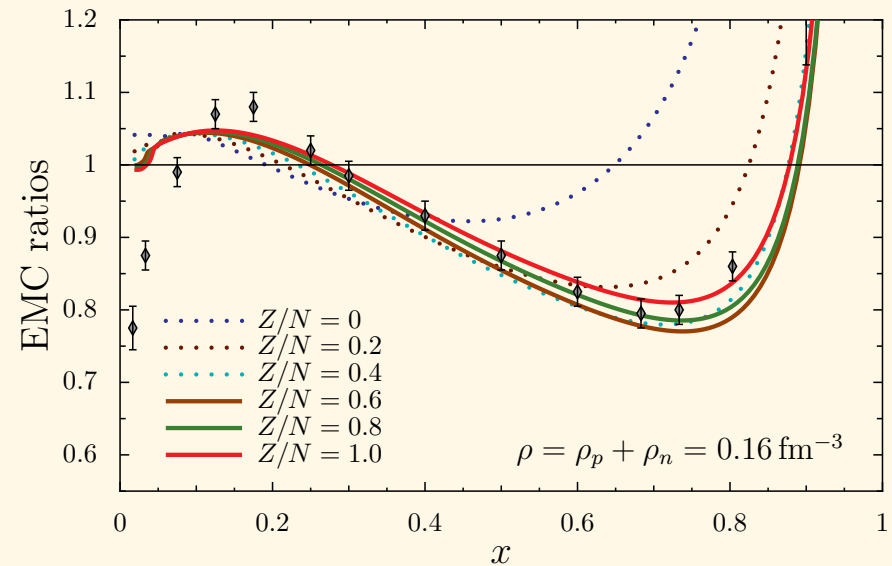
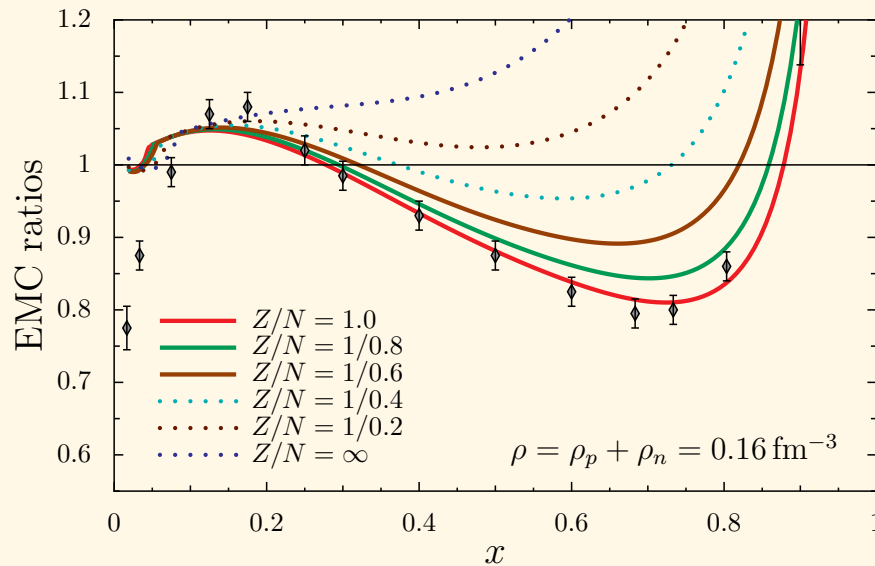
- Recall: quark propagator: $S_q(k) = [\not{k} - M^* - V_q]^{-1}$

Results: Nuclear Matter



- $\rho_p + \rho_n = \text{fixed}$ – Differences arise from:
 - ◆ **naive:** different number protons and neutrons
 - ◆ **medium:** p & n Fermi motion and $V_{u(d)}$ differ $\rightarrow u_p(x) \neq d_n(x), \dots$

Isvector EMC Effect



- **EMC ratio:**
$$R^\gamma = \frac{F_{2A}}{F_{2A}^{\text{naive}}} \sim \frac{4 u_A(x) + d_A(x)}{4 u_0(x) + d_0(x)}, \quad u(x) = \frac{Z}{A} u_p(x) + \frac{N}{A} u_n(x) \dots$$
- **Effect comes largely from the changing ρ_0 field**
- **Proton rich:** $u(x) > d(x)$ and $V_u > V_d$
- **Neutron rich:** $u(x) < d(x)$ and $V_u < V_d$
- **Density is fixed, only Z/N changes \implies non-trivial isospin dependence**

Paschos-Wolfenstein ratio

- Paschos-Wolfenstein ratio motivated the NuTeV study:

$$R_{PW} = \frac{\sigma_{NC}^{\nu A} - \sigma_{NC}^{\bar{\nu} A}}{\sigma_{CC}^{\nu A} - \sigma_{CC}^{\bar{\nu} A}}, \quad NC \implies Z^0, \quad CC \implies W^\pm$$

- Expressing R_{PW} in terms of quark distributions:

$$R_{PW} = \frac{\left(\frac{1}{6} - \frac{4}{9} \sin^2 \theta_W\right) \langle x u_A^- \rangle + \left(\frac{1}{6} - \frac{2}{9} \sin^2 \theta_W\right) \langle x d_A^- + x s_A^- \rangle}{\langle x d_A^- + x s_A^- \rangle - \frac{1}{3} \langle x u_A^- \rangle}$$

- For an isoscalar target $u_A \simeq d_A$ and if $s_A \ll u_A + d_A$

$$R_{PW} = \frac{1}{2} - \sin^2 \theta_W + \Delta R_{PW}$$

- NuTeV measured R_{PW} on an Fe target ($Z/N \simeq 26/30$)
- Correct for neutron excess \Leftrightarrow isoscalar corrections

Isvector EMC correction to NuTeV

- General form of isoscalarity corrections

$$R_{PW} = \left(\frac{1}{2} - \sin^2 \theta_W \right) + \left(1 - \frac{7}{3} \sin^2 \theta_W \right) \frac{\langle x u_A^- - x d_A^- \rangle}{\langle x u_A^- + x d_A^- \rangle}$$

- NuTeV assumed nucleons in Fe are like free nucleons
 - ❖ Ignored some medium effects: Fermi motion & ρ^0 -field
- Use our medium modified “Fe” quark distributions

$$\begin{aligned} \Delta R_{PW} &= \Delta R_{PW}^{\text{naive}} + \Delta R_{PW}^{\text{Fermi}} + \Delta R_{PW}^{\rho^0} \\ &= - (0.0107 + 0.0004 + 0.0028) . \end{aligned}$$

- Recall NuTeV requires $\Delta R_{PW} = -0.005$

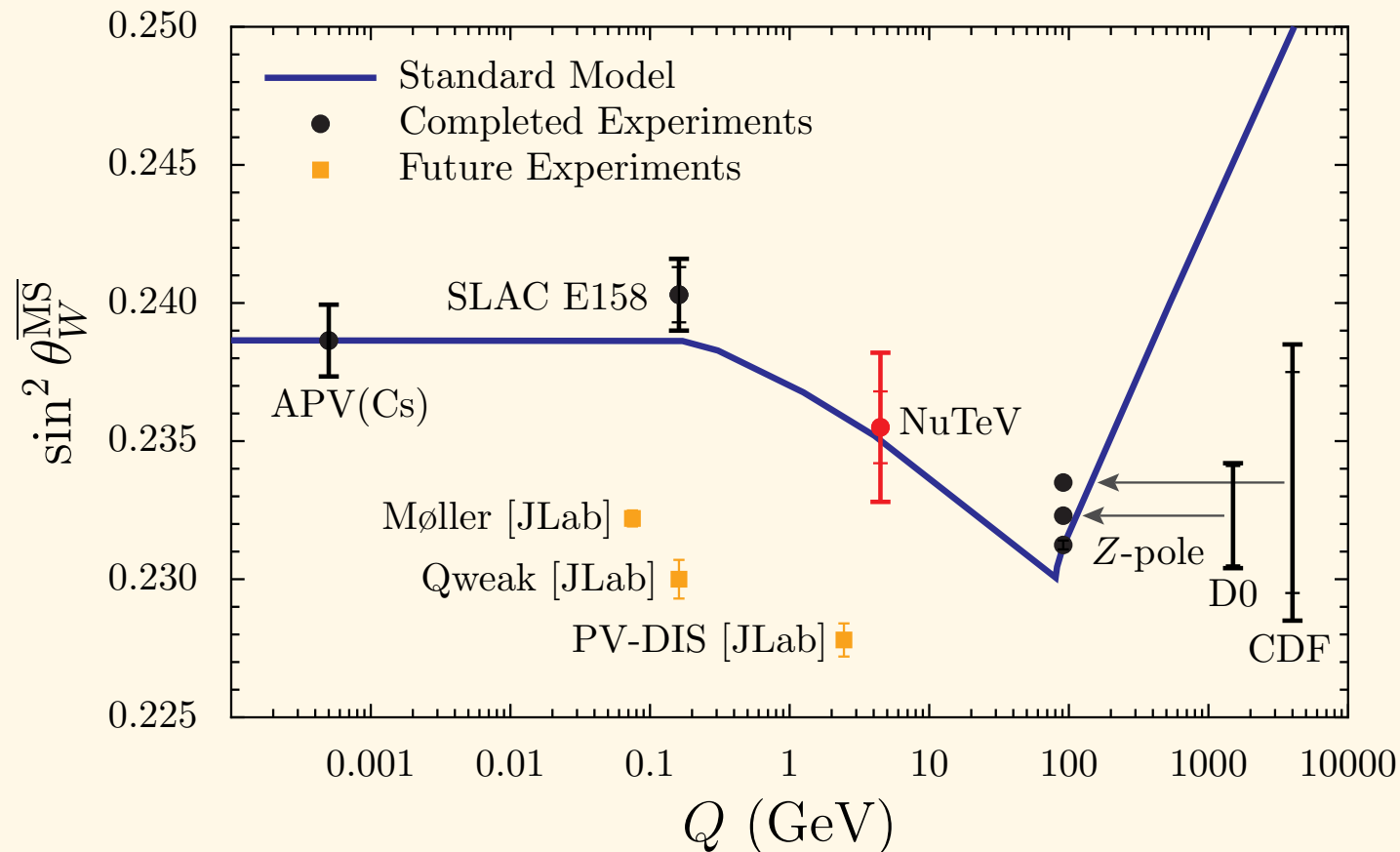
$$\begin{aligned} R_{PW}^{\text{SM}} &\equiv 0.2773 \pm \dots \quad (= \frac{1}{2} - \sin^2 \theta_W) \\ R_{PW}^{\text{NuTeV}} &= 0.2723 \pm \dots \end{aligned}$$

- Isoscalarity ρ^0 correction can explain up to 65% of anomaly

NuTeV anomaly cont'd

- Also correction from $m_u \neq m_d$ - Charge Symmetry Violation
 - ❖ CSV + $\rho_0 \implies$ no NuTeV anomaly
 - ❖ No evidence for physics beyond the Standard Model
- Instead “NuTeV anomaly” is evidence for medium modification
 - ❖ Equally interesting
 - ❖ EMC effect has over 850 citations [J. J. Aubert *et al.*, Phys. Lett. B **123**, 275 (1983).]
- Model dependence?
 - ❖ **sign of correction** is fixed by nature of **vector fields**
$$q(x) = \frac{p^+}{p^+ - V^+} q_0 \left(\frac{p^+}{p^+ - V^+} - \frac{V_q^+}{p^+ - V^+} \right), \quad N > Z \implies V_u < V_d$$
 - ❖ ρ^0 -field shifts momentum from u - to d -quarks
 - ❖ **size of correction** is constrained by **Nucl. Matt. symmetry energy**
- ρ_0 vector field reduces NuTeV anomaly – Model Independent!!

Total NuTeV correction



- Small increase in systematic error
- NuTeV anomaly interpreted as evidence for medium modification
- Equally profound as evidence for physics beyond Standard Model

Consistent with other observables?

- We claim Isovector EMC effect explains $\sim 1.5\sigma$ of NuTeV result
 - ❖ but can this mechanism be observed elsewhere?

- **Yes!!** Parity violating DIS – Z^0 interaction violates parity

$$A^{PV} = \frac{d\sigma_{R^-} - d\sigma_L}{d\sigma_{R^+} + d\sigma_L} \propto [a_2(x) + \dots]; \quad a_2(x) = g_A^e \frac{F_2^{\gamma Z}}{F_2^{\gamma}}$$

- Parton model expressions

$$F_2^{\gamma Z} = 2x \sum e_q g_V^q (q + \bar{q}), \quad g_V^q = \pm \frac{1}{2} - 2e_q \sin^2 \theta_W$$

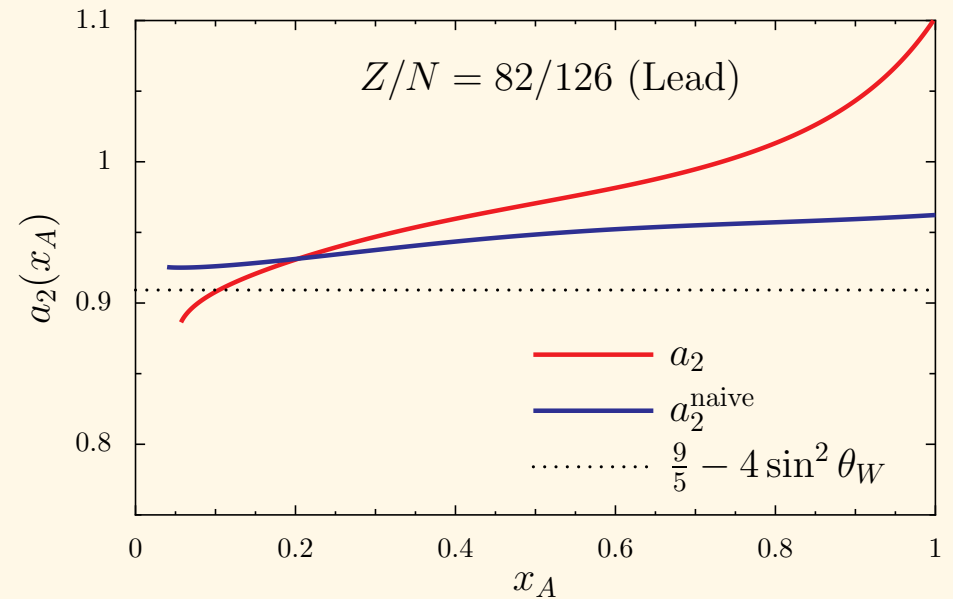
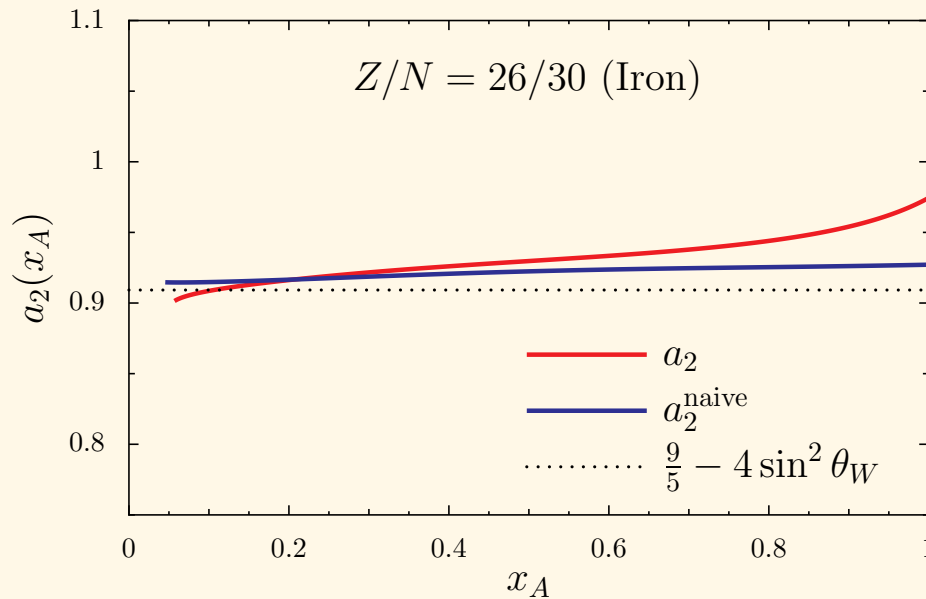
- Measuring $a_2 \implies F_2^{\gamma Z}$ or $\sin^2 \theta_W$

- For $N \simeq Z$ target

$$a_2(x) \simeq \left(\frac{9}{5} - 4 \sin^2 \theta_W \right) - \frac{12}{25} \frac{u_A^+(x) - d_A^+(x)}{u_A^+(x) + d_A^+(x)}$$

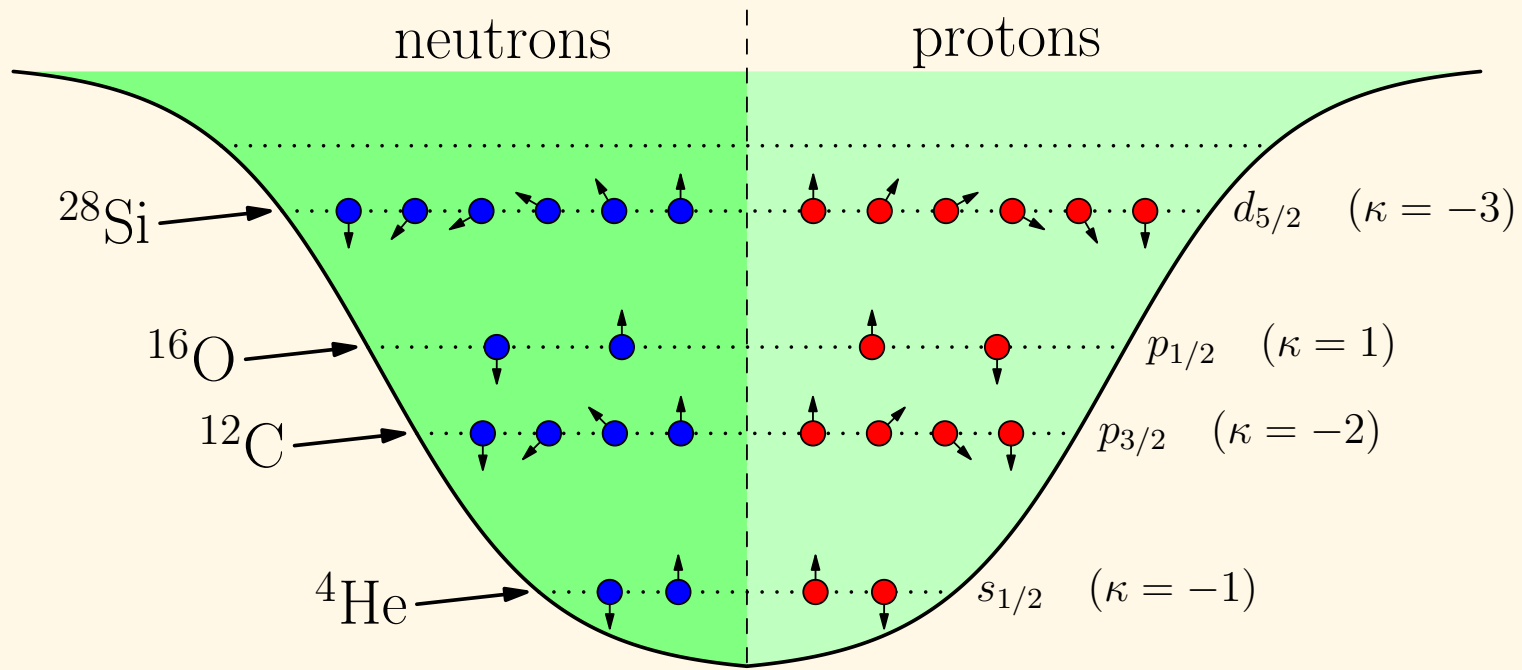
- Measurement of $a_2(x)$ at each $x \implies$ a NuTeV experiment!!

Parity Violating DIS: a_2 ratios



- $a_2(x) \simeq \frac{9}{5} - 4 \sin^2 \theta_W - \frac{12}{25} \frac{u_A^+(x) - d_A^+(x)}{u_A^+(x) + d_A^+(x)}$
- Isoscalar corrections are independent of $\sin^2 \theta_W$
 - ❖ An advantage over Paschos-Wolfenstein ratio
- After naive isoscalar corrections medium effects still very large
- Large x dependence of $a_2(x)$, even after naive correction
 - Cannot be from $\sin^2 \theta_W$
 - Evidence for medium modification

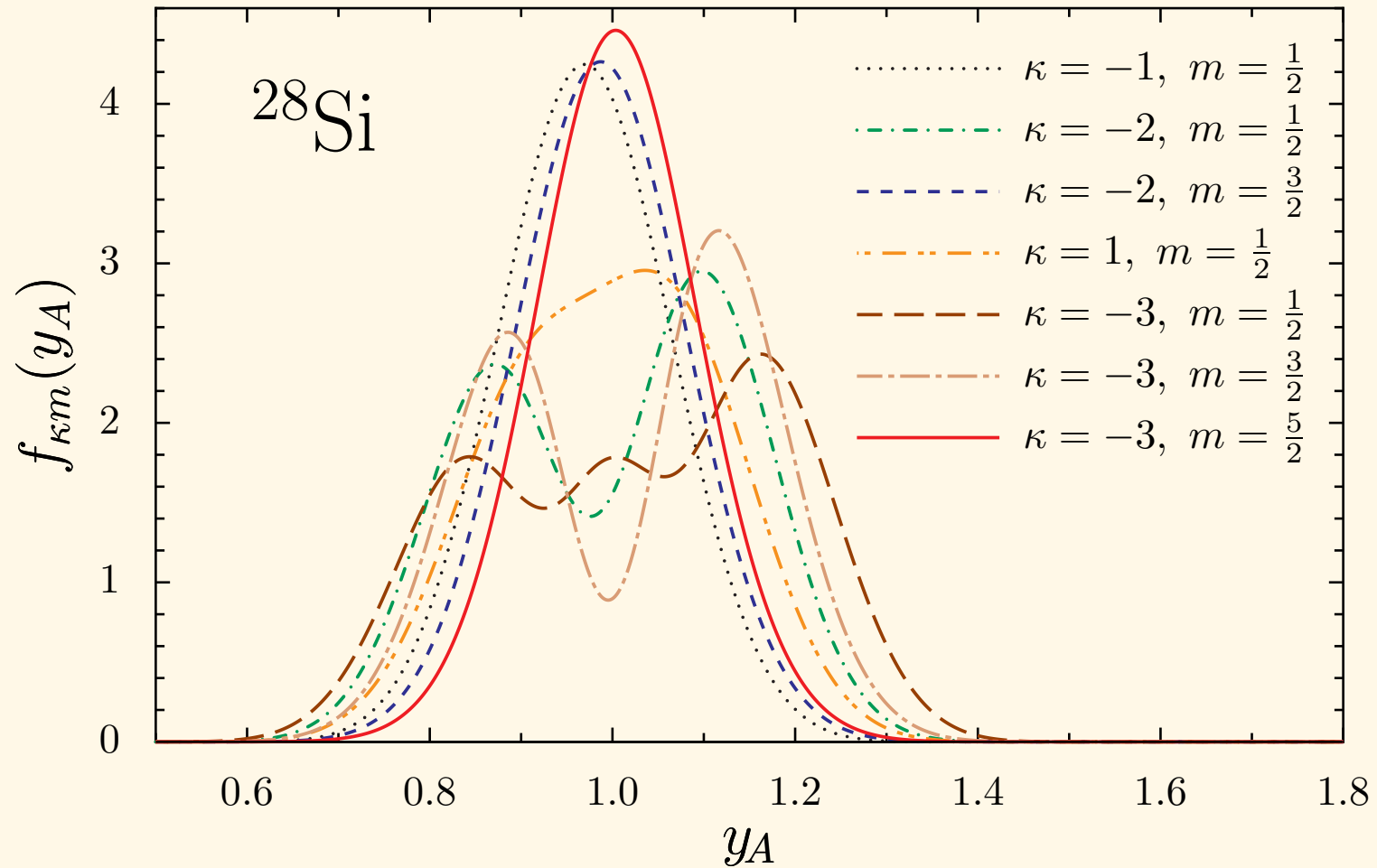
Recall Shell Model Picture



$$q_A(x_A) = \sum_{\alpha, \kappa, m} \int dy_A \int dx \delta(x_A - y_A x) f_{\alpha, \kappa, m}(y_A) q_{\kappa}(x)$$

- Finite nucleus calculation

Nucleon distributions: ^{28}Si



EMC effects

- EMC ratio

$$R = \frac{F_{2A}}{F_{2A}^{\text{naive}}} = \frac{F_{2A}}{Z F_{2p} + N F_{2n}}$$

- ❖ Least model dependent way to definite EMC effect

- Polarized EMC ratio

$$R_s^{JH} = \frac{g_{1A}^{JH}}{g_{1A,\text{naive}}^{JH}} = \frac{g_{1A}^{JH}}{P_p^{JH} g_{1p} + P_n^{JH} g_{1n}}$$

- Spin-dependent cross-section is suppressed by $1/A$

- ❖ Must choose nuclei with $A \lesssim 27$

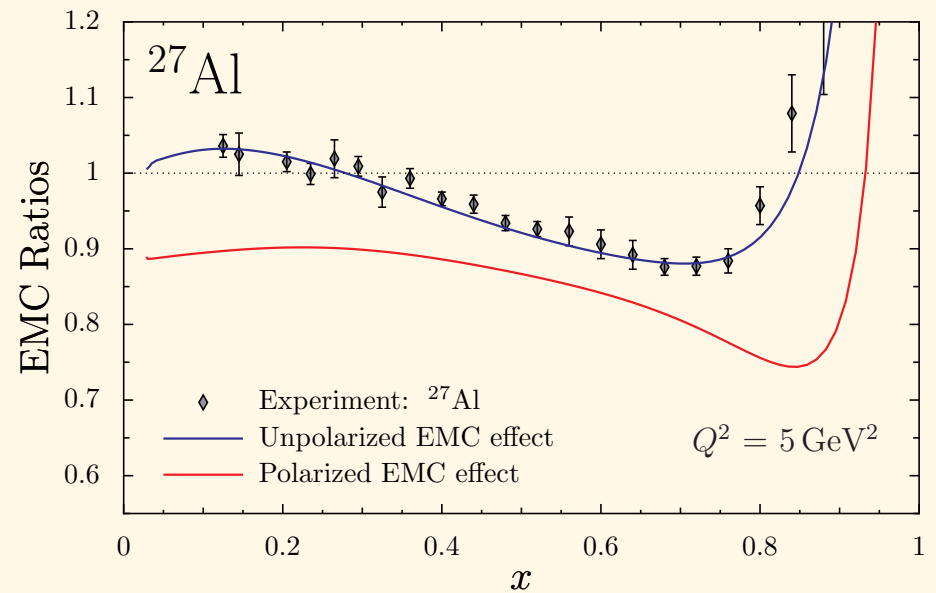
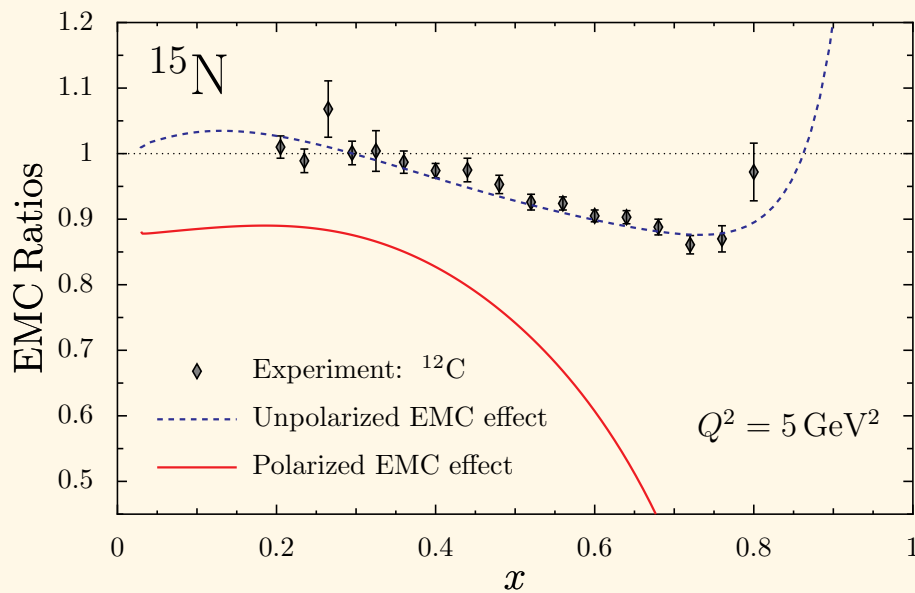
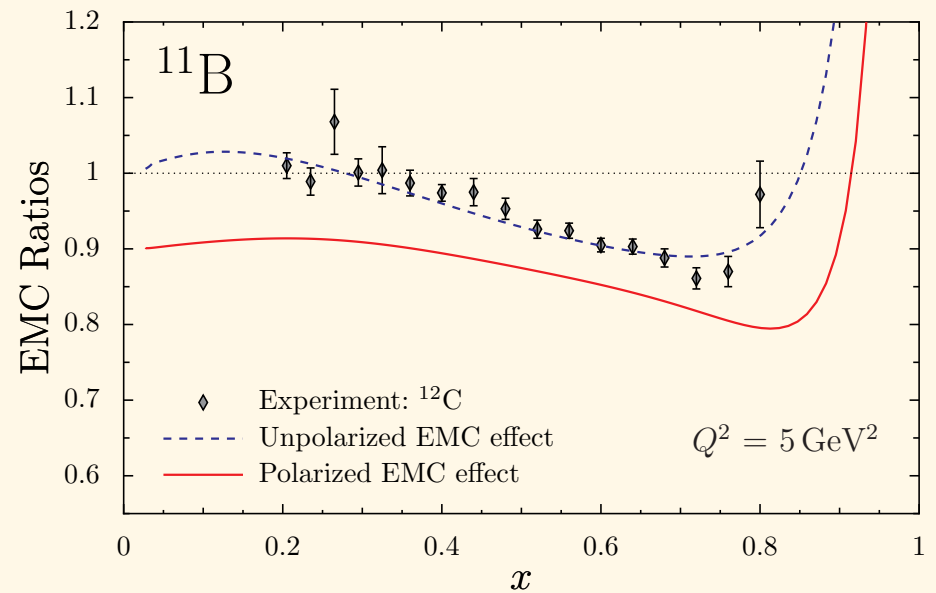
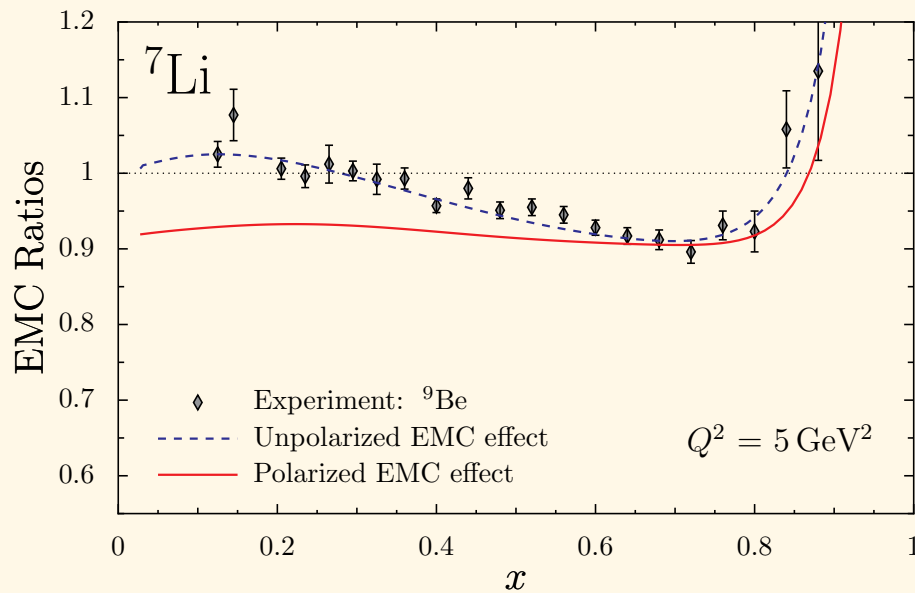
- ❖ protons should carry most of the spin e.g. $\implies {}^7\text{Li}, {}^{11}\text{B}, \dots$

- Ideal nucleus is probably ${}^7\text{Li}$

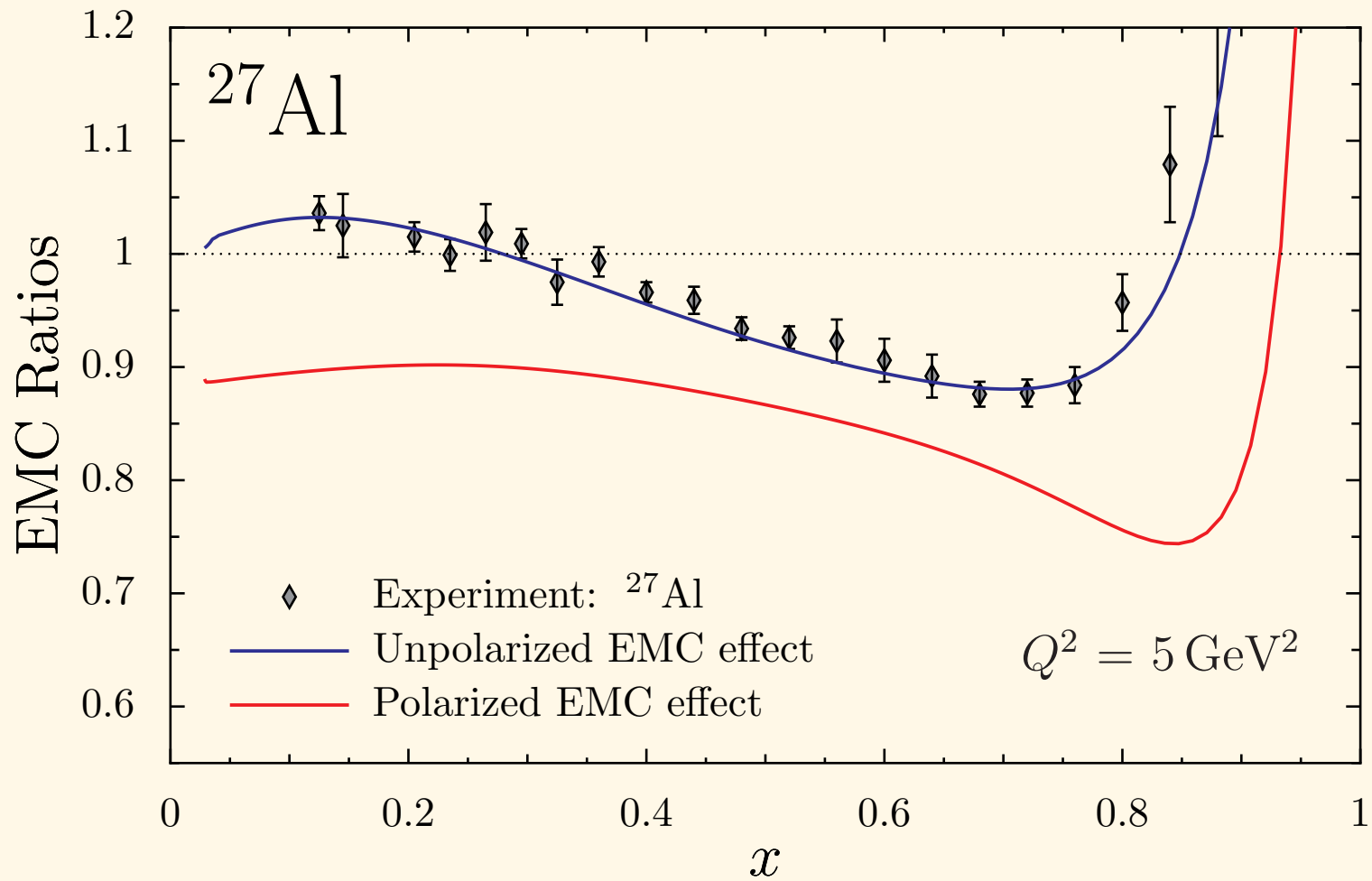
- ❖ From Quantum Monte-Carlo: $P_p^{JJ} = 0.86$ & $P_n^{JJ} = 0.04$

- Ratios equal 1 in non-relativistic and no-medium modification limit.

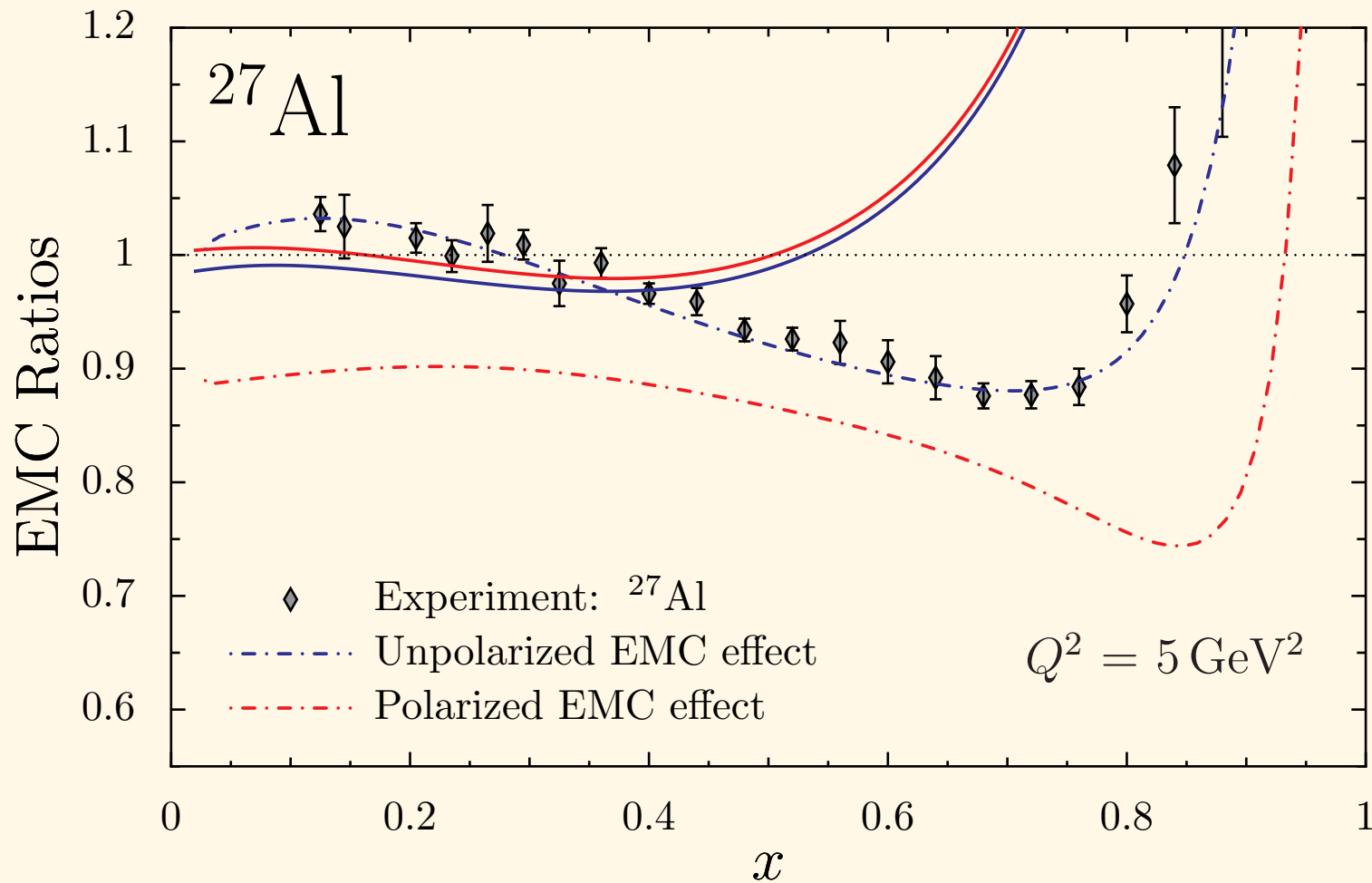
EMC ratio ${}^7\text{Li}$, ${}^{11}\text{B}$, ${}^{15}\text{N}$ and ${}^{27}\text{Al}$



Is there medium modification



Is there medium modification



- Medium modification of nucleon has been switched off

Nuclear Spin Sum

	Δu	Δd	Σ	g_A
p	0.97	-0.30	0.67	1.267
${}^7\text{Li}$	0.91	-0.29	0.62	1.19
${}^{11}\text{B}$	0.88	-0.28	0.60	1.16
${}^{15}\text{N}$	0.87	-0.28	0.59	1.15
${}^{27}\text{Al}$	0.87	-0.28	0.59	1.15
Nuclear Matter	0.79	-0.26	0.53	1.05

- Angular momentum of nucleon: $J = \frac{1}{2} = \frac{1}{2} \Delta\Sigma + L_q + J_g$
- In-medium lower components of quark wavefunctions are enhanced
 - ❖ since $M^* < M$ and therefore quarks are more relativistic
 - ❖ lower components have $L = 1$
 - ❖ $\Delta q(x)$ very sensitive to lower components because of γ_5
- Conclusion: **quark spin \rightarrow orbital angular momentum** in-medium

Conclusion

- Effective quark theories can be used to incorporate quarks into a traditional description of nuclei
 - ❖ fundamentally different approach to nuclear physics
- The major outstanding discrepancy with Standard Model predictions for Z^0 was NuTeV anomaly
 - ❖ resolved by CSV and isovector EMC effect corrections
- EMC effect and NuTeV anomaly are interpreted as evidence for medium modification of the bound nucleon wavefunction
- This result can be tested using PV DIS measurements
 - ❖ predict large medium modification in PV DIS
 - ❖ predict flavour dependence of EMC effect can be large
- In nuclei quark spin converted to orbital angular momentum
 - Polarized EMC effect
- Important implications for nuclear physics

Model Parameters

- Free Parameters:

$$\Lambda_{IR}, \Lambda_{UV}, M_0, G_\pi, G_s, G_a, G_\omega \text{ and } G_\rho$$

- Constraints:

- ❖ $f_\pi = 93 \text{ MeV}, m_\pi = 140 \text{ MeV} \quad \& \quad M_N = 940 \text{ MeV}$

- ❖ $\int_0^1 dx (\Delta u_v(x) - \Delta d_v(x)) = g_A = 1.267$

- ❖ $(\rho, E_B/A) = (0.16 \text{ fm}^{-3}, -15.7 \text{ MeV})$

- ❖ $a_4 = 32 \text{ MeV}$

- ❖ $\Lambda_{IR} = 240 \text{ MeV}$

- We obtain [MeV]:

- ❖ $\Lambda_{UV} = 644$

- ❖ $M_0 = 400, \quad M_s = 690, \quad M_a = 990, \quad \dots$

- Can now study a very large array of observables:

- ❖ e.g. meson and baryon: quark distributions, form factors, GPDs, finite temp. and density, neutron stars

Regularization

- Proper-time regularization

$$\frac{1}{X^n} = \frac{1}{(n-1)!} \int_0^\infty d\tau \tau^{n-1} e^{-\tau X}$$
$$\longrightarrow \frac{1}{(n-1)!} \int_{1/(\Lambda_{UV})^2}^{1/(\Lambda_{IR})^2} d\tau \tau^{n-1} e^{-\tau X}$$

- Λ_{IR} eliminates unphysical thresholds for the nucleon to decay into quarks: \rightarrow simulates confinement

❖ D. Ebert, T. Feldmann and H. Reinhardt, Phys. Lett. B **388**, 154 (1996).

- E.g.: Quark wave function renormalization

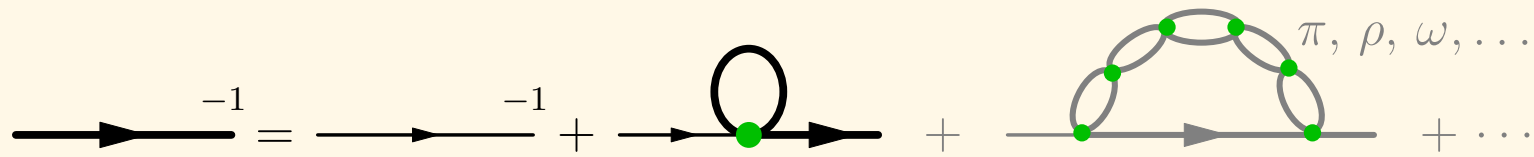
$$\text{❖ } Z(k^2) = e^{-\Lambda_{UV}(k^2 - M^2)} - e^{-\Lambda_{IR}(k^2 - M^2)}$$

$$\rightarrow Z(k^2 = M^2) = 0 \quad \implies \quad \text{no free quarks}$$

- Needed for: nuclear matter saturation, Δ baryon, etc

❖ W. Bentz, A.W. Thomas, Nucl. Phys. A **696**, 138 (2001)

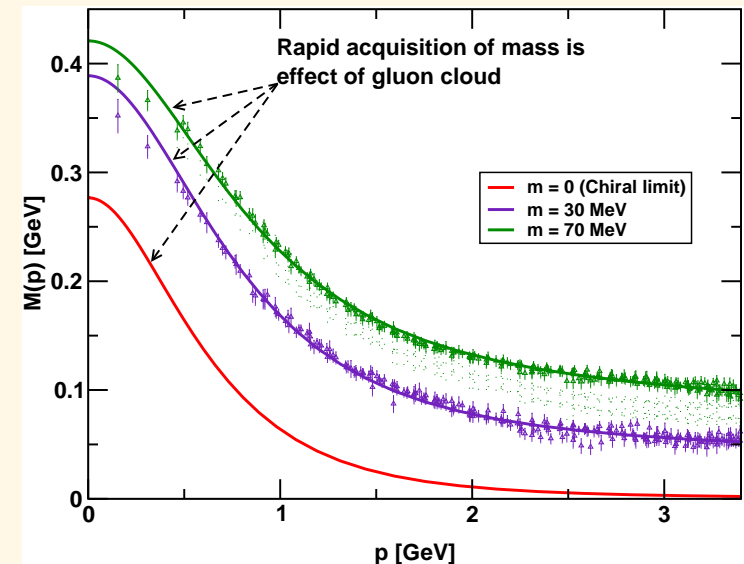
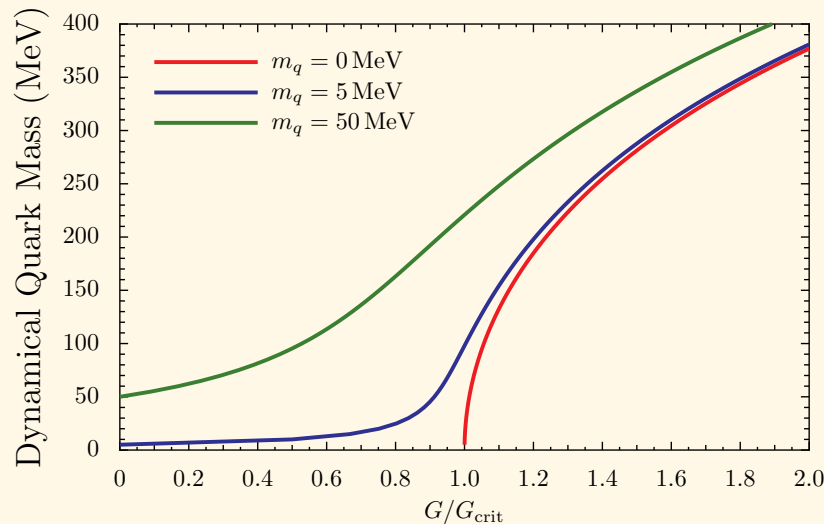
Gap Equation & Mass Generation



- Quark Propagator:

$$\frac{1}{\not{p} - m + i\epsilon} \rightarrow \frac{1}{\not{p} - M + i\epsilon}$$

- Mass is generated via interaction with vacuum



- Dynamically generated quark masses $\iff \langle \bar{\psi}\psi \rangle \neq 0 \iff D\chi SB$

- Proper-time regularization: Λ_{IR} and Λ_{UV}

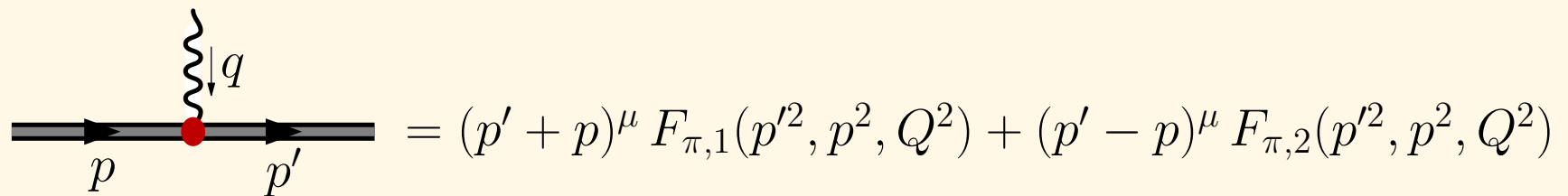
\rightarrow No free quarks \implies Confinement $[Z(k^2 = M^2) = 0]$

Off-Shell Effects

- For an off-shell nucleon, photon–nucleon vertex given by

$$\Gamma_N^\mu(p', p) = \sum_{\alpha, \beta = +, -} \Lambda^\alpha(p') \left[\gamma^\mu f_1^{\alpha\beta} + \frac{i\sigma^{\mu\nu} q_\nu}{2M} f_2^{\alpha\beta} + q^\mu f_3^{\alpha\beta} \right] \Lambda^\alpha(p)$$

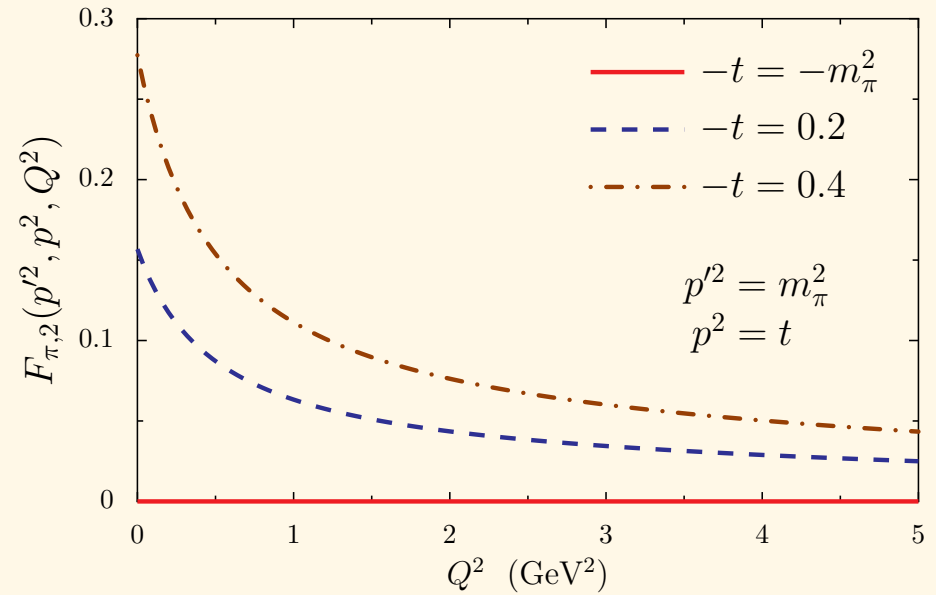
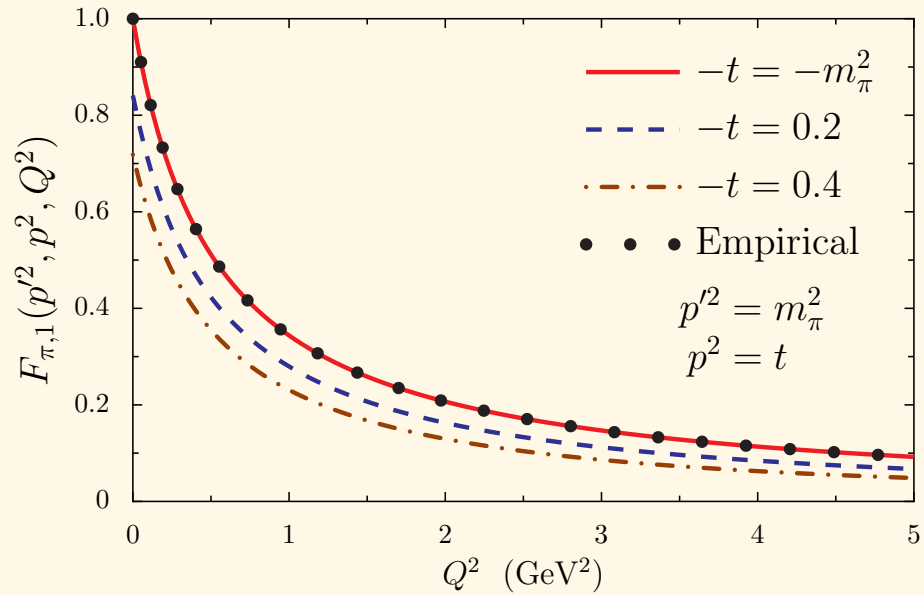
- In-medium nucleon is off-shell, extremely difficult to quantify effects
 - ❖ However must understand to fully describe in-medium nucleon
- Simpler system: off-shell pion form factors
 - ❖ relax on-shell constraint $p'^2 = p^2 = m_\pi^2$
 - ❖ Very difficult to calculate in many approaches, e.g. Lattice QCD



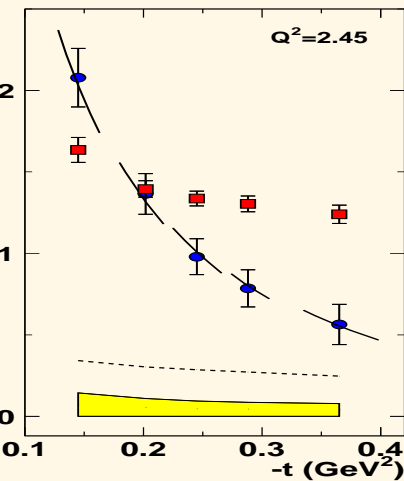
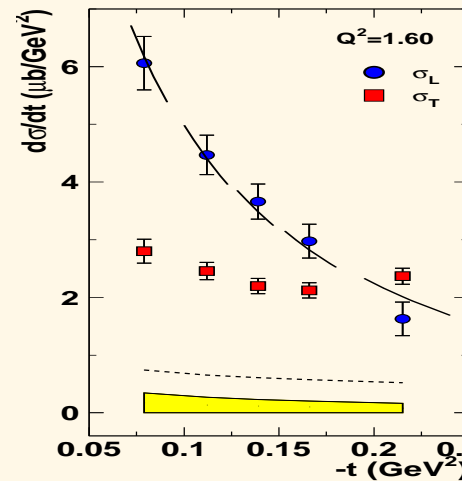
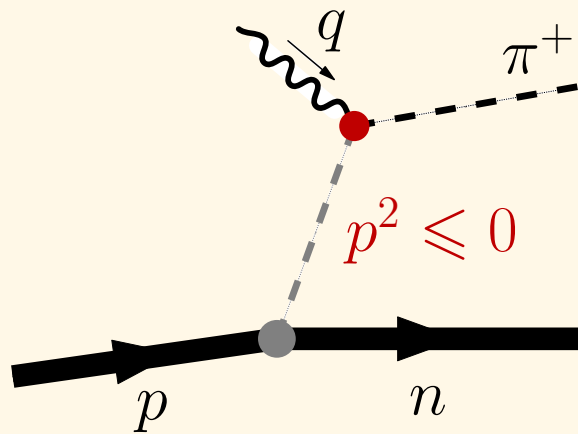
$$= (p' + p)^\mu F_{\pi,1}(p'^2, p^2, Q^2) + (p' - p)^\mu F_{\pi,2}(p'^2, p^2, Q^2)$$

- For $p'^2 = p^2 = m_\pi^2$ we have $F_{\pi,1} \rightarrow F_\pi$ and $F_{\pi,2} = 0$

Pion Off-Shell Form Factors

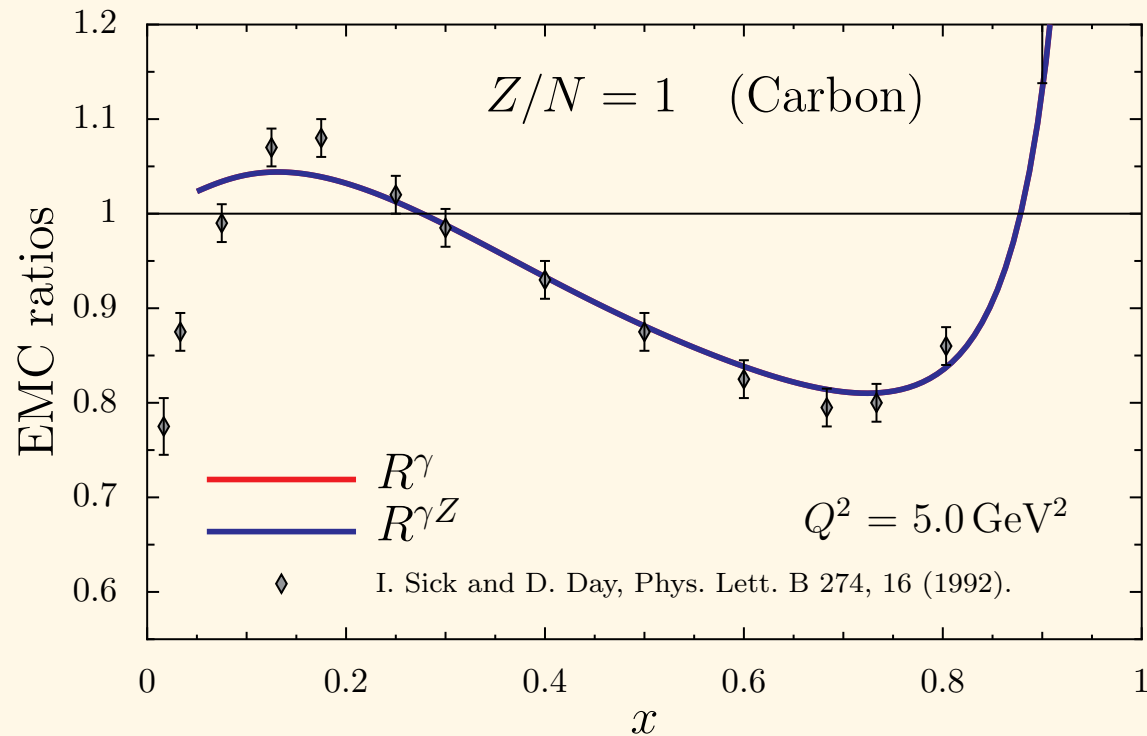


- Potentially important for experimental extraction of F_π



- May also be important for extracting G_E/G_M ratio from ${}^4\text{He}(e,e'p){}^3\text{H}$

F_2^γ and $F_2^{\gamma Z}$ EMC ratios – “Carbon”

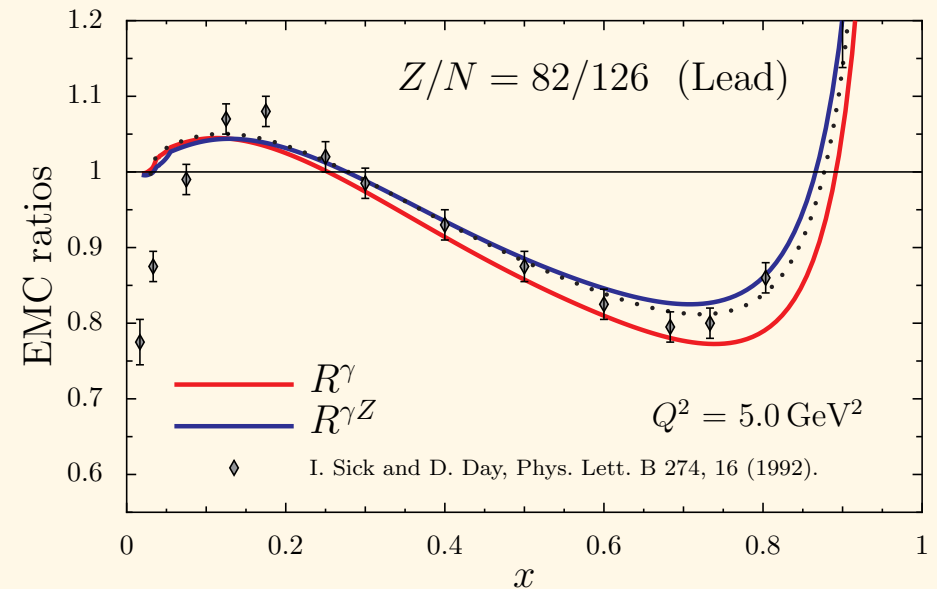
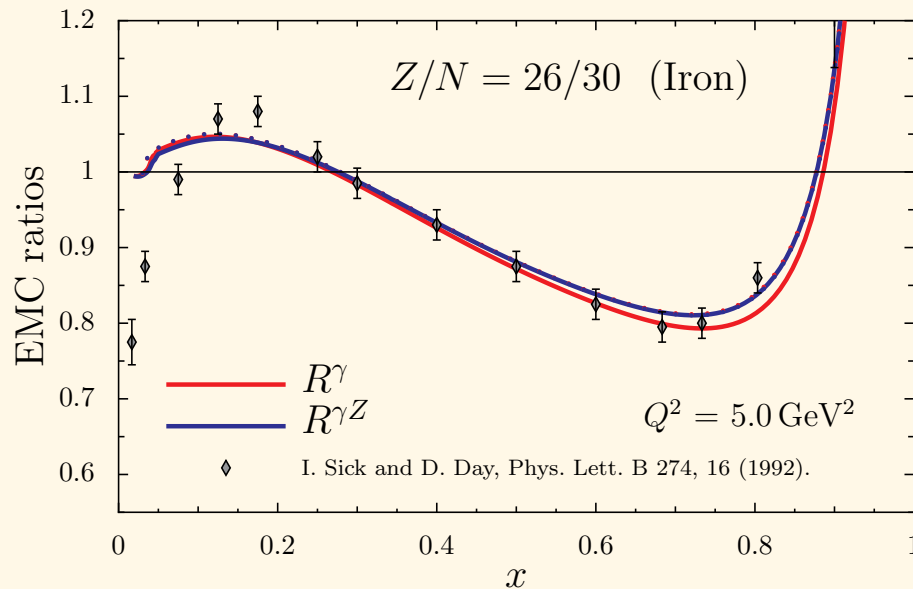


- Recall EMC ratio:

$$R^i = \frac{F_{2A}^i}{F_{2A}^{i,\text{naive}}} = \frac{F_{2A}^i}{Z F_{2p}^i + N F_{2n}^i} \quad i \in \gamma, \gamma Z, \dots$$

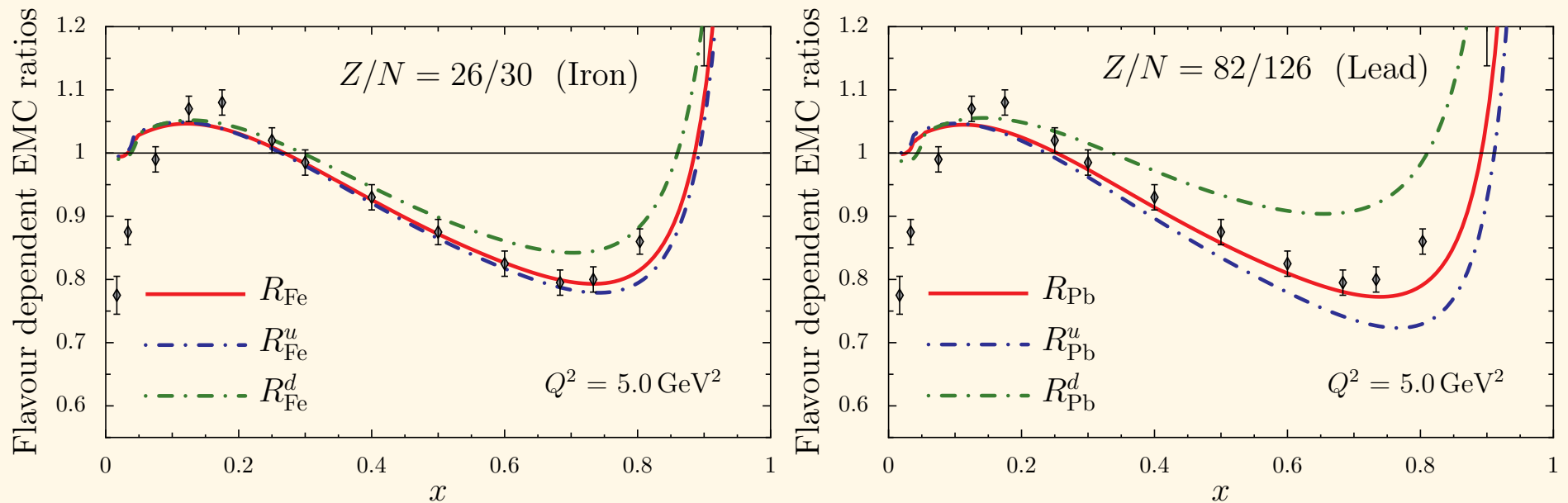
$$R^\gamma \sim \frac{4 u_A(x) + d_A(x)}{4 u_0(x) + d_0(x)}, \quad R^{\gamma Z} \sim \frac{1.16 u_A(x) + d_A(x)}{1.16 u_0(x) + d_0(x)}$$

F_2^γ and $F_2^{\gamma Z}$ EMC ratios – “Iron” & “Lead”



- $R^\gamma \sim \frac{4u_A(x) + d_A(x)}{4u_0(x) + d_0(x)}$ & $R^{\gamma Z} \sim \frac{1.16u_A(x) + d_A(x)}{1.16u_0(x) + d_0(x)}$
- Neutron rich – $Z/N < 1$:
 - ❖ $u_A(x) < d_A(x)$
 - ❖ medium modification of u_A increases & d_A decreases
- u_A dominates R^γ – however $R^{\gamma Z}$ almost isoscalar ratio
- ρ_0 -field $\implies R^{\gamma Z} > R^\gamma$ – Model Independent

Flavour Dependence of EMC effect



- Flavour dependence is defined above by

$$R_A = \frac{F_{2A}}{F_{2A}^{\text{naive}}} = \frac{\sum_q F_{2A}^q}{\sum_q F_{2A}^{q,\text{naive}}} \longrightarrow R_A^q = \frac{F_{2A}^q}{F_{2A}^{q,\text{naive}}} \simeq \frac{q_A}{q_0}$$

- Flavour dependence determined by measuring e.g. F_A^γ and $F_A^{\gamma Z}$
- If observed \implies strong evidence for medium modification