

Hyperon Nucleon Interactions and Dense Matter

Martin J. Savage
University of Washington
June 2012, Lattice 2012
Cairns, Australia



NPLQCD



Silas Beane
New Hampshire



Emmanuel Chang
Barcelona



William Detmold
William+Mary



Huey-Wen Lin
U. of Washington



Tom Luu
LLNL



Saul Cohen
U. of Washington



Kostas Orginos
William+Mary



Assumpta Parreno
Barcelona



Marton Savage
U. of Washington



Aaron Torok
Indiana



Andre Walker-Loud
LBNL

+

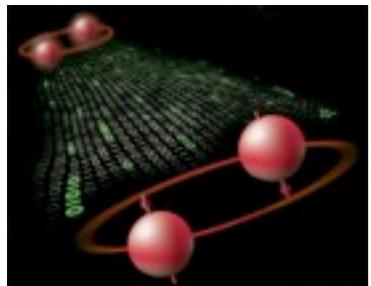


Jefferson Lab

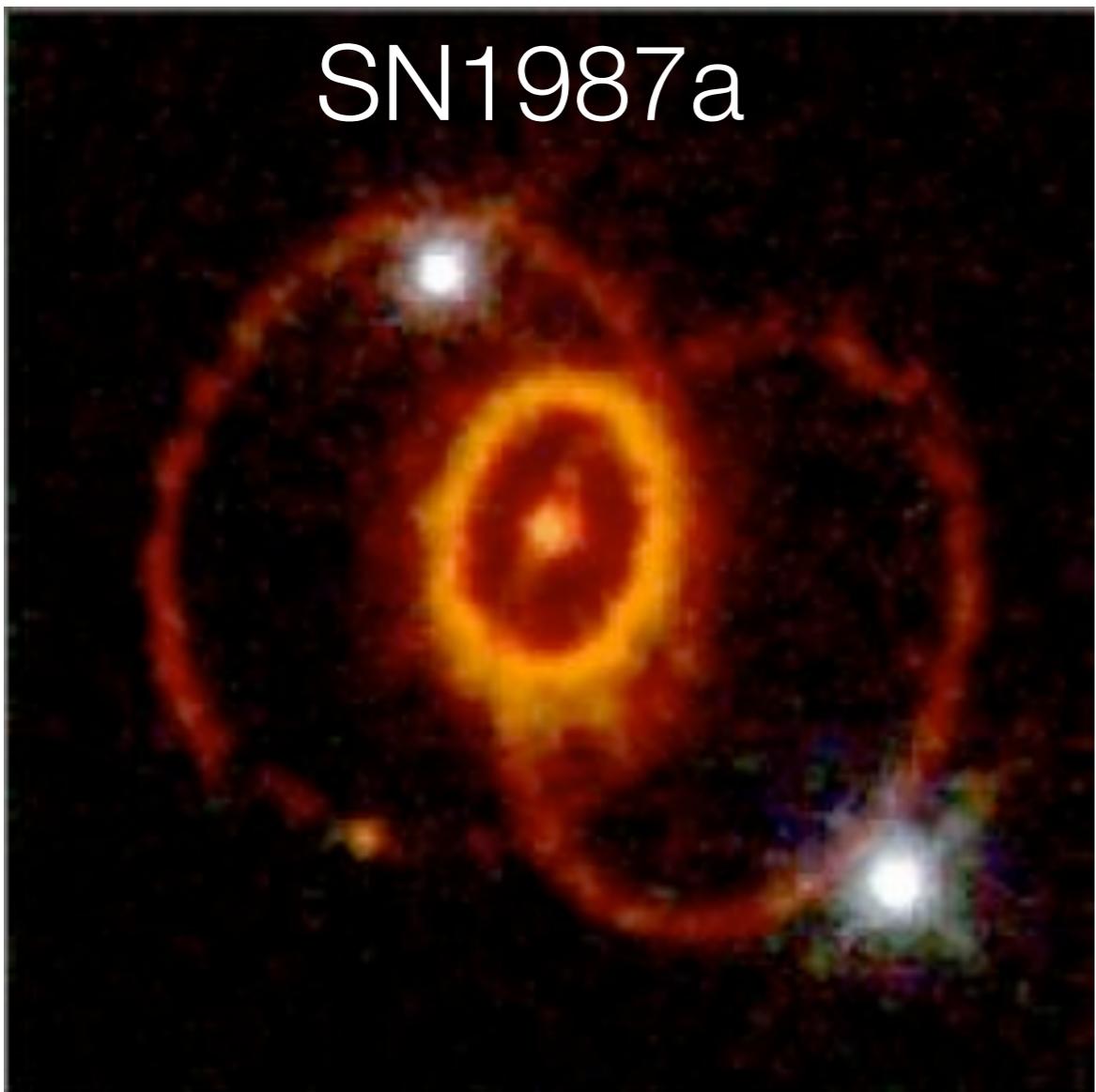
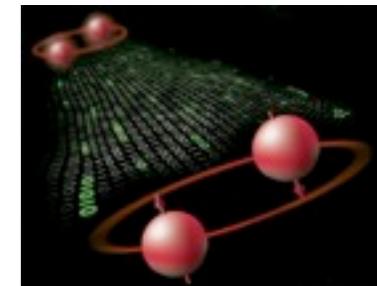
... to make predictions for the structure and interactions of nuclei using lattice QCD.



US Lattice Quantum Chromodynamics

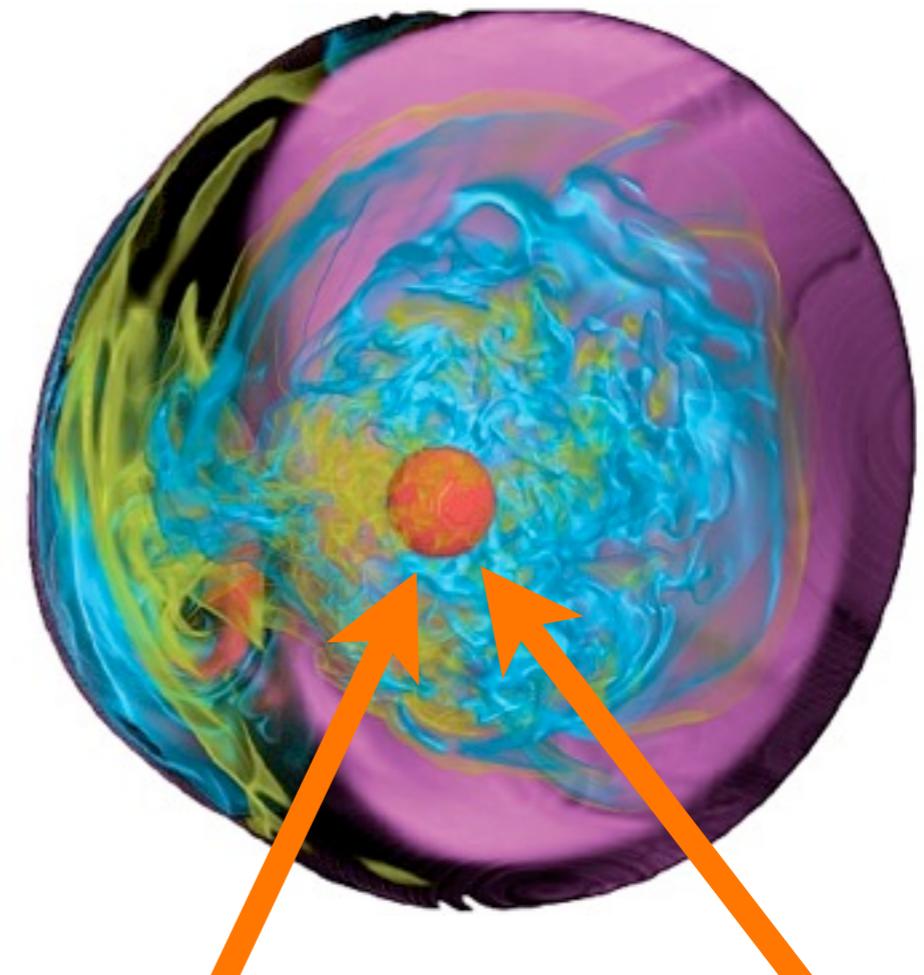


Core-Collapse Supernova and the Heavy Elements



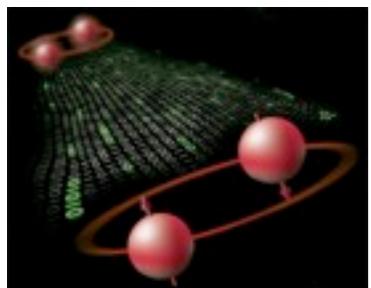
SN1987a

(Mezzacappa *et al*)

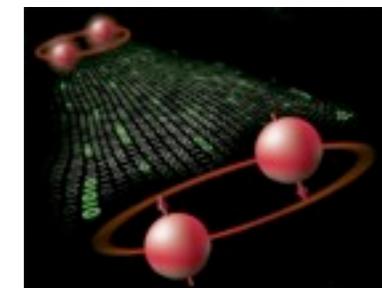


Black-Hole or
Neutron Star ?

Nuclear EoS



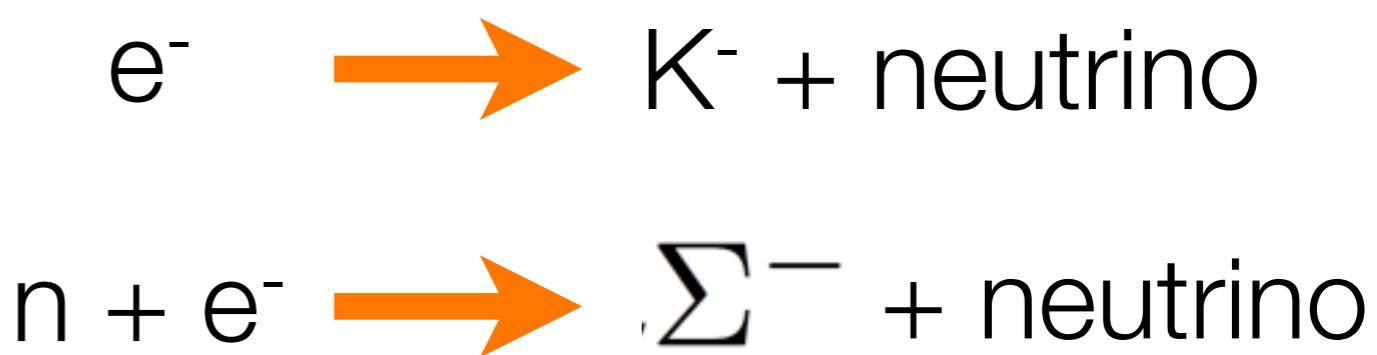
Core-Collapse Supernova and the Heavy Elements



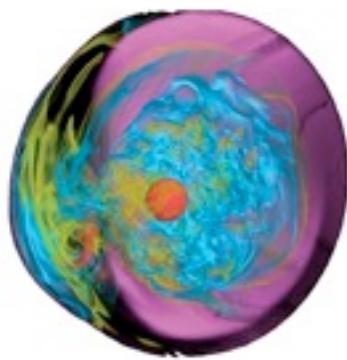
(Mezzacappa *et al*)



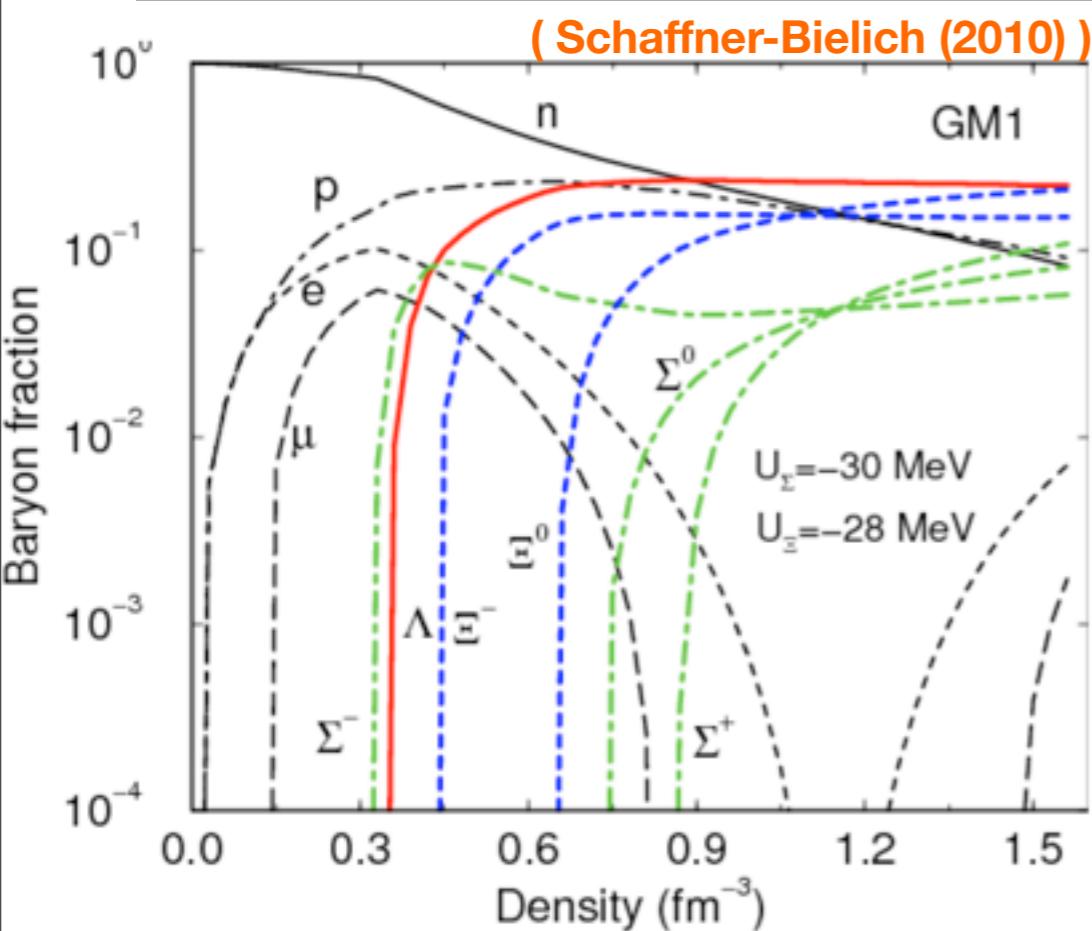
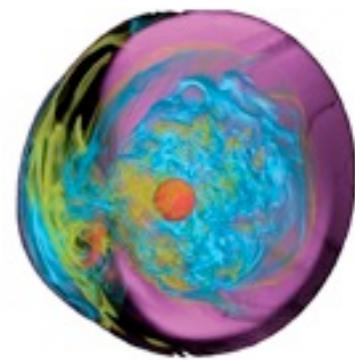
Nuclear EoS



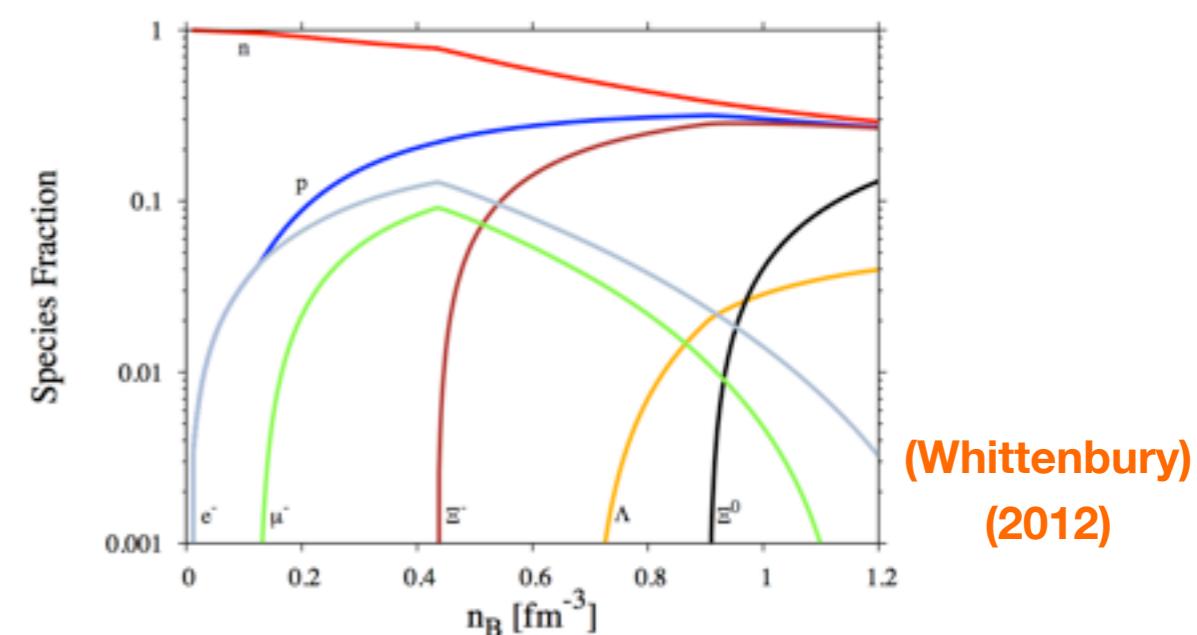
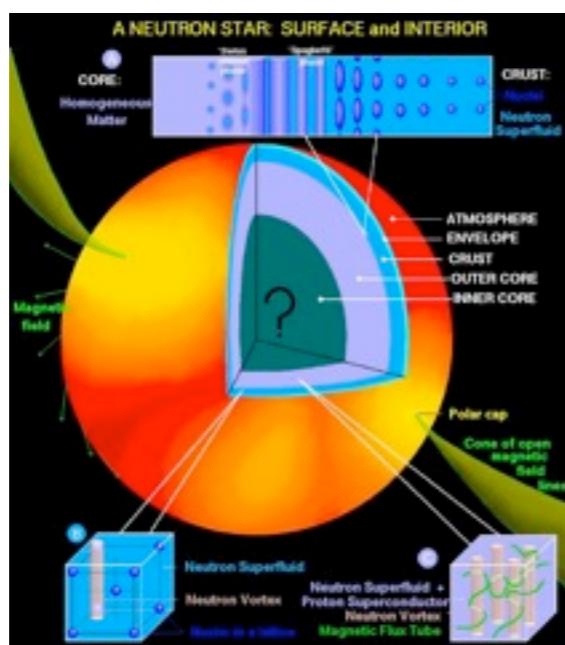
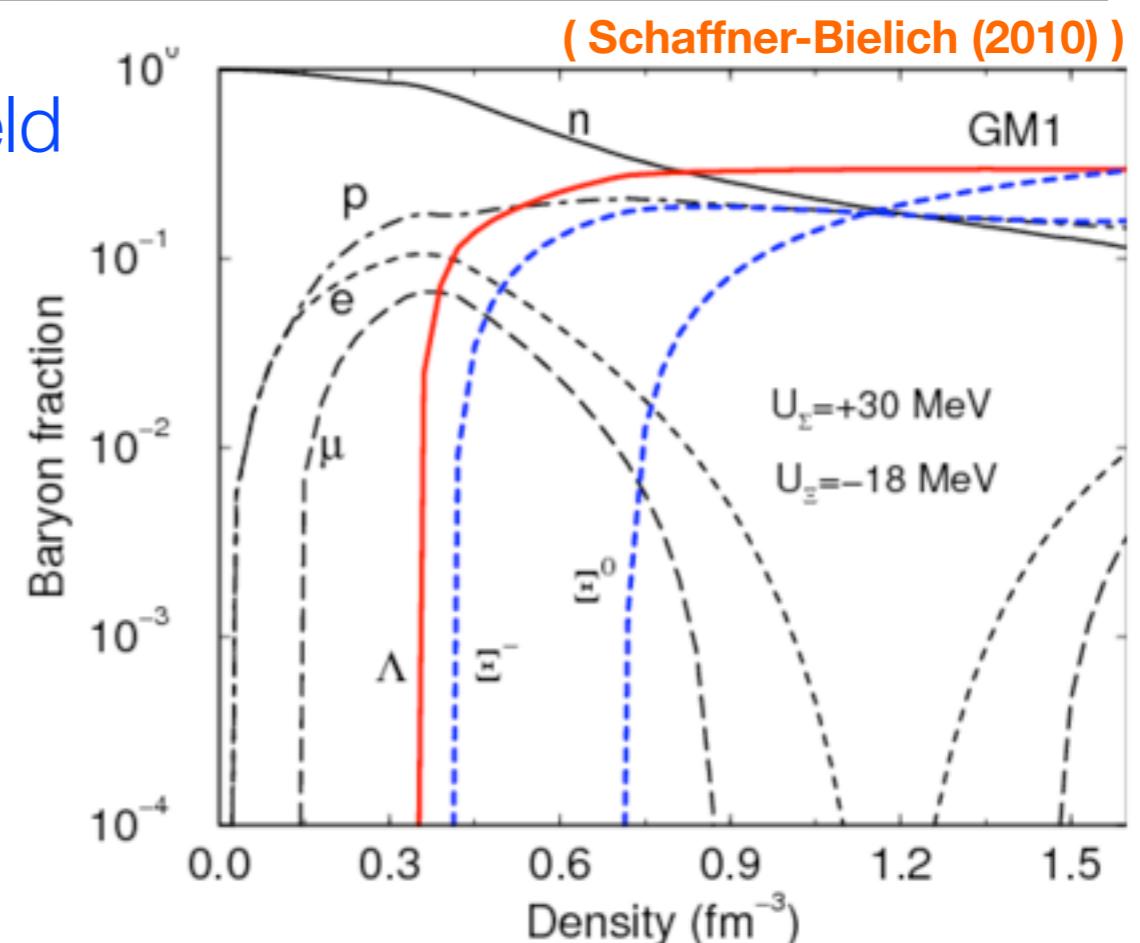
Role depends upon Interactions



Hyperons in Matter : Present Predictive Capability



Mean-Field
Models





Multi-Volume Study by NPLQCD

2009 - 2011

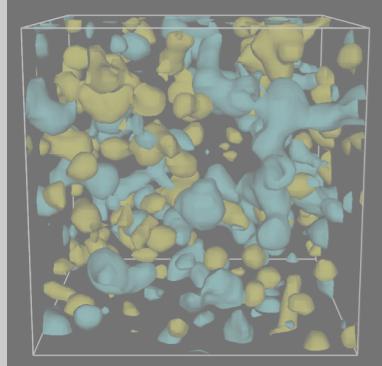


lattice spacing : $b \sim 0.123$ fm

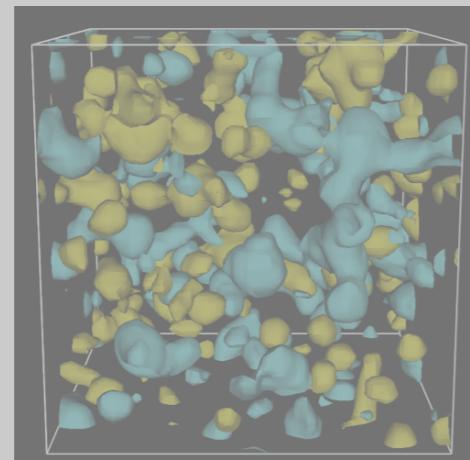
pion mass : $m_\pi \sim 390$ MeV

fermion action : Clover

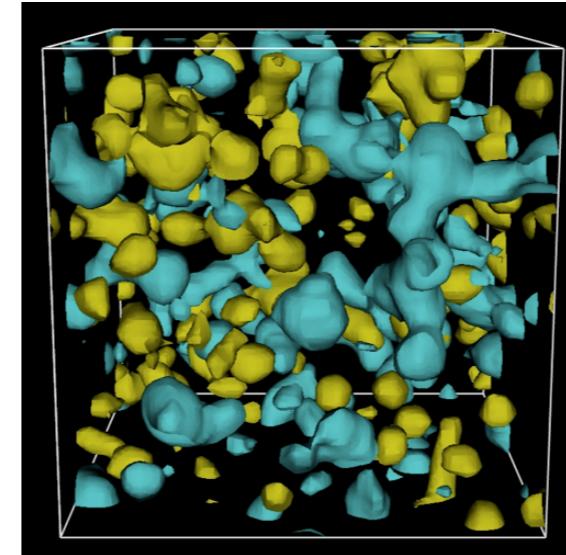
anisotropy : $\xi_t \sim 3.5$



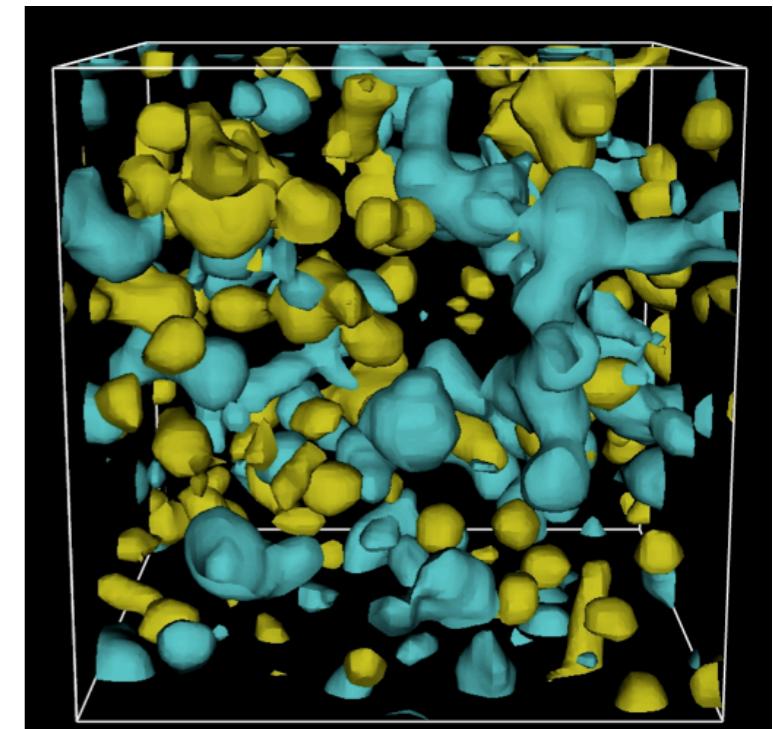
$L \sim 2$ fm



$L \sim 2.5$ fm



$L \sim 3$ fm



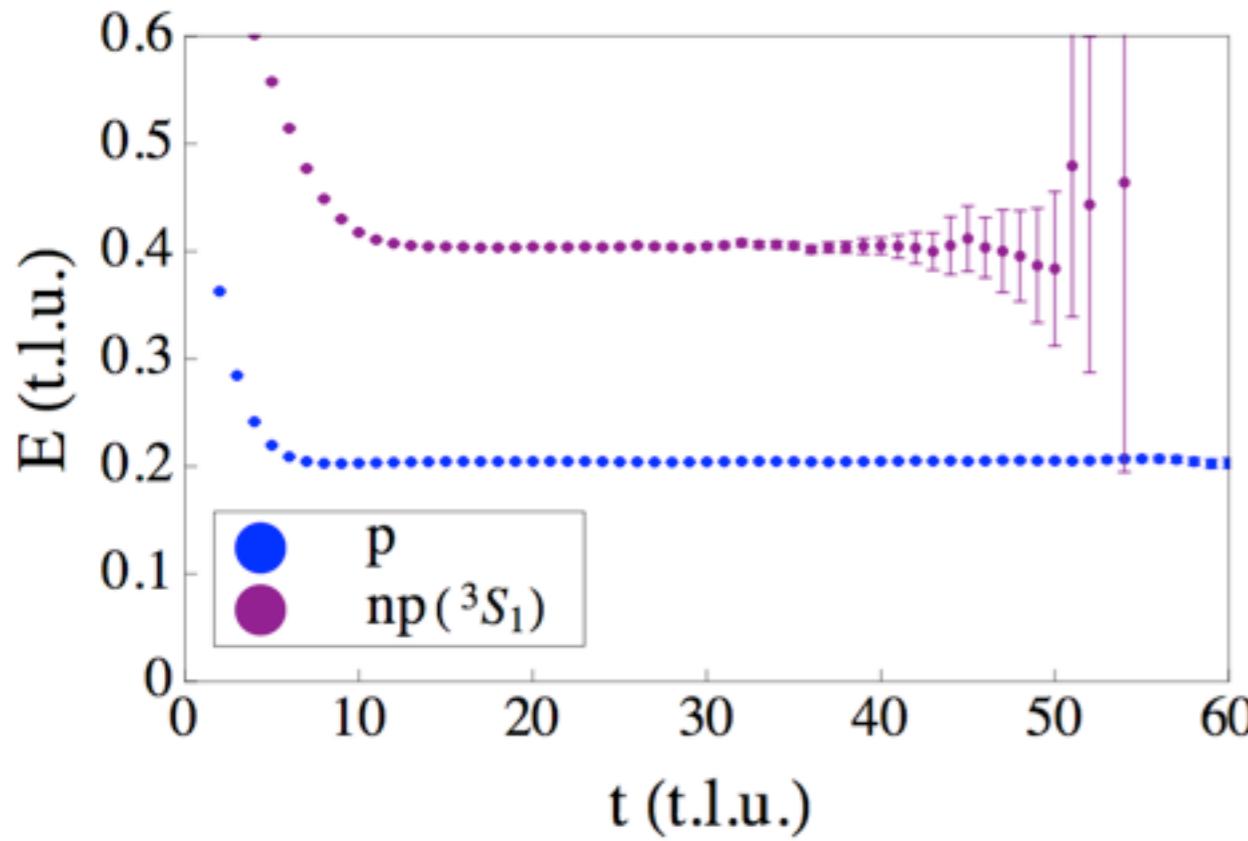
$L \sim 4$ fm

resources : $\sim 80 \times 10^6$ core hrs

$m_\pi L \sim 4, 5, 6, 8$ $m_\pi T \sim 9, 9, 9, 18$



Multi-Volume Study by NPLQCD 2009 - 2011



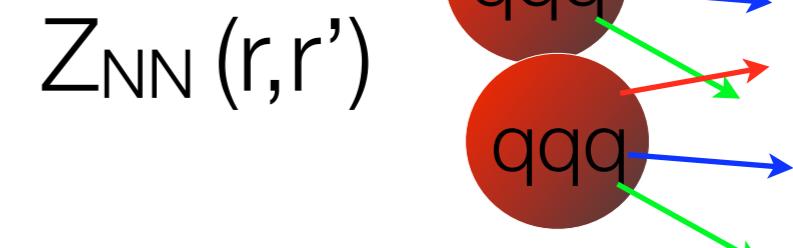
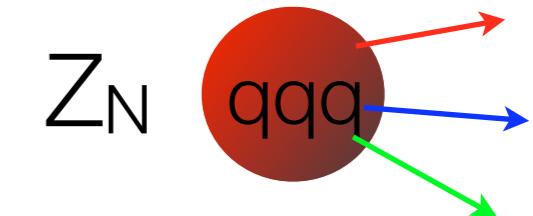
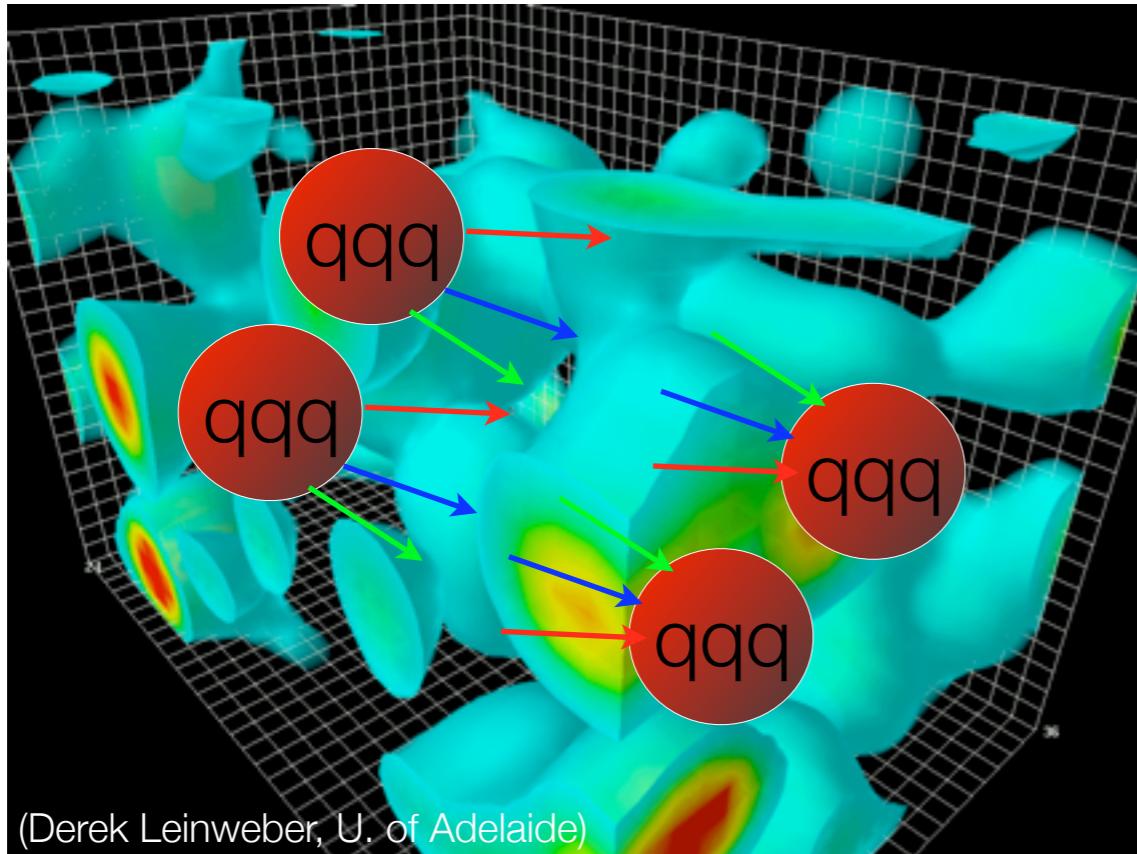
L	cfgs	srcs
24	2215	390,000
32	739	135,000

$L^3 \times T$	$16^3 \times 128$	$20^3 \times 128$	$24^3 \times 128$	$32^3 \times 256$	Extrapolation
L (fm)	~ 2.0	~ 2.5	~ 3.0	~ 4.0	∞
$m_\pi L$	3.86	4.82	5.79	7.71	∞
$m_\pi T$	8.82	8.82	8.82	17.64	∞
M_N (t.l.u.)	0.21004(44)(85)	0.20682(34)(45)	0.20463(27)(36)	0.20457(25)(38)	0.20455(19)(17)
M_Λ (t.l.u.)	0.22446(45)(78)	0.22246(27)(38)	0.22074(20)(42)	0.22054(23)(31)	0.22064(15)(19)
M_Σ (t.l.u.)	0.22861(38)(67)	0.22752(32)(43)	0.22791(24)(31)	0.22726(24)(43)	0.22747(17)(19)
M_Ξ (t.l.u.)	0.24192(38)(63)	0.24101(27)(38)	0.23975(20)(32)	0.23974(17)(31)	0.23978(12)(18)

n n

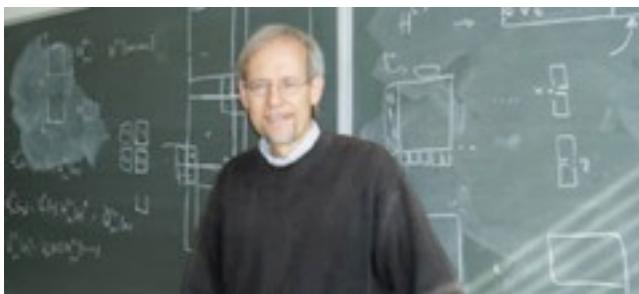
Generic Calculations of 2-Body Interactions

n n

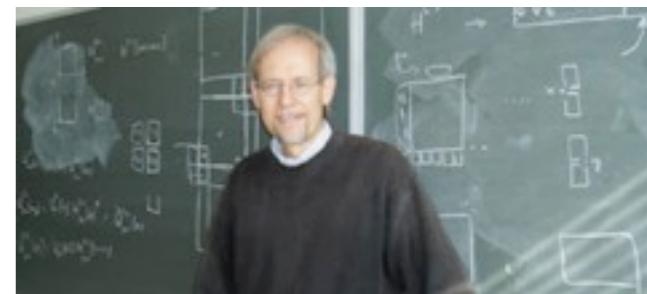


1) Maiani-Testa Theorem

2) Luscher : Measure energy-eigenvalues of the two-hadron system



A Primer - 1990 : Lüscher says



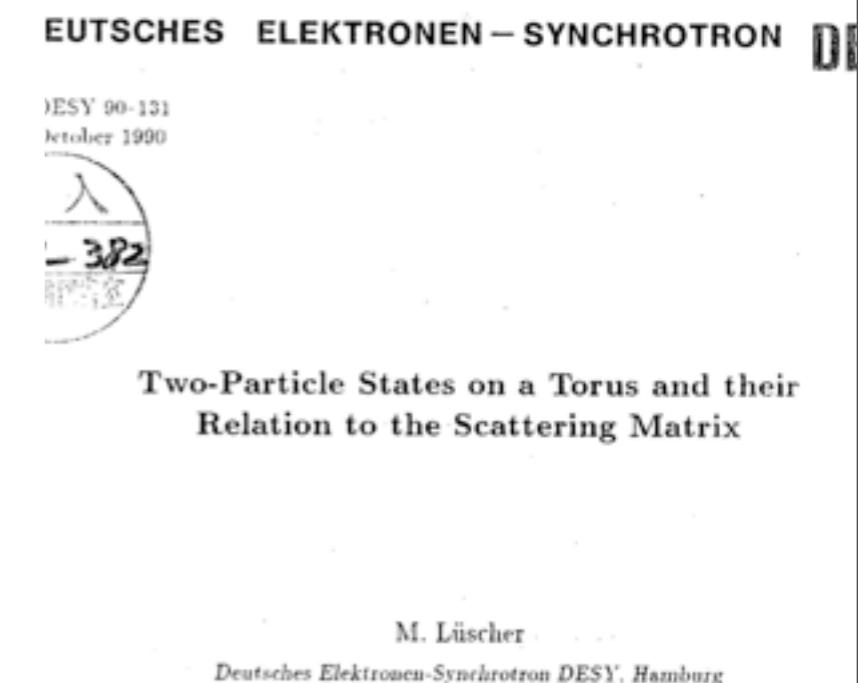
Explicitly, the stationary effective Schrödinger equation in the centre-of-mass frame reads

$$-\frac{1}{2\mu} \Delta \psi(\mathbf{r}) + \frac{1}{2} \int d^3 r' U_E(\mathbf{r}, \mathbf{r}') \psi(\mathbf{r}') = E \psi(\mathbf{r}), \quad (7.1)$$

where the parameter E is related to the true energy W of the system through

$$W = 2\sqrt{m^2 + mE}. \quad (7.2)$$

The “potential” $U_E(\mathbf{r}, \mathbf{r}')$ is the Fourier transform of the modified Bethe-Salpeter kernel $\hat{U}_E(\mathbf{k}, \mathbf{k}')$ introduced in ref.[3]. It depends analytically on



38

E in the range $-m < E < 3m$ and is a smooth function of the coordinates \mathbf{r} and \mathbf{r}' , decaying exponentially in all directions \mathbf{f} . Furthermore, the potential

It therefore follows that....

Taking U to be energy-independent is a model-dependent assertion and not a QCD prediction

n n

Two-Particle Energy Levels (Luscher)

n n

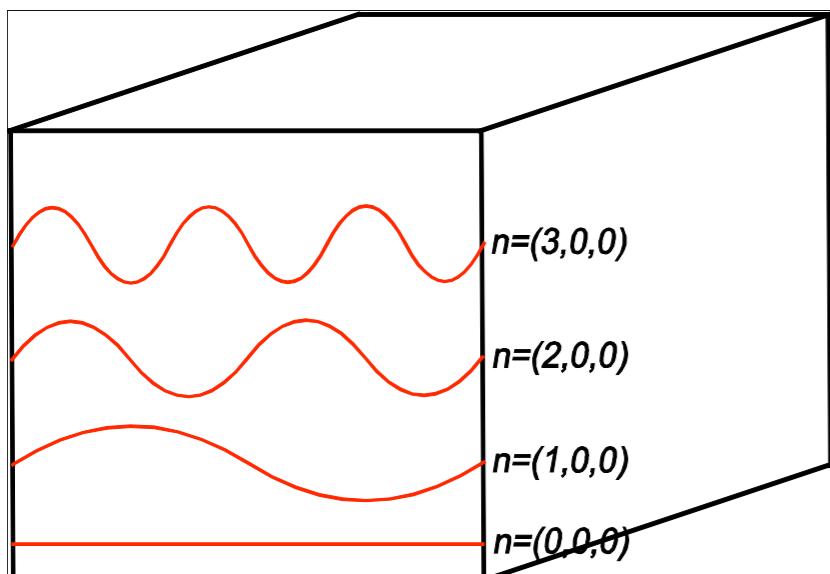
Below Inelastic Thresholds :

Measure on lattice



$$\delta E = 2\sqrt{p^2 + m^2} - 2m$$

$$p \cot \delta(p) = \frac{1}{\pi L} \mathbf{S} \left(\left(\frac{Lp}{2\pi} \right)^2 \right)$$



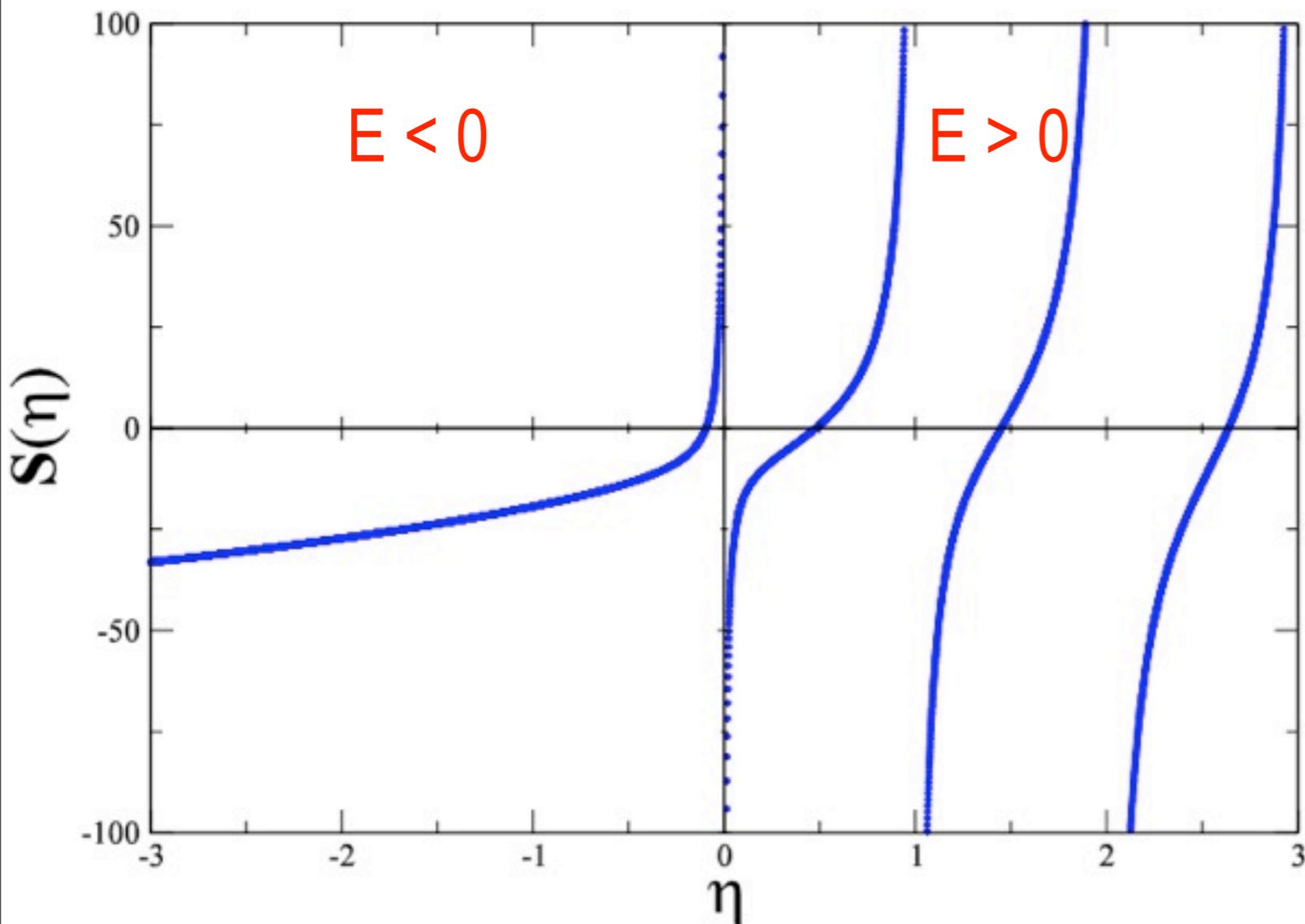
$$\mathbf{S}(\eta) \equiv \sum_j \frac{1}{|\mathbf{j}|^2 - \eta} - 4\pi \Lambda_j$$

Gives the scattering amplitude at δE

n n

Luscher Eigenvalue Relation

n n



A_1^+
Bound-state or
Scattering state ?

$$p \cot \delta(p) = \frac{1}{\pi L} \mathbf{S} \left(\left(\frac{Lp}{2\pi} \right)^2 \right)$$

Non-interacting particles

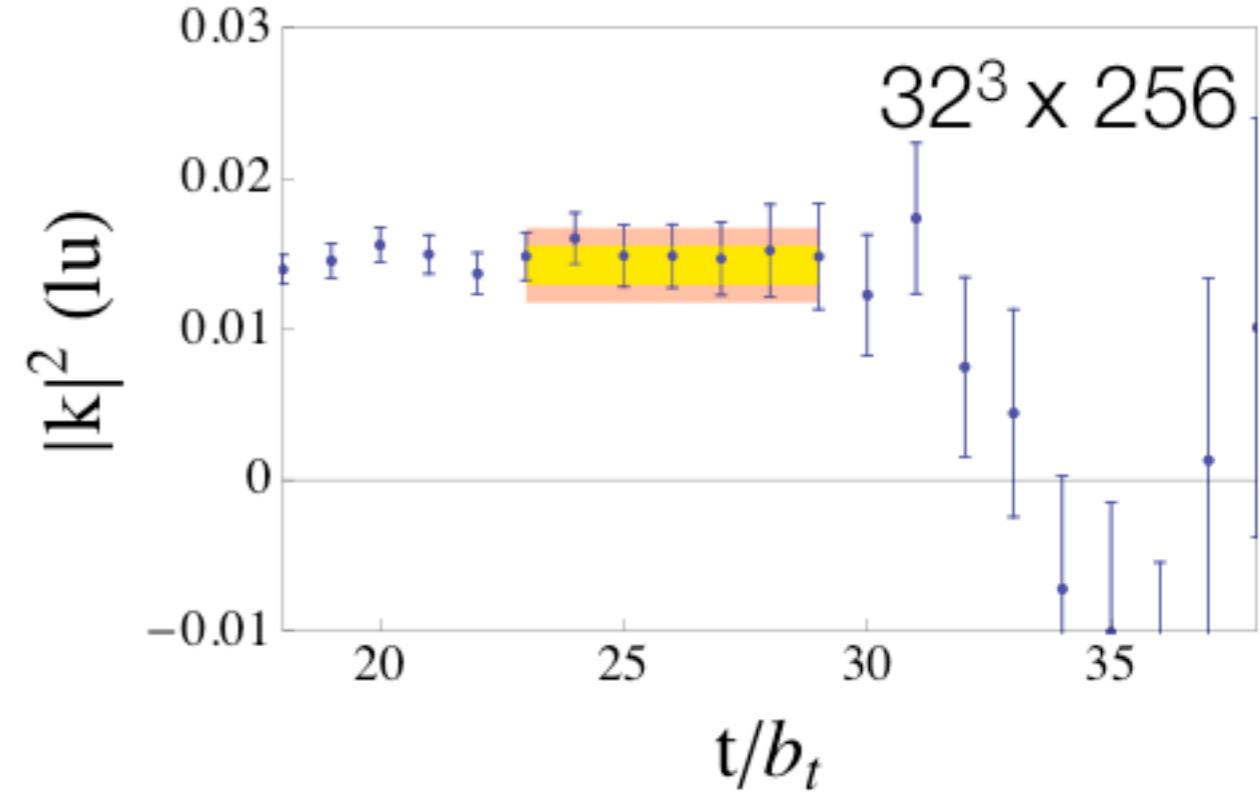
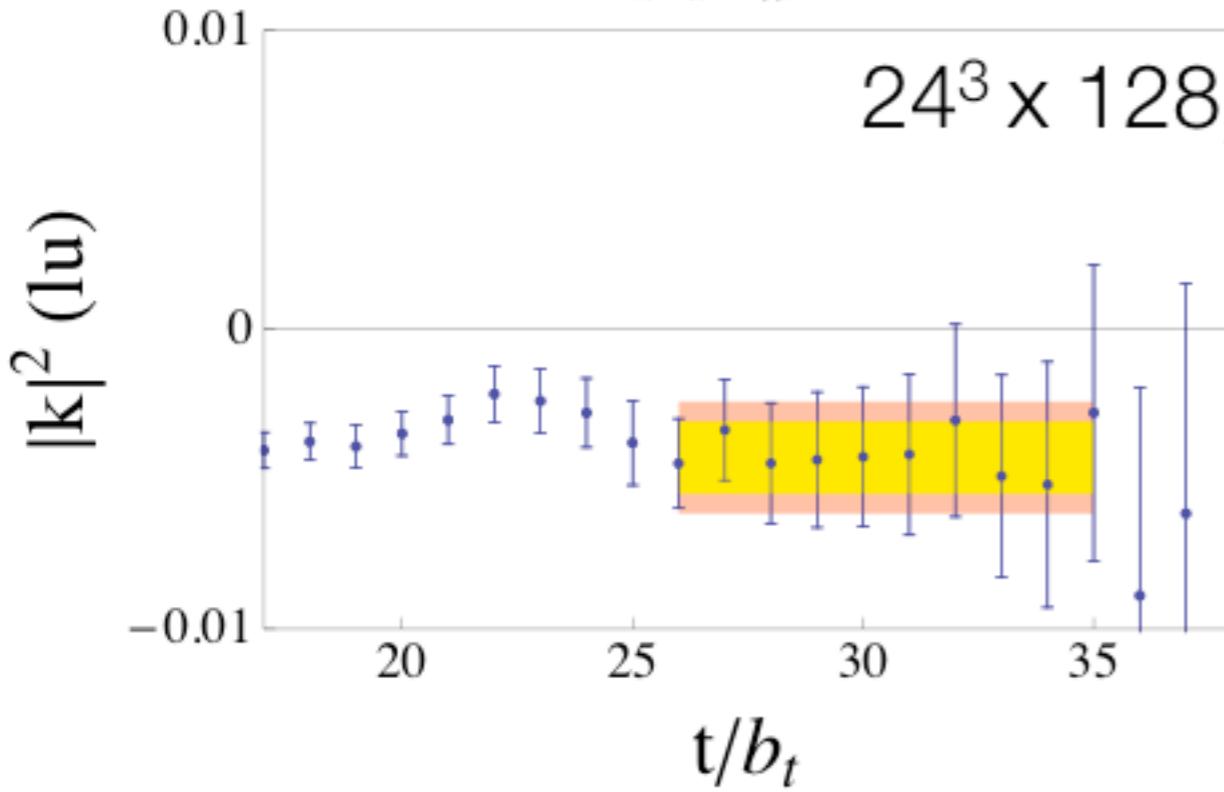
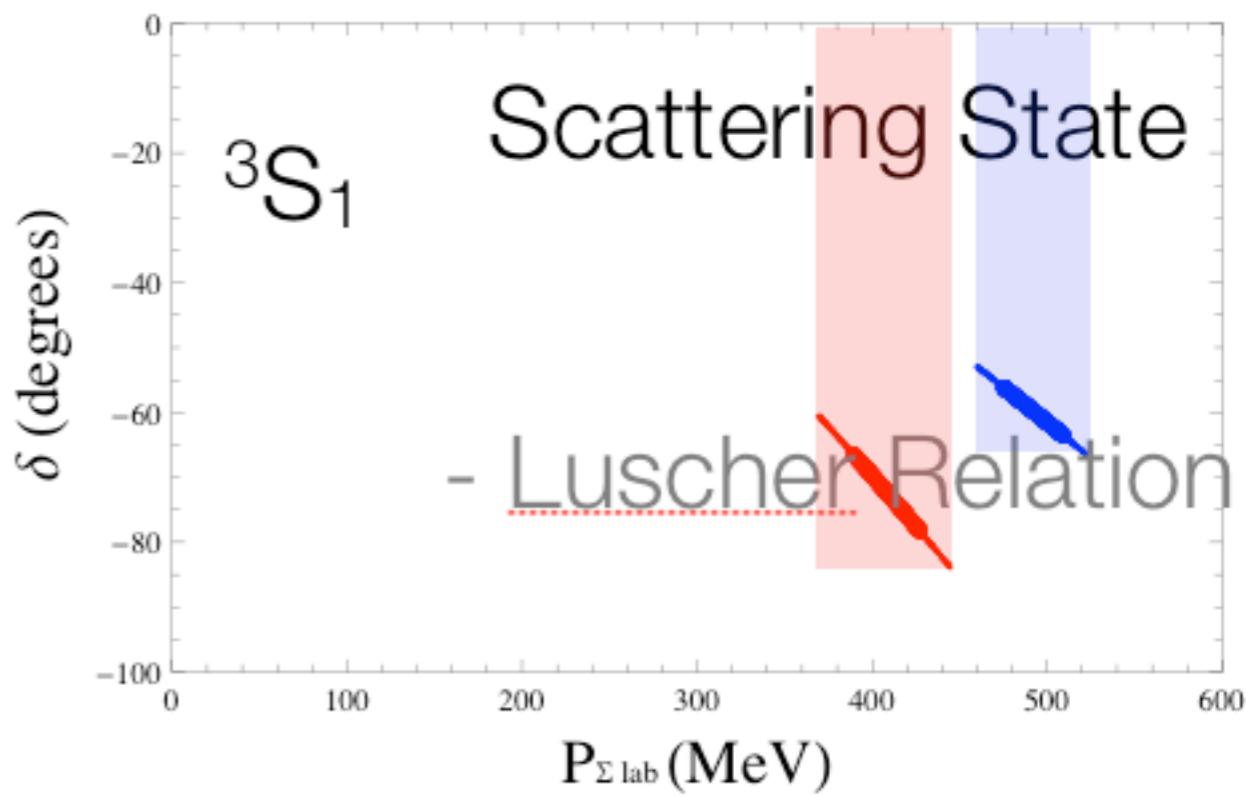
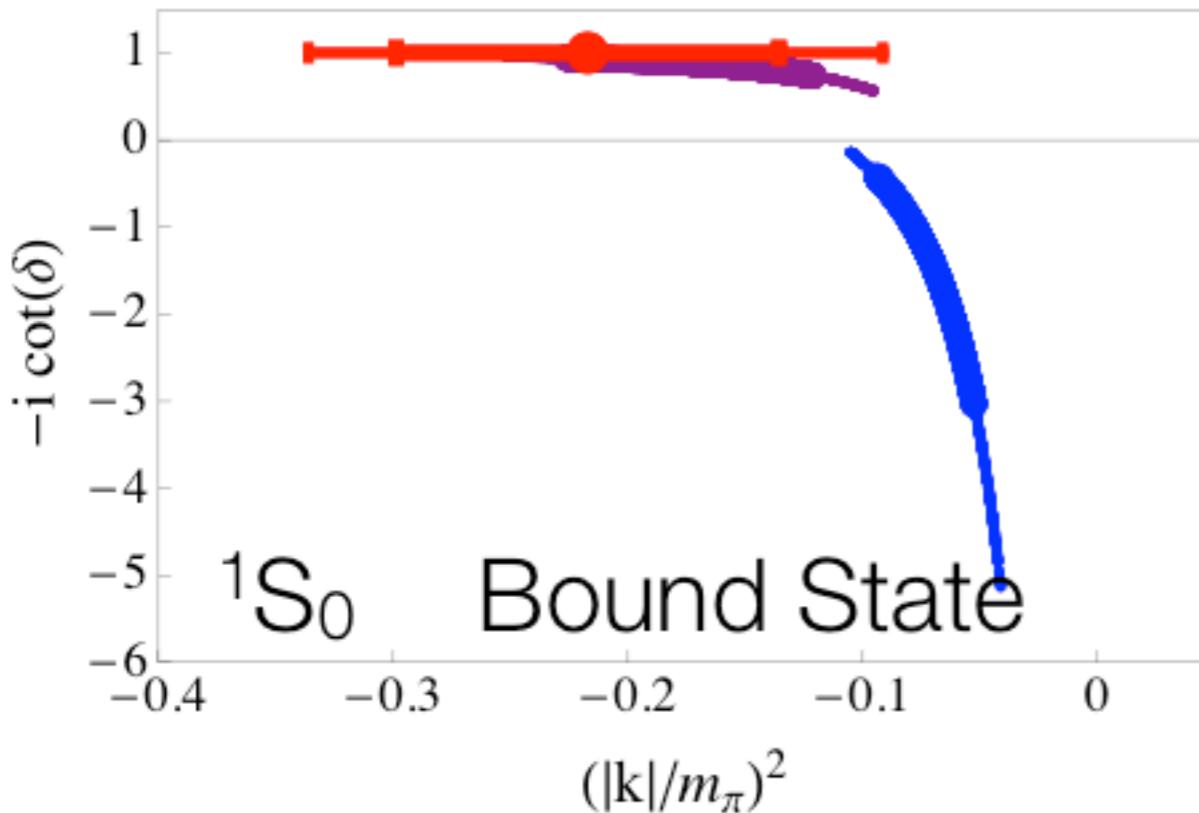
$$\begin{aligned} V &= 0 & \rightarrow & \quad a = r = 0 \\ S &= \infty \end{aligned}$$

$$k = \frac{2\pi}{L} n$$

$$n = (nx, ny, nz)$$



$n\Sigma^-$ at a pion mass of ~ 390 MeV

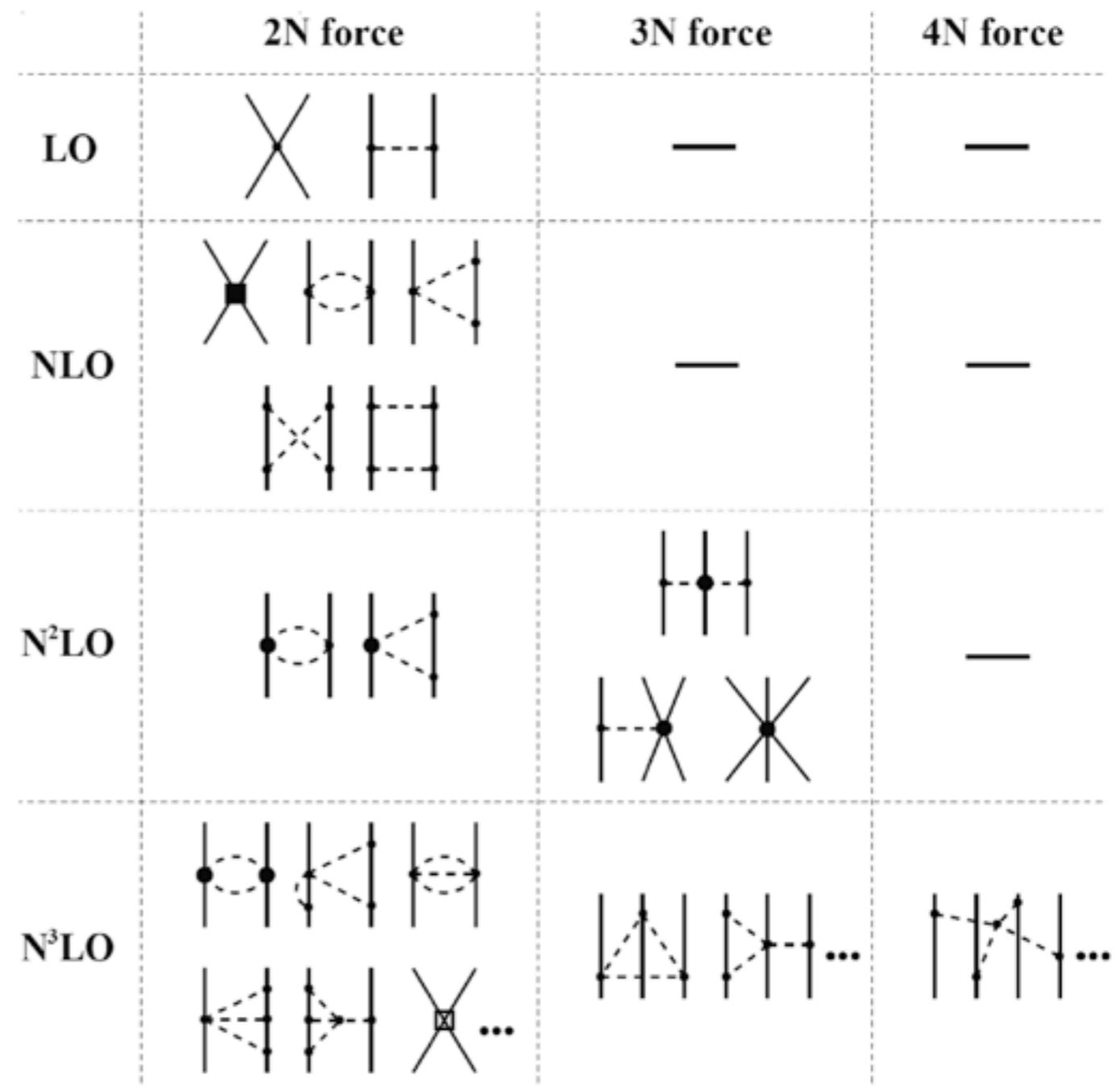




QCD-Based Organization of Nuclear Forces

Effective Field Theory introduced by Weinberg in the early 1990's to systematize nuclear forces

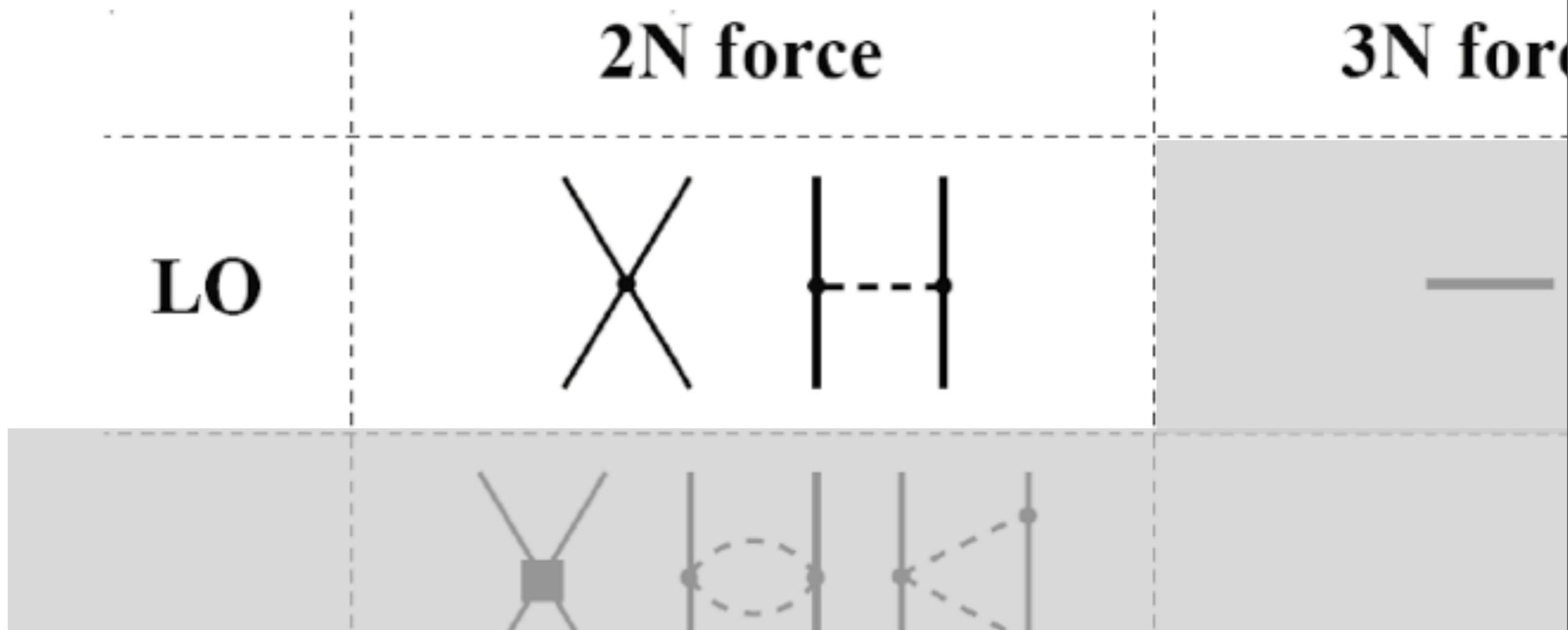
- Low-energy EFT of QCD
- Chiral symmetries of QCD
- Quark mass dependence
- Renormalization Group
 - Softer Interactions
 - V_{lowk} , SRG





LO Weinberg in $n\Sigma^-$

- 1 : local 4-baryon contact interaction (1 parameter)
- 2 : one meson exchange (0 new parameters)





Convergence of (Systematic) Expansions of Potentials

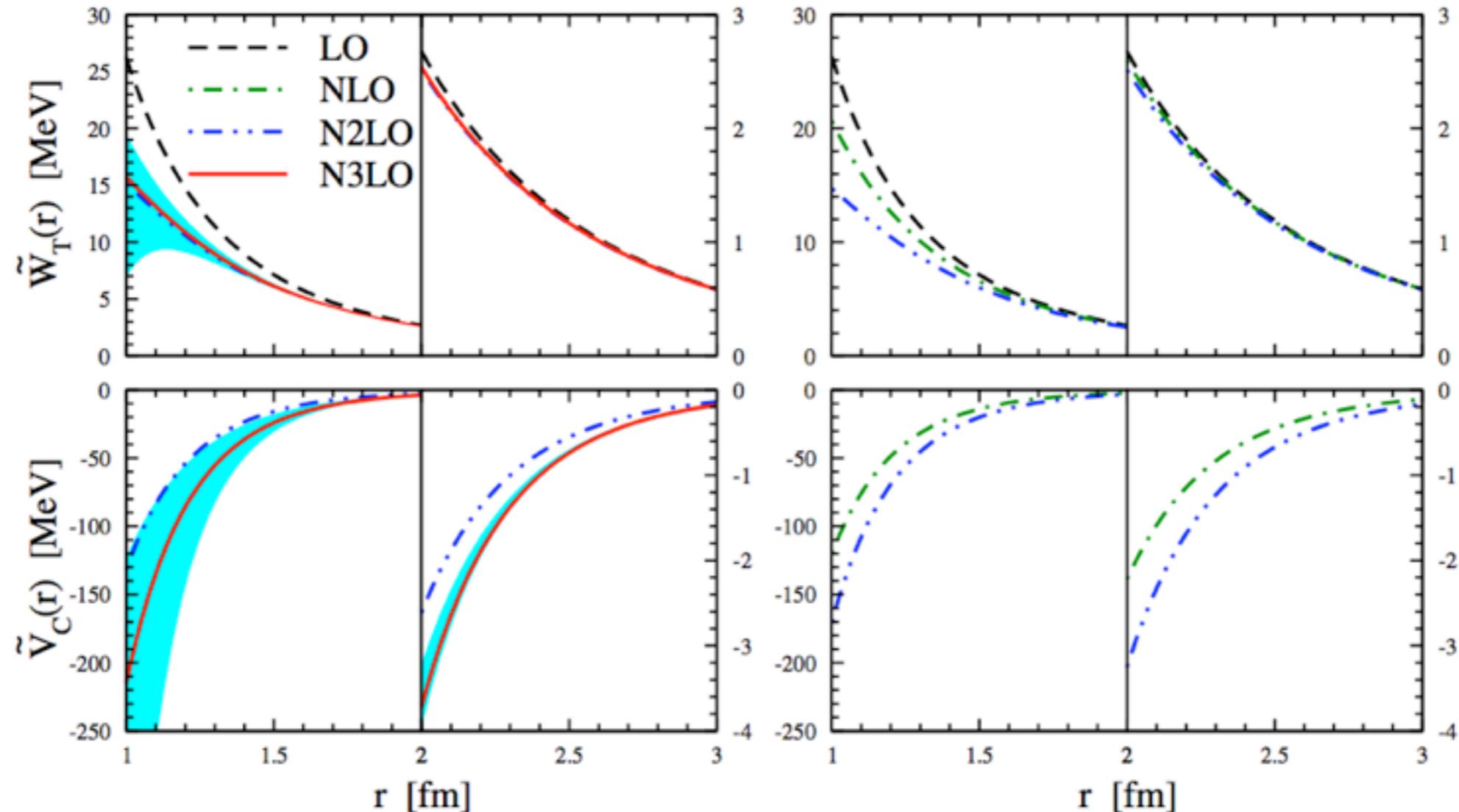


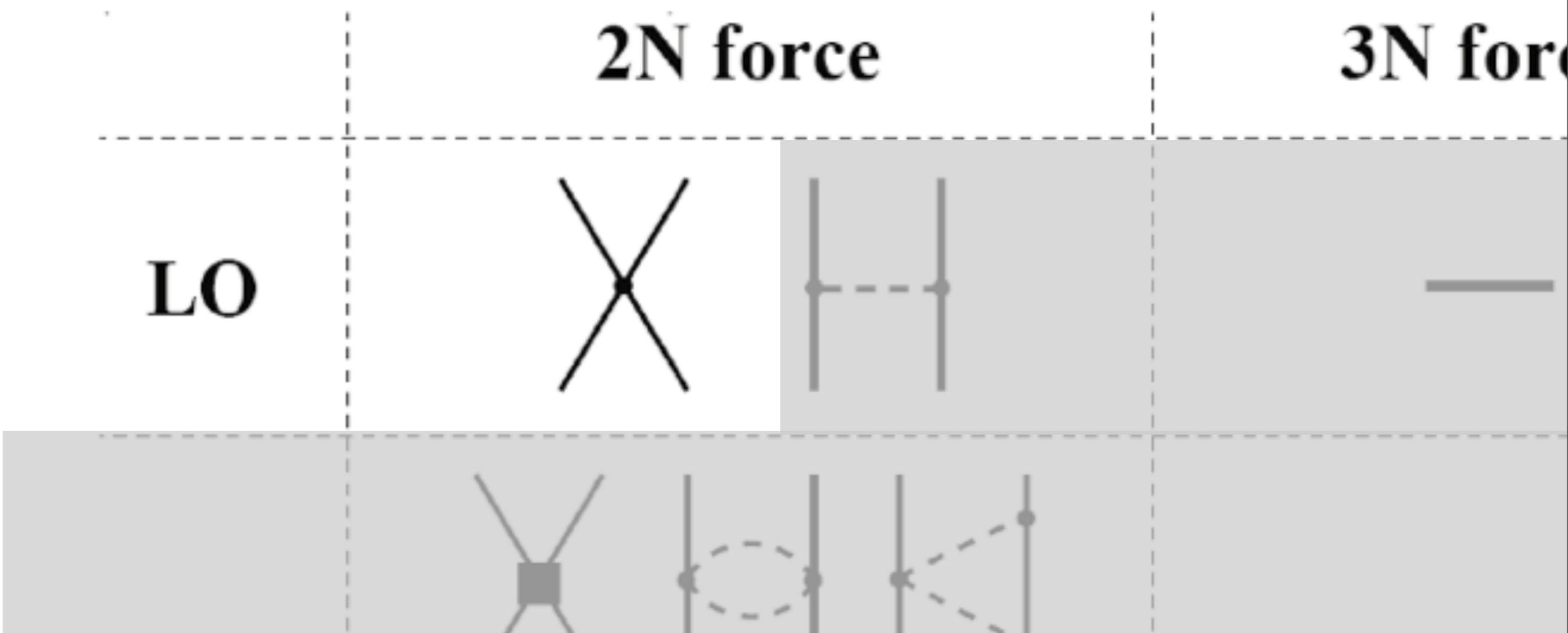
Figure 3: Chiral expansion of the isovector-tensor (upper row) and isoscalar central (lower row) long-range potentials $\tilde{W}_T(r)$ and $\tilde{V}_C(r)$, respectively. The left (right) panel shows the results for the EFT without (with) explicit $\Delta(1232)$ degrees of freedom. The light-shaded band shows the estimation of the intrinsic model dependence associated with the short-range components as explained in the text (only shown for the theory without deltas).



LO Weinberg in $n\Sigma^-$

Require regulation - use simple compact shape

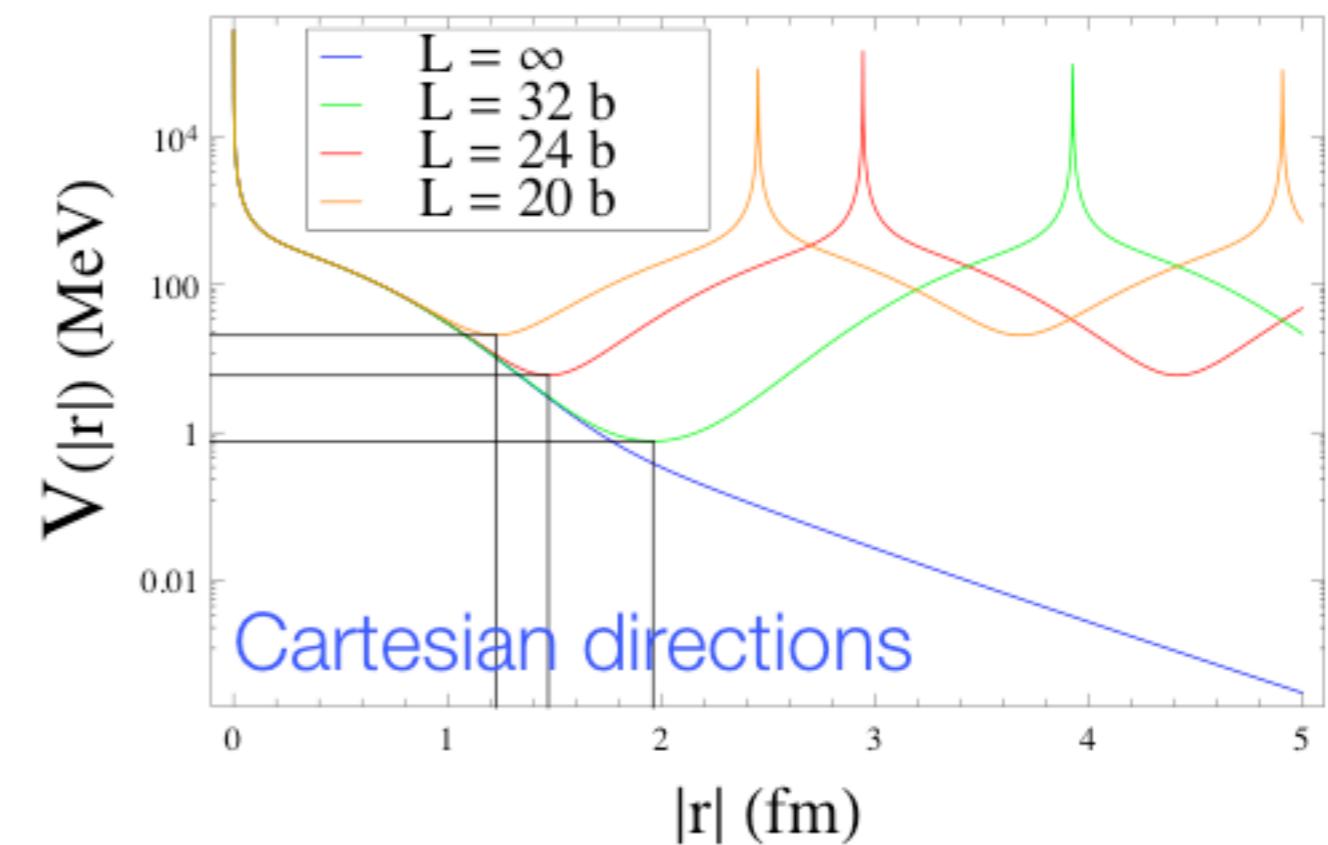
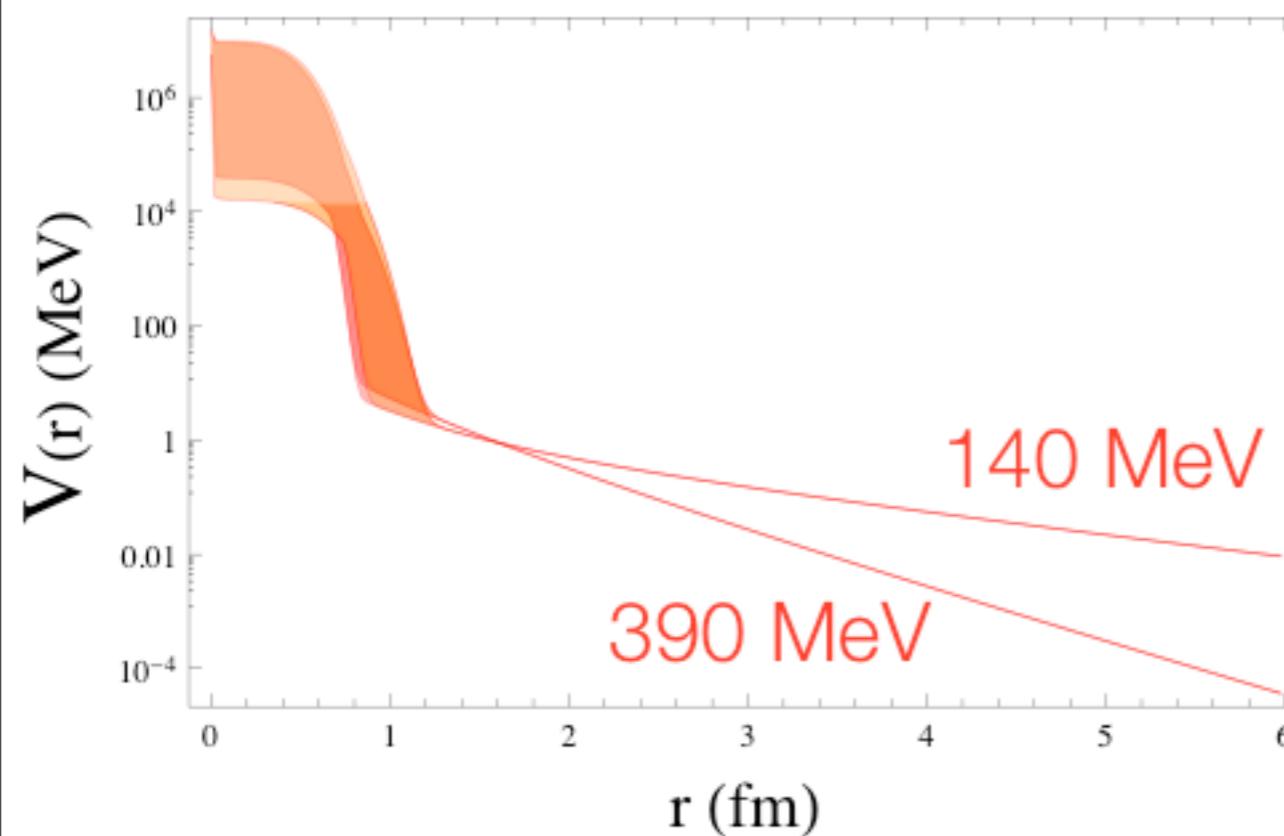
- square-well, Gaussian, exponential
- one length scale, one coupling





3S_1 : 3-d Schrodinger, Modifications to Luscher's Relation ?

- diagonalize H in full 3-d mom. space (constrained by L and a)
- choose $R \ll 1/m_{\text{mes}}$ and fix C_0 to energy-eigenvalue
- extended repulsive core - Luscher ?
- use both Luscher and Weinberg EFT
 - phase-shifts are same within uncertainties!

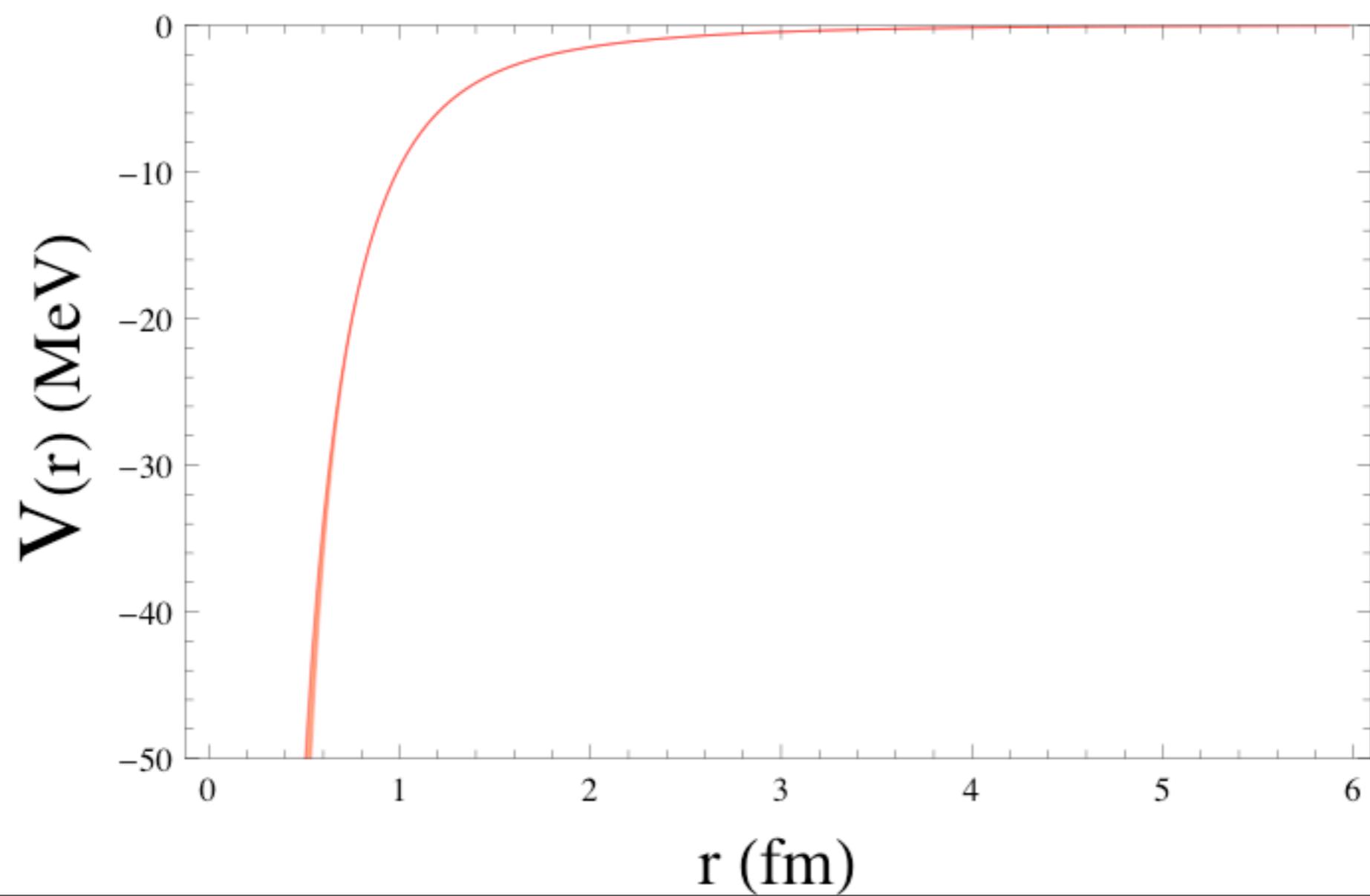


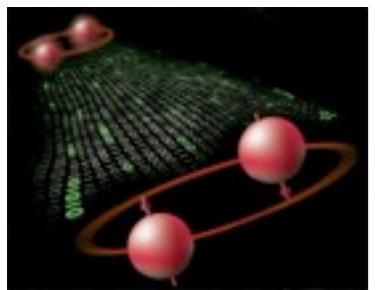


1S_0 : 3-d Schrodinger, Modifications to Luscher's Relation ?

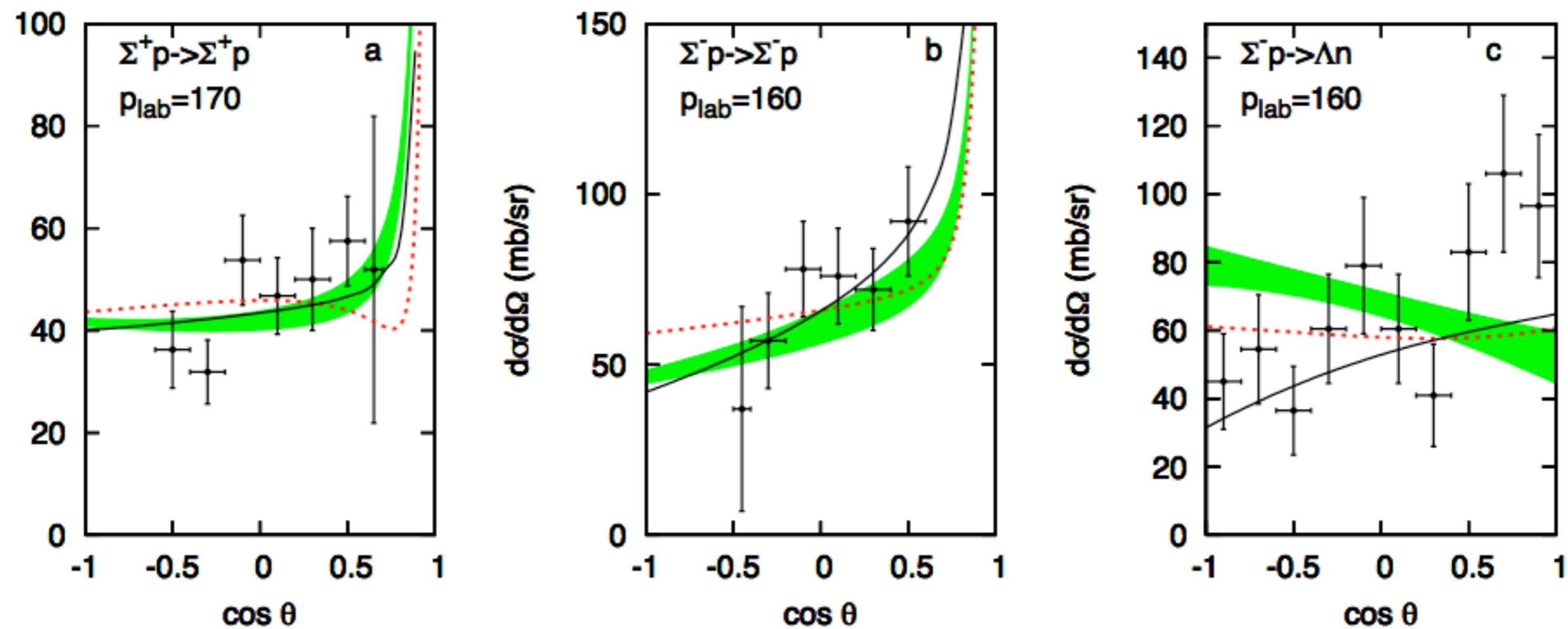


Attractive core is compact - Luscher's relation is valid

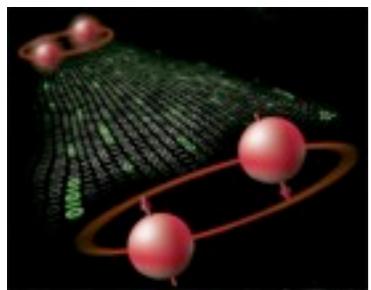




Hyperon Nucleon Interactions



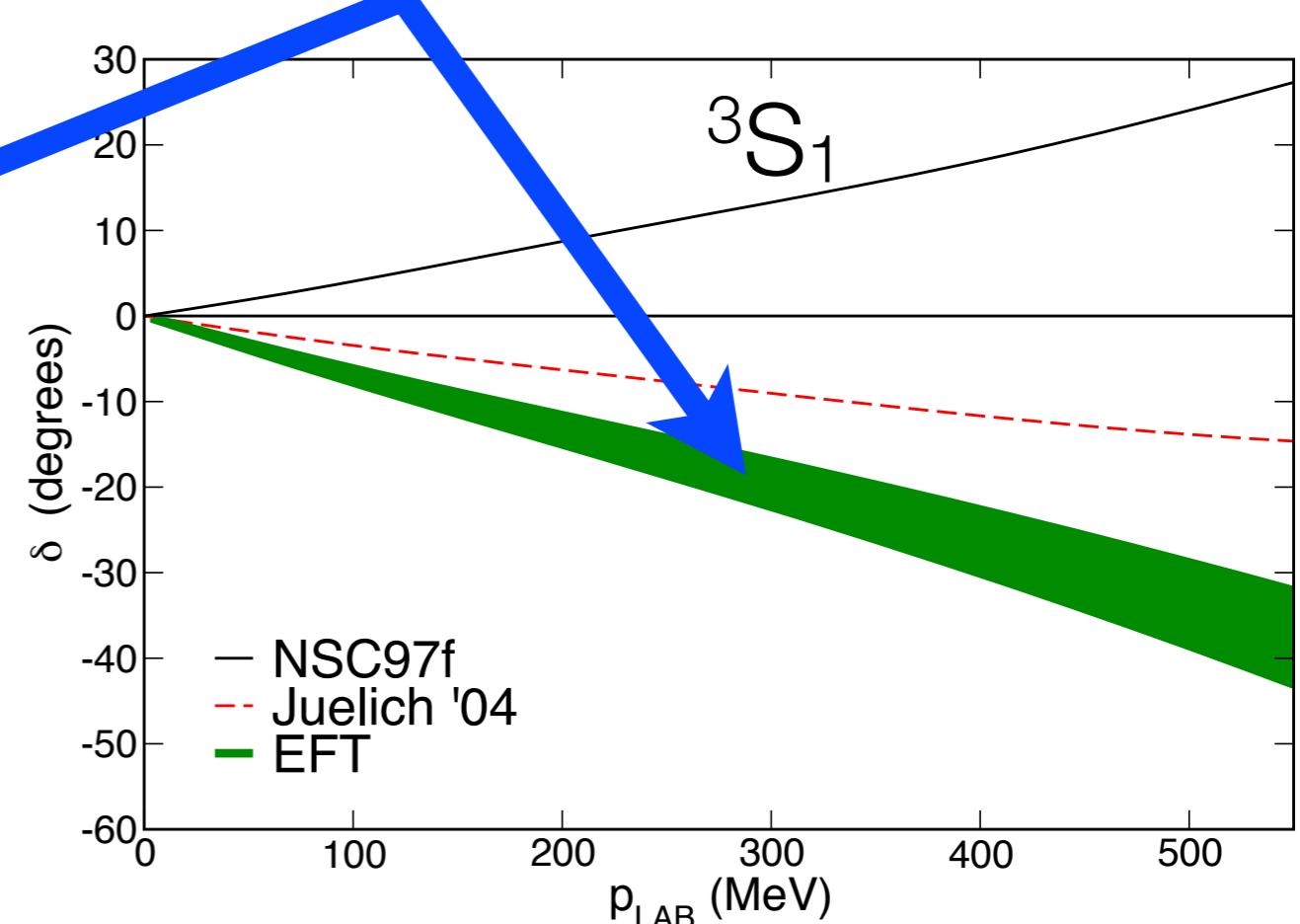
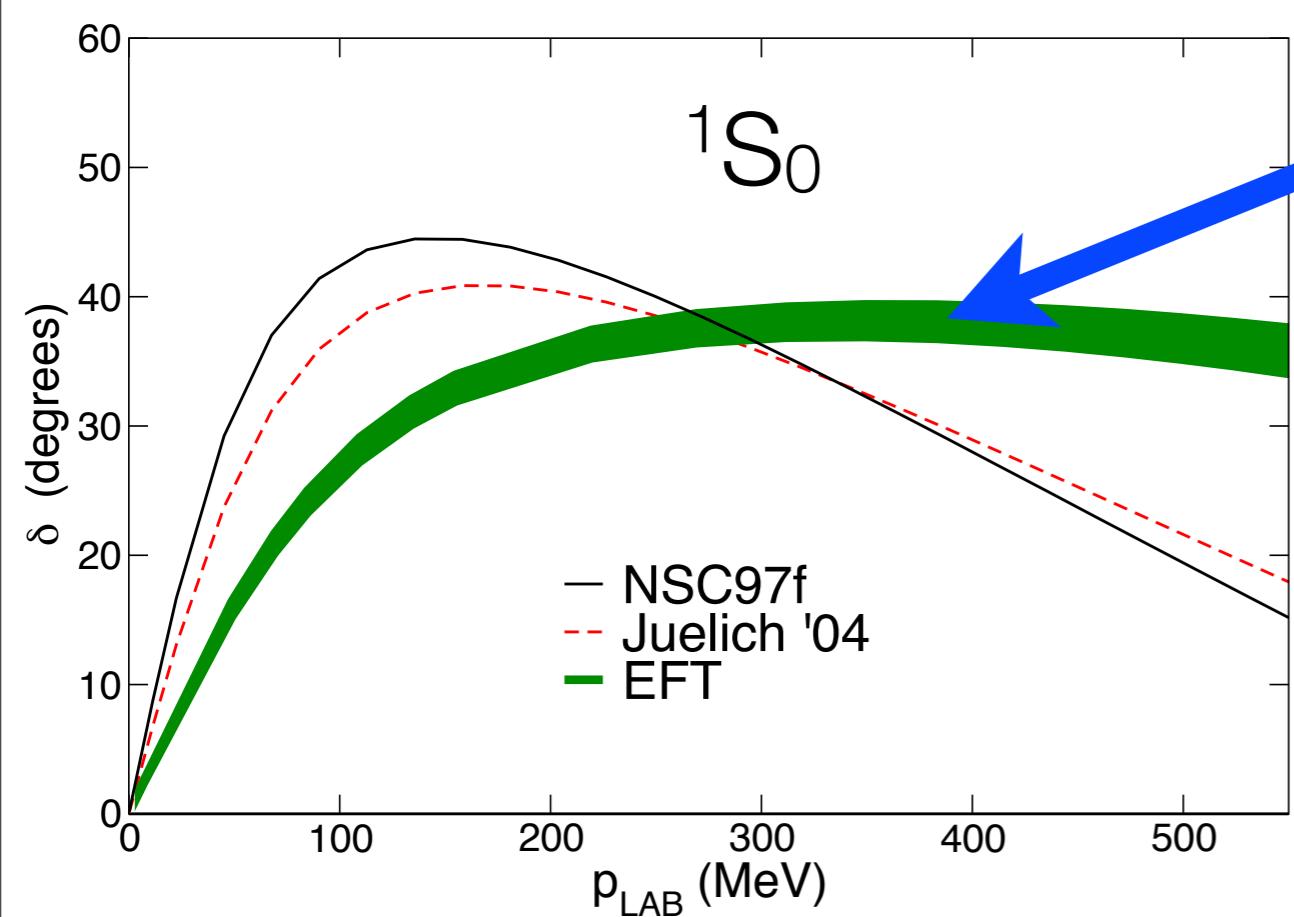
Haidenbauer and Meissner (2007)

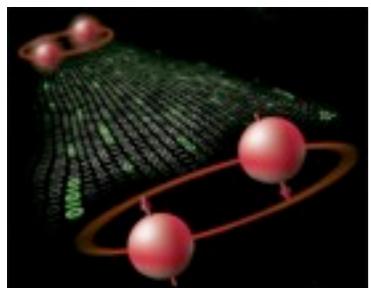


Hyperon Nucleon Interactions



Meissner+Haidenbauer - Experiment + YN-EFT (LO)

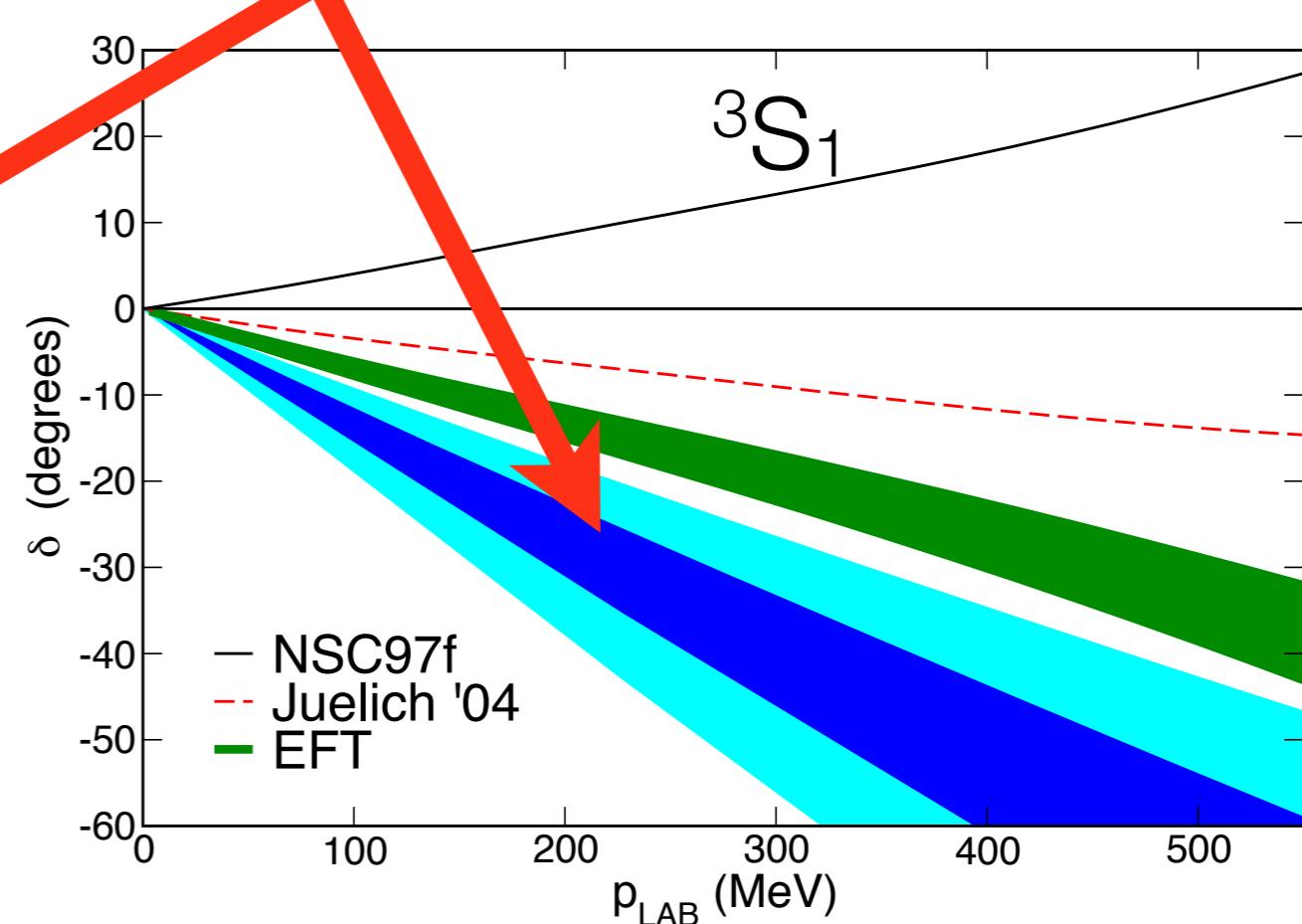
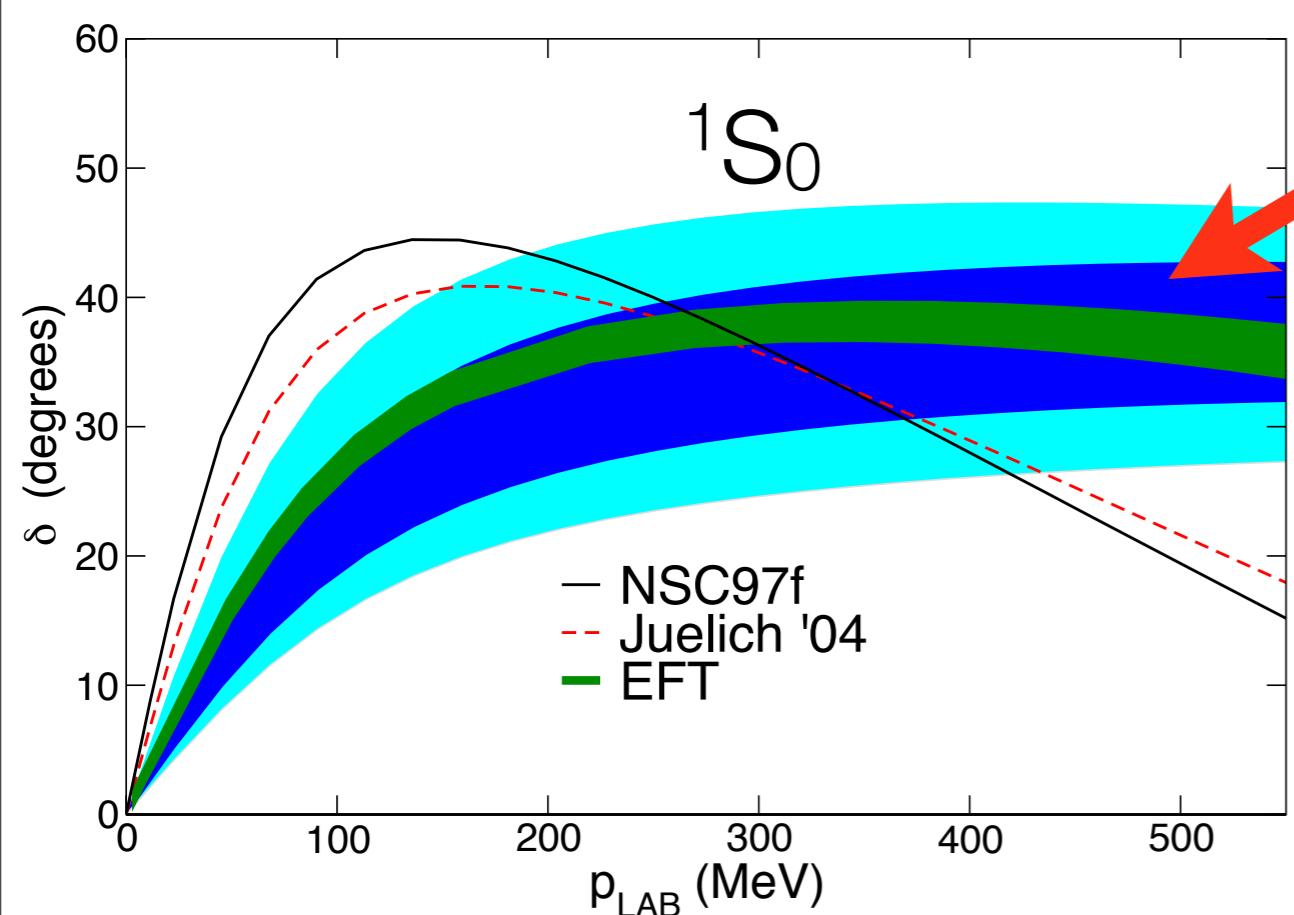


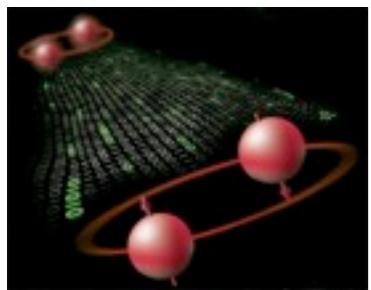


Hyperon Nucleon Interactions

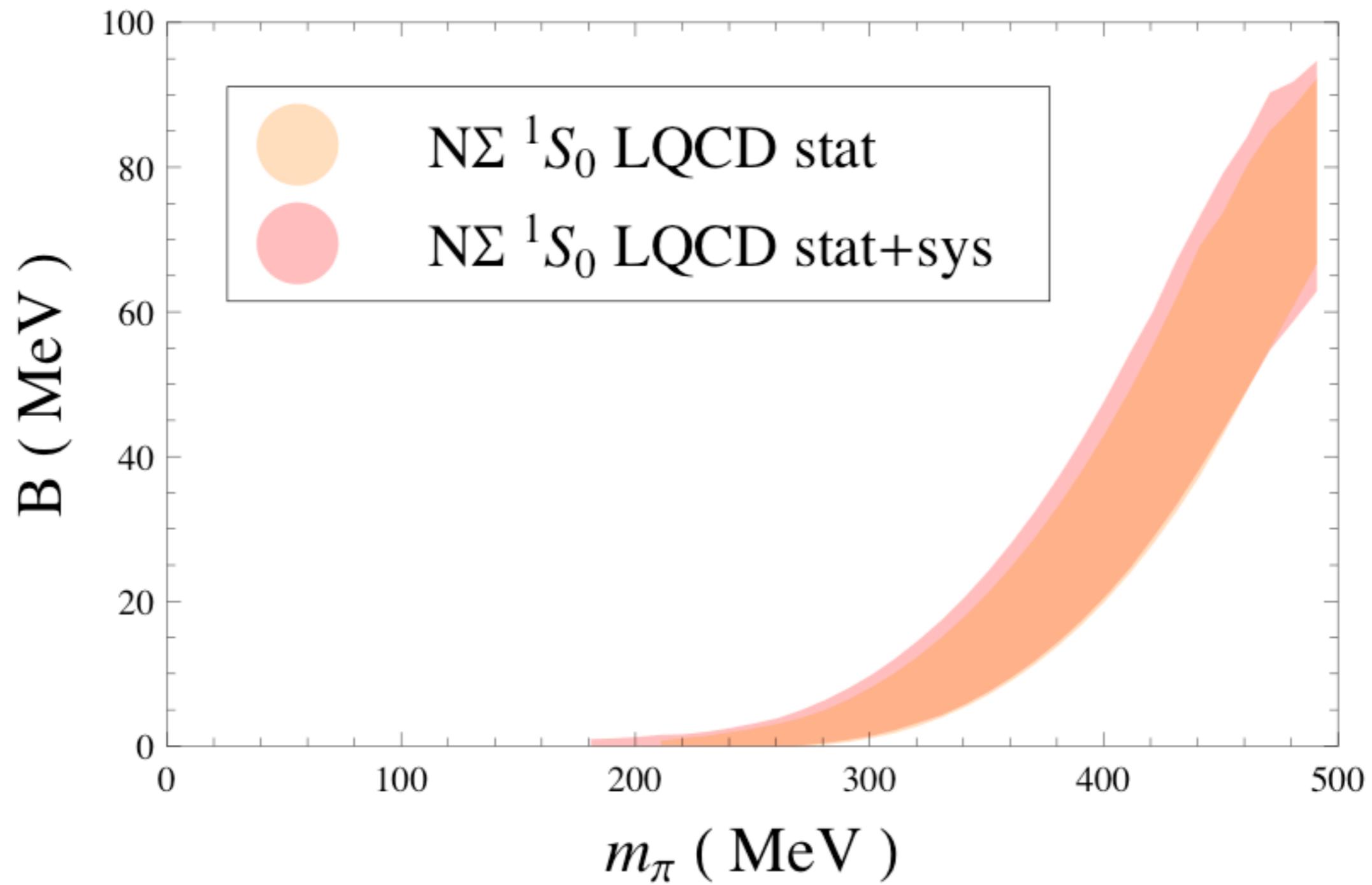


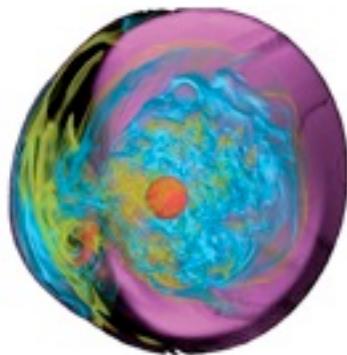
NPLQCD - Lattice QCD + YN-EFT (LO)





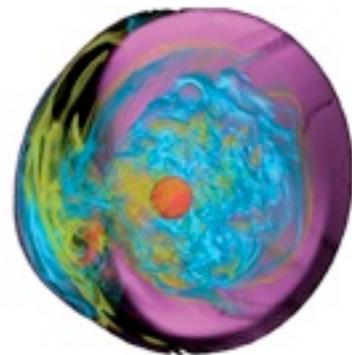
Binding in the Singlet Channel



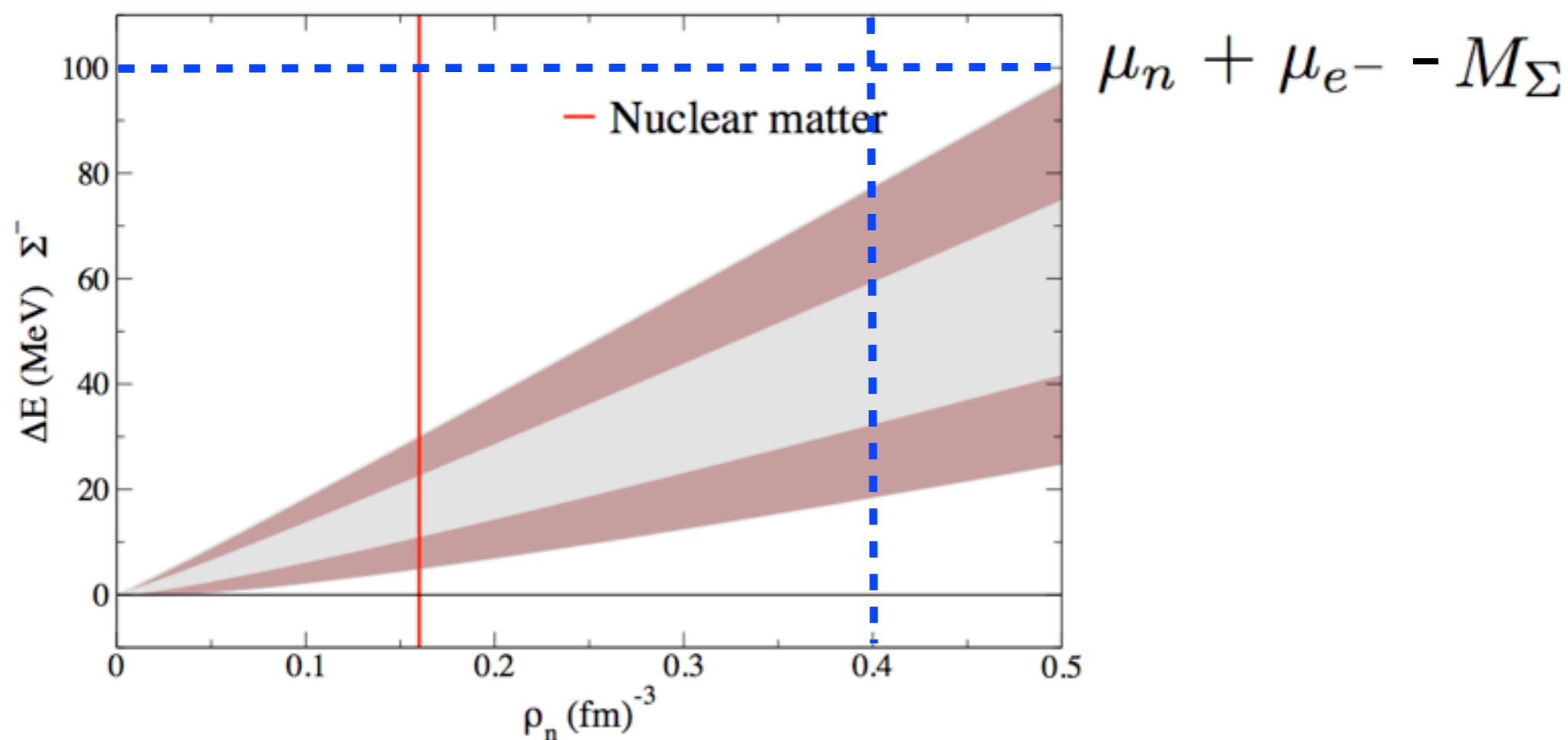


Σ^- in Dense Matter

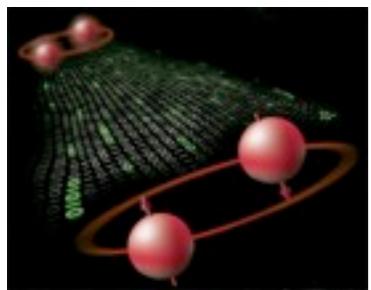
Fumi Limit Approx. (assertions)



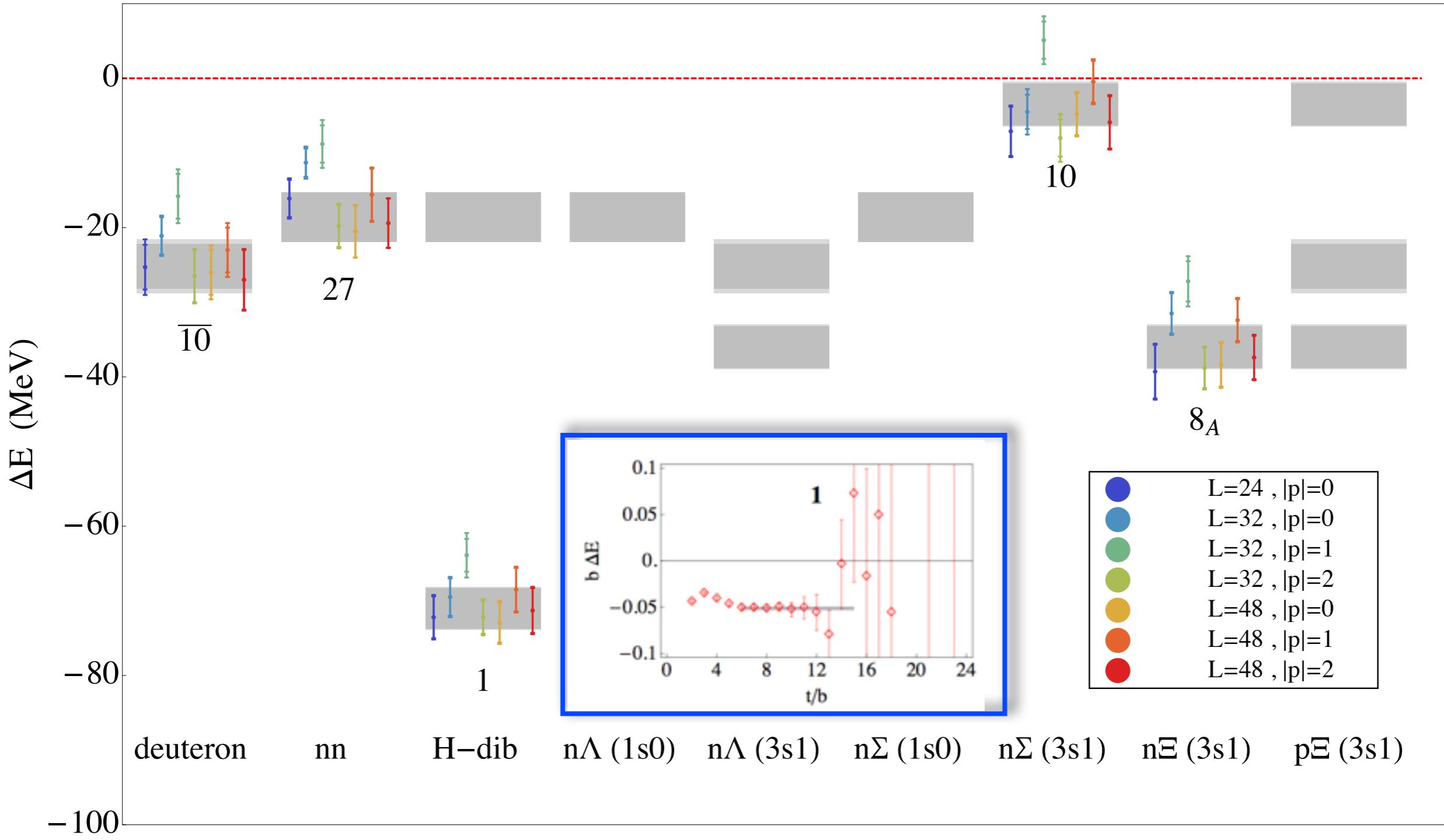
$$\Delta E = -\frac{1}{\pi\mu} \int_0^{k_f} dk k \left[\frac{3}{2}\delta_{^3S_1}(k) + \frac{1}{2}\delta_{^1S_0}(k) \right]$$



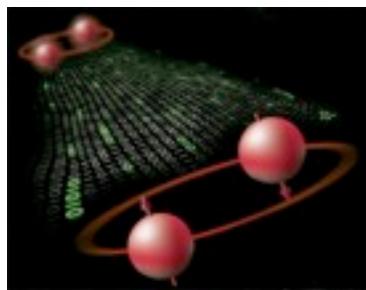
Cancellation between channels in dense matter
energy-shift of hyperon



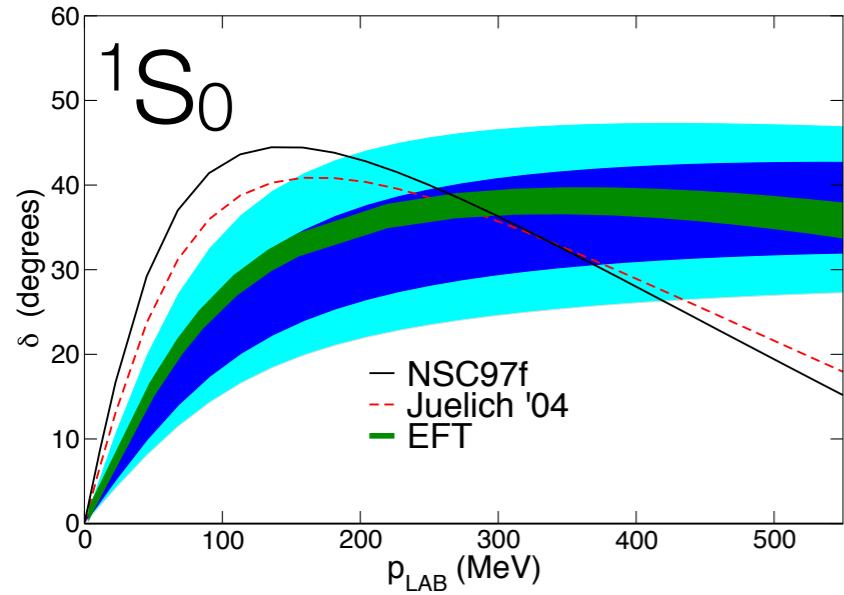
SU(3) Limit - Isotropic Clover



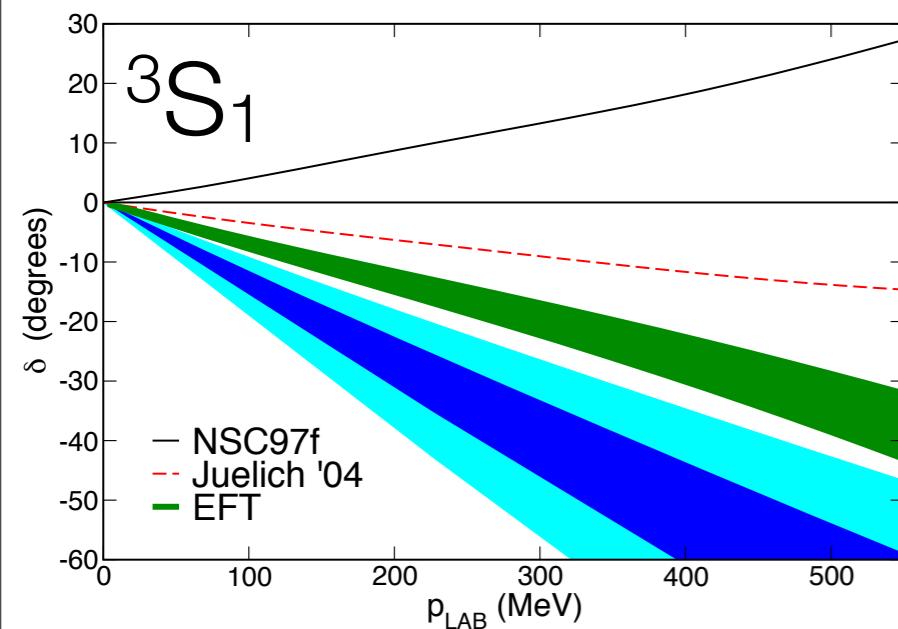
NPLQCD : e-Print: arXiv:1206.5219 [hep-lat]



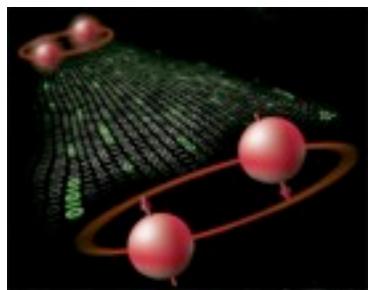
Closing Remarks



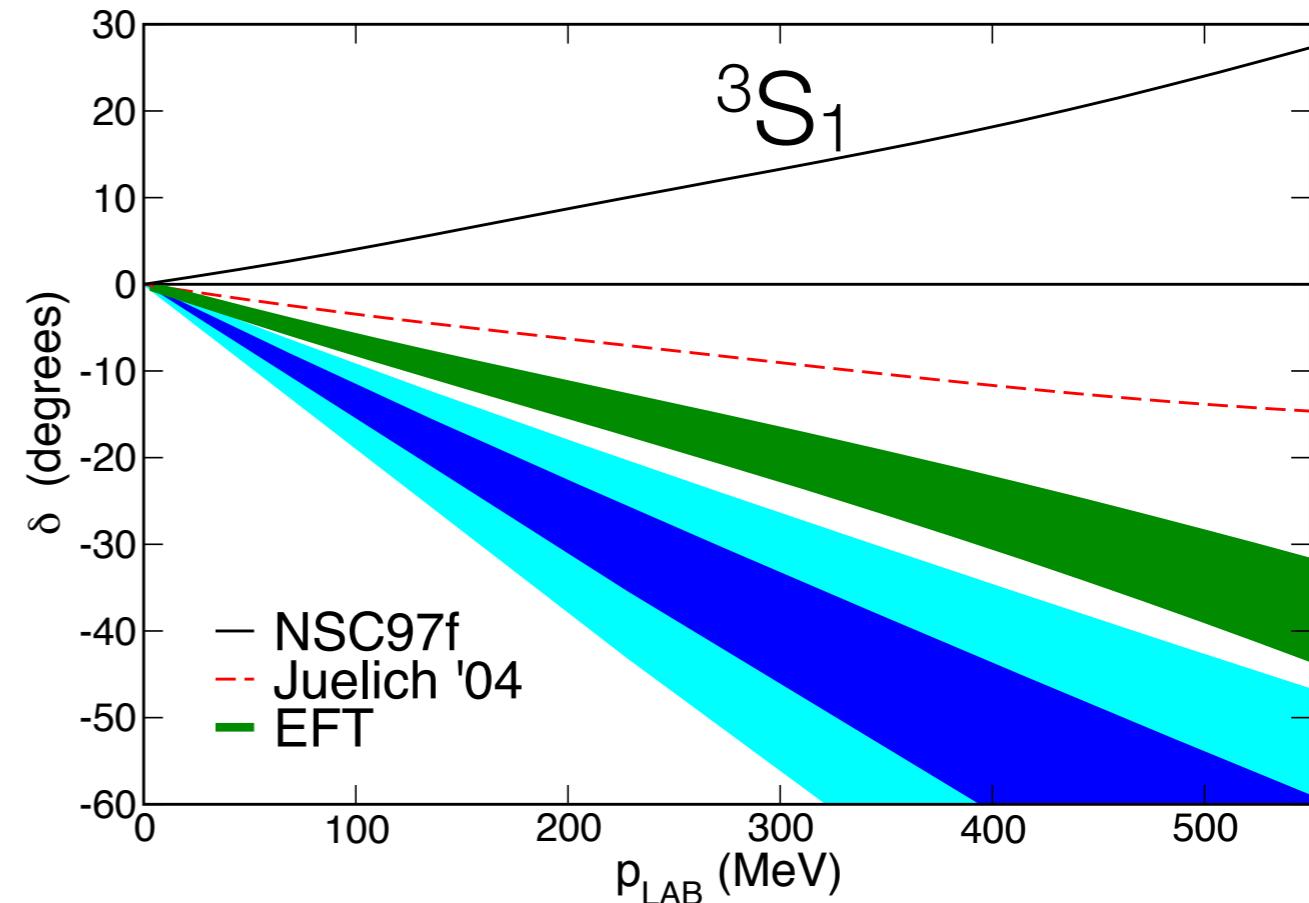
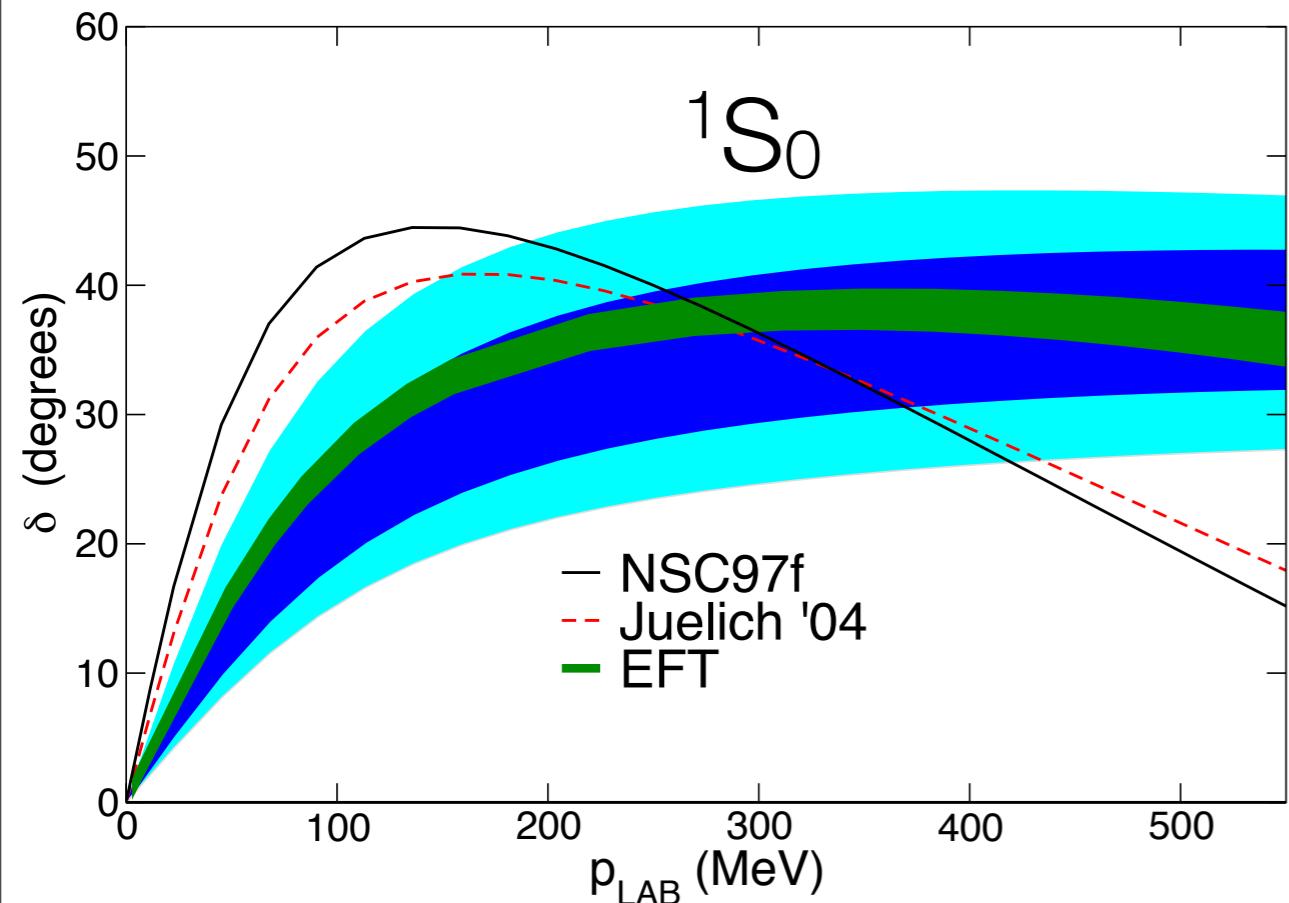
- LQCD calculations of $n\Sigma^-$
- Luscher and 3-d SE consistent
- Extrapolation with (W)EFT
- Consistent with phase-shift analysis of (limited) expt data
- Future LQCD calculations will supersede experiment
- Refine understanding of dense matter
 - Further theoretical developments required



END



Hyperon Nucleon Interactions



- LQCD + (W)EFT consistent with limited data sets
- Next generation of LQCD will be more precise than expt