

Precise Determinations for the **Decay Constants** of **B** and **D** mesons

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HPQCD collaboration

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Outline

- Heavy quark treatments in HPQCD
 - NRQCD, HISQ, and Heavy HISQ
- B and B_s meson decay constants with 2% total errors
 - f_{B_s} with the Heavy HISQ method
 - Decay constants with the NRQCD + Heavy HISQ method
 - $\text{Br}(B \rightarrow \tau \nu)$ and $\sin(2\beta)$ tension
- $|V_{cd}|$ from D meson leptonic decays
 - Decay constants with HISQ charm quarks
 - f_{D_s} saga revisited, and lattice scale determination
- Summary



• Heavy quark treatments in HPQCD

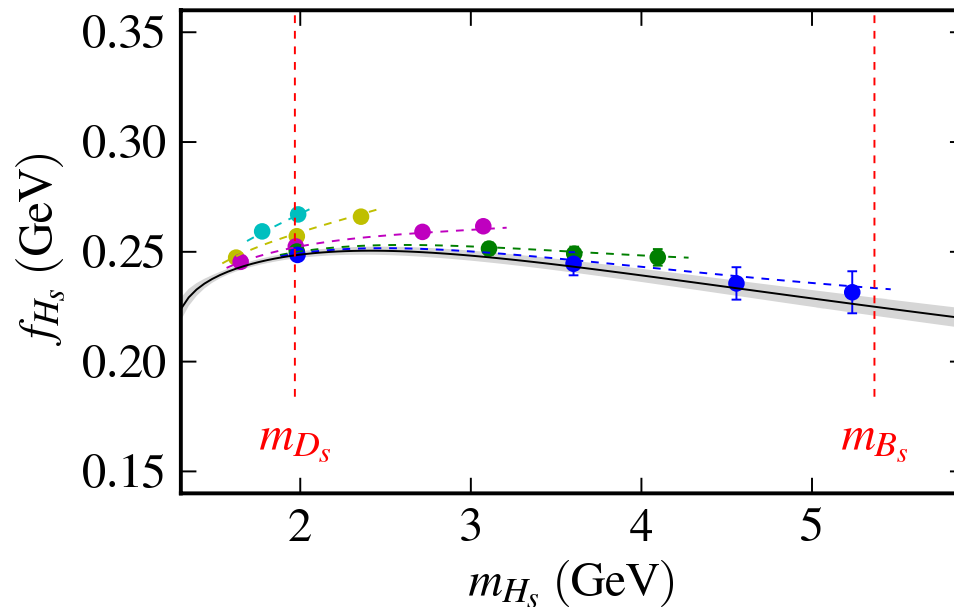
- Heavy quarks need a special treatment to put on the lattice.
 - Typical cut off (typical lattice size) = 2 GeV
 - Charm quark ~ 1 GeV, bottom quark ~ 4 GeV
- NRQCD for charm and bottom
 - Theoretically well known, easy to tune the quark mass
 - Large operator matching errors
- HISQ (Highly Improved Staggered Quark) for charm
 - It is so highly improved!
 - **Leading error** starts at $O(\alpha_s (am_h)^2 v^2/c^2)$ and $O((am_h)^4 v^2/c^2)$
(If $am_c=0.6$, it is about 2%)
 - So, we can treat charm quarks as other u,d, and s quarks
 - No operator matching needed, very easy to tune the quark mass
- Heavy HISQ for bottom
 - For very coarse lattice ($a \sim 0.15\text{fm}$), $am_c \sim 0.85$: it worked great!
 - Simulate heavy HISQ quark: lighter than bottom, up to $am_h = 0.85$
 - Extrapolate to the bottom quark mass using HQET



• f_{B_s} from the Heavy HISQ method

C. McNeile et al. (HPQCD)
PRD 85 (2012) 031503

- Using MILC asqtad staggered $N_f=2+1$ dynamic gauge configurations
- Simulate heavy HISQ quark: **lighter than bottom**, up to $am_h = 0.85$
- Five lattice spacings (0.15fm, 0.12fm, 0.09fm, 0.06fm, and 0.045fm)



- $f_{B_s} = 225(4)$ MeV
previously 231(15) MeV
(First 2% level calculations in b physics!)
- $f_{H_s} \sim 1/\sqrt{m_{H_s}}$?
: Yes! fitted $b = -0.51(13)$
(First empirical evidence!)
- $f_{B_s}/f_{D_s} = 0.906(14)$

$$f_{H_s}(a, m_{H_s}, m_{\eta_s}) = (m_{H_s})^b \left(\frac{\alpha_V(m_{H_s})}{\alpha_V(m_{D_s})} \right)^{-2/\beta_0} \sum_{i=0}^{N_m-1} C_i(a) \left(\frac{1}{m_{H_s}} \right)^i + c_s(m_{\eta_s}^2 - m_{\eta_{s,p}}^2)$$

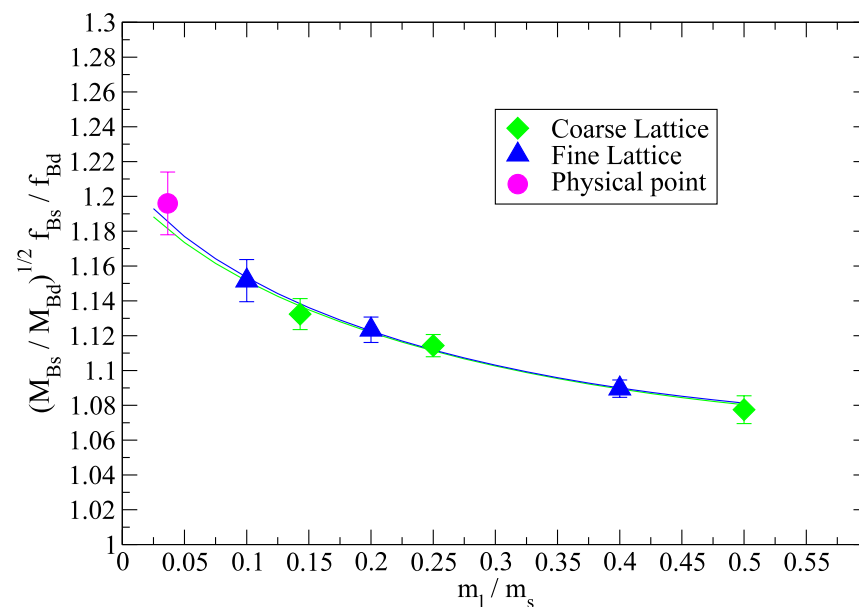
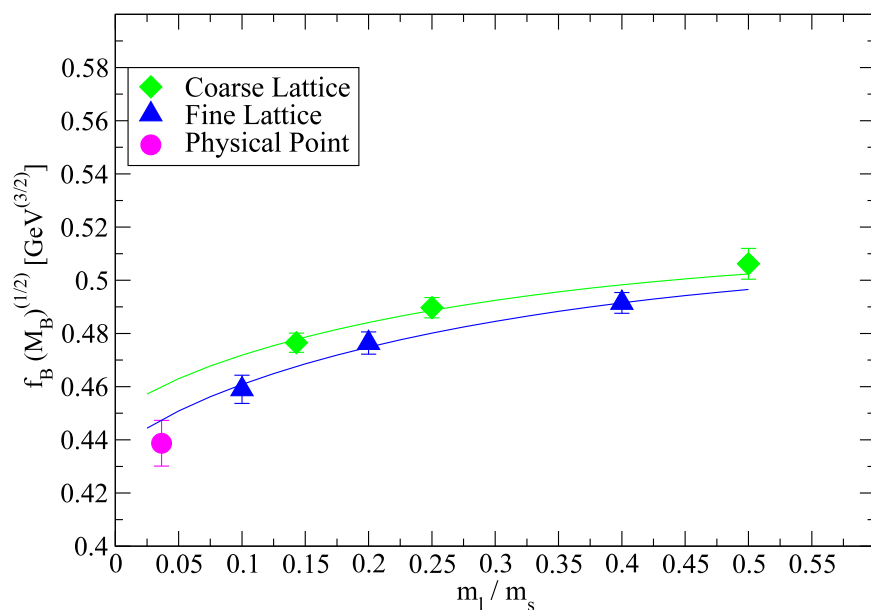
$$C_i(a) = \sum_{j,k,l=0}^{N_a-1} c_{ij} \left(\frac{am_h}{\pi} \right)^{2j} \left(\frac{am_s}{\pi} \right)^{2k} \left(\frac{a\Lambda_{QCD}}{\pi} \right)^{2l}$$



• f_{B_s}/f_B from NRQCD

HN et al. (HPQCD)
arXiv:1202.4914

- Using MILC asqtad staggered $N_f=2+1$ dynamic gauge configurations
- NRQCD for the b quark, and HISQ for the light and strange quarks
- Two lattice spacings (0.12fm, and 0.09fm)
- Matching heavy-light currents with NRQCD and HISQ quarks
 - Chris Monahan's talk on Thursday from 3:30pm



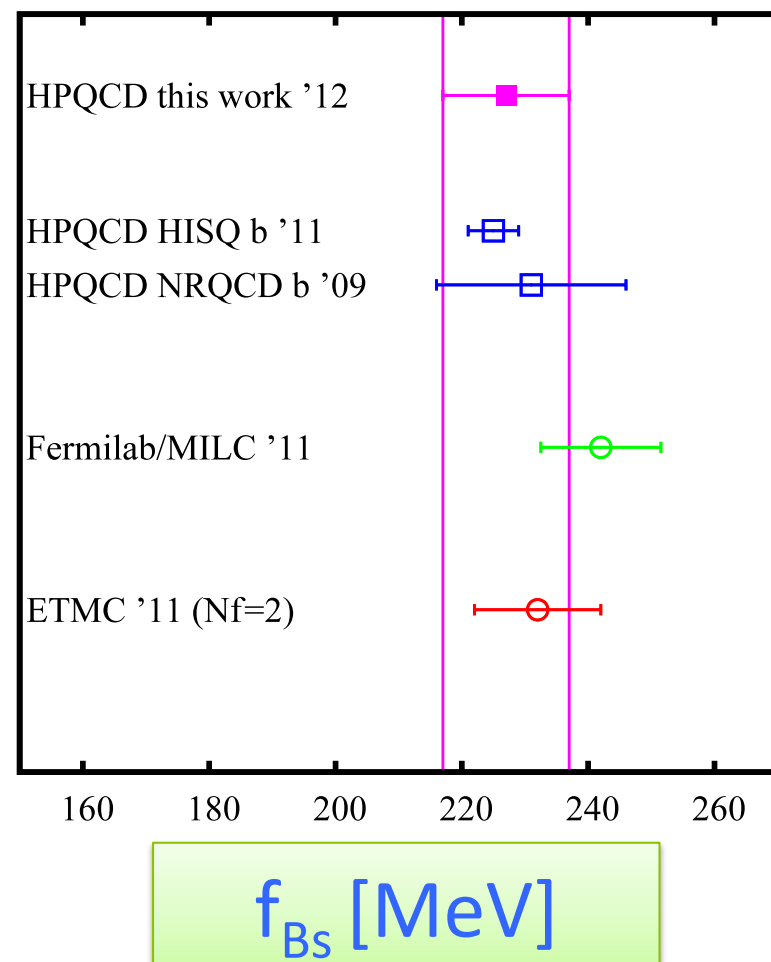
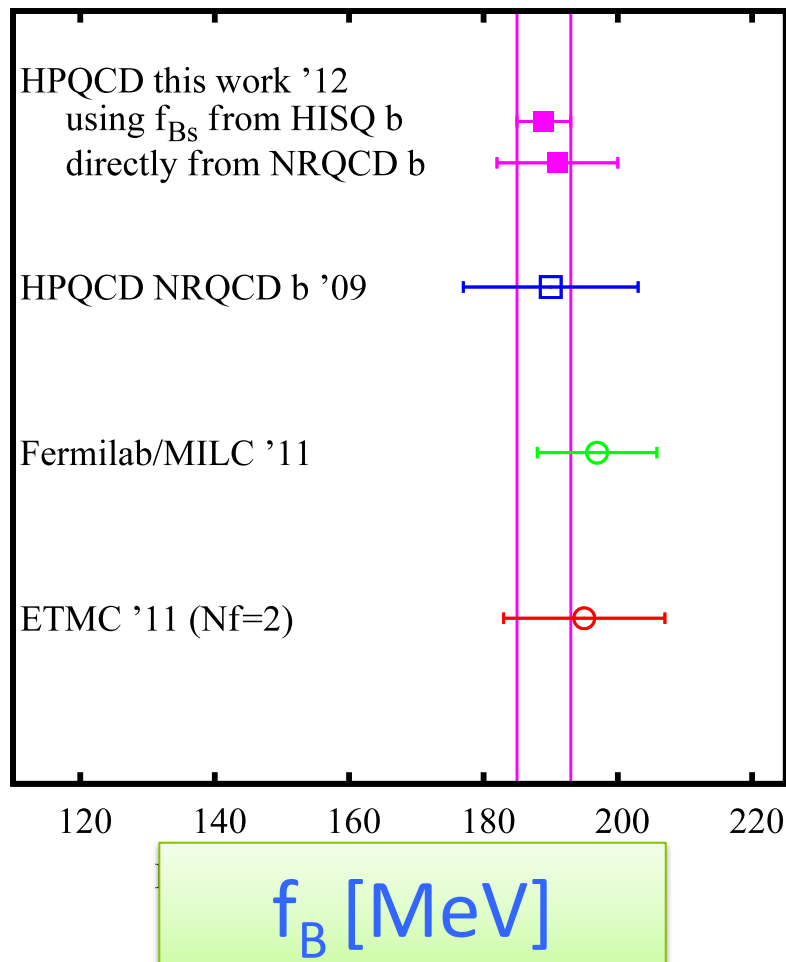
- $f_B = 191(9)$ MeV, $f_{B_s} = 228(10)$ MeV, and $f_{B_s}/f_B = 1.188(18)$



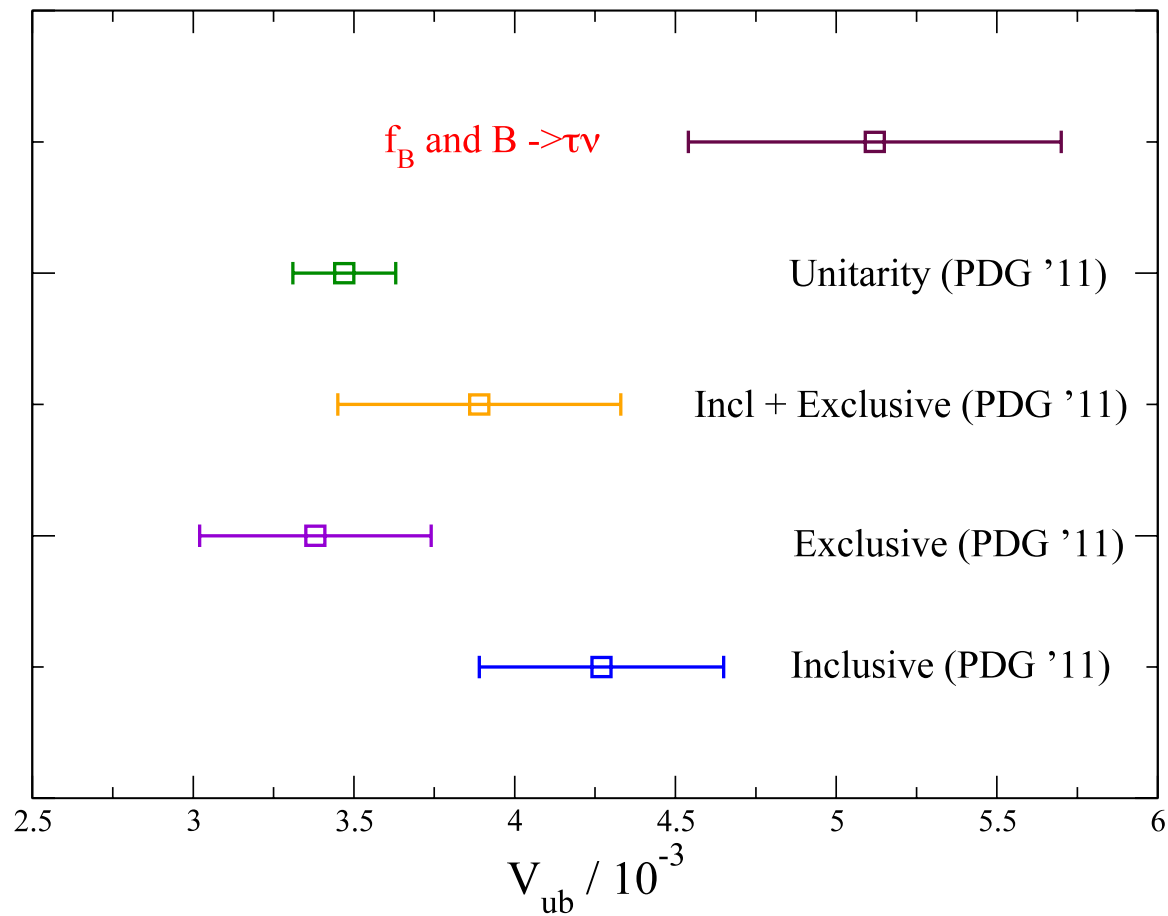
• f_B from the NRQCD + Heavy HISQ method

HN et al. (HPQCD)
arXiv:1202.4914

- We have very accurate f_{B_s}/f_B from the NRQCD method
- And, f_{B_s} from the Heavy HISQ method.
- $f_B = 189(4)$ MeV and $f_{B_s} = 225(4)$ MeV: the most precise results, so far.



- $|V_{ub}|$ from f_B and $\text{Br}(B \rightarrow \tau \nu)$

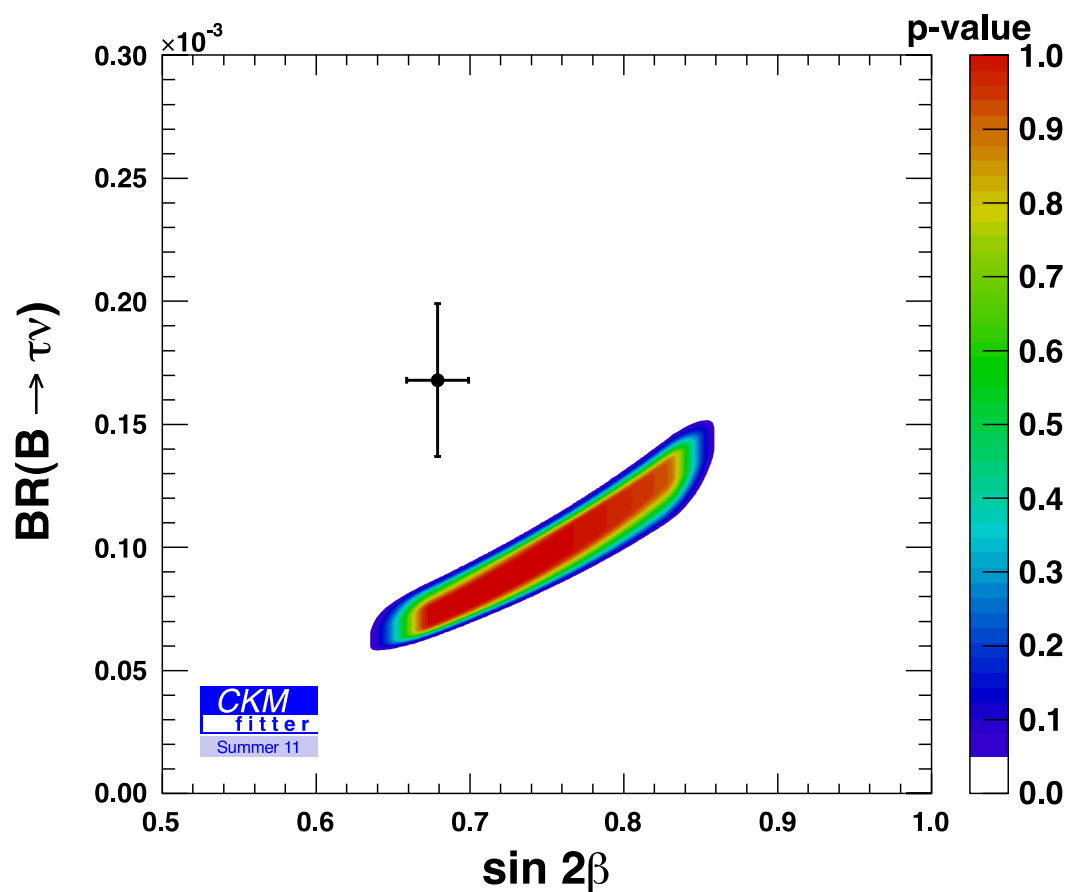


Direct 2.8 σ tension between the Standard Model!



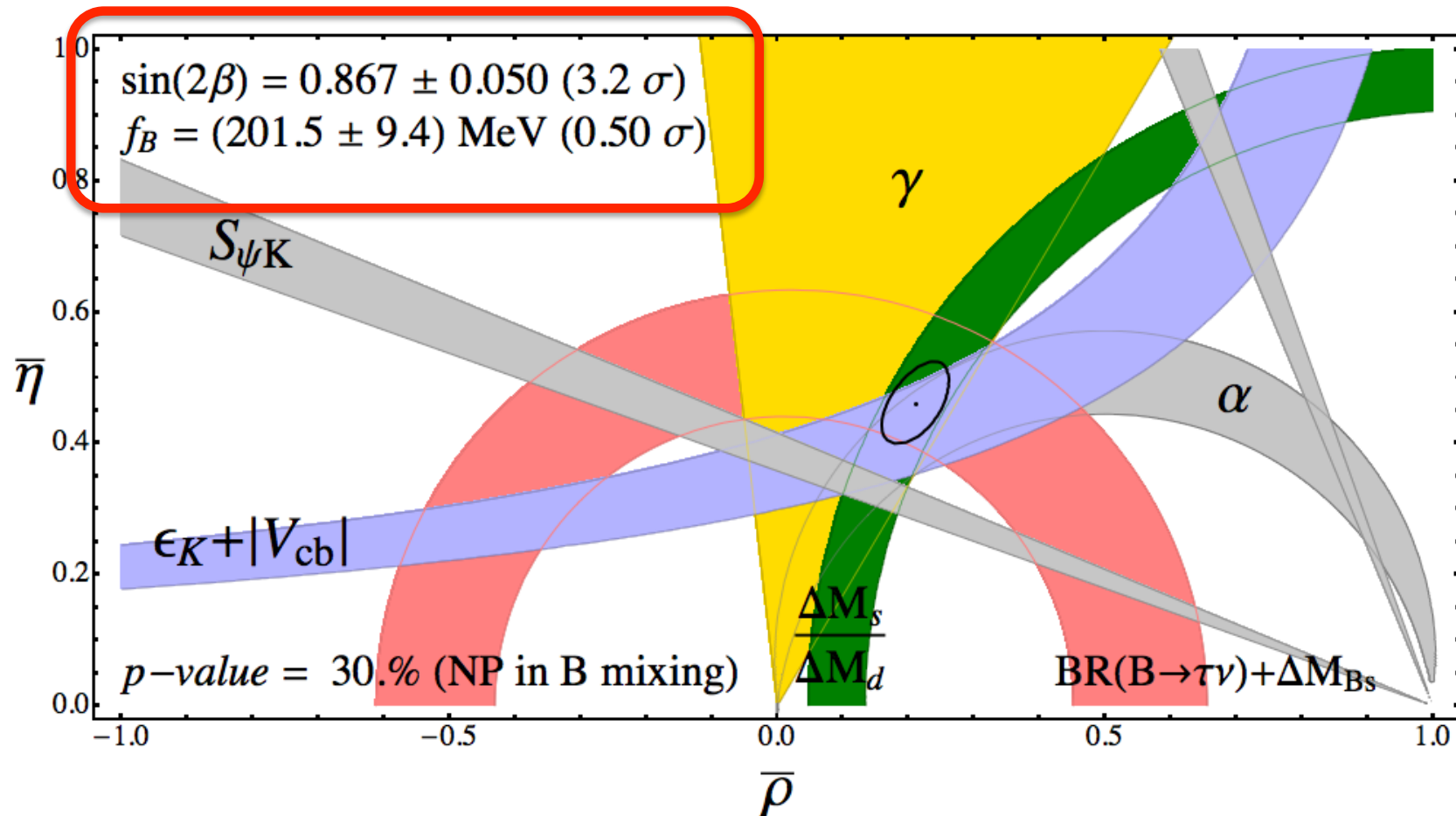
• Br(B $\rightarrow\tau\nu$) and sin(2 β) tension

- Tree level B leptonic decay is helicity suppressed.
- From BaBar and Belle: Br(B $\rightarrow\tau\nu$) = $(1.64 \pm 0.34) \times 10^{-4}$ (HFAG)
- Currently, 2.8 σ tension between sin(2 β)



- Br(B→τν) and sin(2β) tension

- Lunghi and Soni (arXiv:1104.2117)

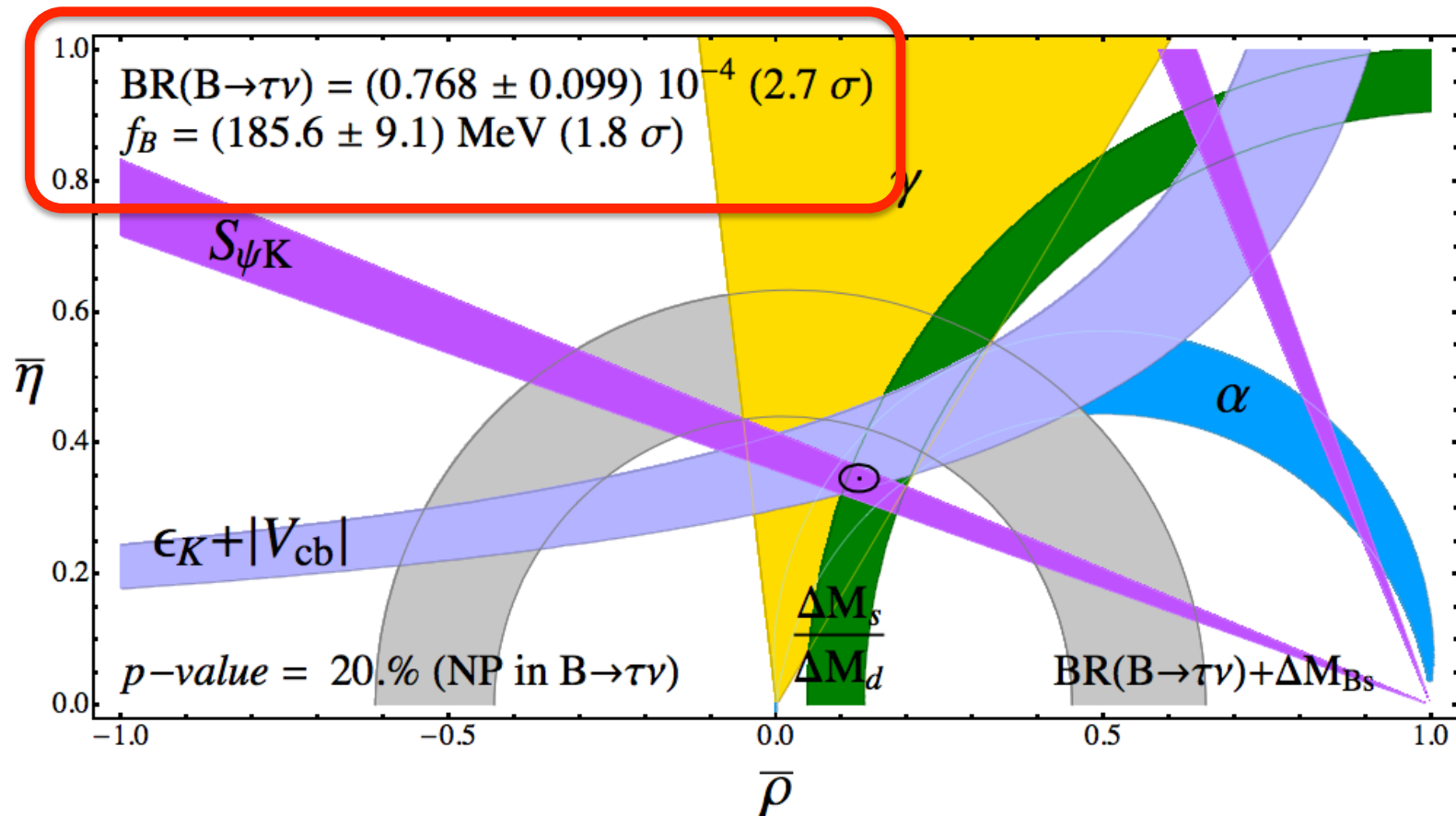


without sin(2β), with Br(B→τν)



- Br(B→τν) and sin(2β) tension

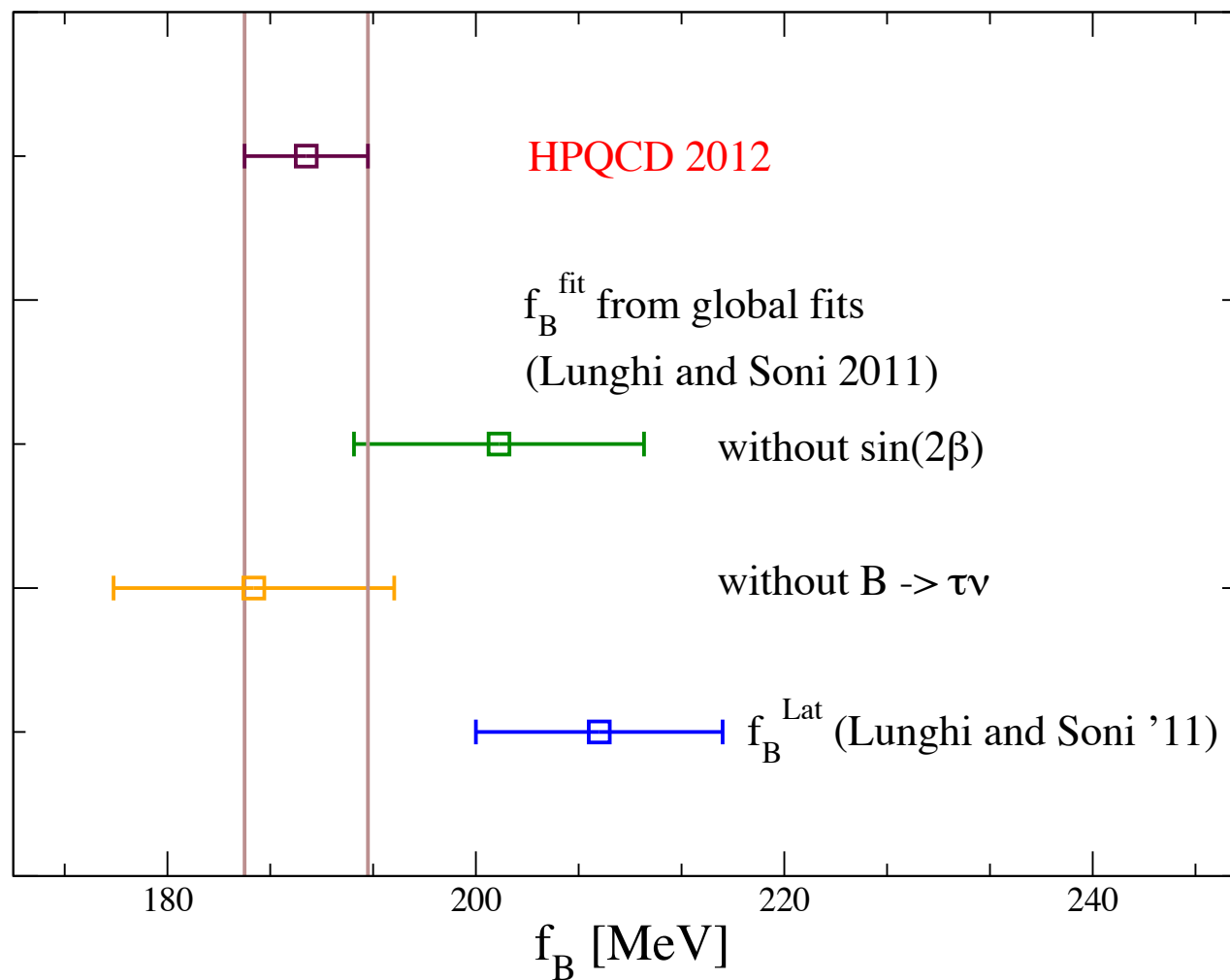
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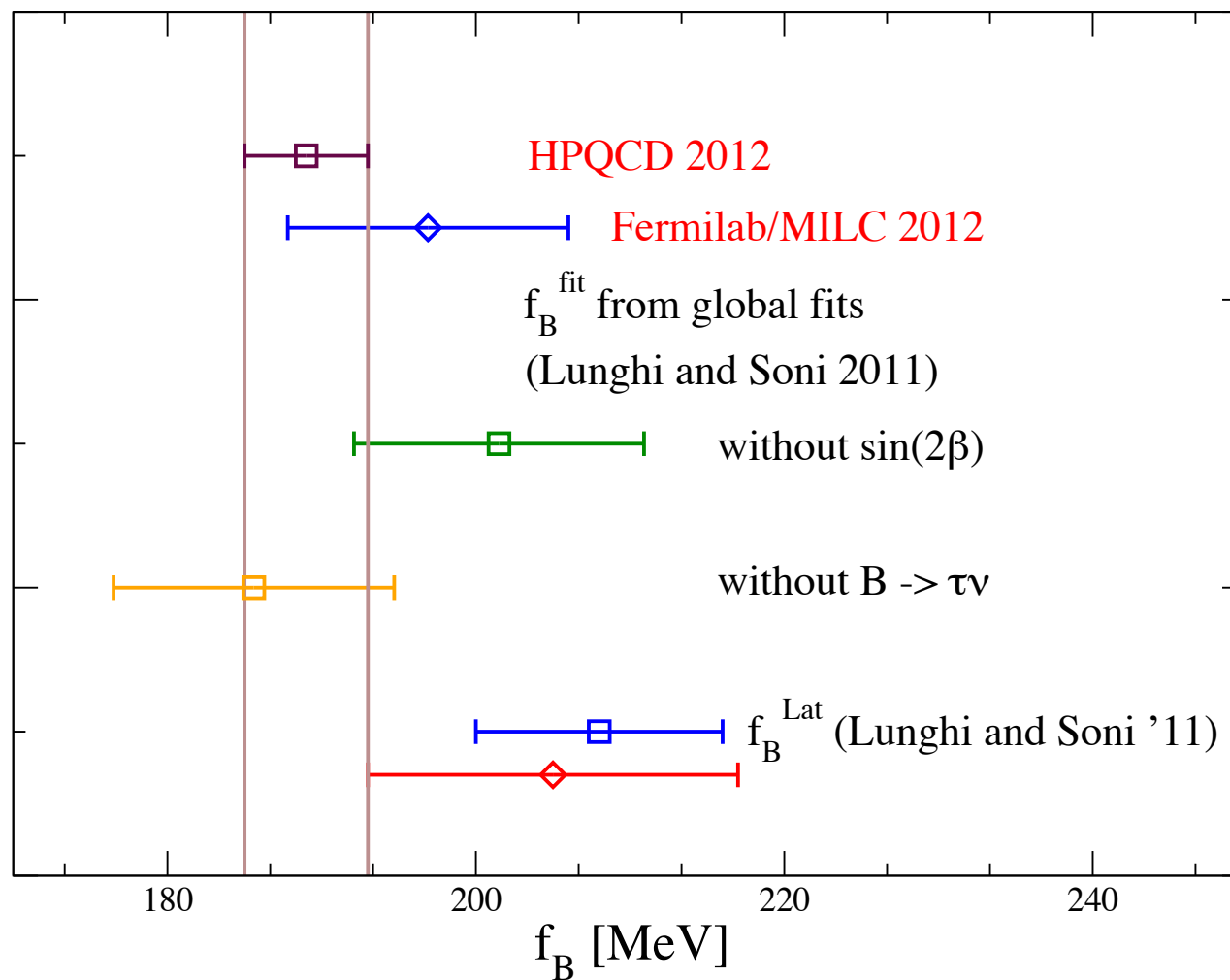
without Br(B→τν), with sin(2β)



- Br(B $\rightarrow\tau\nu$) and sin(2 β) tension

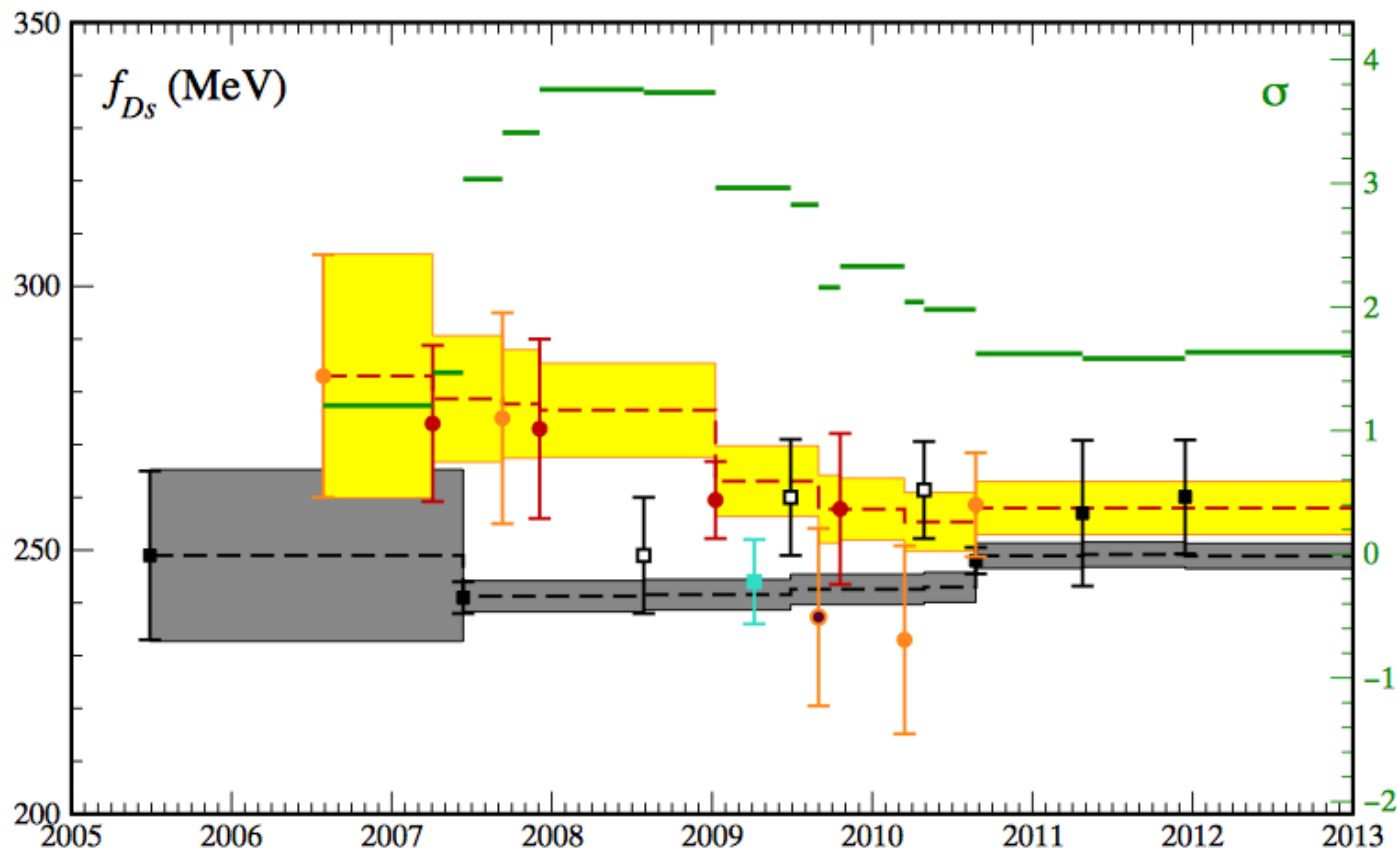


- Br(B $\rightarrow\tau\nu$) and sin(2 β) tension



• D and D_s meson decay constants: f_{D_s} saga revisited!

- HPQCD has some history on f_{D_s}
- Previously, 3.8σ tension between the experiments
- Now, it has fallen to 1.6σ
- $r_1 = 0.321(5)$ fm before 2010, $r_1 = 0.3133(23)$ fm after 2010

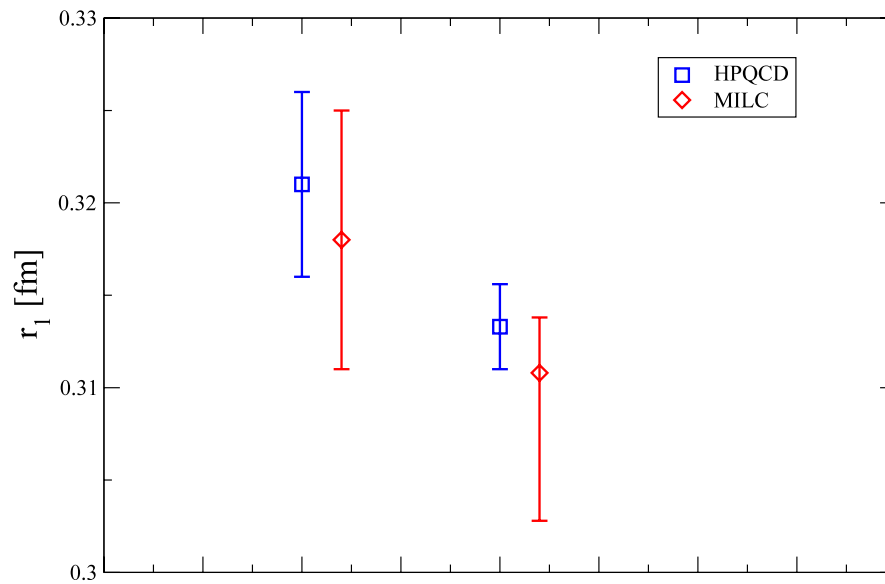


Plot from A. Kronfeld, 1203.1204



• Lattice spacing determinations

- Pion decay constant in lattice units: $a f_{\pi}^{\text{lat}}$
- $a = (a f_{\pi}^{\text{lat}})/f_{\pi}^{\text{phys}}$
- Better quantity? r_1 or r_0 is broadly used.
- $r_1^2 F(r_1) = 1$, $F(r) = dV/dr$, $V(r) = \text{static potential}$
- r_1 can be determined with sub-percent errors
 - It is in the lattice, so it is really r_1/a
- $a M^{\text{lat}} \rightarrow r_1/a * a M^{\text{lat}} = r_1 M^{\text{lat}}$ (in r_1 unit)
 - $\rightarrow r_1 = (r_1 M^{\text{lat}})/M^{\text{phys}}$
- Physical r_1 [fm] can be determined with around 1 percent errors



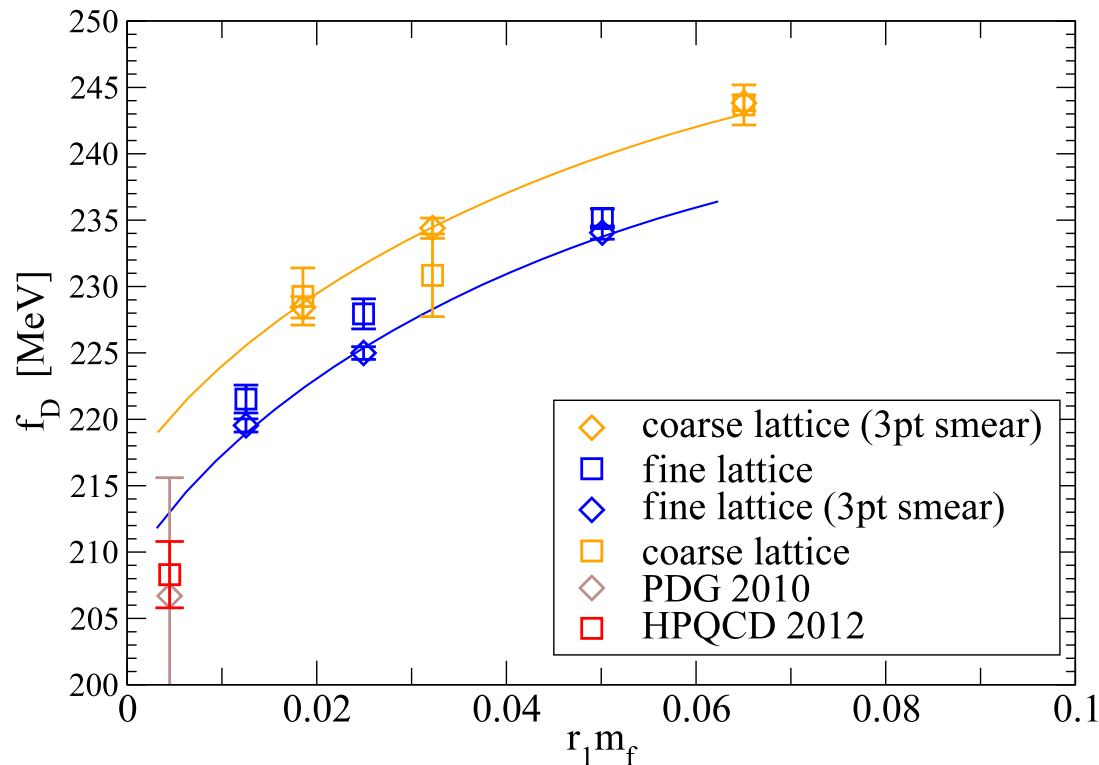
- HPQCD
0.321(5) $\rightarrow$ 0.3133(23)
- MILC
0.318(7) $\rightarrow$ 0.3108(15)($^{+30}_{-80}$)



• D meson decay constants

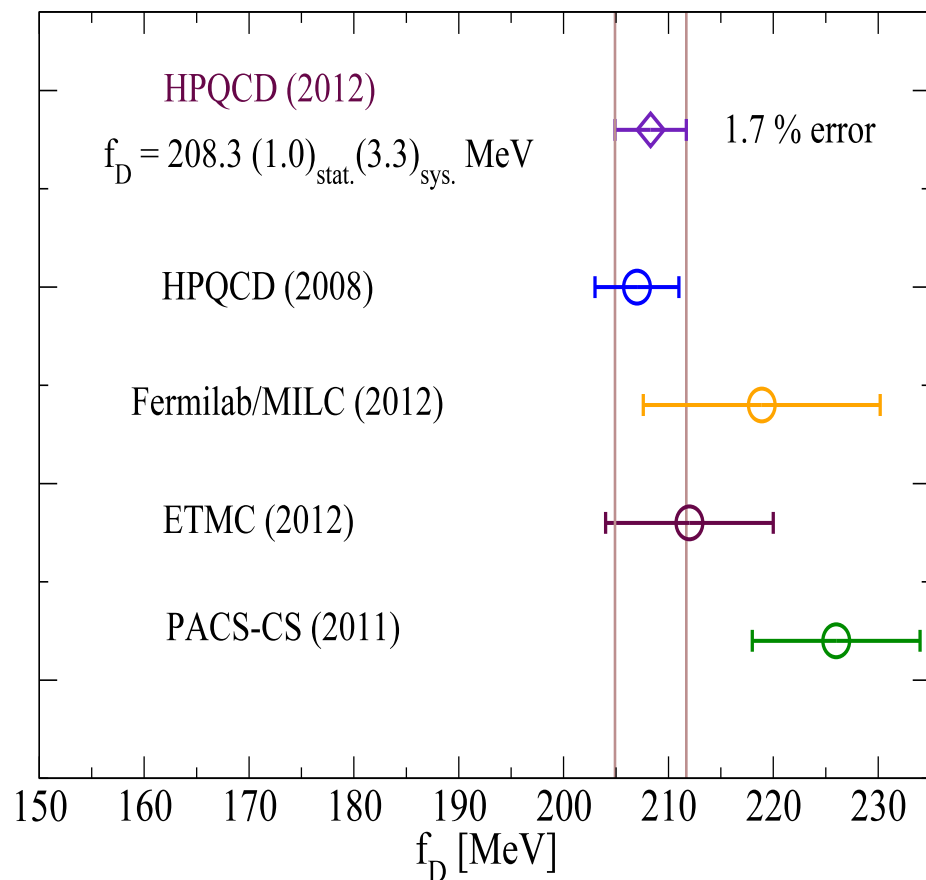
HN et al. (HPQCD)
arXiv:1206.4936

- Update f_D with updated r_1
- Also, calculate f_{D_s} and f_{D_s}/f_D
- Using MILC asqtad staggered $N_f=2+1$ dynamic gauge configurations
- HISQ fermion action for the strange and charm quarks
- Two lattice spacings (0.12fm, 0.09fm)
- Using 3pt smearing: Simultaneous fit with 3 point functions for D to K l ν semileptonic decays



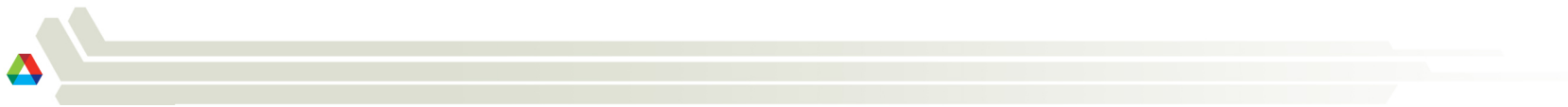
D meson decay constants

HN et al. (HPQCD)
arXiv:1206.4936



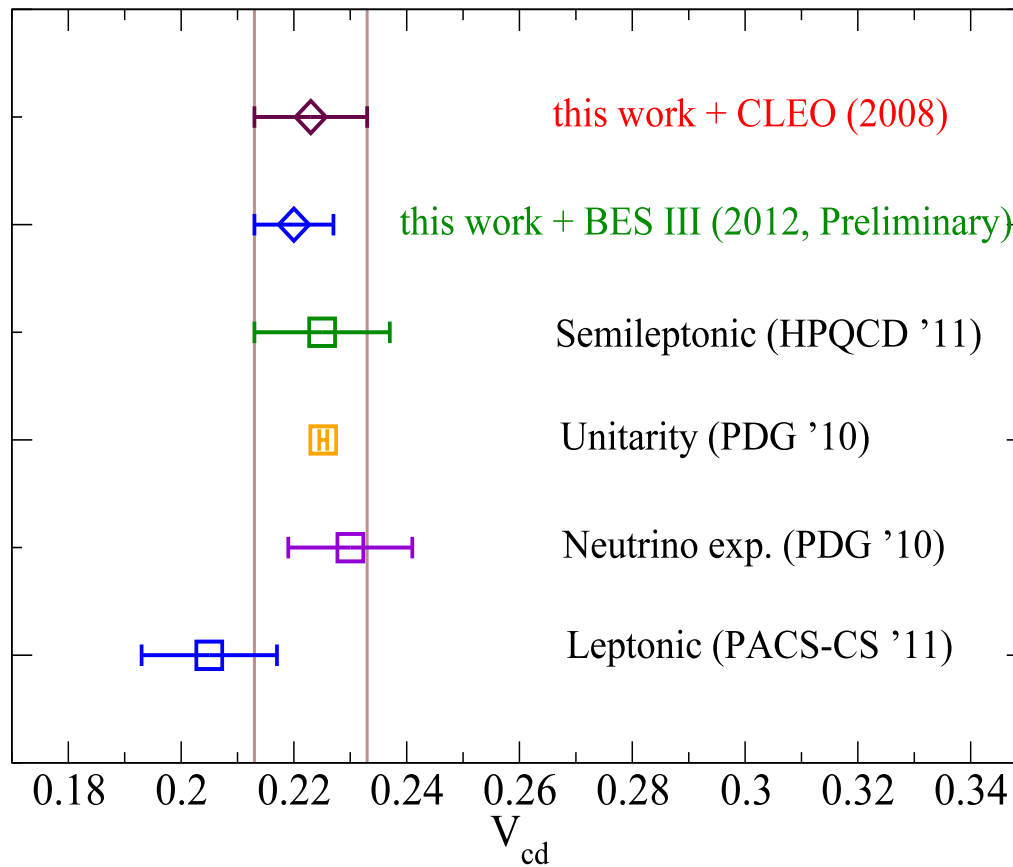
- $f_D = 208.3 (1.0)_{\text{stat.}} (3.3)_{\text{sys.}}$
- $f_{D_s} = 246.0 (0.7)_{\text{stat.}} (3.5)_{\text{sys.}}$
- $f_{D_s}/f_D = 1.187 (4)_{\text{stat.}} (12)_{\text{sys.}}$

	f_D	f_{D_s}	f_{D_s}/f_D
statistics/fitting	0.5	0.3	0.3
scale r_1	0.7	0.7	-
r_1/a	0.04	0.05	-
continuum extrap.	1.2	1.2	0.9
chiral extrap. & $g_{D^*\pi}$	0.7	0.2	0.5
mass tunings	0.1	0.2	0.2
finite volume	0.3	0.1	0.3
Total	1.7 %	1.5 %	1.1 %



- $|V_{cd}|$ from D meson leptonic decays

HN et al. (HPQCD)
arXiv:1206.4936



- $|V_{cd}| = 0.223 (10)_{\text{exp.}} (4)_{\text{lat.}}$

- $[f_+^{D \rightarrow \pi}(0) / f_D]_{\text{lat.}} = 3.20(15) \text{ GeV}^{-1}$

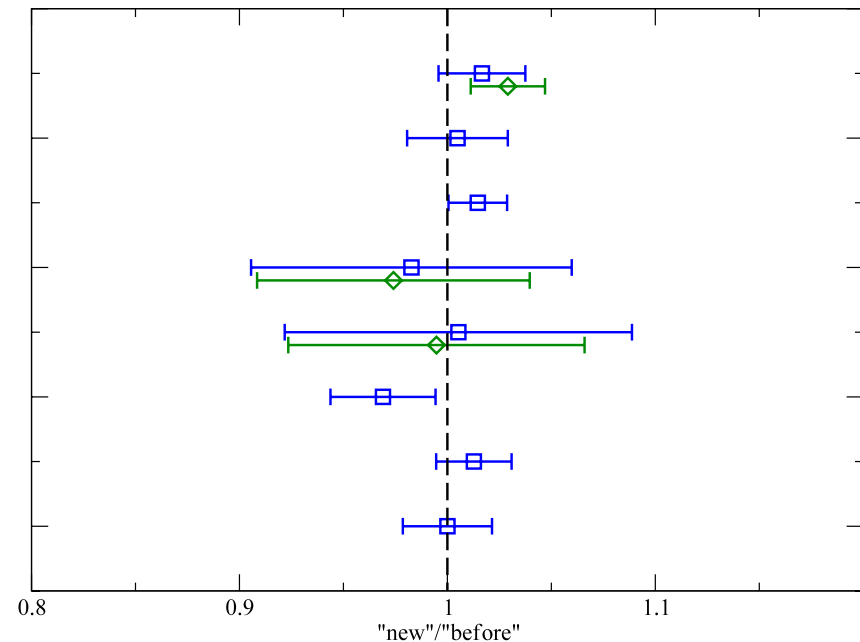
- $[f_+^{D \rightarrow \pi}(0) / f_D]_{\text{exp.}} = 3.19(18) \text{ GeV}^{-1}$



• Old r_1 vs. new r_1

- Old $r_1 = 0.321(5)$ fm
- New $r_1 = 0.3133(23)$ fm

	before	now
fDs	241(3)	246(4) [248(3)]
fD	207(4)	208(3)
fDs/fD	1.164(11)	1.187(12)
fBs	231(15)	228(10) [225(4)]
fB	190(13)	191(9) [189(4)]
fBs/fB	1.226(26)	1.188(18)
fK	157(2)	159(2)
f π	132(2)	132(2)

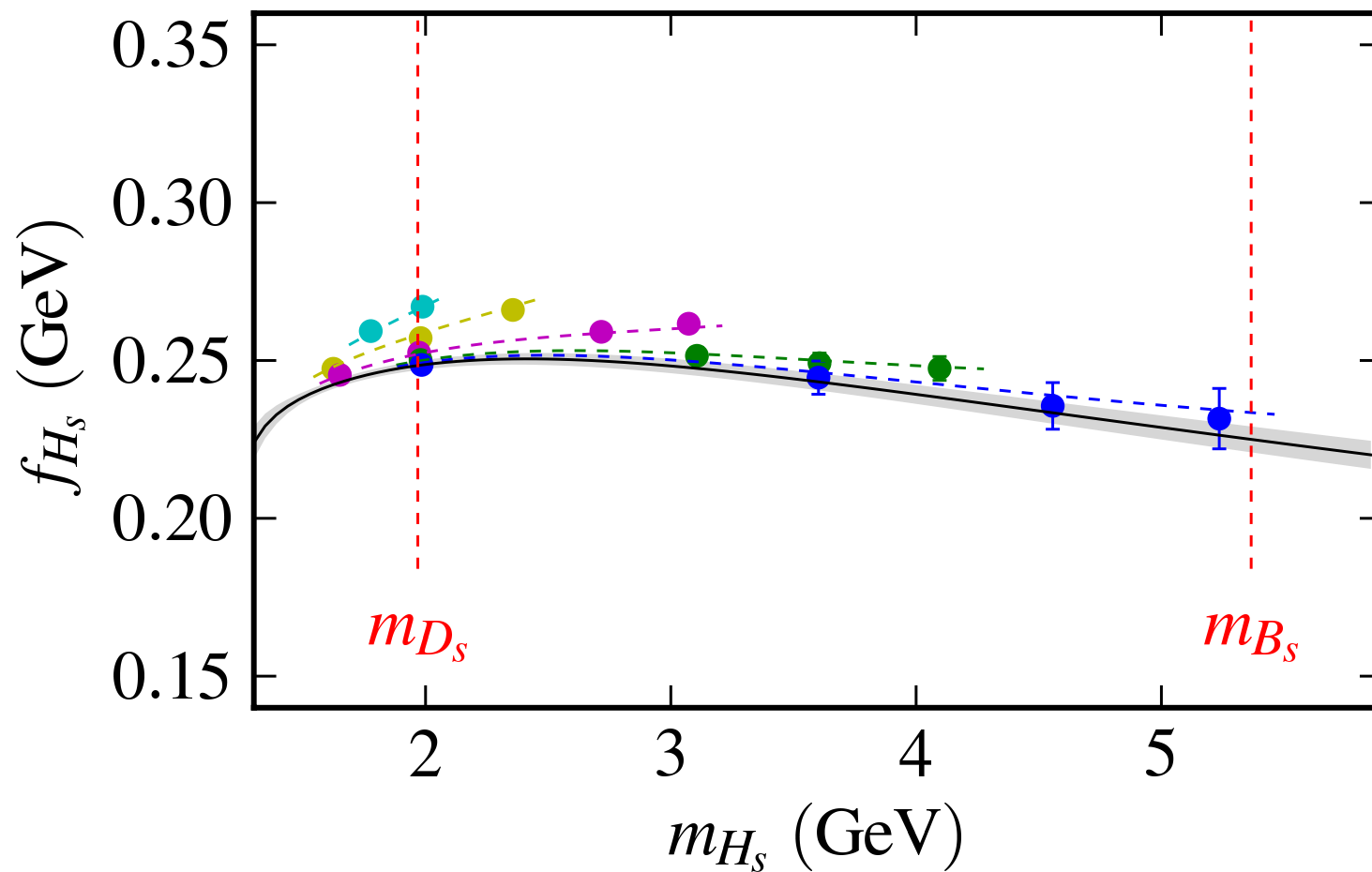


- The effect due to the scale changing is small.
- f_{Ds} is a special case!

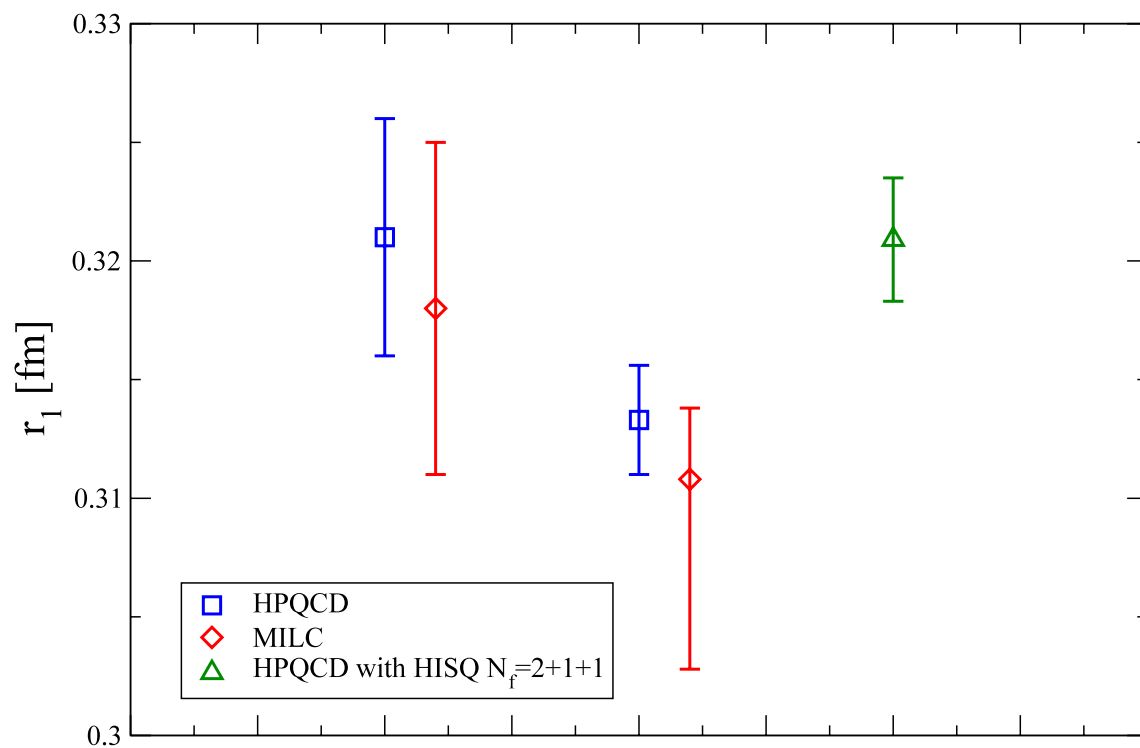


- Old r_1 vs. new r_1

- Old $r_1 = 0.321$ (5) fm
- New $r_1 = 0.3133$ (23) fm

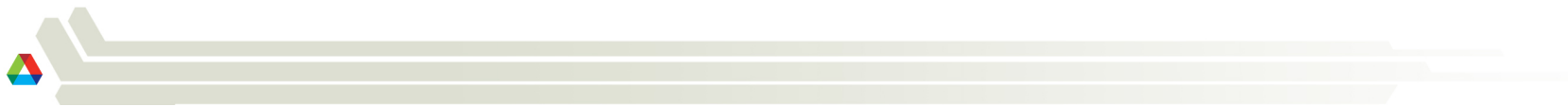


• Lattice spacing determinations: f_{D_s} saga revisited!



- HPQCD
0.321(5) $\rightarrow$ 0.3133(23)
- MILC
0.318(7) $\rightarrow$ 0.3108(15)($^{+30}_{-80}$)
- HPQCD with HISQ confs
0.3209(29) (1110.6887)

- f_{D_s} at HISQ $N_f=2+1+1$ would be very interesting!
 - Talks by Doug Toussaint and Jongjeong Kim on Friday





• Summary

- HPQCD have been used NRQCD, HISQ, and Heavy HISQ for handling the heavy quarks.
- Using the Heavy HISQ and NRQCD methods, we obtained B and B_s decay constants with about 2% error.
 - Keep increasing precision would help to understand, for example, the B $\rightarrow$ $\tau\nu$ tension.
- We calculate $|V_{cd}|$ from the D decay constants with updated r_1
 - Good agreement with $|V_{cd}|$ from the semileptonic decay study.
 - Updated r_1 effects are small, except for f_{D_s}
 - f_{D_s} at HISQ $N_f=2+1+1$ configuration would be very interesting.



Back up



• V_{cs} and V_{cd} from the leptonic decays

Preliminary!

$$f_+^{D \rightarrow \pi l \nu}(0) |V_{cd}| = 0.145(4)(1) + 0.150(5)(2) \Rightarrow 0.148(5)(2)$$

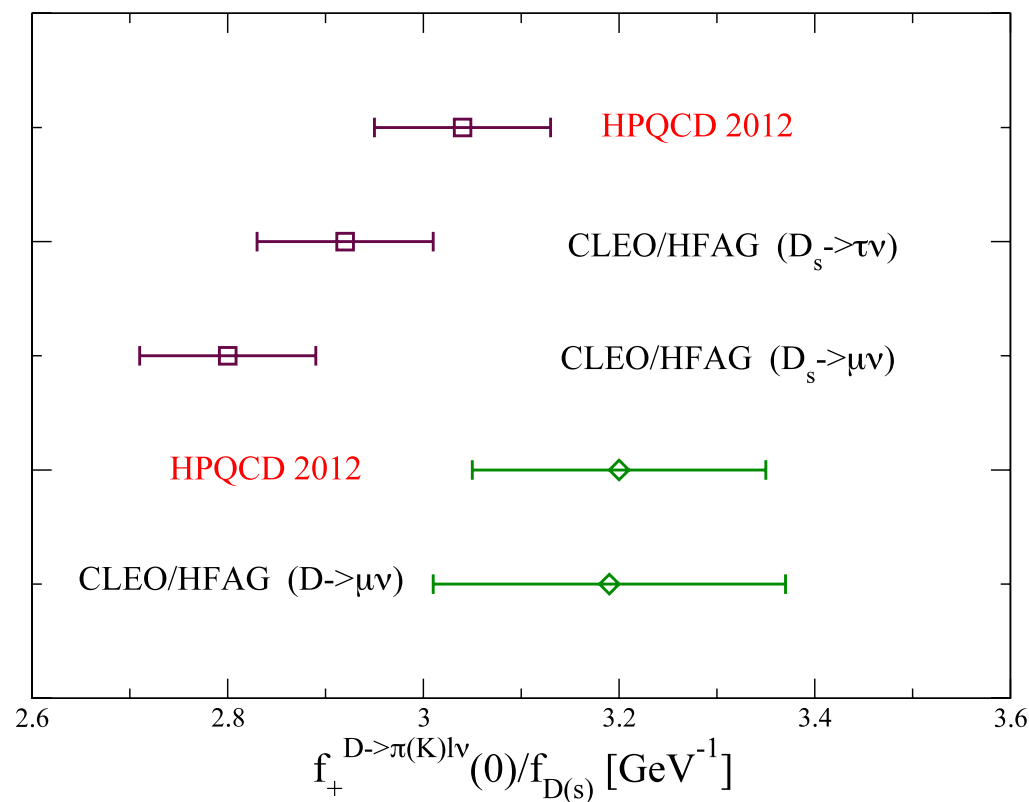
$$f_+^{D \rightarrow K l \nu}(0) |V_{cs}| = 0.717(6)(4) + 0.716(7)(9) \Rightarrow 0.717(7)(9)$$

CLEO, PRD 80 (2009) 032005

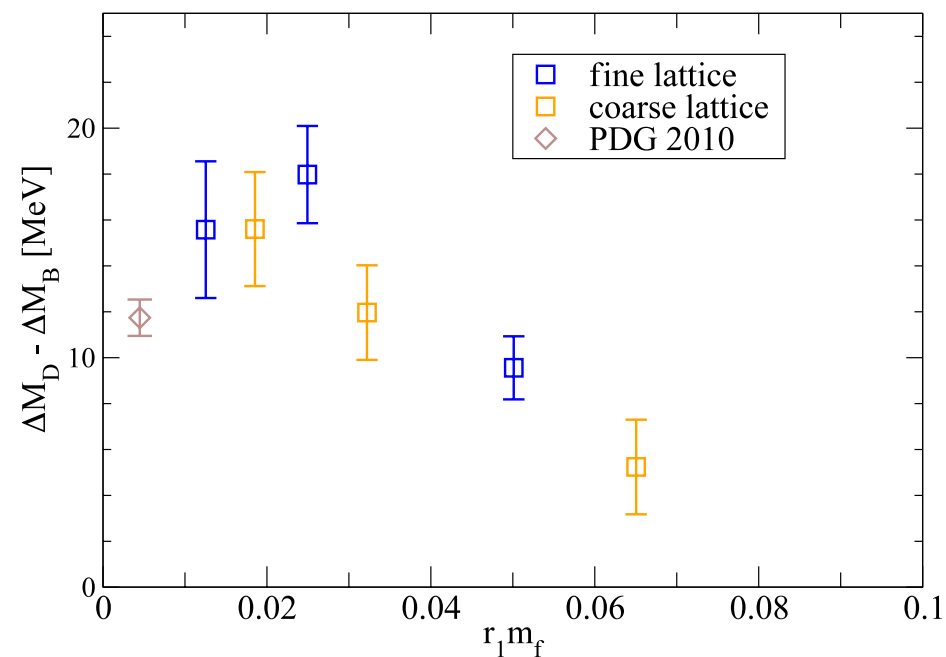
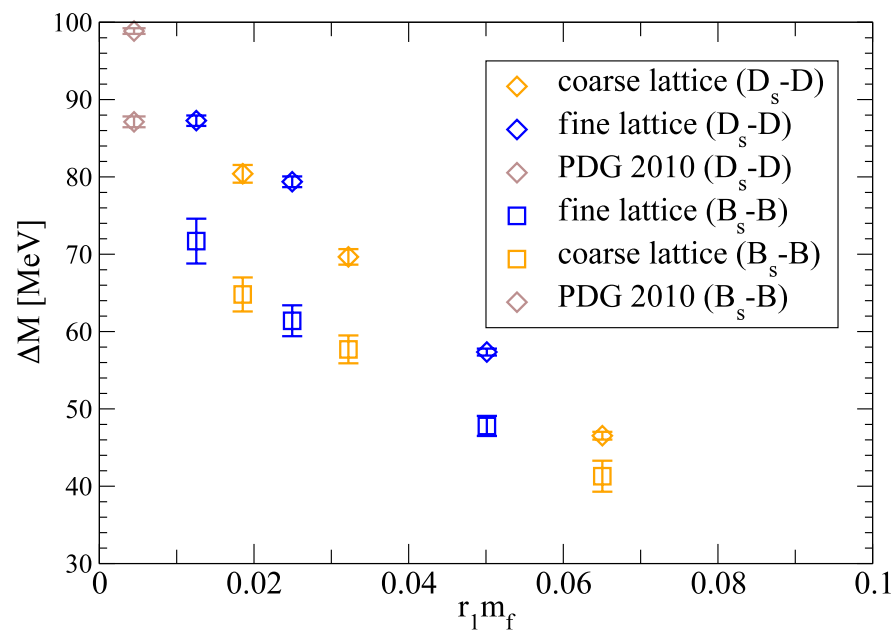
$$f_D |V_{cd}| = 46.4 \pm 2.0 \text{ MeV}$$

$$f_{D_s}(D_s \rightarrow \tau \nu) |V_{cs}| = 245.6 \pm 6.7 \text{ MeV}$$

$$f_{D_s}(D_s \rightarrow \mu \nu) |V_{cs}| = 256.3 \pm 7.4 \text{ MeV}$$



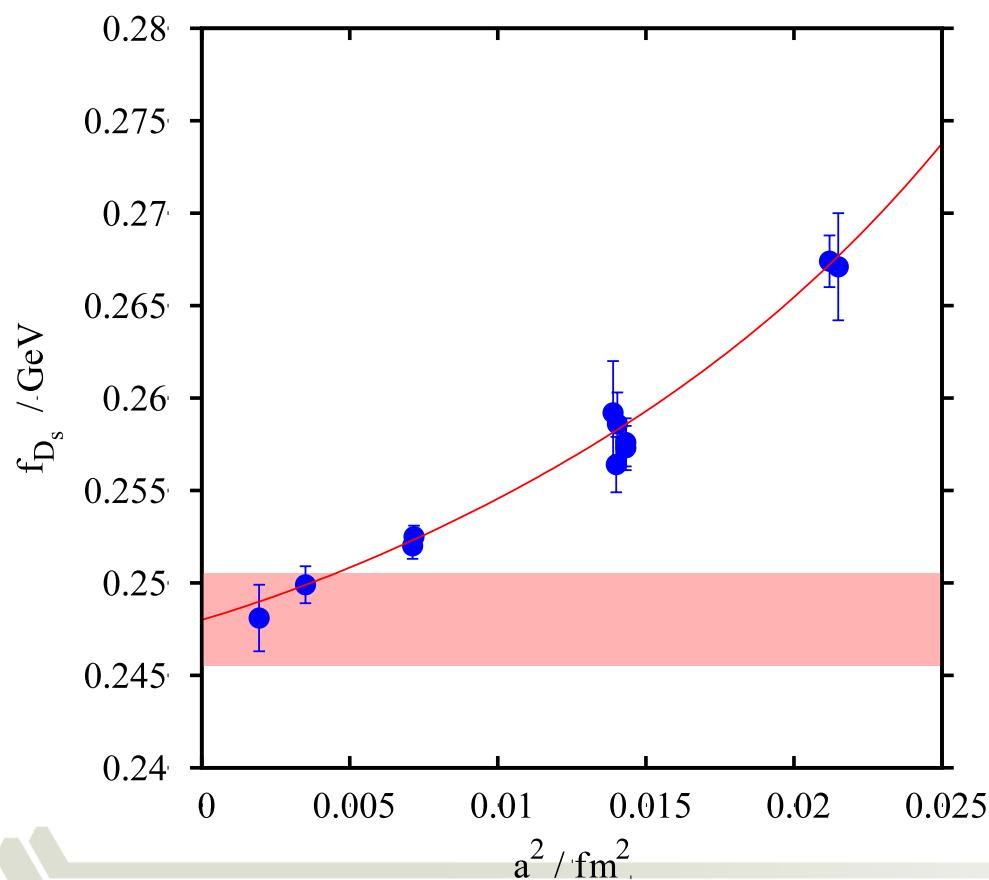
- M_{hs} - M_{hl} mass splittings



• D and D_s meson decay constants

C. Davies et al. (HPQCD)
PRD 82 (2010) 114504

- Update f_{D_s} with updated r_1 and more data sets
- Using MILC asqtad staggered $N_f=2+1$ dynamic gauge configurations
- HISQ fermion action for the strange and charm quarks
- Five lattice spacings (0.15fm, 0.12fm, 0.09fm, 0.06fm, and 0.045fm)
- $f_{D_s} = 241(3) \text{ MeV} \rightarrow 248.0(2.5) \text{ MeV}$



- Tension?: $\text{Br}(B \rightarrow \tau \nu)$ & $\sin(2\beta)$

- Leptonic decays: $\text{Br}(B \rightarrow \tau \nu)$

- BaBar

Hadronic tag : $(1.80^{+0.57}_{-0.54} \pm 0.26) \times 10^{-4}$ Preliminary. NEW

Semileptonic tag : $(1.7 \pm 0.87 \pm 0.2) \times 10^{-4}$

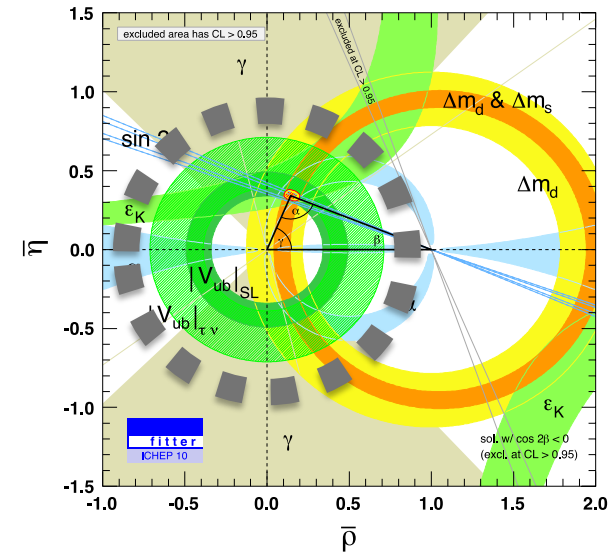
Combined result : $(1.76 \pm 0.49) \times 10^{-4}$

- Belle

Hadronic tag : $(1.79^{+0.56}_{-0.49} {}^{+0.46}_{-0.51}) \times 10^{-4}$

Semileptonic tag : $(1.54^{+0.38}_{-0.37} {}^{+0.29}_{-0.31}) \times 10^{-4}$ NEW!

Final result : $(1.64 \pm 0.34) \times 10^{-4}$ (HFAG)



R. Barlow,
CKM 2010



• Unitarity triangle and Lattice QCD

$$V = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| & |V_{ts}| & |V_{tb}| \end{pmatrix} = \begin{pmatrix} (1 - \lambda^2/2) & (\lambda) & (A\lambda^3(\rho - i\eta)) \\ 0.97425 (22) & 0.2252 (9) & (3.89 \pm 0.44) \times 10^{-3} \\ (-\lambda) & (1 - \lambda^2/2) & (A\lambda^2) \\ 0.230 (11) & 1.023 (36) & (40.6 \pm 1.3) \times 10^{-3} \\ (A\lambda^3(1 - \rho - i\eta)) & (-A\lambda^2) & (1) \\ (8.4 \pm 0.6) \times 10^{-3} & (38.7 \pm 2.1) \times 10^{-3} & 0.88 \pm 0.07 \end{pmatrix}$$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$= A\lambda^3(\rho + i\eta) - A\lambda^3 + A\lambda^3(1 - \rho - i\eta) + \mathcal{O}(\lambda^4)$$

