

MCRG Study of $SU(3)$ Gauge Theories with 8 and 12 Fundamental Fermions

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28 June 2012

Anqi Cheng, Anna Hasenfratz, David Schaich

Motivation

❖ MCRG ❖ 8 Flavor Result ❖ 12 Flavor Result ❖ Conclusion

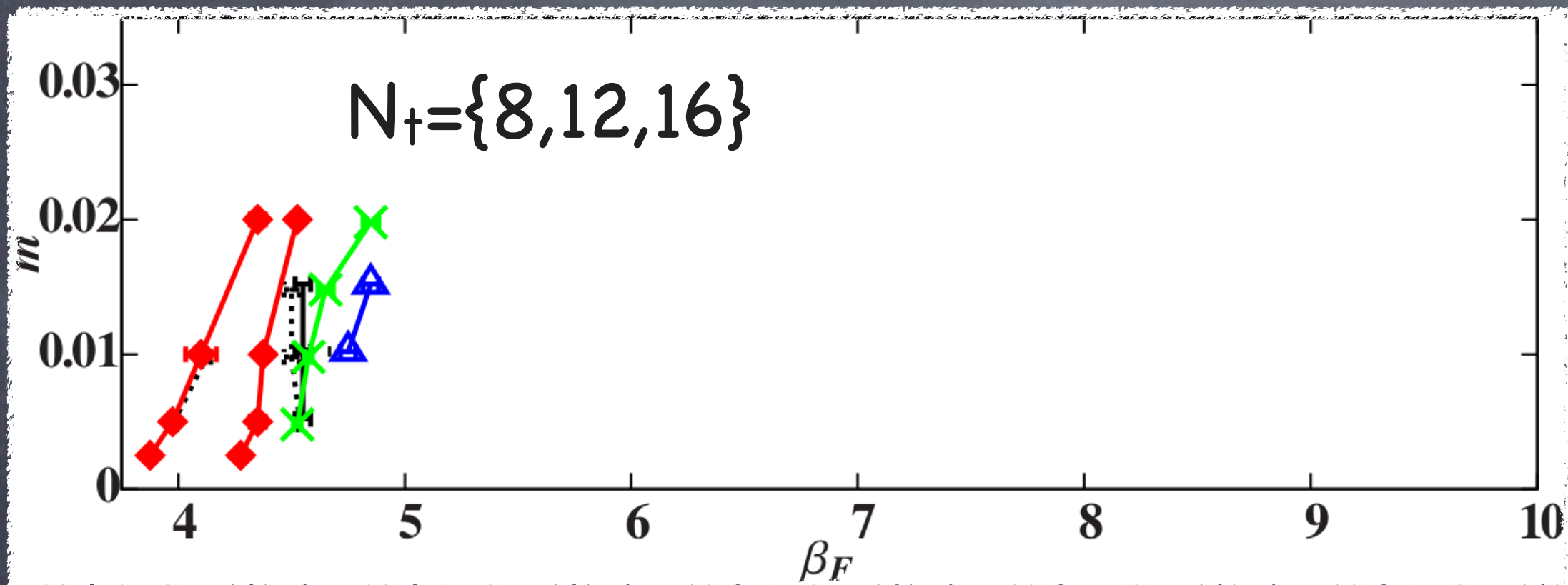
Colorado NHYP BSM

- Anna Hasenfratz
- David Schaich
- Gregory Petropoulos
- Anqi Cheng

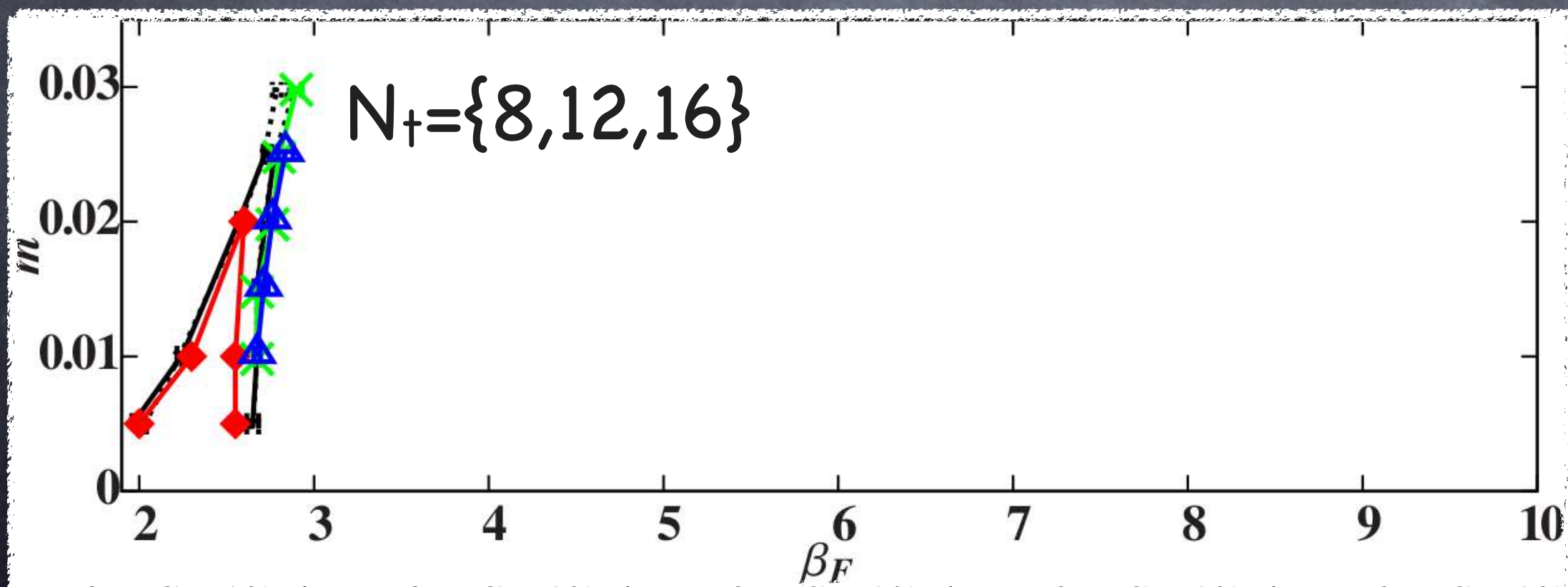
- $SU(3)$ Gauge Group
- Fundamental Fermions
- NHYP smeared staggered action
- Fundamental & Adjoint gauge action

Motivation

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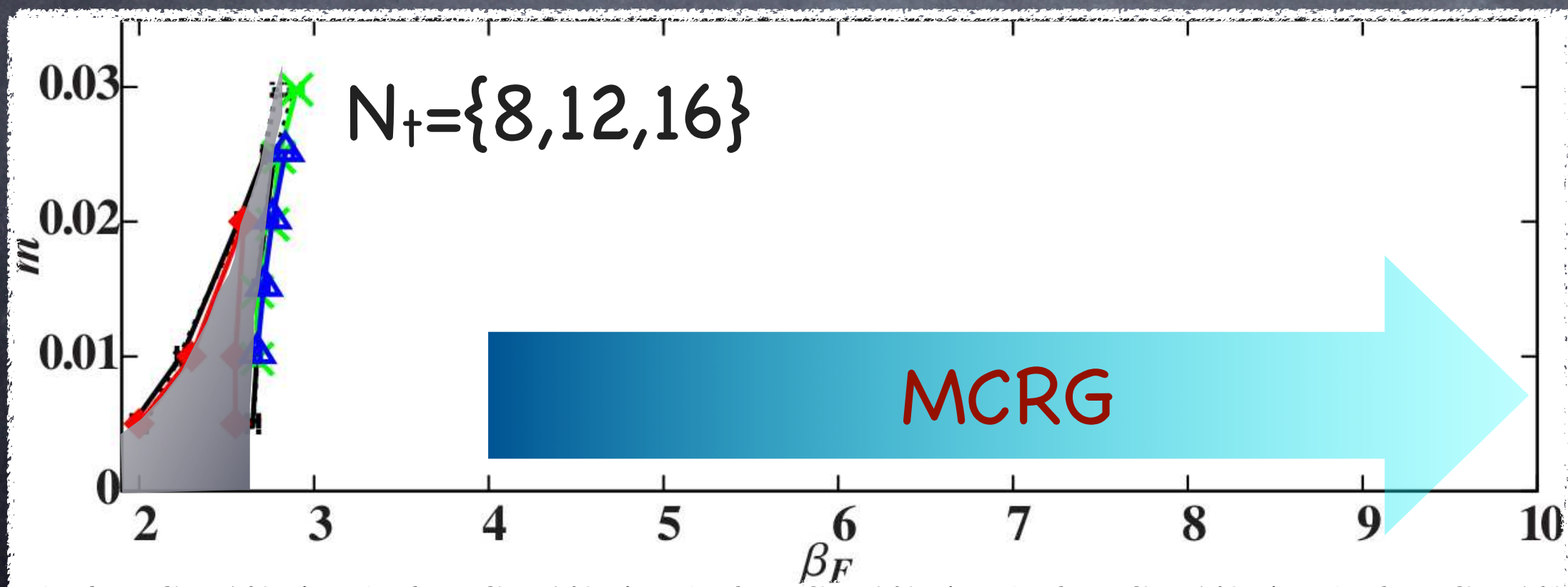
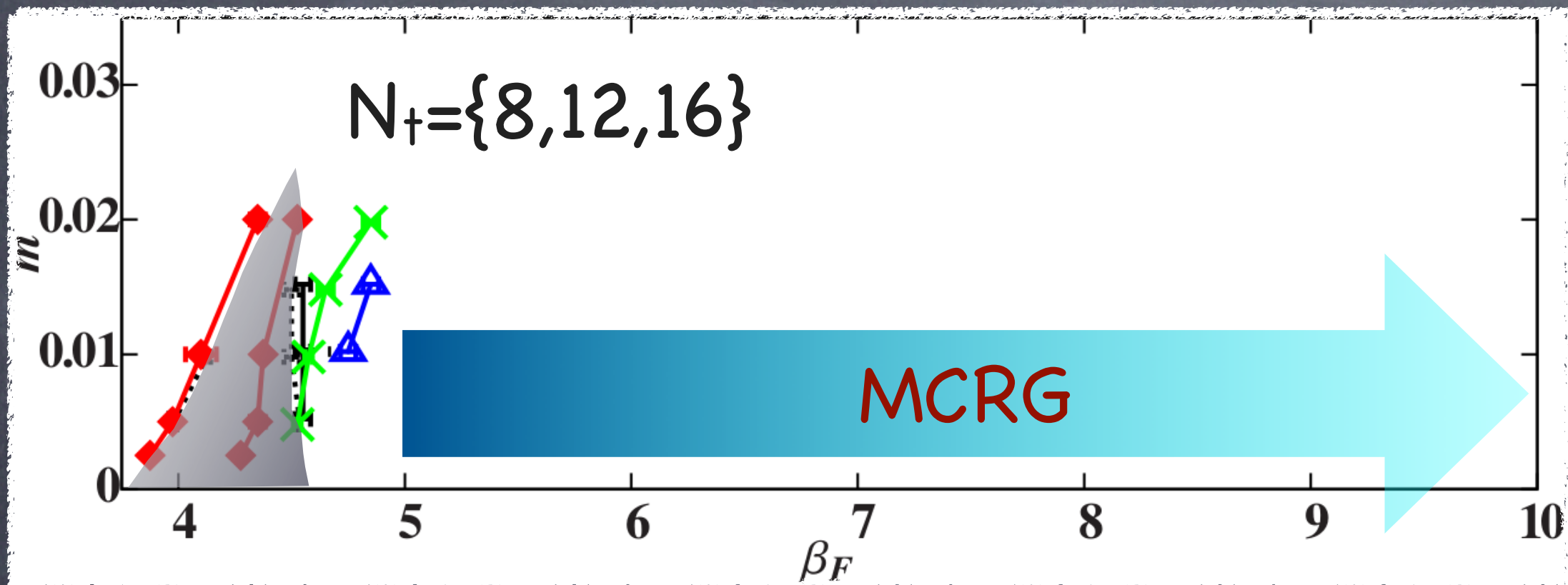
8 flavor finite
temperature
phase diagram



12 flavor finite
temperature
phase diagram

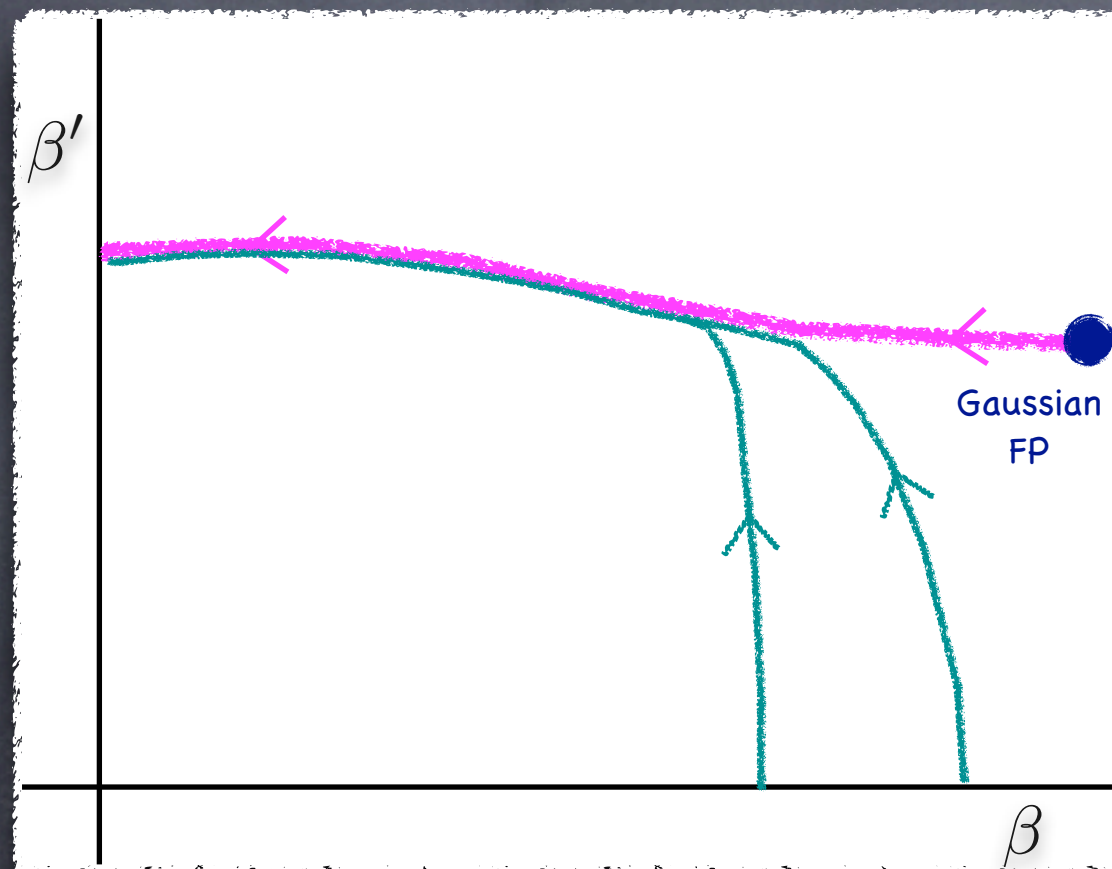
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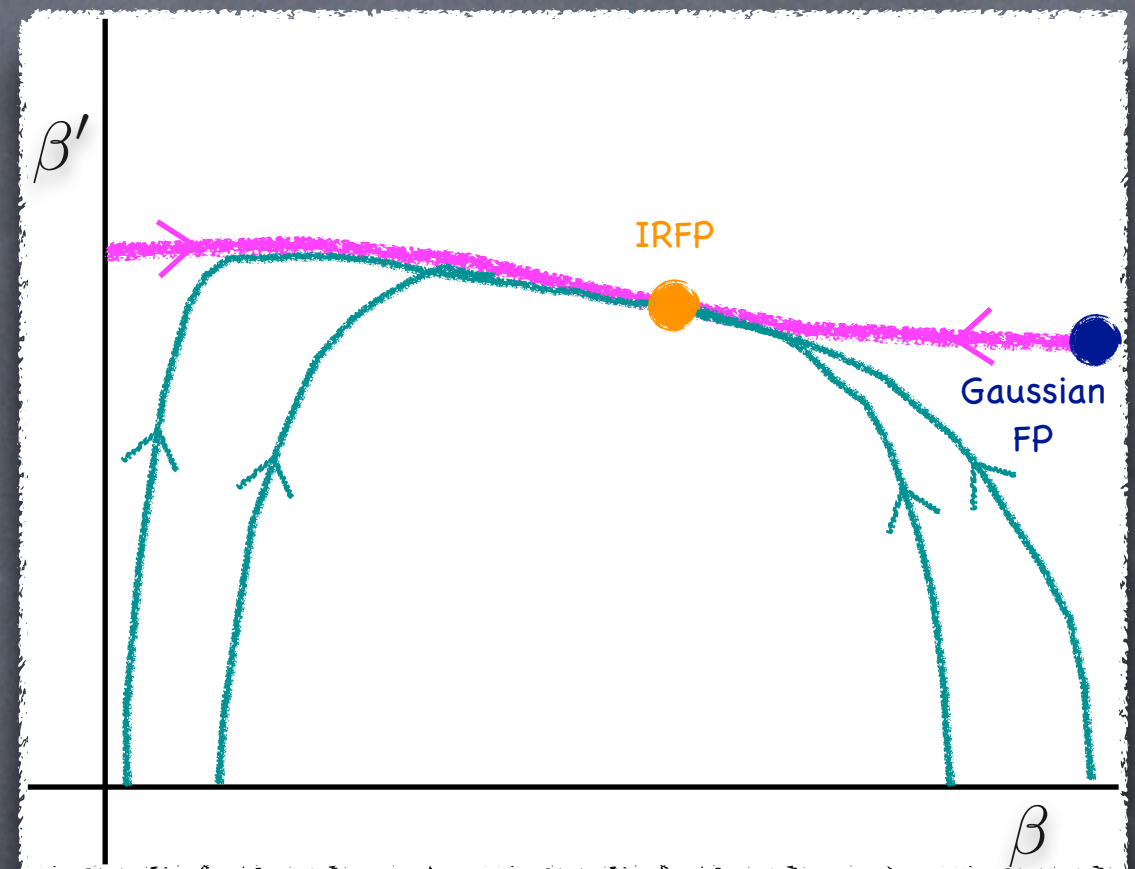


MCRG

Motivation ♦ 8 Flavor Result ♦ 12 Flavor Result ♦ Conclusion



QCD-like Renormalized Trajectory

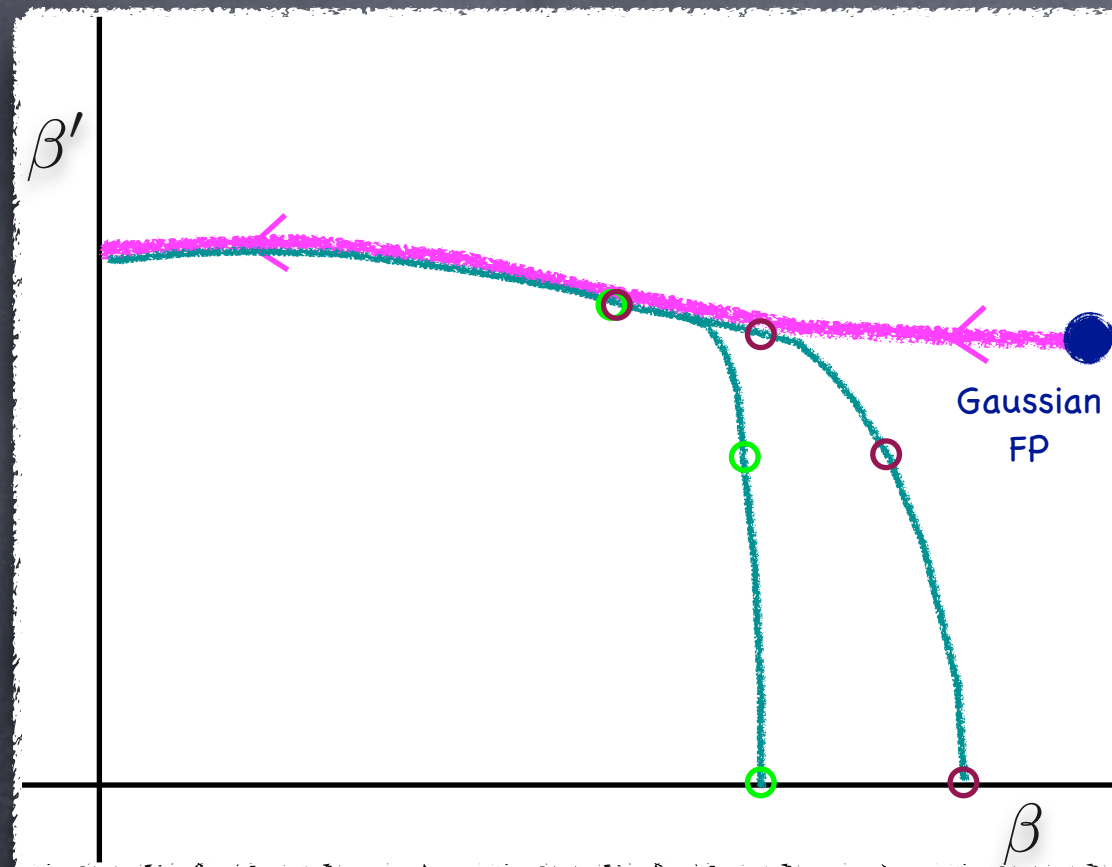


Conformal Renormalized Trajectory

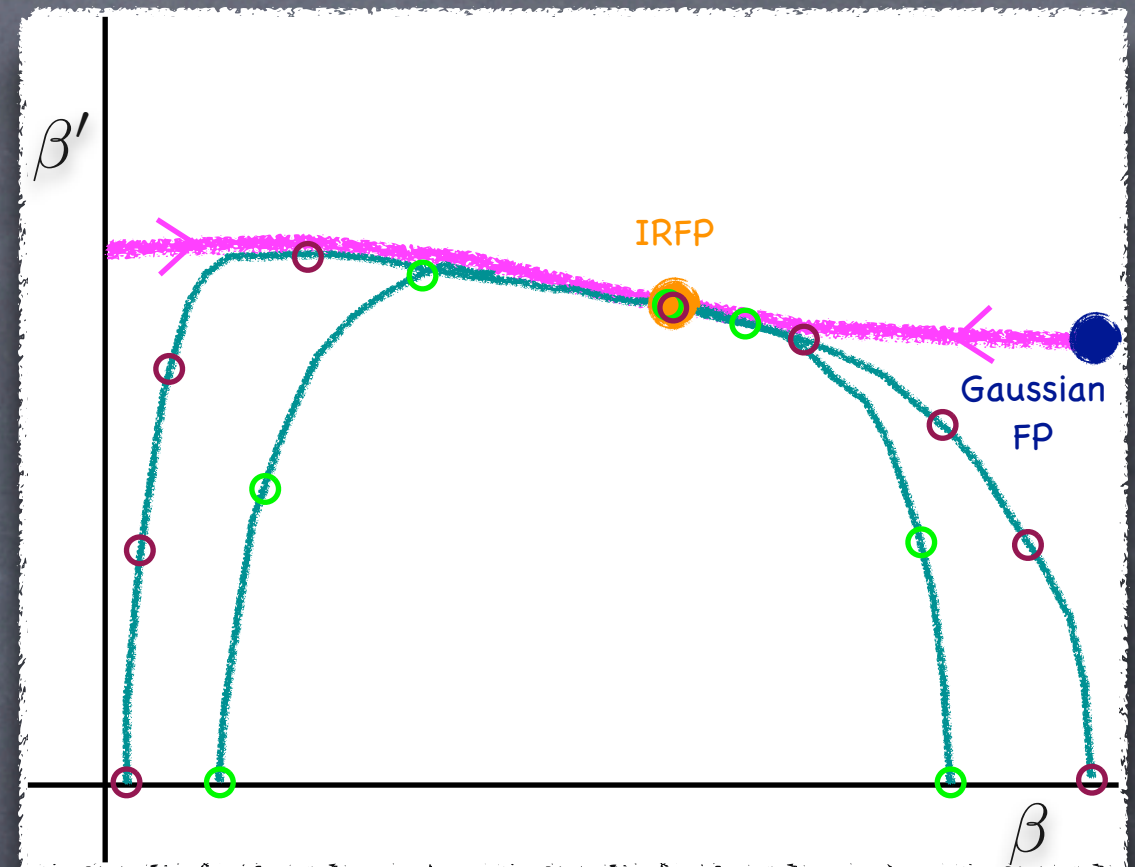
Renormalized flow on the $m=0$ critical surface

MCRG

Motivation ❖ 8 Flavor Result ❖ 12 Flavor Result ❖ Conclusion



QCD-like Renormalized Trajectory



Conformal Renormalized Trajectory

Renormalized flow on the $m=0$ critical surface

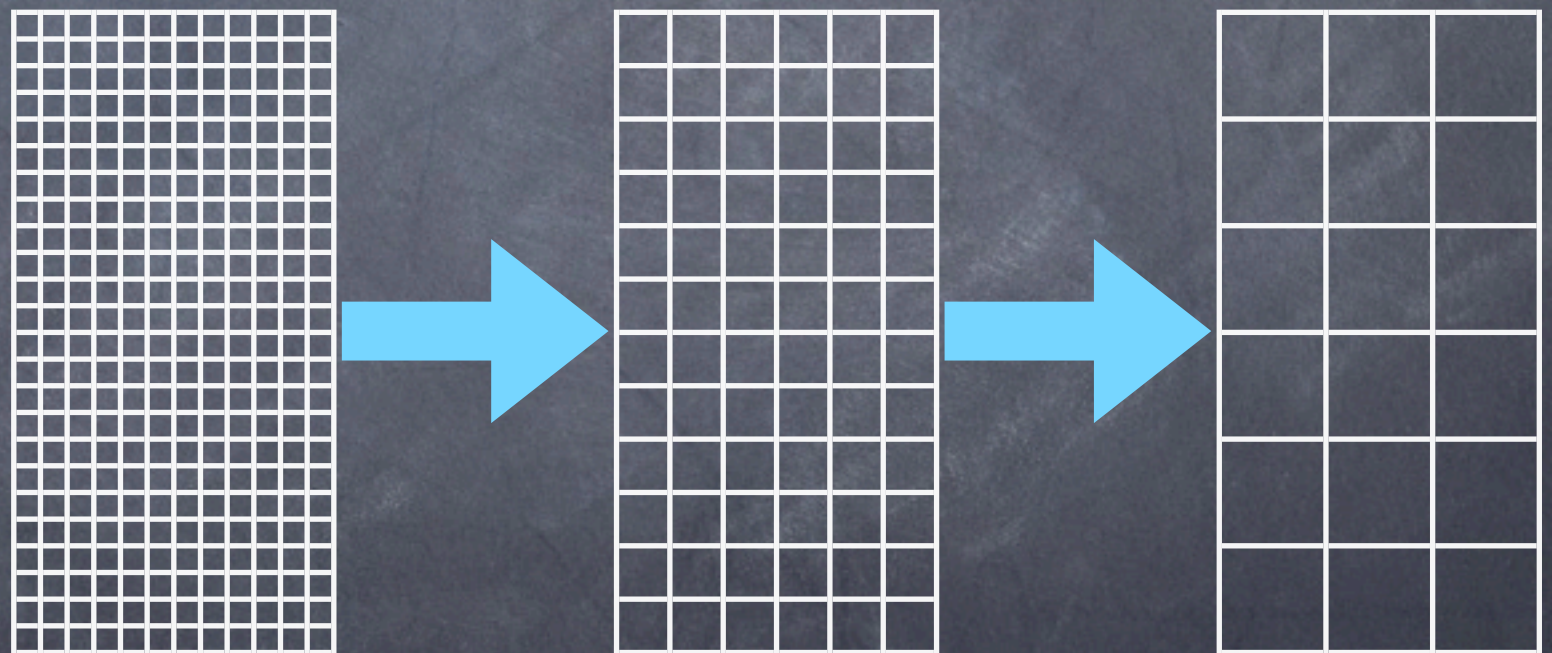
Step 1/3: Blocking

NHYP smeared block
transformation

Inner Smearing: 0.2
Outer Smearing: α

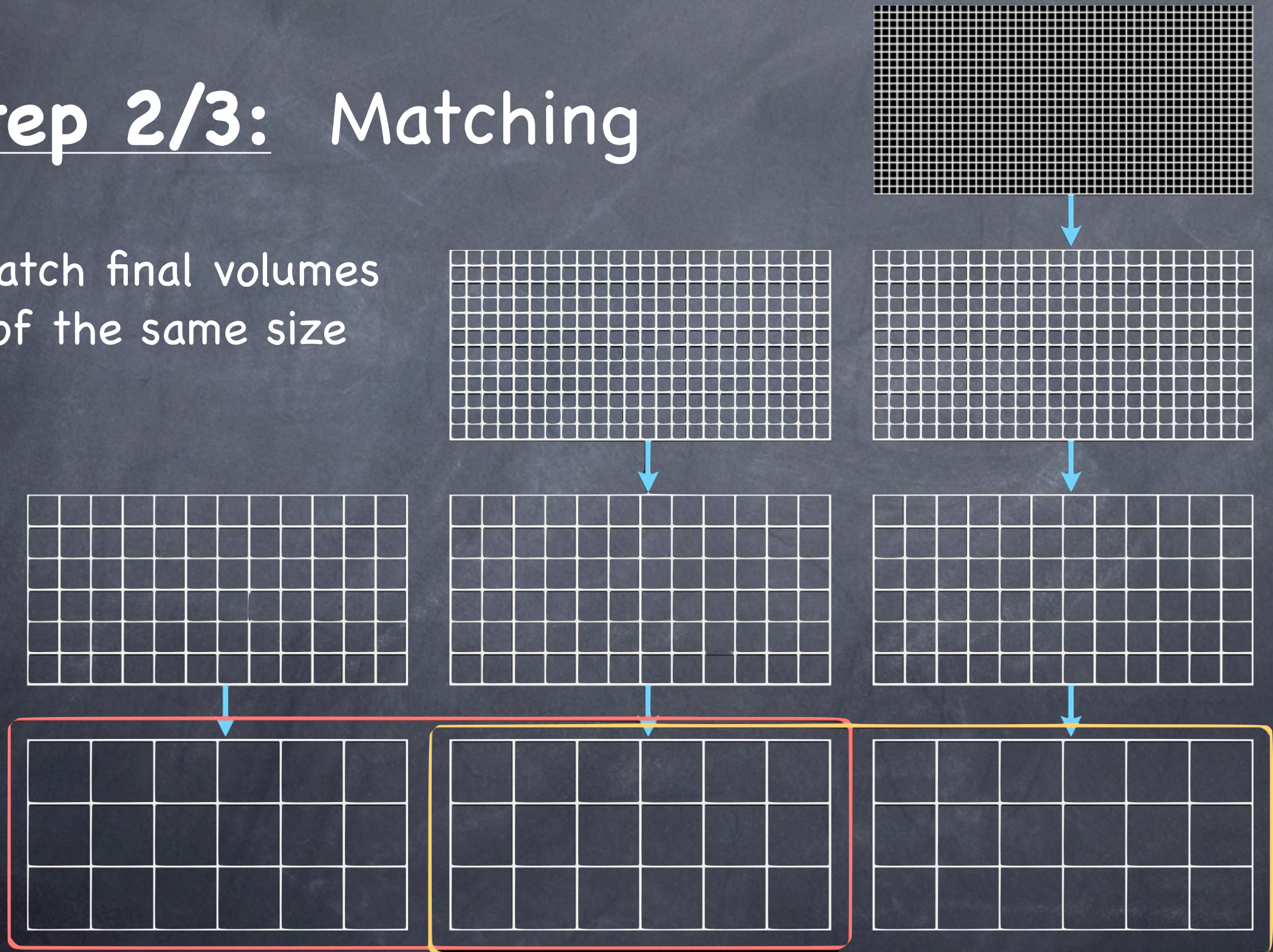
Measure:

- plaquette
- 6 link loops
- 8 link loop

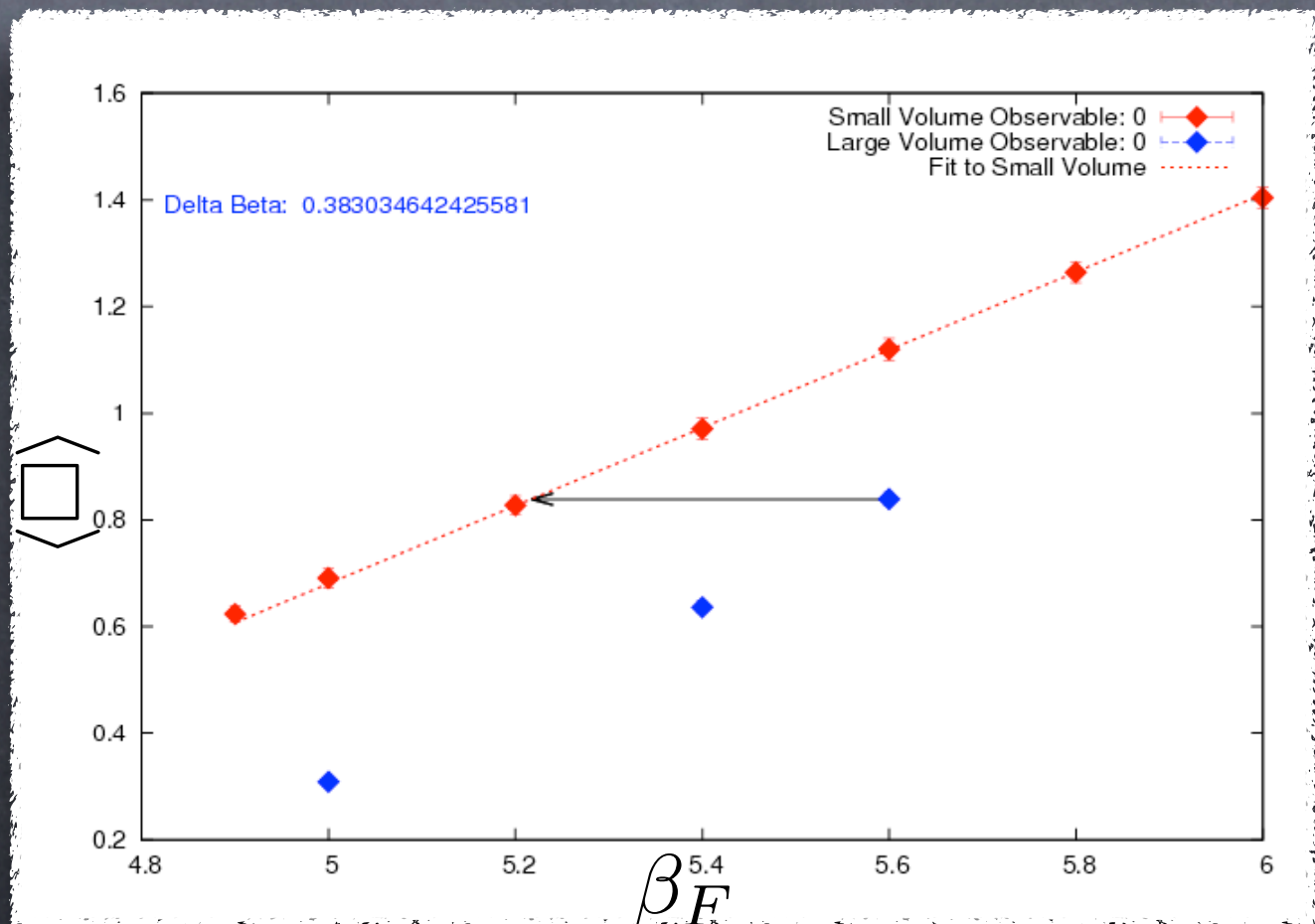
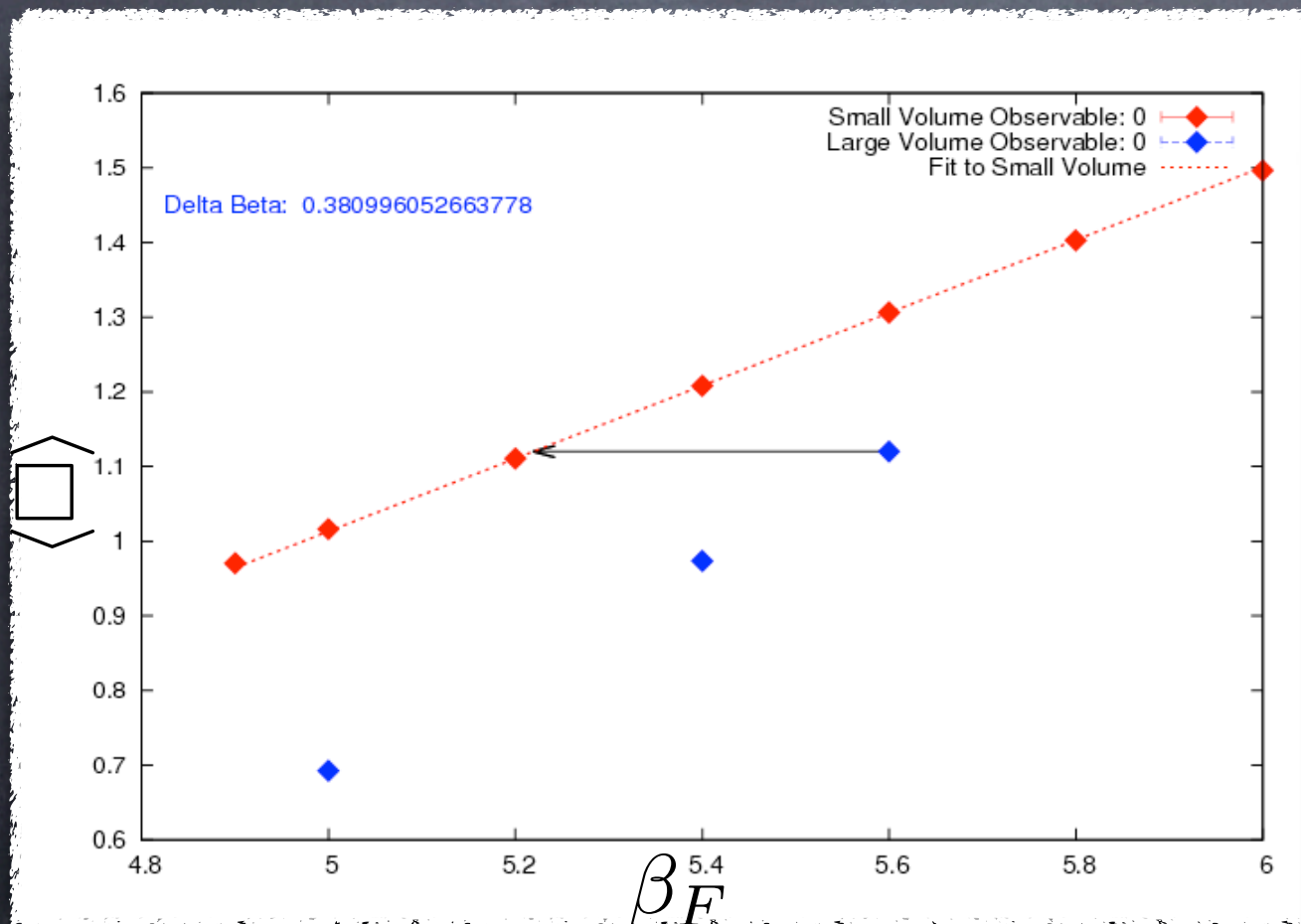


Step 2/3: Matching

Match final volumes
of the same size



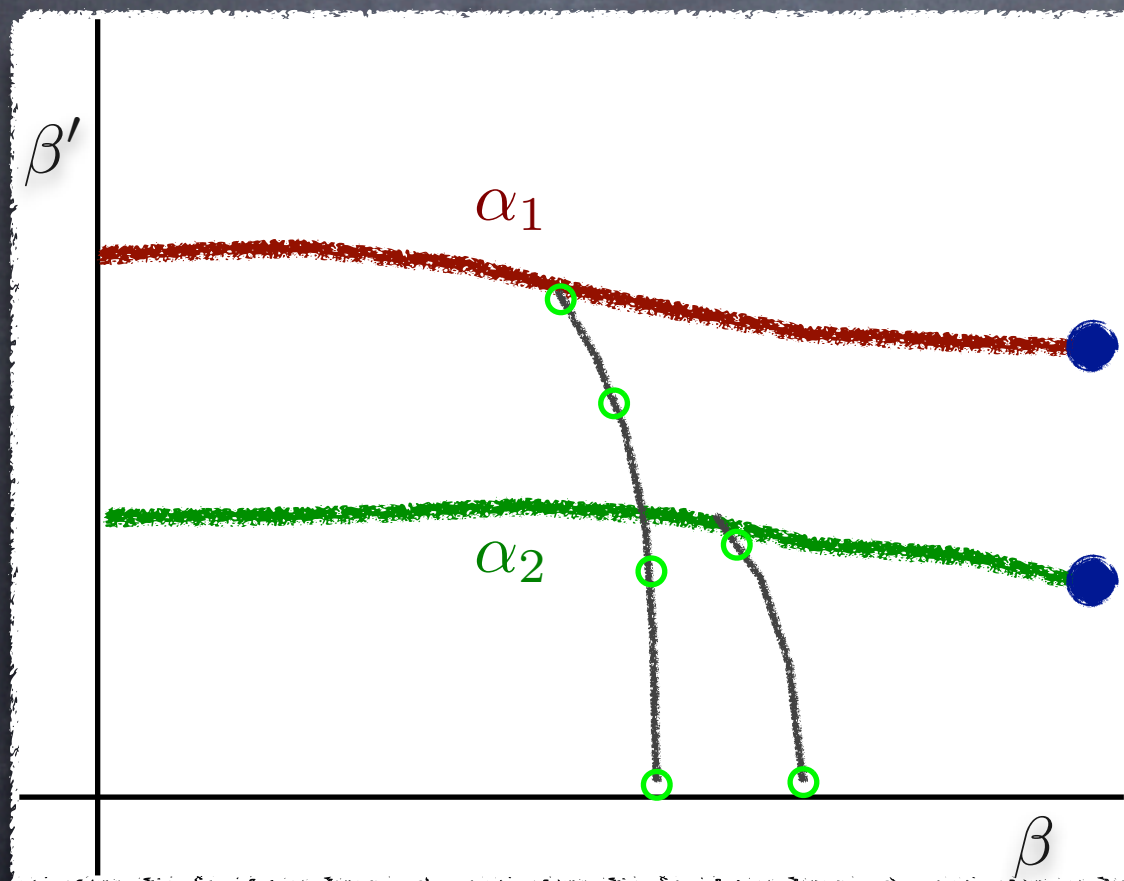
Step 2/3: Matching to find $\Delta\beta$



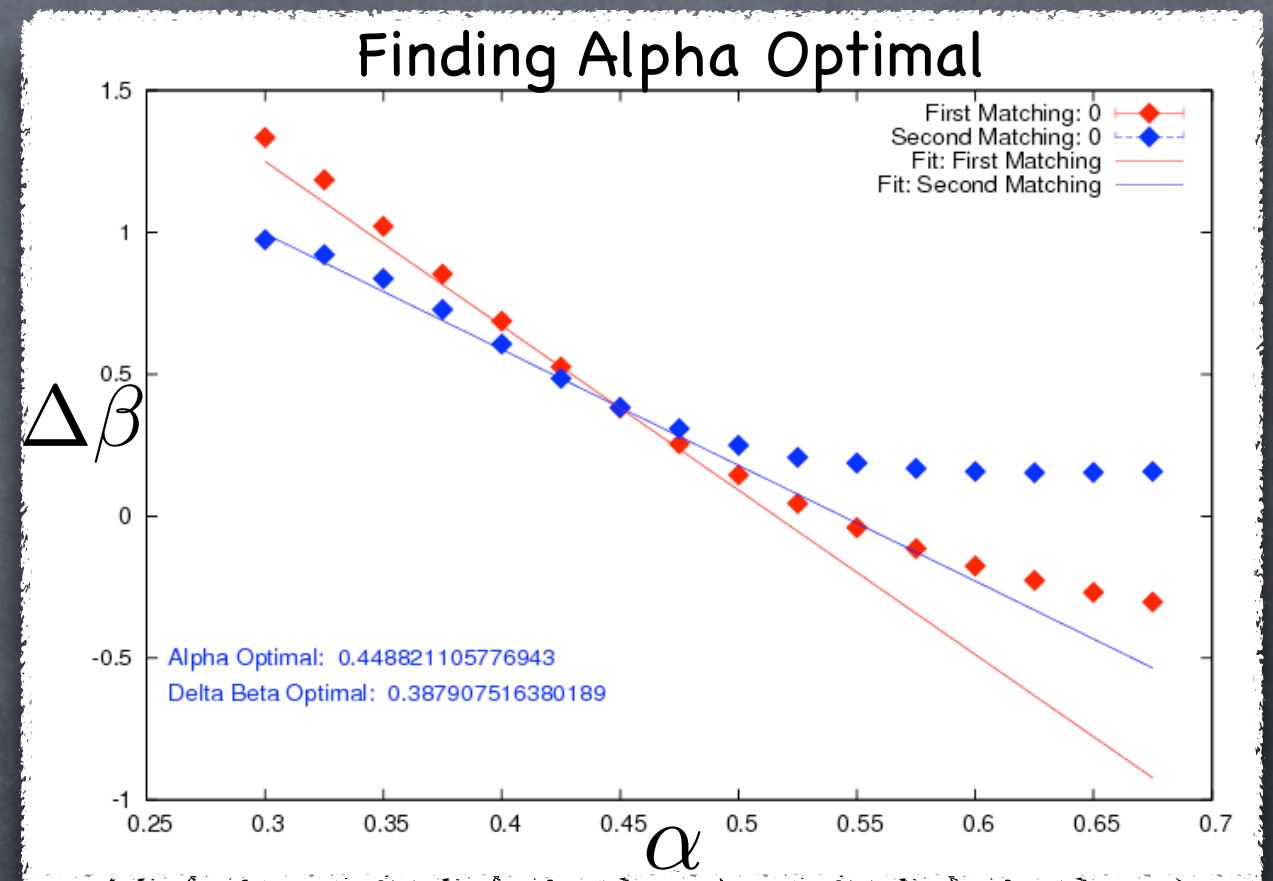
Matching between
 $24^3 \times 48$ blocked to $6^3 \times 12$
 $12^3 \times 24$ blocked to $6^3 \times 12$

Matching between
 $24^3 \times 48$ blocked to $3^3 \times 6$
 $12^3 \times 24$ blocked to $3^3 \times 6$

Step 3/3: Optimize α



Scan over α to find the block transformation that reaches the renormalized trajectory the quickest.

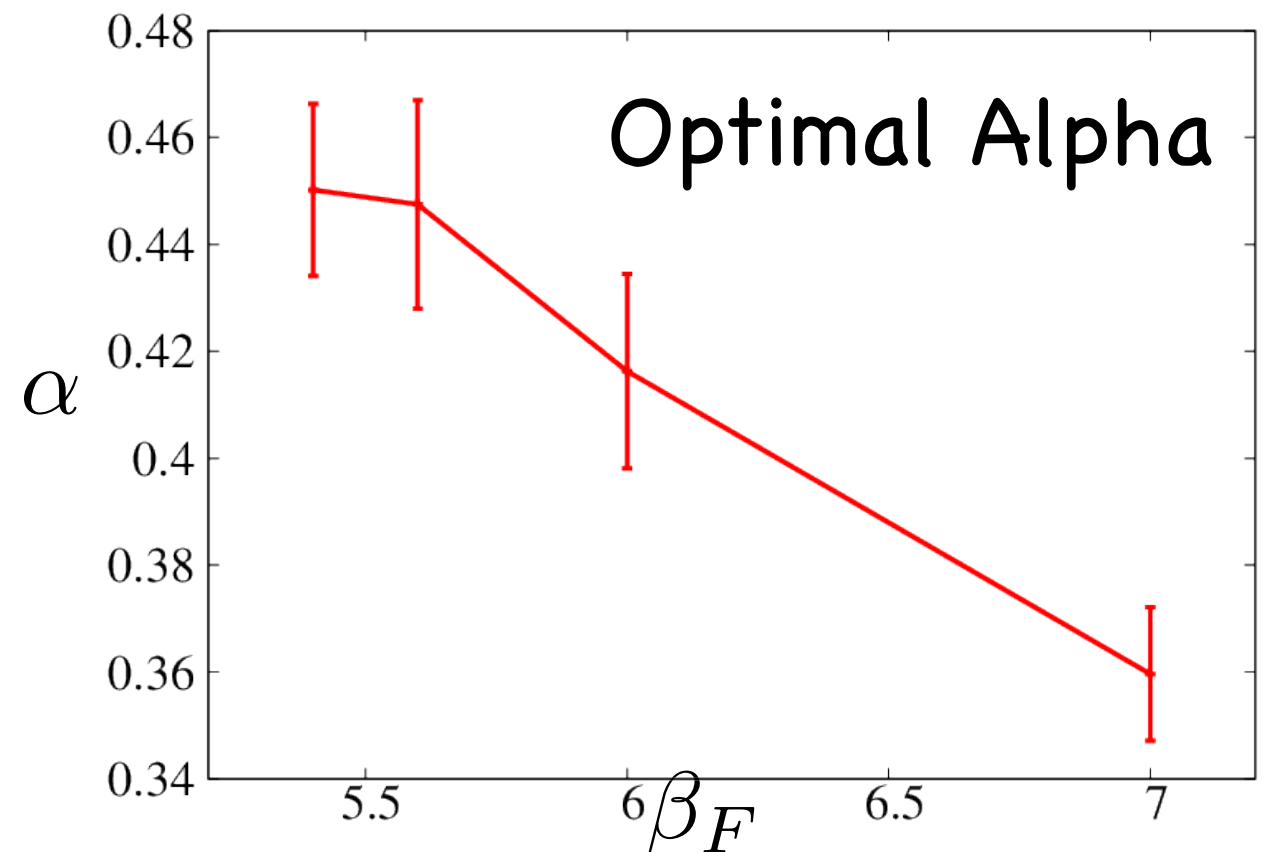
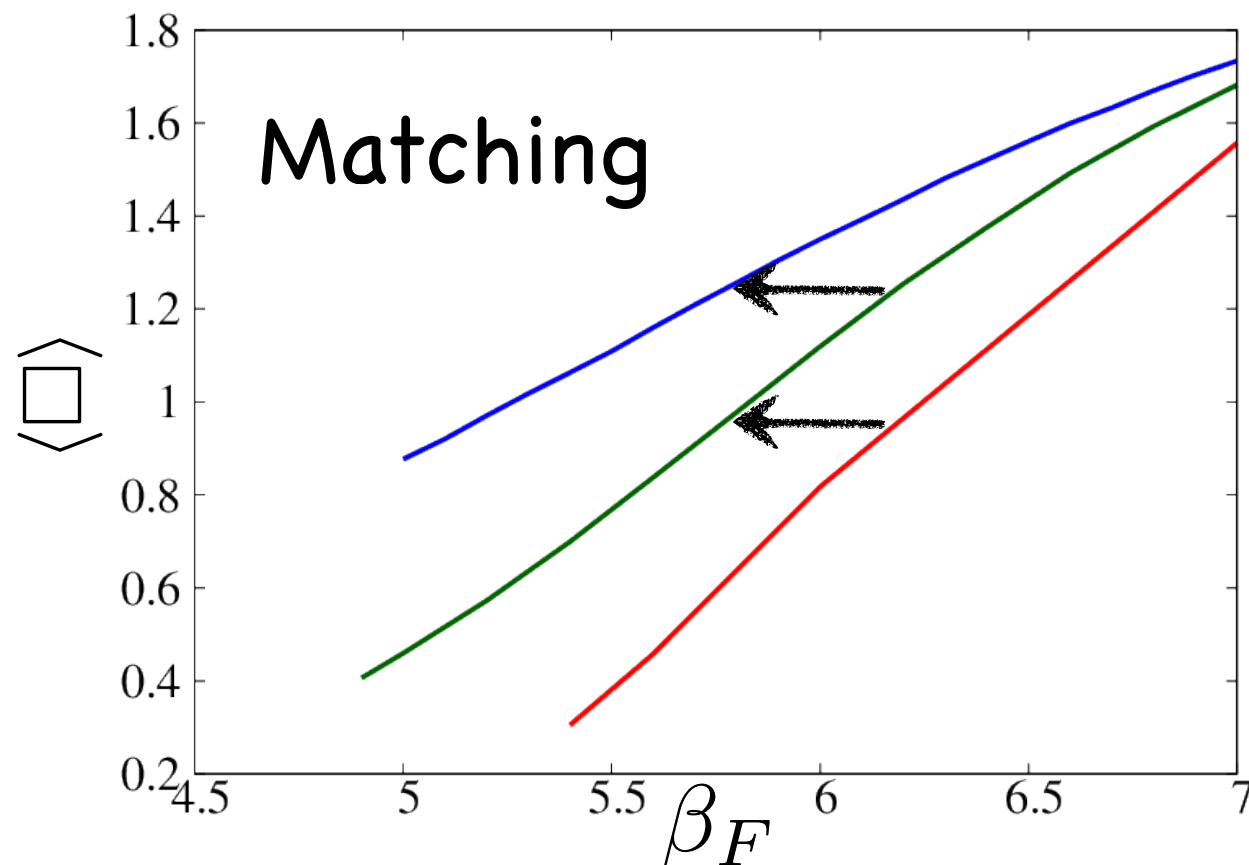


Step scaling function, S_b defined where $\Delta\beta$ for both levels of blocking are equal.

8 Flavor Result

Motivation ♦ MCRG ♦

12 Flavor Result ♦ Conclusion



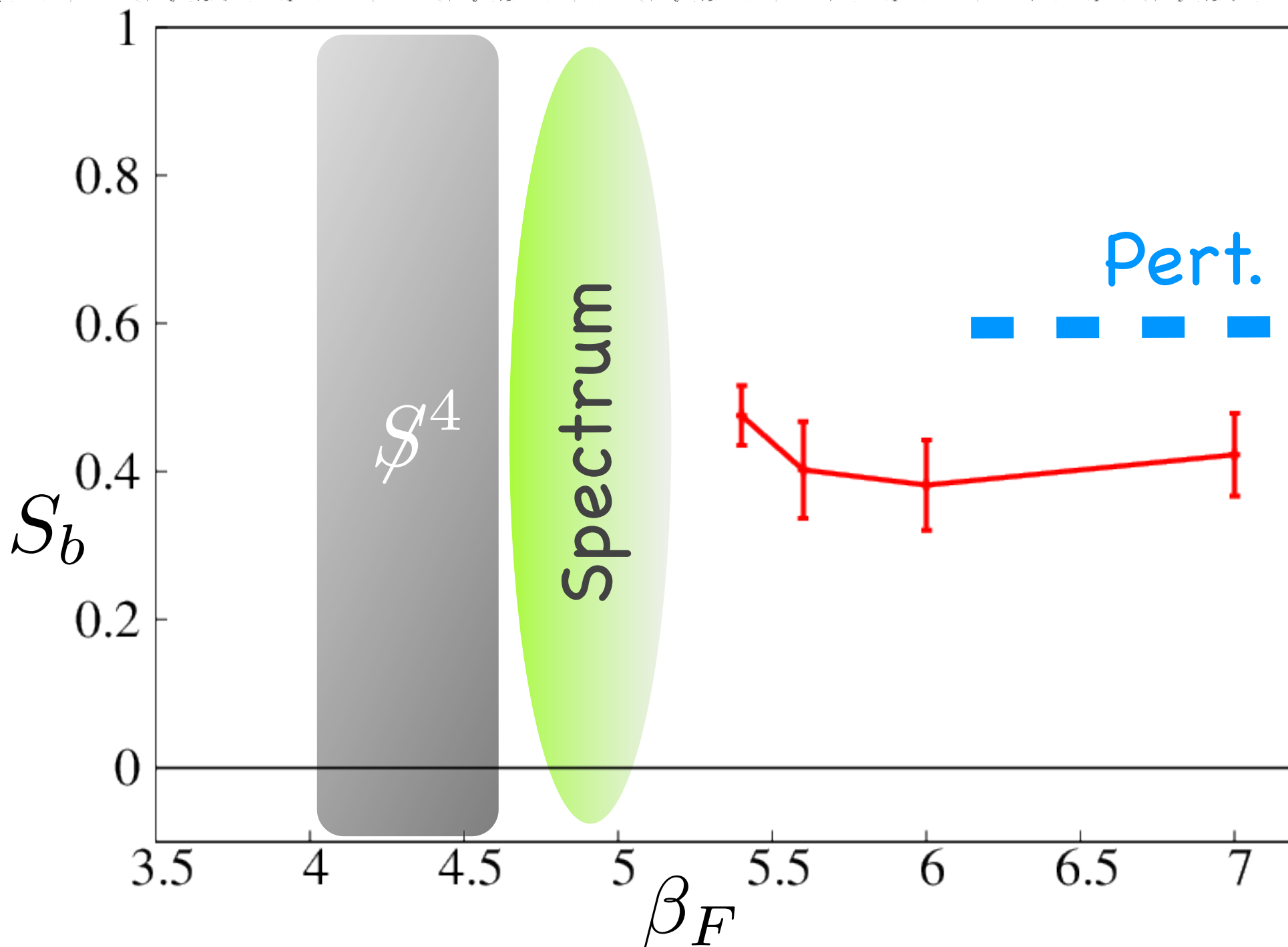
Matching between
 $24^3 \times 48$ blocked to $3^3 \times 6$
 $12^3 \times 24$ blocked to $3^3 \times 6$
 $6^3 \times 12$ blocked to $3^3 \times 6$

The optimal smearing parameter decreases with β .

8 Flavor Result

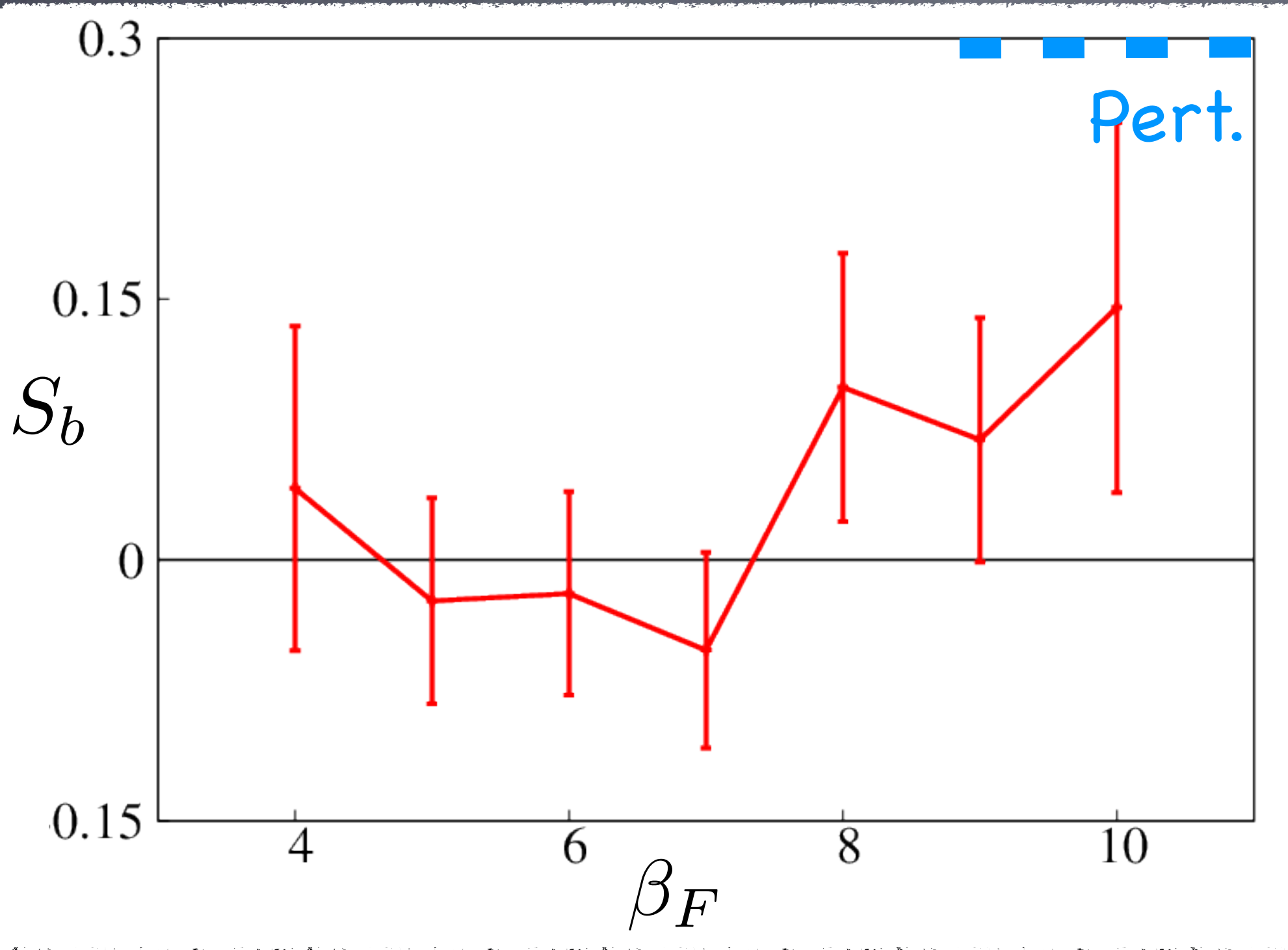
Motivation ♦ MCRG ♦

♦ 12 Flavor Result ♦ Conclusion



The step scaling function is comparable to the 2 loop value and connects perturbative and confining regions

Errors determined by looking at different observables

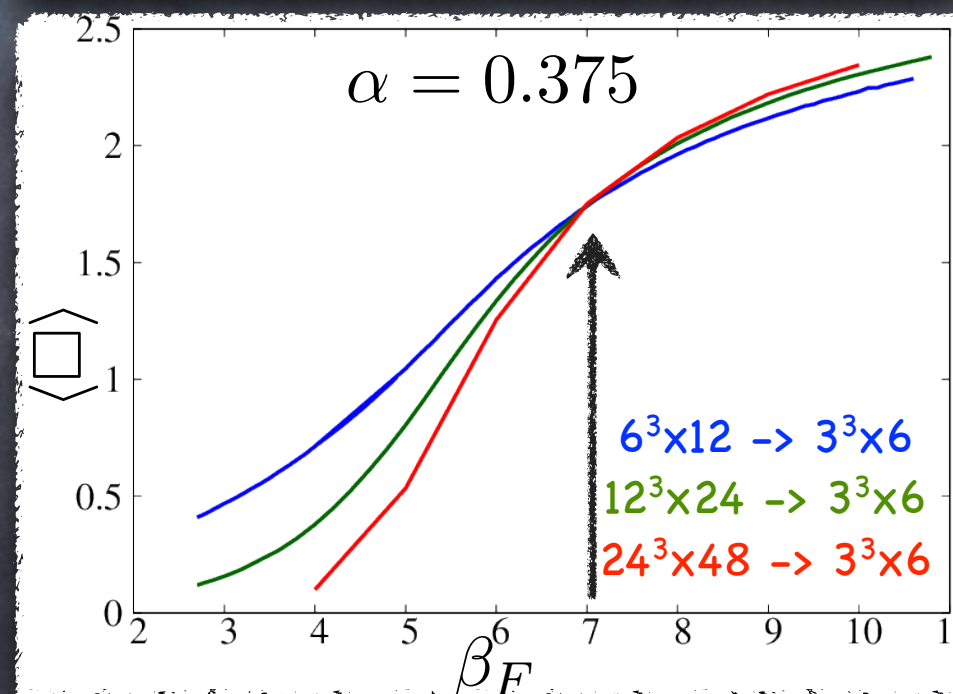
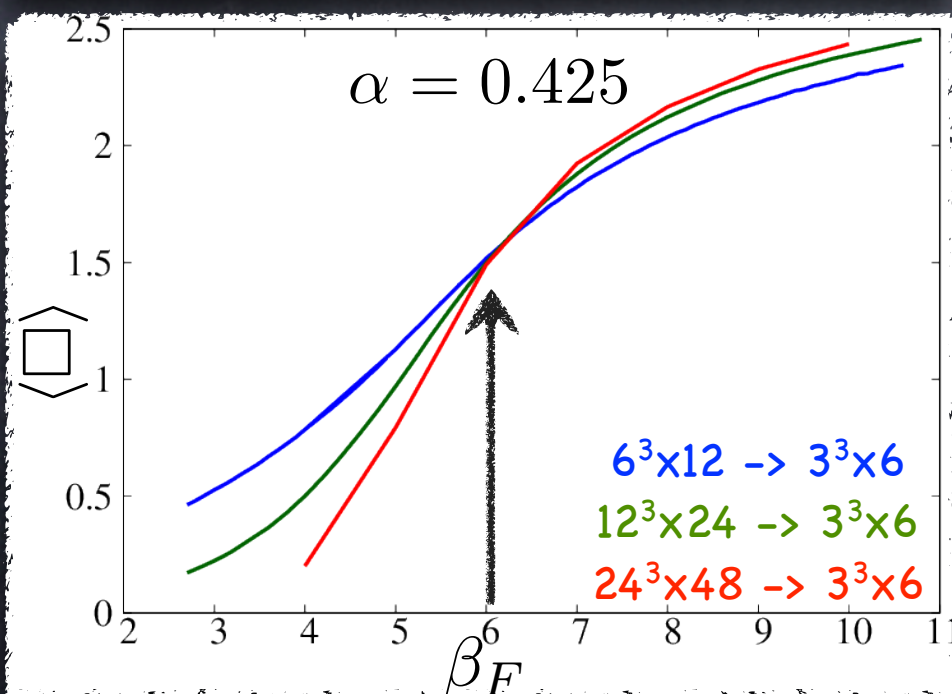
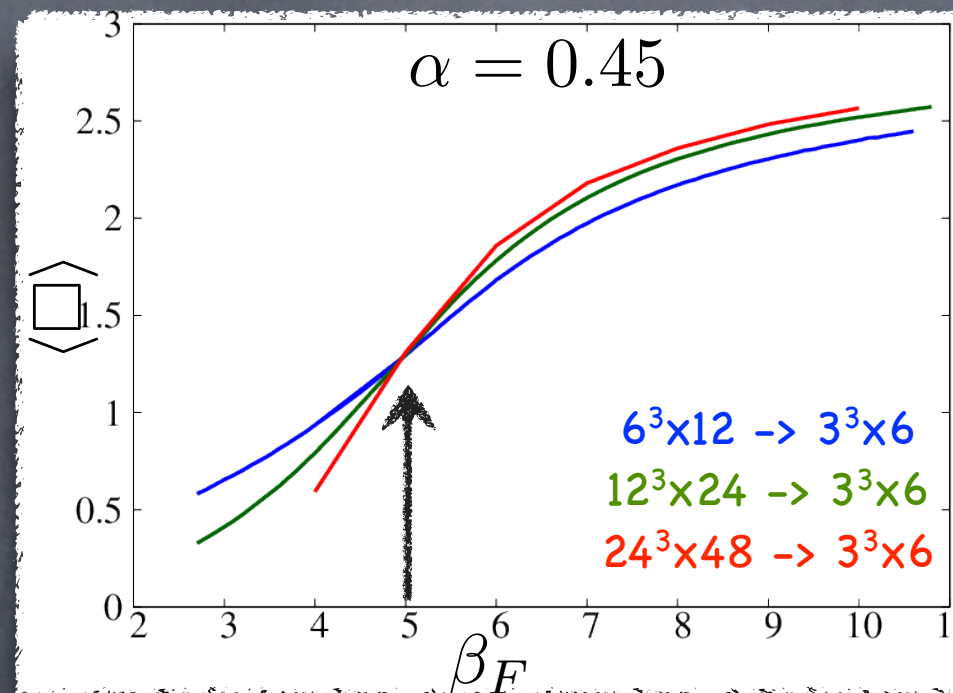
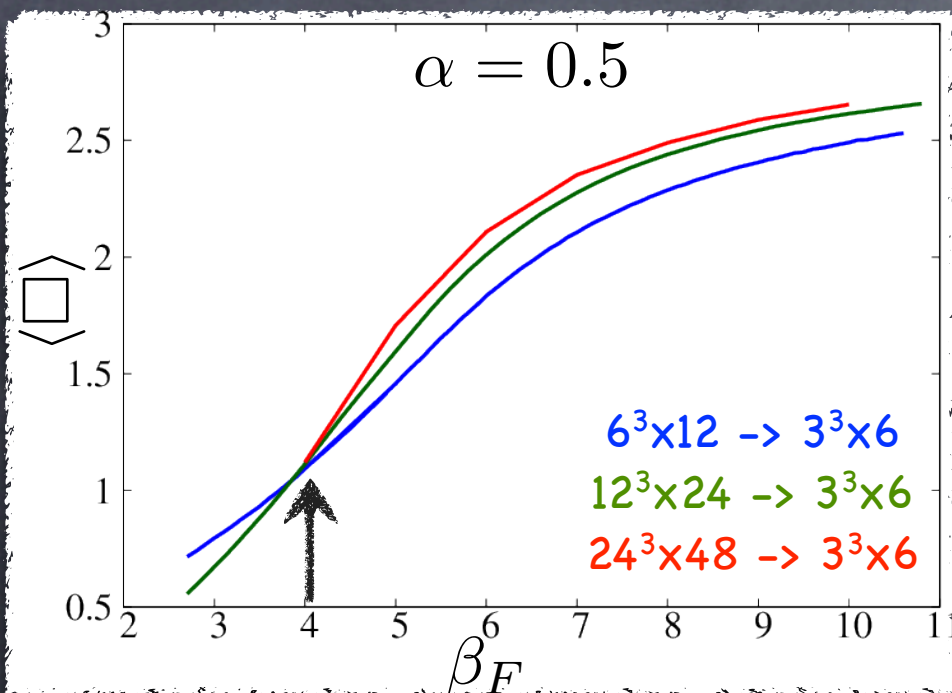


The step scaling function is consistent with zero for $\beta=\{4-8\}$.

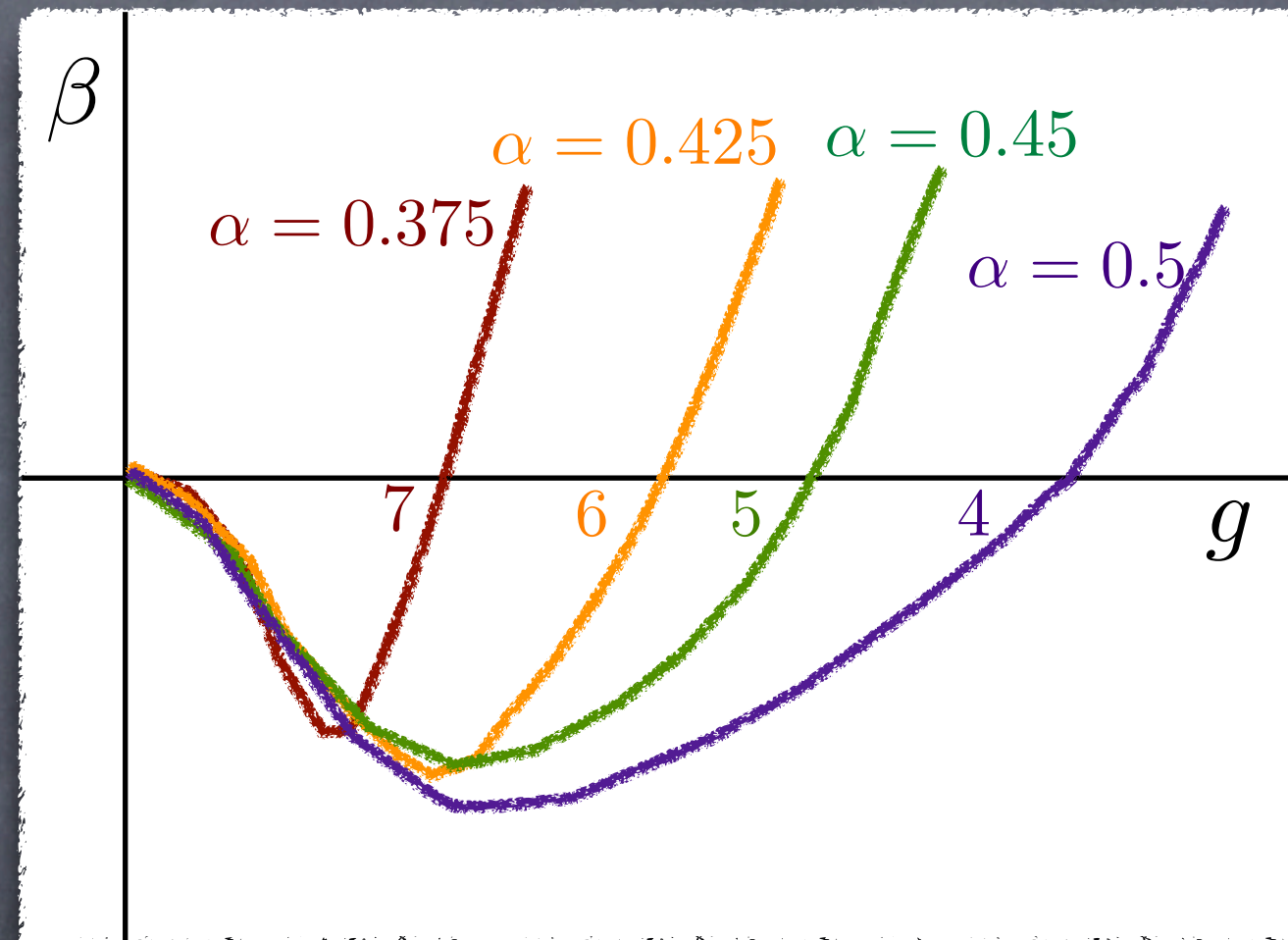
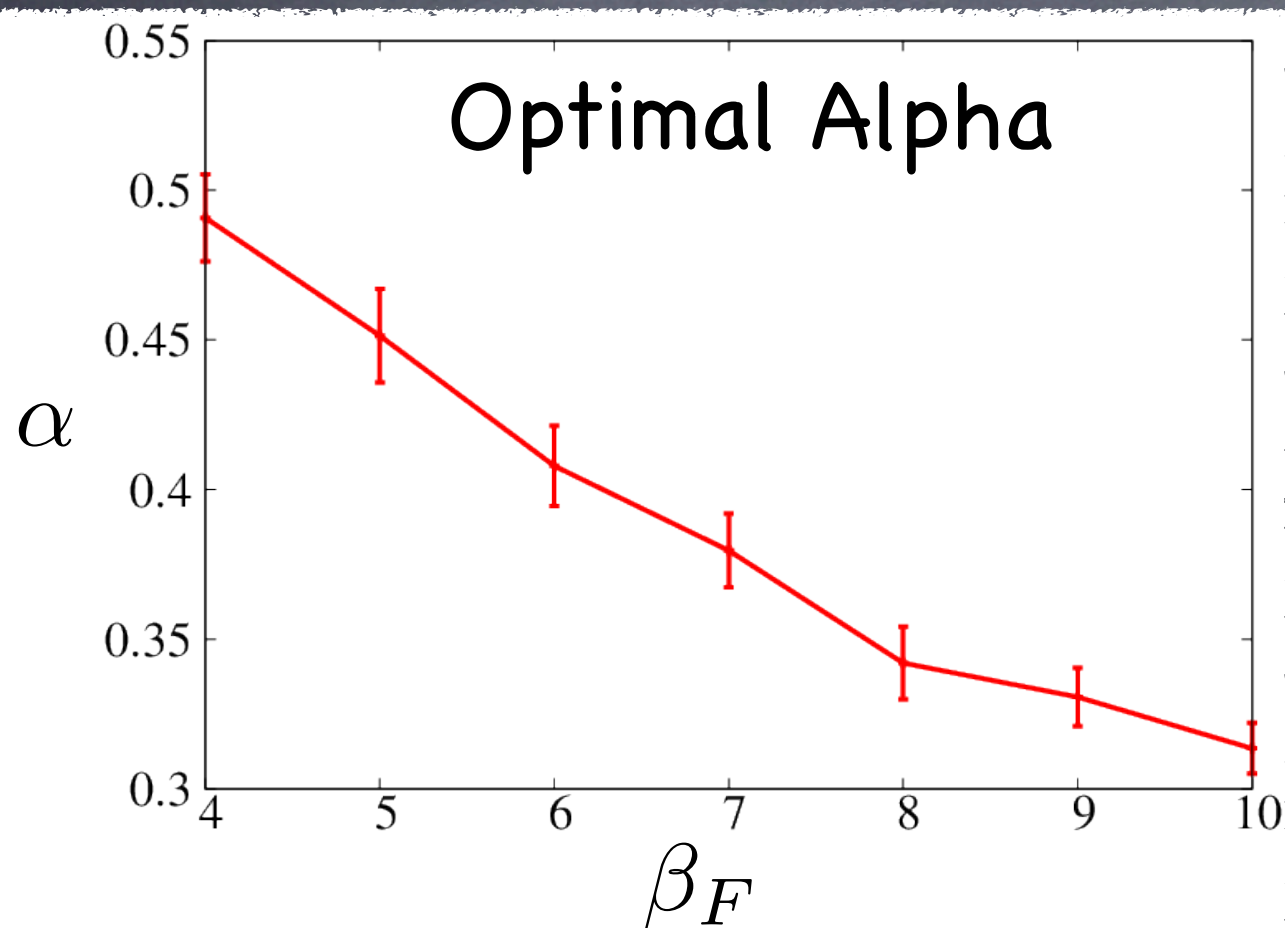
Errors determined by looking at different observables

12 Flavor Result

For different β values, the optimal α predicts $S_b=0$, shown here as the intersection of the three blocking levels.

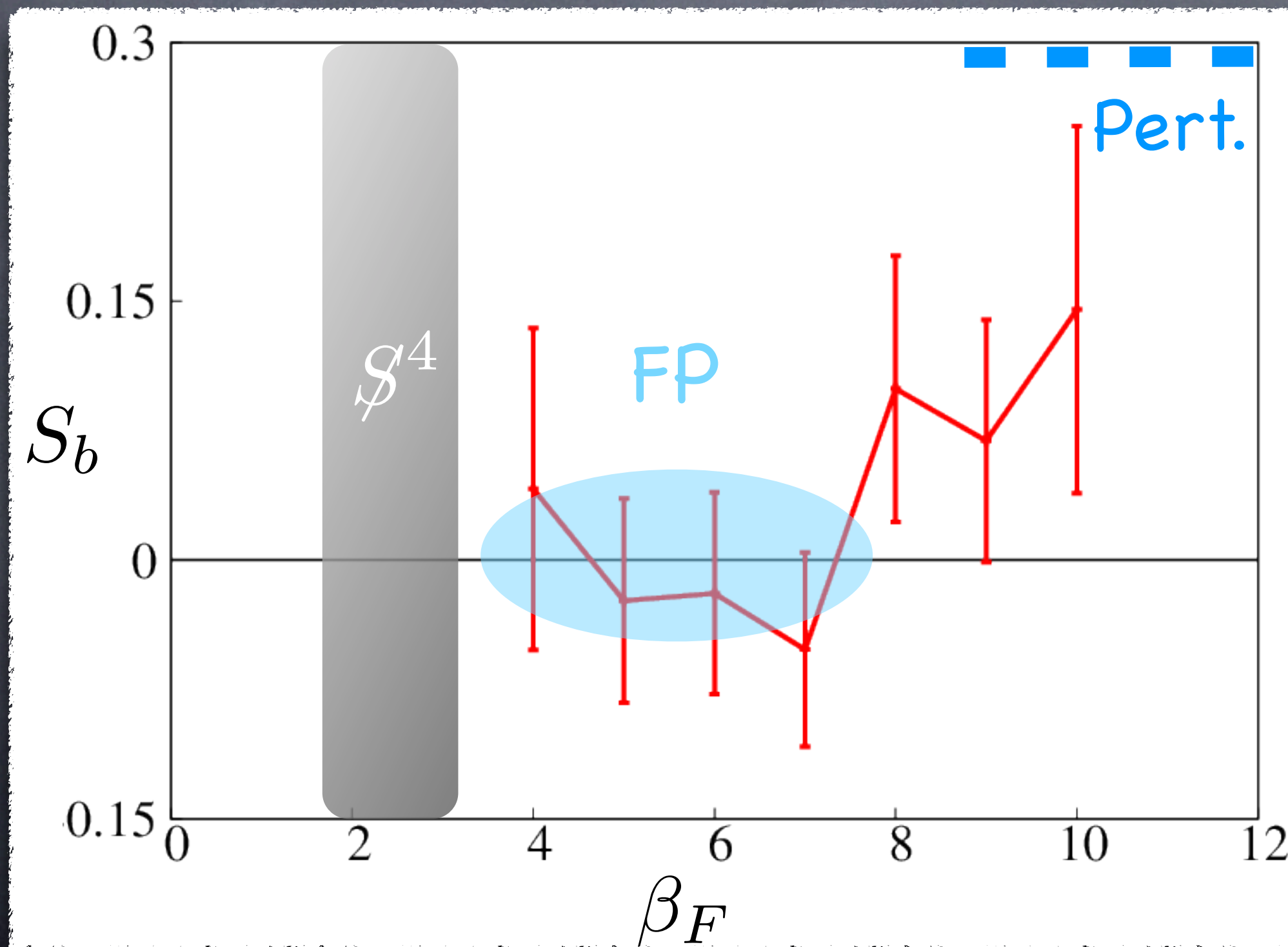


The Infrared Fixed point is moving!

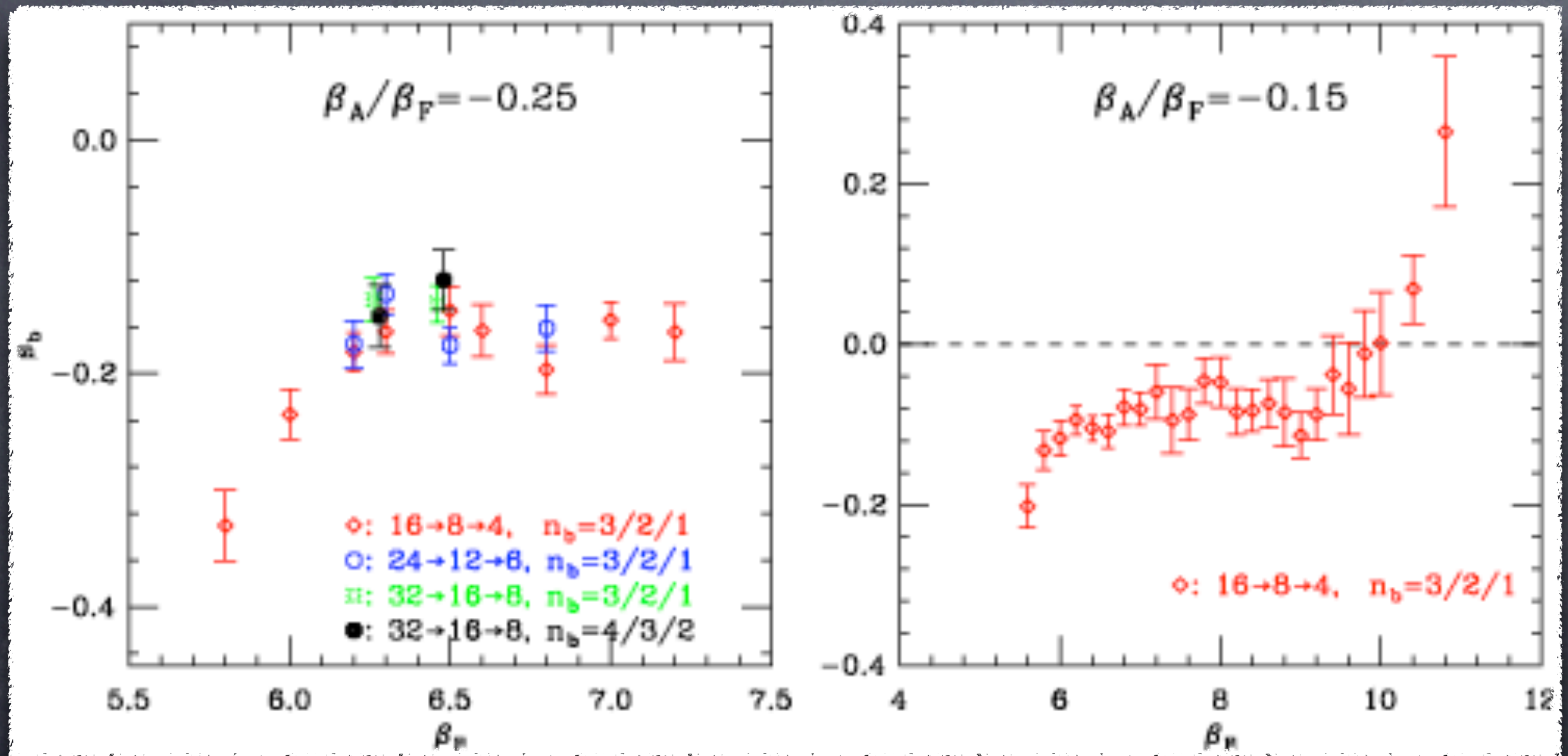


The optimization is choosing a fixed point at the simulation β_F , making the interpretation of MCRG subtle.

12 Flavor Result



12 Flavor Result



Hasenfratz SU(3) $N_f=12$ results from last year using a different action showing similar plateau behavior in strong coupling.

Conclusion

- We studied the MCRG behavior at couplings weaker than the S^4 broken phase at small fermion mass
- MCRG predicted bare step scaling function for 8 flavors is positive (Confining)
- MCRG predicted bare step scaling function for 12 flavors is consistent with an IR fixed point
- Complements Eigenvalues and Finite T studies (previous talks by A. Hasenfratz and D. Schaich)

Acknowledgments

- Anna, David, Anqi
- DOE Office of Science Graduate Fellowship
- USQCD
- University of Colorado Research Computing (Janus)
- NSF XSEDE
- Thank you and have a G'Day

Simulation

	8 Flavor	12 Flavor
Volumes	$6^3 \times 12$ $12^3 \times 24$ $24^3 \times 48$	$6^3 \times 12$ $12^3 \times 24$ $24^3 \times 48$
Couplings	$5.0-7.0$ $4.9-7.0$ $5.4, 5.6, 6.0$	$2.6-9.0$ $2.7-8.8$ $4.0, 5.0, 6.0, 7.0$
Masses	0.02 0.01 0.0025	0.02 0.01 0.0025

$24^3 \times 48 \rightarrow 12^3 \times 24 \rightarrow 6^3 \times 12 \rightarrow 3^3 \times 6$
 $12^3 \times 24 \rightarrow 6^3 \times 12 \rightarrow 3^3 \times 6$
 $6^3 \times 12 \rightarrow 3^3 \times 6$

Blocked observables:

- Plaquette
- 6 Link Loops
- 8 Link Loop

NHYP smeared block transformation:

0.2

0.2

α