

Towards an Understanding of Star Formation: Scaling Relations in the ISM

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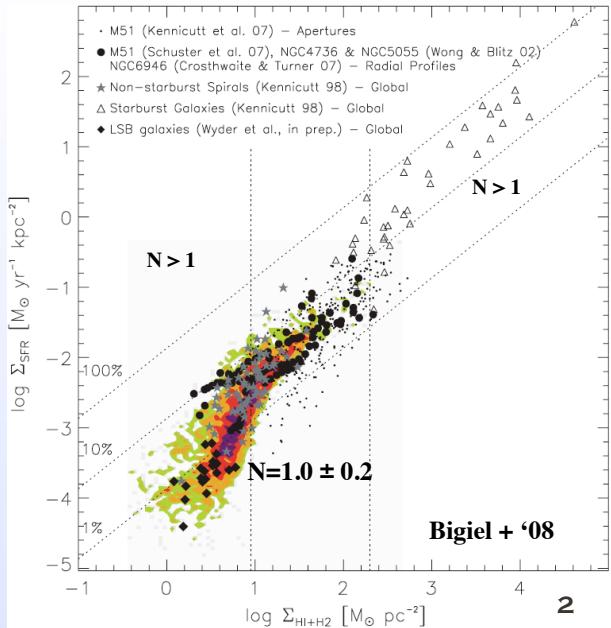
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The Kennicutt-Schmidt Relationship

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^N$$

Schmidt '59
 Buta + '89
 Kennicutt '89
 Kennicutt '98
 Hunter + '98
 Boselli + '02
 Wong & Blitz '02
 Boissier + '03
 Heyer + '04
 Leroy + '05
 Kennicutt + '07
 Leroy + '08
 Bigiel + '08
 Blanc + '09
 Verley + '10
 Daddi + '10
 Genzel + '10
 Liu + '11
 Schruba + '11
 Rahman + '12
 Leroy + '13
 Momose + '13...

Kennicutt & Evans 2012
(and references therein)



Overview

- The Kennicutt-Schmidt (KS) Relationship
- Previous Results
- Fitting the KS relationship: Evidence for diffuse molecular gas
- Outlook: other scaling relations
- Summary

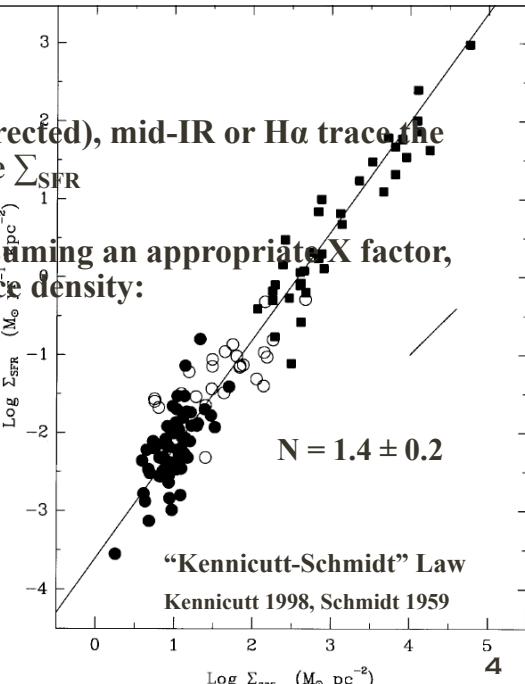
KS: OB

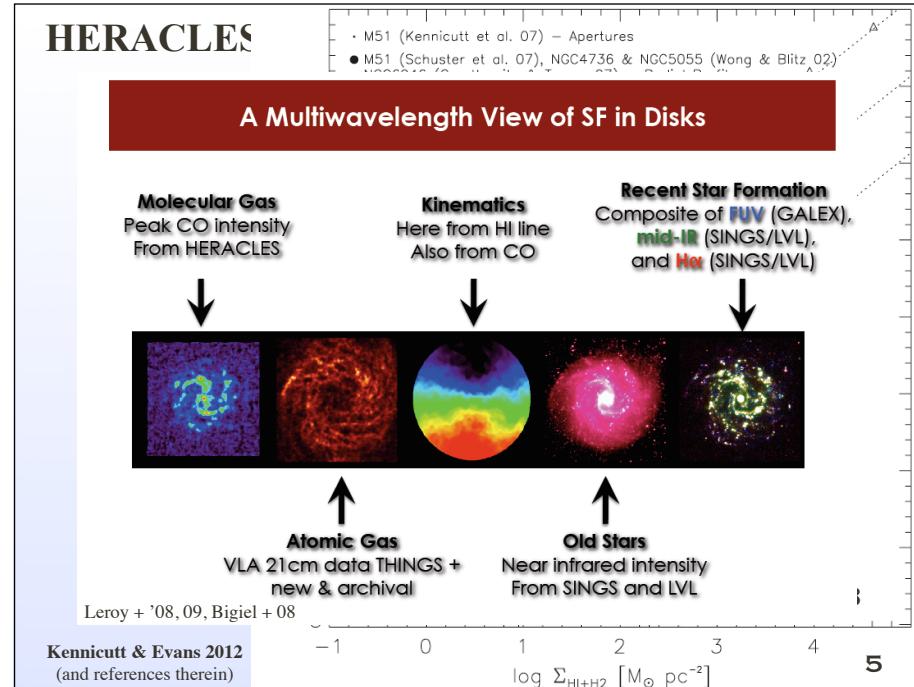
- FUV (extinction corrected), mid-IR or H α trace the Star Formation Rate \sum_{SFR}
- HI and CO lines, assuming an appropriate X factor, trace total gas surface density:

$$\square \quad \sum_{\text{gas}} = \sum_{\text{HI}} + \sum_{\text{H}_2}$$

Observations find:

$$\sum_{\text{SFR}} \propto \sum_{\text{gas}}^N$$

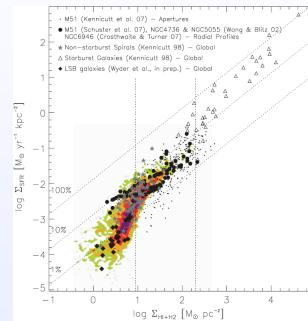




KS Slope Estimates

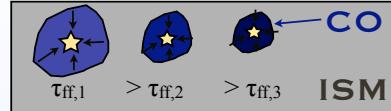
- At intermediate $10 \text{ M}_\odot \text{ pc}^{-2} < \Sigma_{\text{gas}} < 100 \text{ M}_\odot \text{ pc}^{-2}$, Bigiel +'08 find $N \sim 1$

- A linear relationship from resolved galaxies: STING, HERACLES, though with significant scatter (e.g. Bigiel + '08, Rahman + '12, Schruba + '12, Leroy + '13, etc...)



- Super-linear $N \sim 1.5$ KS relationship from unresolved disks (Kennicutt '89, '98) and resolved observations (e.g. Kennicutt + '07, Liu + '11, Momose + '13)

Interpreting the KS Slope



Super-linear KS slope ($N \sim 1.5$)

⇒ decreasing gas depletion time, or higher efficiency, with increasing GMC density

In both paradigms, CO traces star forming ‘GMCs’

Depletion time τ_{dep} a key parameter for theories of star formation (Ostriker+, Dobbs+, Krumholz+, Hopkins+, ...)



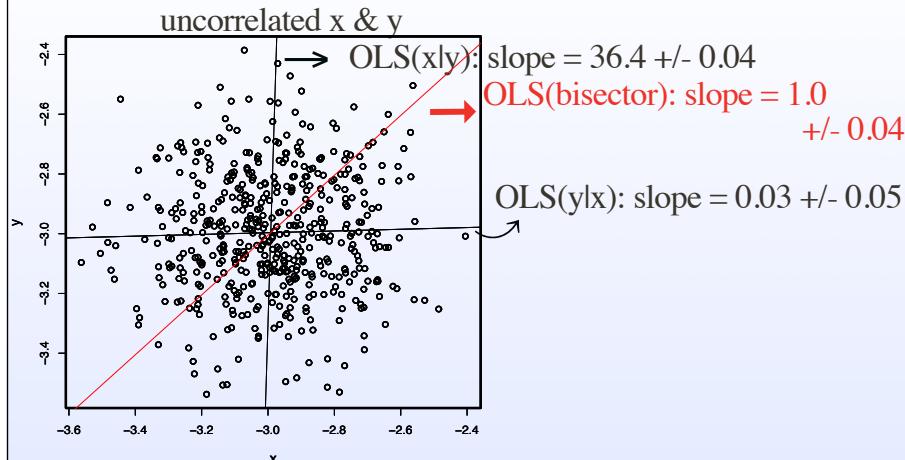
Linear KS slope ($N \sim 1$)

⇒ constant gas depletion time or efficiency of GMCs
(though observations indicate significant scatter)

Statistical Fitting

- Fitting method provides well defined statistics
(OLS methods: $y|x$, $x|y$, bisector)
- Hierarchical modeling for hierarchical data
- Hierarchical Bayesian fitting rigorously treats uncertainties, providing PDFs of all fitted parameters
- Quantifying goodness of fit “By Eye”

TESTING OLS METHODS



Shetty, Kelly, Bigiel '13

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Hierarchical Bayesian Fitting of KS Relationship

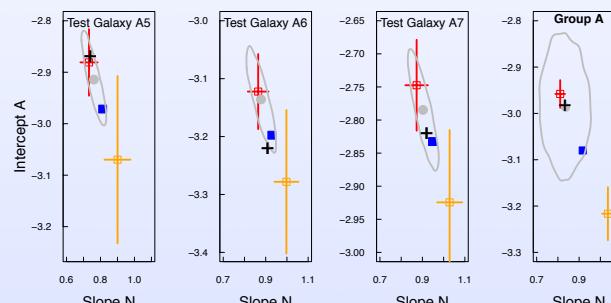
- Monte Carlo methods can account for statistical uncertainties. Bayesian inference is well suited for hierarchical problems, through MCMC methods (Kelly '07, Gelman + '04, Gelman & Hill '07, Kruschke '11)
- Developed and tested Bayesian method, accounting for uncertainties to fit KS parameters of individual galaxies and the population (Shetty + '13, '14)
- Analysis of resolved observations using 7 HERACLES (Leroy + '09, Bigiel + '08) galaxies and 13 STING galaxies (Rahman + '12)

TESTING THE HIERARCHICAL BAYESIAN FIT

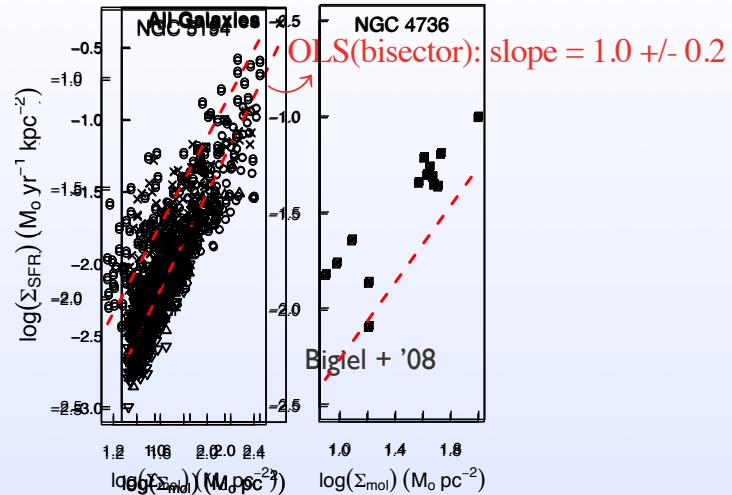
$$\log(\Sigma_{\text{SFR}}) = A + N \log(\Sigma_{\text{mol}}) + \epsilon_{\text{scat}}$$



Subject	True A	True N	True σ_{scat}	Bayes A	Bayes $2\sigma_A$	Bayes N	Bayes $2\sigma_N$	Bayes σ_{scat}
Test Galaxy A1	-2.77	0.72	0.1	-2.79	[-2.9, -2.7]	0.74	[0.64, 0.84]	0.12
Test Galaxy A2	-3.21	0.88	0.1	-3.23	[-3.4, -3.1]	0.86	[0.76, 0.97]	0.12
Test Galaxy A3	-3.18	0.89	0.1	-3.14	[-3.3, -3.0]	0.89	[0.79, 0.99]	0.12
Test Galaxy A4	-2.81	0.78	0.1	-2.91	[-3.0, -2.8]	0.82	[0.72, 0.92]	0.12
Test Galaxy A5	-2.87	0.74	0.1	-2.91	[-3.0, -2.8]	0.76	[0.66, 0.86]	0.12
Test Galaxy A6	-3.22	0.91	0.1	-3.13	[-3.3, -3.0]	0.87	[0.78, 0.98]	0.12
Test Galaxy A7	-2.82	0.92	0.1	-2.78	[-2.9, -2.7]	0.90	[0.80, 1.00]	0.12
Group Parameters ¹	-2.98	0.83	-	-2.99	[-3.2, -2.7]	0.84	[0.65, 1.0]	0.12



The KS Relationship of the Bigiel + '08 Sample

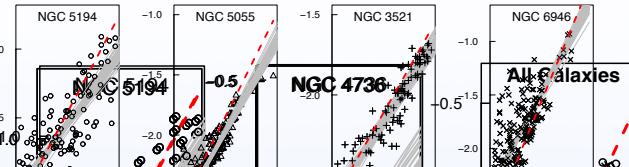


Bigiel + '08

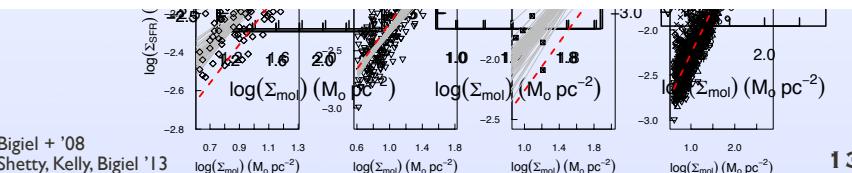
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The KS Relationship of the Bigiel + '08 Sample

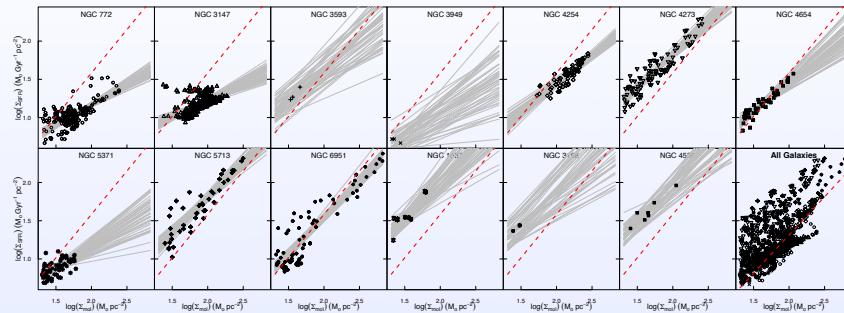
Gray lines:
50 random
draws from
the Bayesian
posterior



Subject	Bayes A	Bayes $2\sigma_A$	Bayes N	Bayes $2\sigma_N$	Bayes σ_{scat}
NGC 5194 (M51)	-2.84	[-3.0, -2.7]	0.72	[0.62, 0.83]	0.06
NGC 5055	-3.20	[-3.3, -3.1]	0.87	[0.79, 0.95]	0.04
NGC 3521	-3.20	[-3.4, -3.0]	0.90	[0.76, 1.03]	0.05
NGC 6946	-2.81	[-2.9, -2.7]	0.78	[0.70, 0.86]	0.11
NGC 628	-2.89	[-3.1, -2.6]	0.76	[0.51, 0.95]	0.05
NGC 3184	-3.24	[-3.4, -3.1]	0.92	[0.79, 1.10]	0.05
NGC 4736	-2.83	[-3.2, -2.4]	0.92	[0.67, 1.20]	0.08
Group Parameters	-3.00	[-3.3, -2.7]	0.84	[0.63, 1.0]	0.14



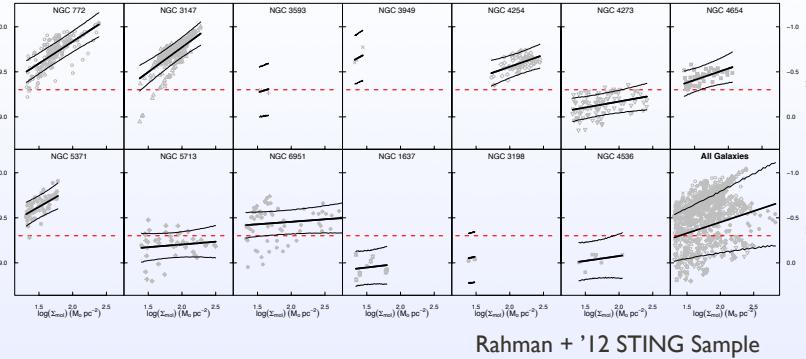
The KS Relationship of the STING Sample



Individual slopes range from 0.42 - 0.95
Mean Slope = 0.76; $2\sigma = [0.58 - 0.94]$

Rahman +'11, '12,
Shetty + '14

Depletion times $\tau_{\text{dep}}^{\text{CO}} = \Sigma_{\text{gas}} / \Sigma_{\text{SFR}}$



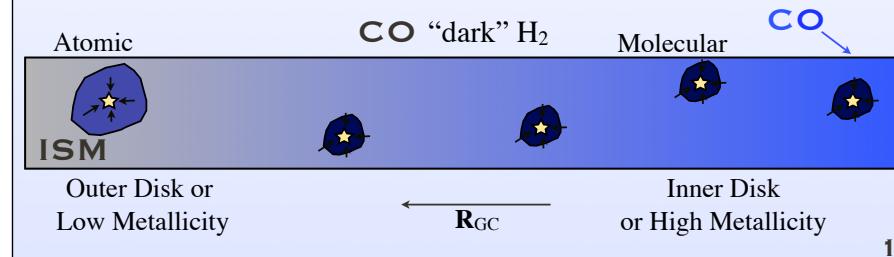
⇒ **No Universal depletion time**
 (Bigiel+’08, Leroy+’09, Schruba+’11, Rahman+’12, etc...)
 ⇒ **2 Gyr not a representative $\tau_{\text{dep}}^{\text{CO}}$, but**
 $\tau_{\text{dep}}^{\text{CO}}$ increases with Σ_{gas} , as traced by CO

Shetty + ’13, ’14a

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Interpreting the variable & sub-linear KS Slope

- No evidence for an “Universal” KS slope: magnetic fields, stellar content, metallicity, molecular gas fraction all affect SF properties of given galaxy
- Significant evidence for sub-linear relationship, for most individual galaxies and for both ensembles: CO tracing some gas that is not associated with star formation?



Diffuse Molecular Gas?

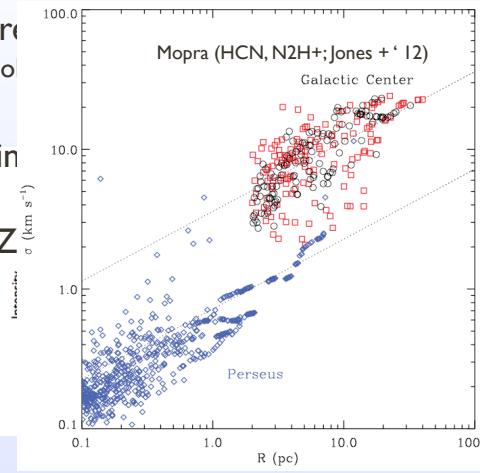
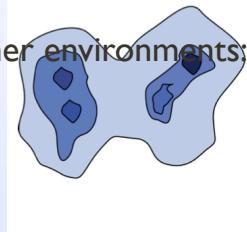
- Presence of non-star forming molecular gas postulated by Elmegreen (1993). Chemistry matters, including metallicity, UV radiation field, ambient density, etc...
- M51 the most sublinear slope (0.72) in Bigiel + '08 sample (see also Blanc + '09): Broad wings in CO suggestive that 50% of emission is from a diffuse molecular component (Pety+ '13, see also Hughes, Meidt, Schinnerer + '13).
- From GRS survey (Jackson + '06), significant fraction of CO luminosity not assigned to 'GMCs'. After accounting for distance ambiguity, quantify the mass fraction...? (Roman-Duval, Clark, RS, Klessen).

Outlook: Quantifying the structure of the ISM

- Other scaling relations, other tracers

- Decomposing the structure of cores: “dendograms” (Rosolowsky et al. 2012)

- Scaling relation: Larson’s law



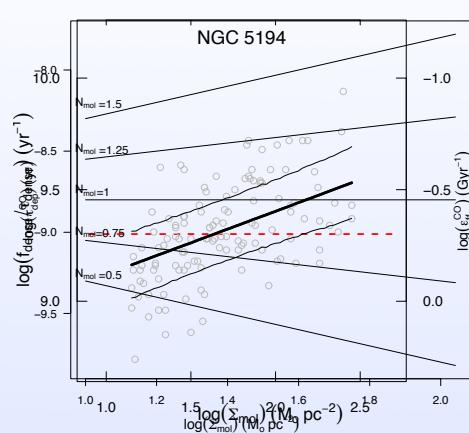
Shetty + '12

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Summary

- Extragalactic observations: 2 datasets evidence a mean sub-linear KS relationship, and sub-linear slopes for most galaxies (Shetty + '13,'14a)
- Implications:
 - T_{dep} = 2 Gyr not representative timescale
 - T_{dep} increases with CO traced surface density
 - indicative of a diffuse CO component? (Shetty + '14b)
- Detailed observations, including various tracers, along with statistical analyses will further our understanding of star formation in the ISM

Variable Depletion Times?

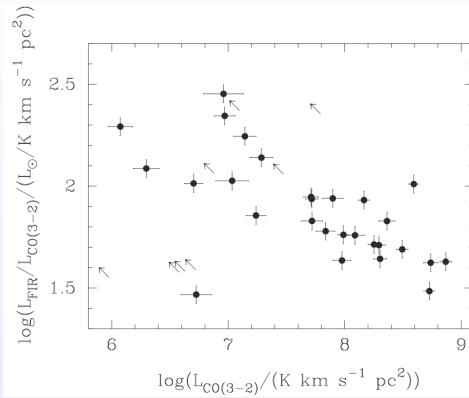


Shetty + '14b, In Prep

- If CO is solely tracing clouds, then clouds have different properties, such as densities or SFRs
- X_{co} varies? X_{co} decreasing with Σ_{mol} . X_{co} - Σ_{mol} relationship must vary between galaxies...
- Presence of diffuse molecular gas, either diffuse (unbound?) clouds, or a pervasive component

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Evidence for diffuse molecular gas



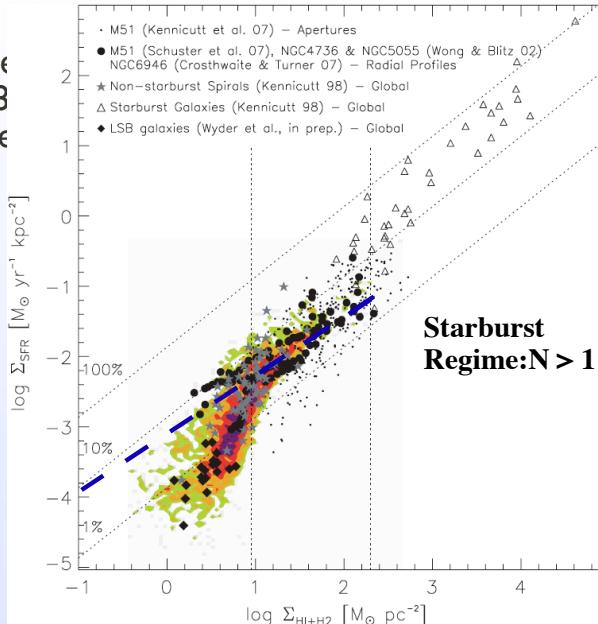
- From CO ($J=3-2$) NGLS, inverse correlations between SF efficiency and molecular gas density
- Higher $^{12}\text{CO}/^{13}\text{CO}$ ratio from unresolved extra-galactic observations compared to Galactic GMCs suggestive of diffuse component (Wilson & Walker '94)

Wilson + '12

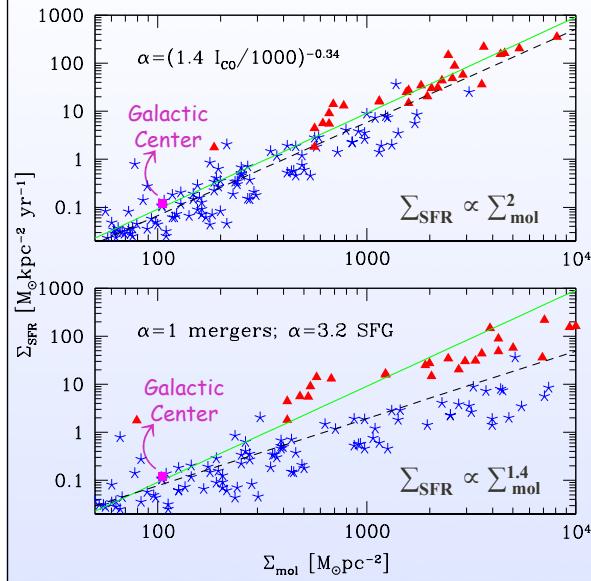
IMPORTANT STARBURST GALACTICAL FITS

- Even without high '08 sample [0.88 relationship (Shetty et al. 2012)]
- By eye fit....?

- Theory of Star Formation Self-Regulation (Ostriker + '10, Ostriker & Shetty '11 Kim et al. '11, '13, Shetty & Ostriker '12)

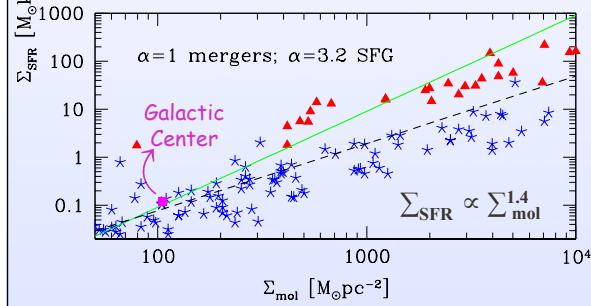


SELF-REGULATION IN OBSERVED SYSTEMS?



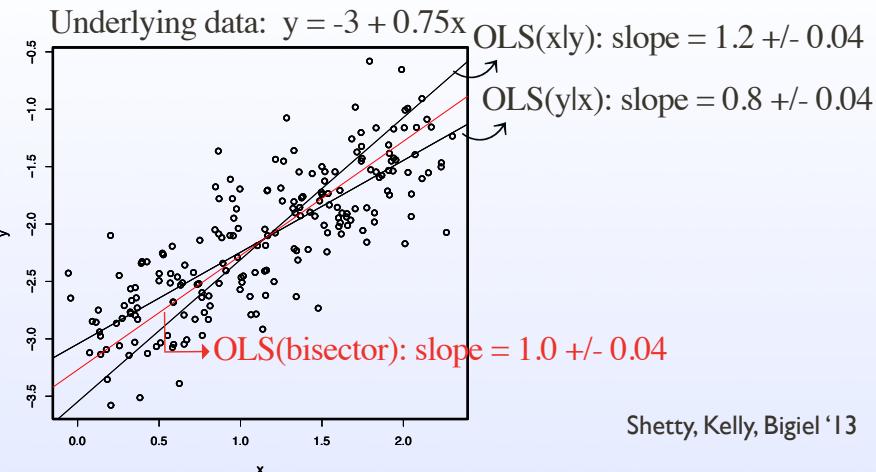
Star forming galaxies
and merger systems
from Genzel + '10

Galactic Center from
Yusef-Zadeh + '09



Continuous X factor?
(Shetty + 11a,b,
Narayanan + '11,'12)

TESTING OLS METHODS



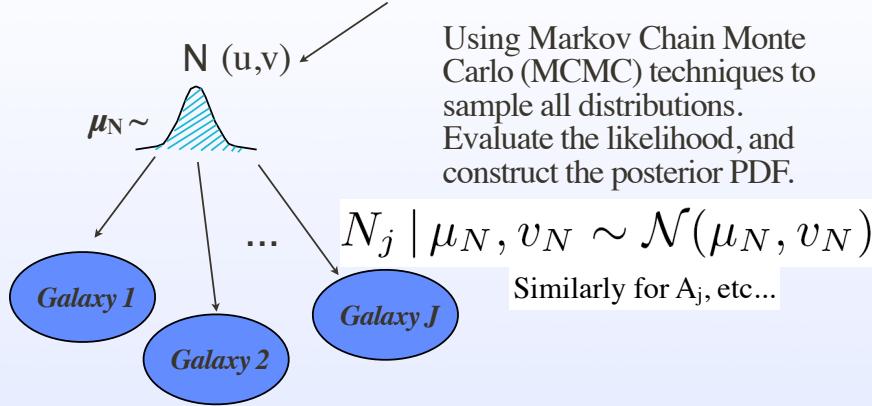
Shetty, Kelly, Bigiel '13

⇒ Bisector does not provide accurate parameter estimates of $y = A + Nx$

⇒ Bisector usually overestimates slope for $N \sim I_{24}$

HIERARCHICAL MODELING

Additional level for population parameters



Using Markov Chain Monte Carlo (MCMC) techniques to sample all distributions. Evaluate the likelihood, and construct the posterior PDF.

$$\log \Sigma_{\text{SFR},ij} | A_j, N_j, \Sigma_{\text{mol},ij}, \sigma_{\text{scat},j}^2 \sim \\ \mathcal{N}(A_j + N_j \log \Sigma_{\text{mol},ij}, \sigma_{\text{scat},j}^2)$$

Caveats

- Diffuse emission affecting SFR? (Kennicutt + '07, Liu + '11)
- Conversion factors...?
 - e.g. X factor, old stellar population, IMF...?
 - Correlations b/w parameters (Shetty, Kelly, Bigiel '13)?
- slope and scatter depend on scale
 - Schruba + '11, Kruijssen & Longmore '13
- Single dish for STING (checked NGC 4254 in Shetty + '13b)

INPUT/OUTPUT OF A HIERARCHICAL BAYESIAN FIT

