

CTA OZ CONSORTIUM 2017

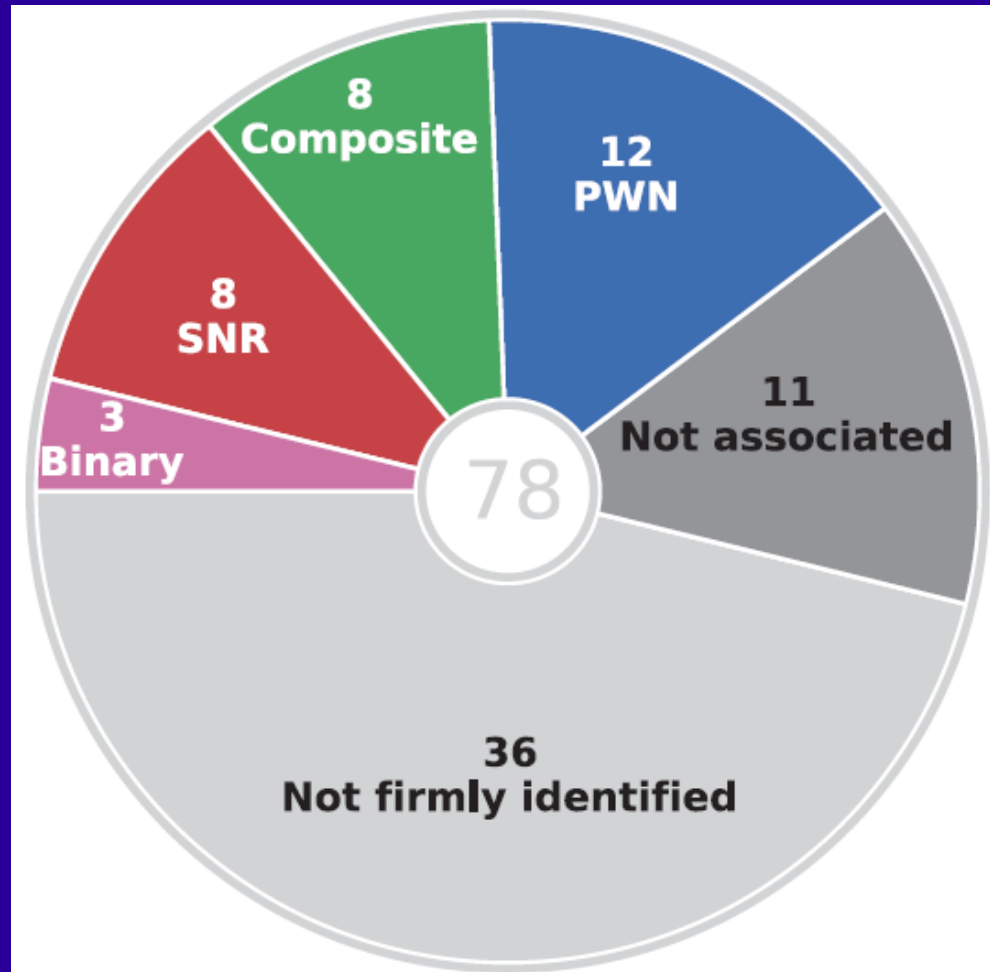


Modeling of TeV emission from propagating CRs and electrons

Fabien Voisin



UNIDENTIFIED TeV SOURCE (1)

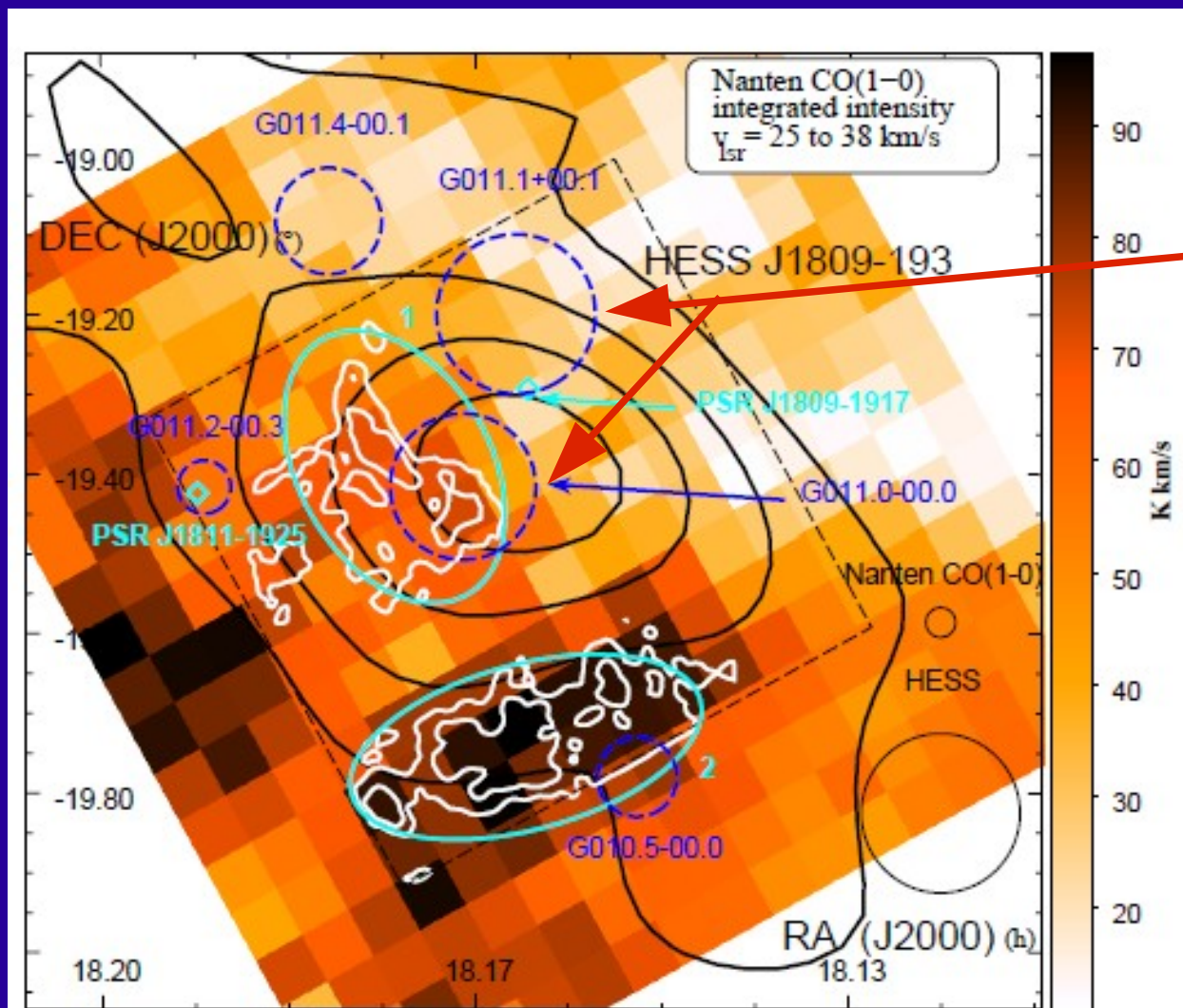


→ A large number of unidentified TeV sources :

- Dark sources (e.g HESS J1616-518, see James talk)
- TeV sources with multiple accelerators possibly contributing to the TeV source

Number of TeV sources detected by HESS
(Donath et al, 2017)

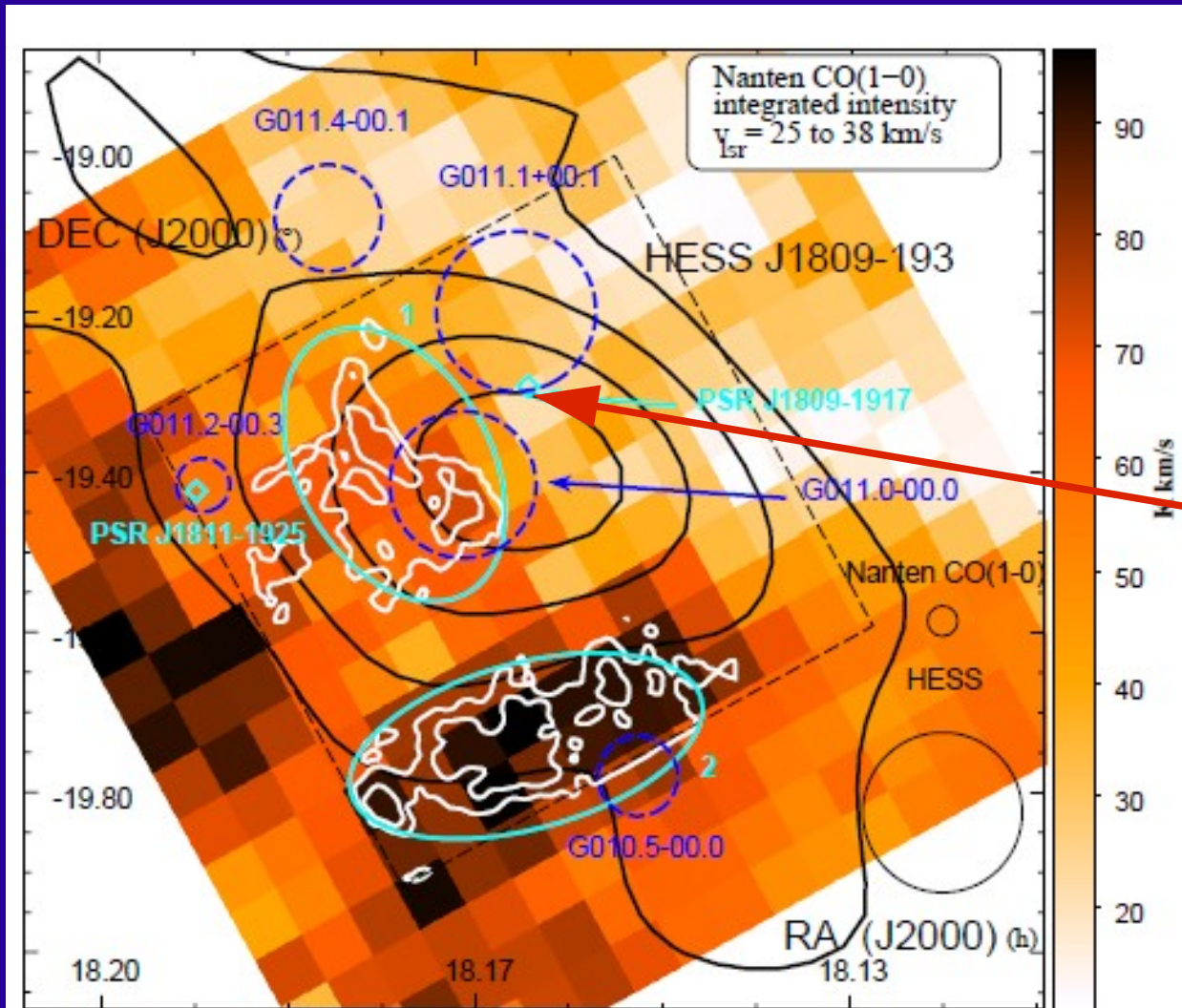
UNIDENTIFIED TeV SOURCE (2) HESS J1809-193



Overlapping accelerators :

→ 2 SNRs **G011.0-00.0**
G011.1+00.1
(no info on age or distance)

UNIDENTIFIED TeV SOURCE (2) HESS J1809-193



Overlapping accelerators :

→ 2 SNRs **G011.0-00.0**
G011.1+00.1
(no info on age or distance)

→ 1 PWNe powered by
PSR J1809-1917 :
 $\dot{E}_{SD} = 1.8 \times 10^{36}$ erg/s
 $d = 3.7$ kpc
 $\tau = 51$ kyr

(see James 's talk for
more detail)

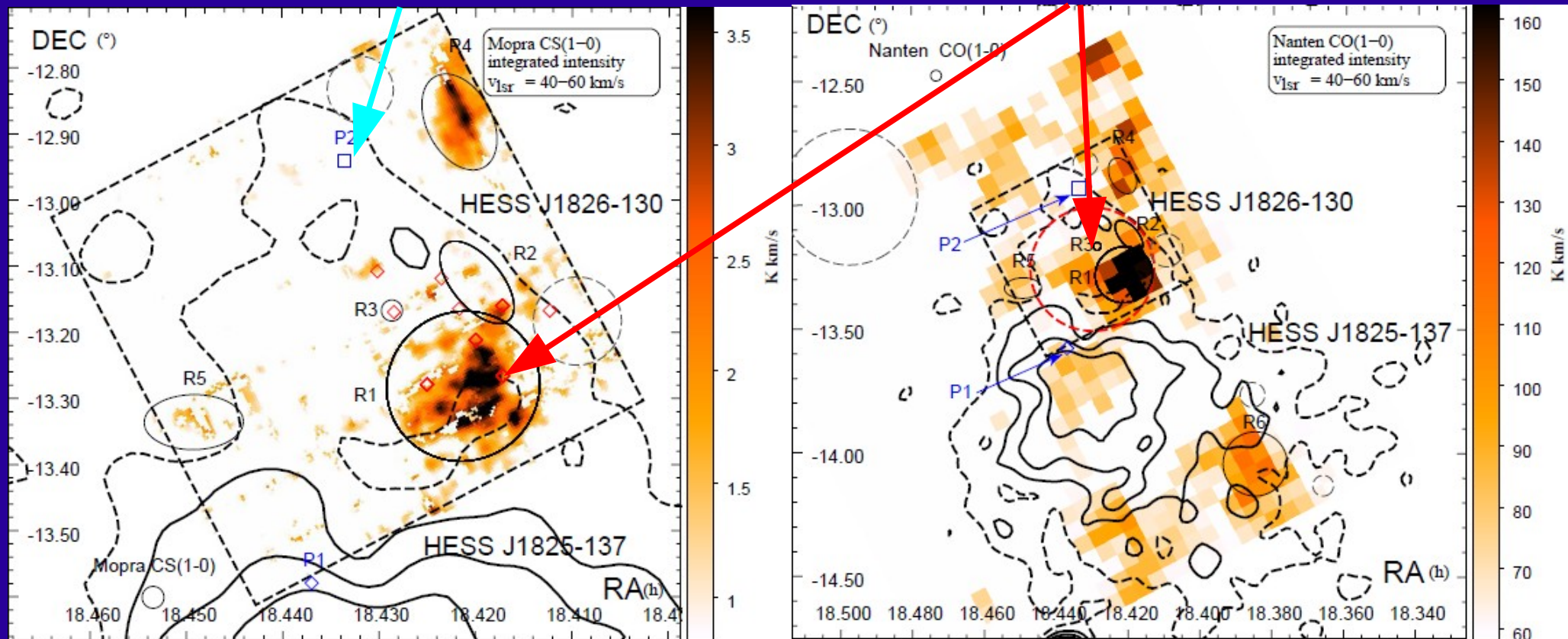
=> NEED TO STUDY THE CONTRIBUTION OF EACH ACCELERATOR

UNIDENTIFIED TeV SOURCE (3) HESS J1826-130

(See Voisin et al, 2016,
Anguner et al, 2017
And references therein)

PWN G18.4-0.5 powered by radio quiet
gamma-ray pulsar **PSR J1826-1256 (P2)**
=> **Leptonic γ -rays** from IC radiation ?

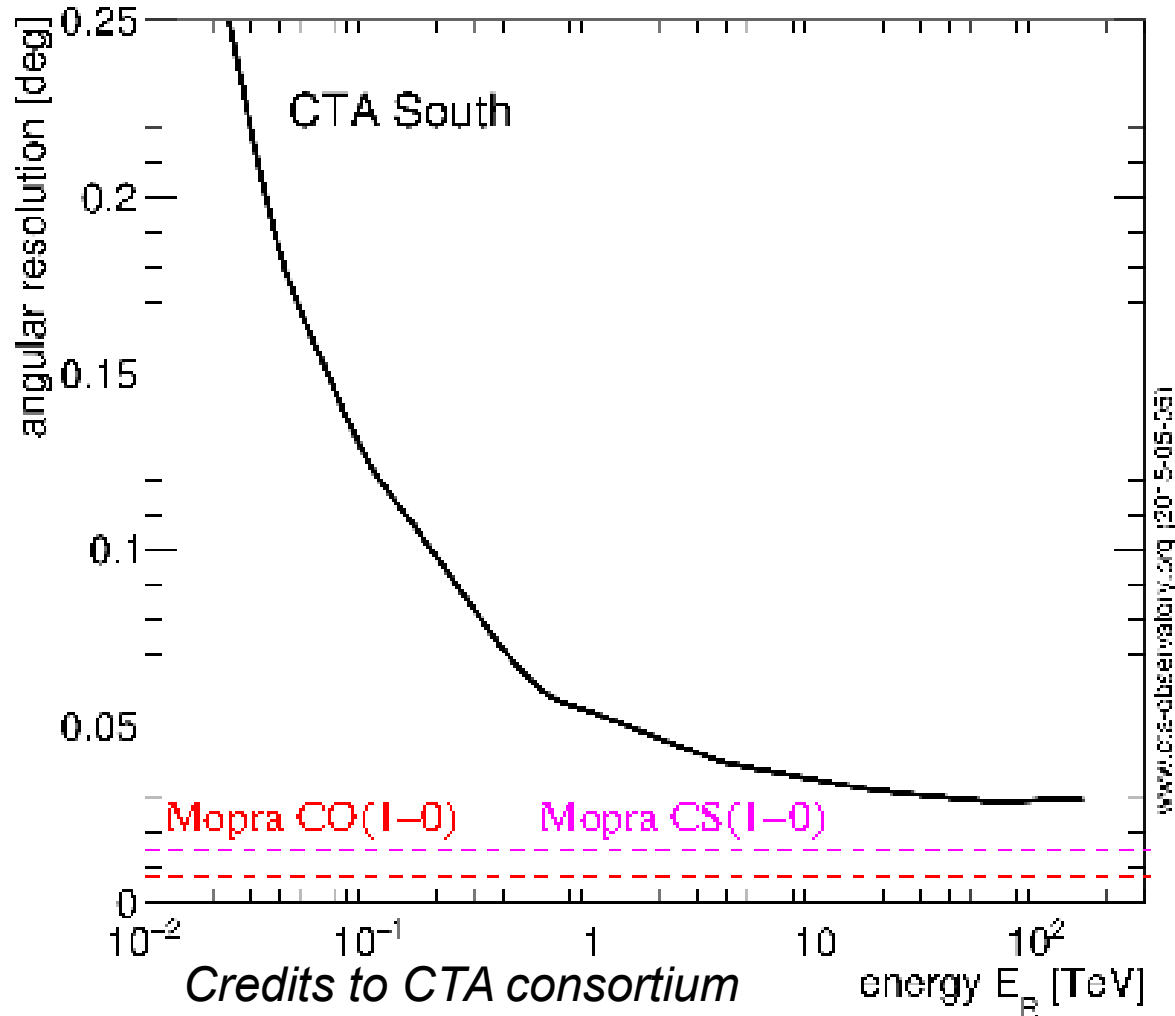
Overlapping **dense molecular clouds**
associated with HESS J1825-137 at d~4 kpc
=> **Hadronic γ -rays** from CRs escaping
progenitor SNR of HESS J1825-137 ?



**=> CONFUSION IN DETERMINING THE CONTRIBUTION
FROM EACH HIGH ENERGY SOURCE**

CTA PERFORMANCE

→ A factor of **10**
better sensitivity
compared to HESS



CTA beam size at 10 TeV :

$$\rightarrow \theta_{68} [10 \text{ TeV}] \sim 0.035^\circ$$

Comparable with Mopra
data :

$$\theta_{68} [\text{CS}(1-0)] \sim 0.016^\circ$$

$$\theta_{68} [\text{CO}(1-0)] \sim 0.008^\circ$$

=> Study the influence of the structure of molecular clouds on the morphology of the TeV emission

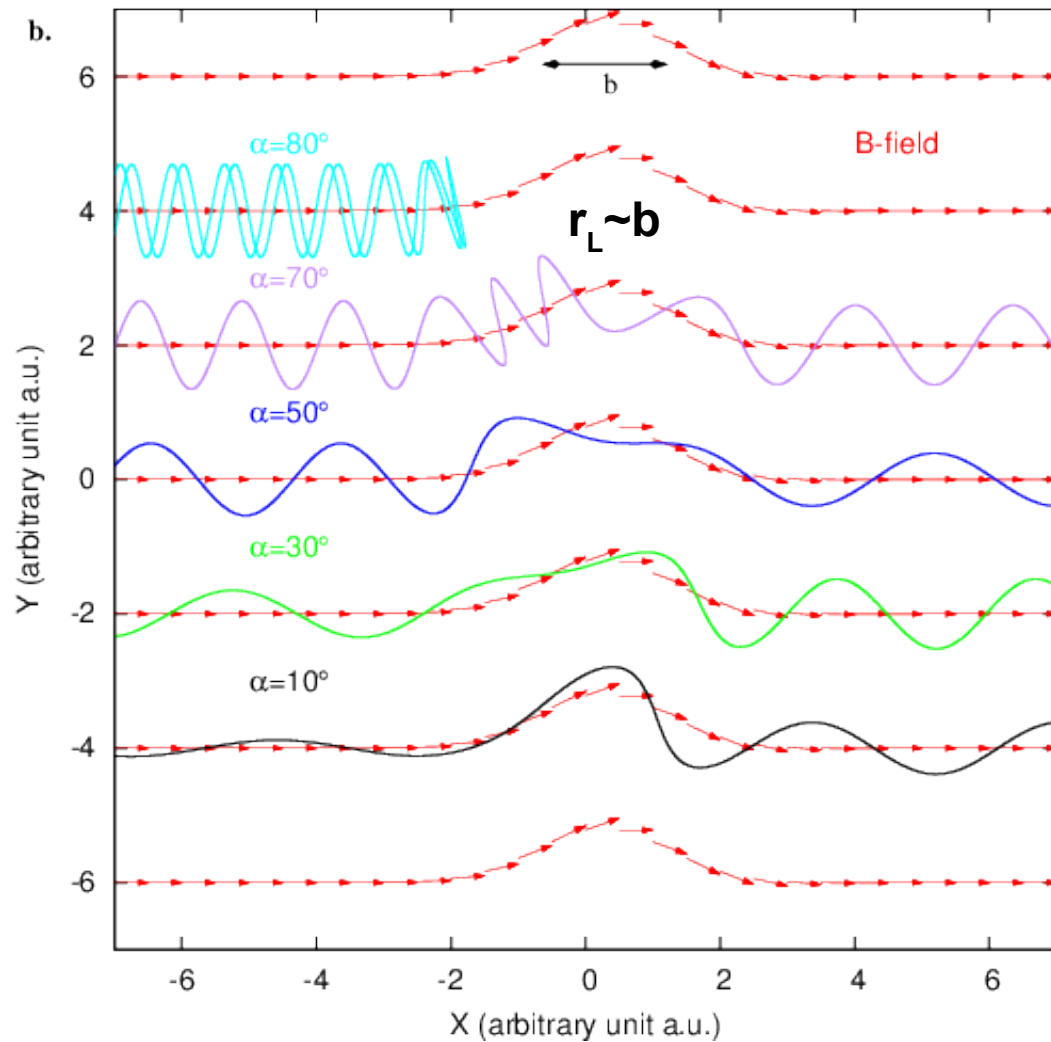
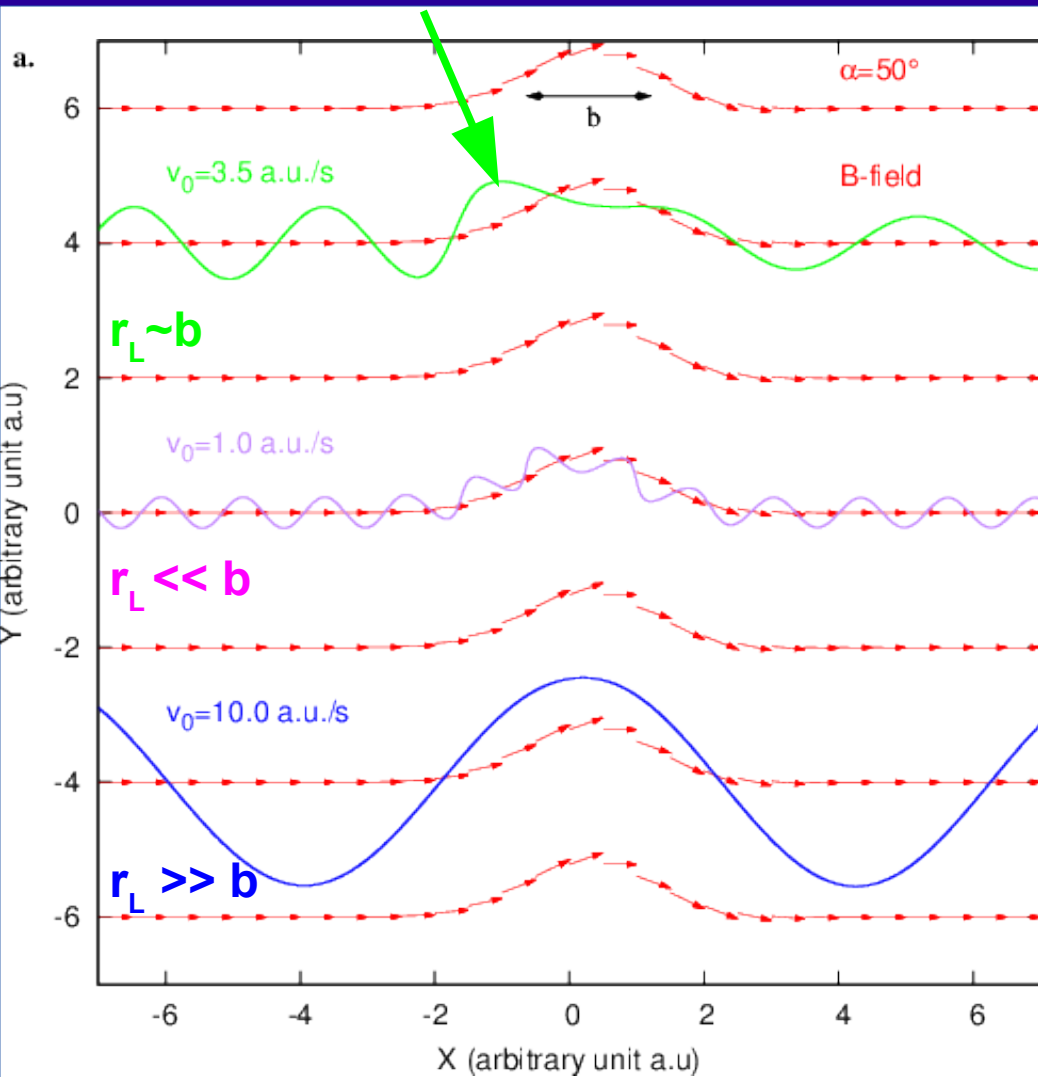
MOTIVATION

- Study the effects of molecular clouds on the propagation of CRs and high energy electrons escaping **impulsive/continuous** energy sources.
- Predict key spectral and morphological features in the hadronic/leptonic TeV gamma-ray emission that could be detected by CTA.
- Identify high energy sources that could be detected by CTA
- Disentangle TeV sources with multiple associations (e.g HESS J1809-193)

CR Diffusion physics (1)

$r_L = \gamma mc^2 / (ZeBc) \rightarrow$ Larmor radius

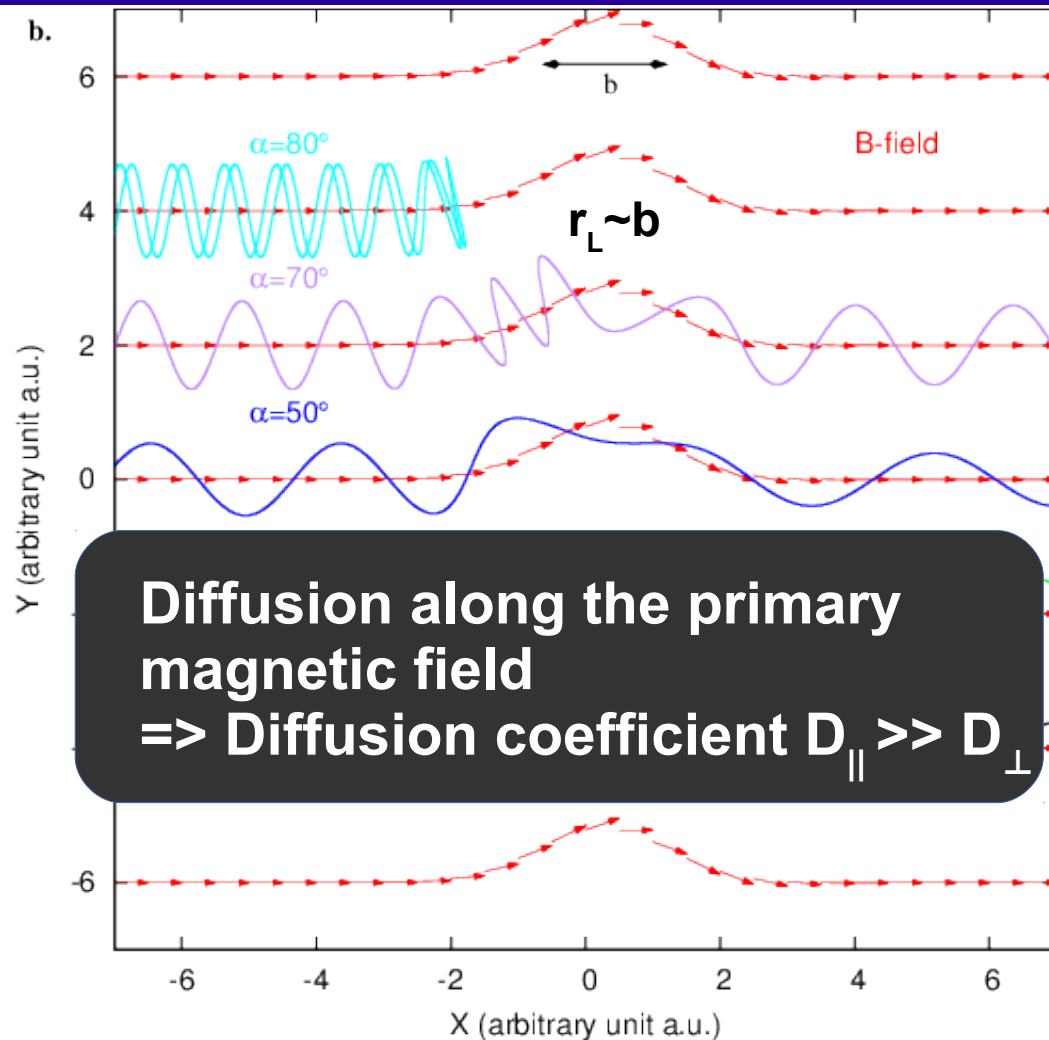
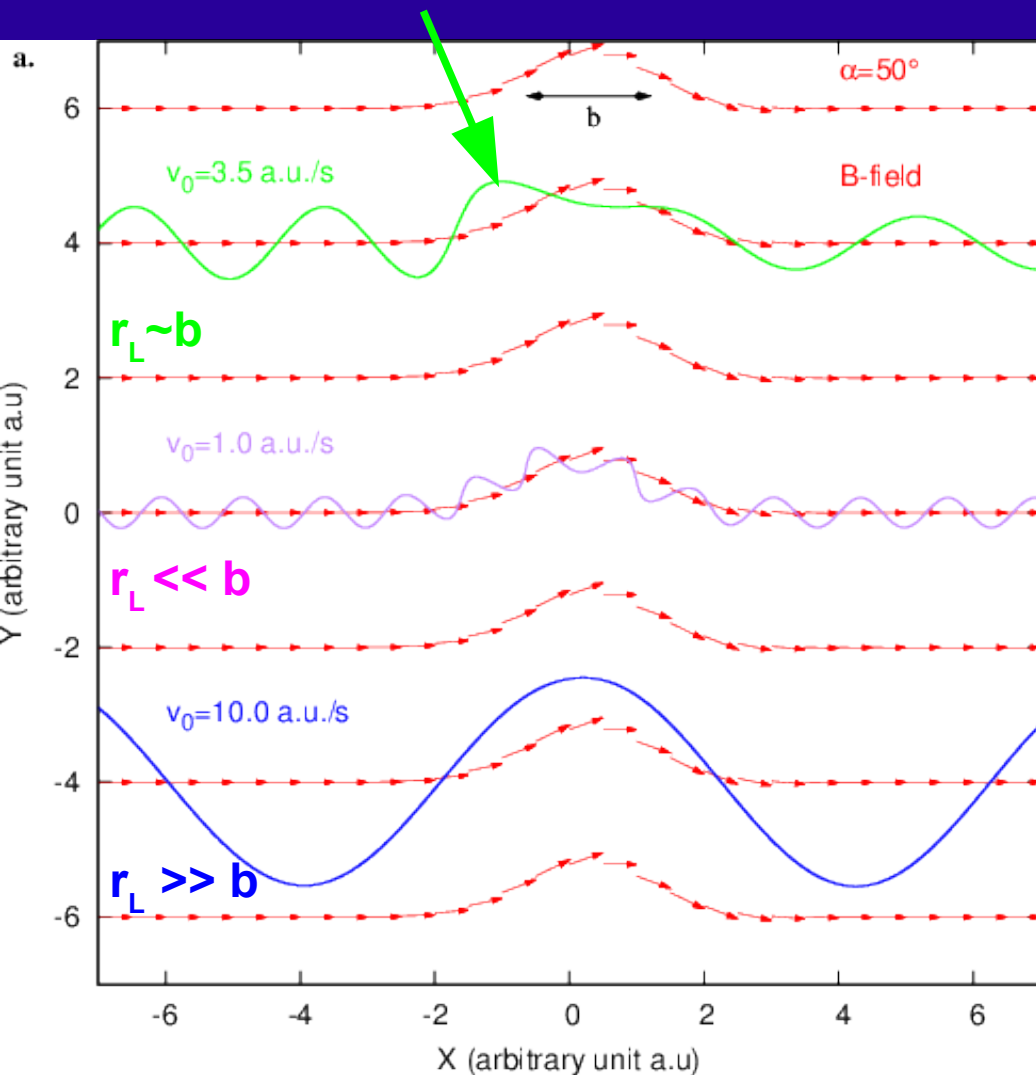
Efficient scattering of the particle trajectory only if $r_L \sim b$ $\delta B_y \ll B_0$ with scale b



CR Diffusion physics (1)

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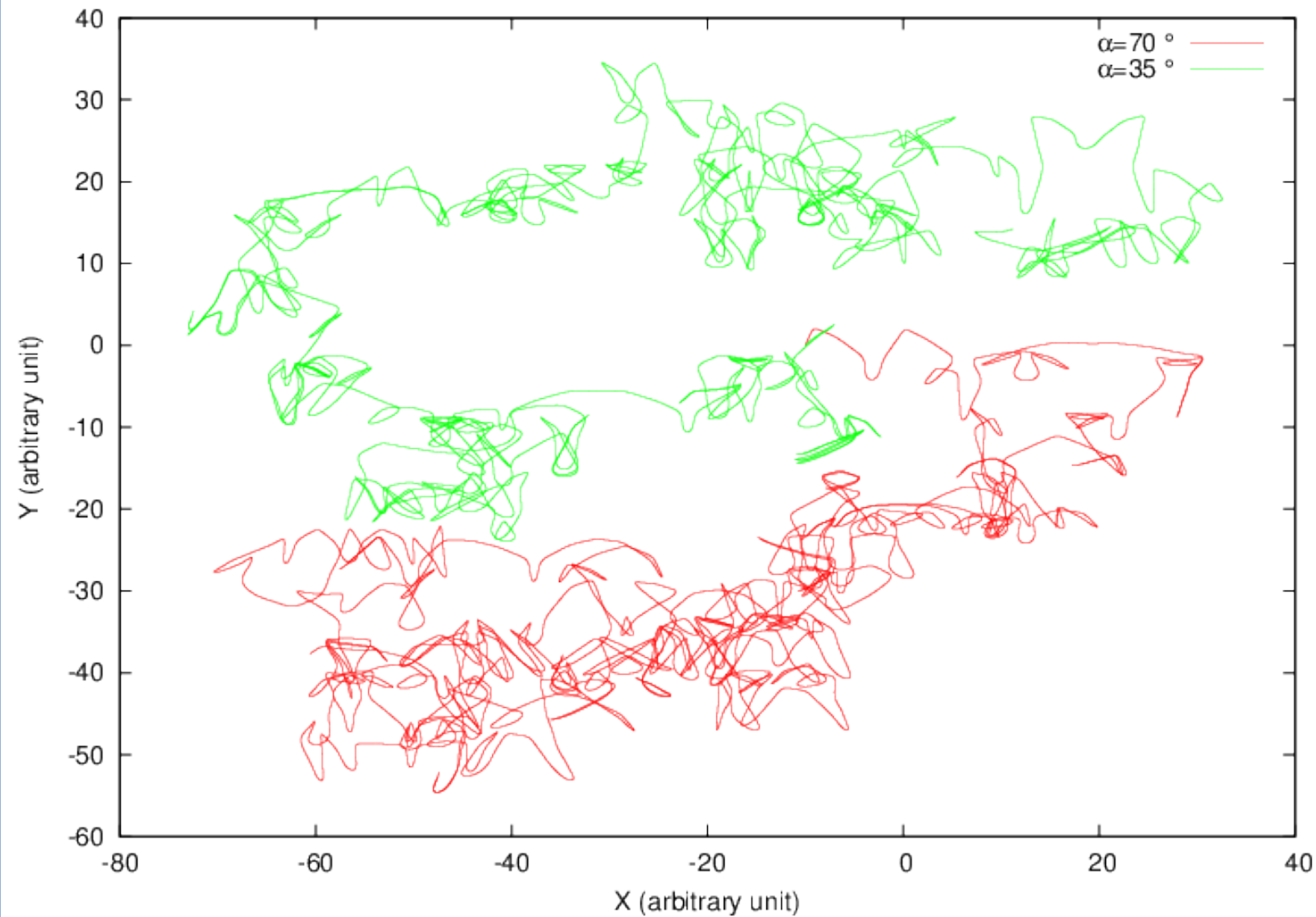
Efficient scattering of the particle trajectory only if $r_L \sim b$ $\delta B_y \ll B_0$ with scale b



Diffusion along the primary magnetic field
 \Rightarrow Diffusion coefficient $D_{\parallel} \gg D_{\perp}$

CR Diffusion physics (2)

In the case where $\delta B \sim B \Rightarrow$ ISOTROPIC DIFFUSION OF CRs



→ Random walk propagation

→ $D_{xx} \sim D_{yy} \sim D_{zz}$

CR Diffusion physics (3)

=> Diffusion of CRs dependent on the magnetic turbulence

- **Shocks (e.g SNRs) can produce these turbulence**
- **Turbulence caused by precursors CRs (Skilling et al,1975)**

Magnetic turbulence can be described as a combination of wave functions with wavenumber $k=2\pi/b$

$$\delta\mathbf{B}(k) \propto \exp(i\mathbf{k}\cdot\mathbf{x})$$

Power-law turbulence distribution

$$I(k) \propto k^{-s}$$

- **$s=5/3$ (Kolmogorov spectrum) $\rightarrow D(\gamma) \propto \gamma^{1/3}$**
- **$s=3/2$ (Kraichnan spectrum) $\rightarrow D(\gamma) \propto \gamma^{1/2}$**
- **Bohm diffusion $\rightarrow D(\gamma) \propto \gamma$**

CR Diffusion physics (4) : Transport equation

$n=n(\gamma,r,t)=dn/d\gamma \rightarrow$ energy density distribution of CRs/high energy electrons

General equation :

$$\begin{aligned} \frac{\partial n}{\partial t} = & -\nabla \cdot (n\mathbf{v}_A) - \nabla \cdot (\overline{\overline{D}} \cdot \nabla n) + \frac{\partial}{\partial \gamma} \left(\dot{\gamma} n - \frac{\gamma}{3} (\nabla \cdot \mathbf{v}_A) n \right) \\ & + \frac{\partial}{\partial \gamma} \left(\gamma^2 D_{\gamma\gamma} \frac{\partial}{\partial \gamma} \left(\frac{n}{\gamma^2} \right) \right) + S(\gamma, \mathbf{r}, t) \end{aligned}$$

$\overline{\overline{D}} \equiv \overline{\overline{D}}(x,y,z,\gamma) \rightarrow$ Diffusion coefficient tensor

$\dot{\gamma}(\gamma) \rightarrow$ Energy loss rate of a CR/high energy electron with Lorentz factor γ (Synchrotron , IC, Bremsstrahlung, p-p interaction)

$\mathbf{v}_A \rightarrow$ Advection speed (e.g jets)

$D_{\gamma\gamma} \rightarrow$ Diffusion in energy space (e.g 2nd order reacceleration)

CR Diffusion physics (4) : Transport equation

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General equation :

$$\frac{\partial n}{\partial t} = \cancel{-\nabla \cdot (n\mathbf{v}_A)} - \nabla \cdot (\overline{\overline{D}} \cdot \nabla n) + \frac{\partial}{\partial \gamma} \left(\dot{\gamma} n - \cancel{\frac{\gamma}{3} (\nabla \cdot \mathbf{v}_A)} \right) + \cancel{\frac{\partial}{\partial \gamma} \left(\gamma^2 D_{\gamma\gamma} \frac{\partial}{\partial \gamma} \left(\frac{n}{\gamma^2} \right) \right)} + S(\gamma, \mathbf{r}, t)$$

\rightarrow In our code, **advection term**, **adiabatic losses** and **2nd order reacceleration** of CRs/high energy electrons are NEGLECTED

\rightarrow We also assume the diffusion to be isotropic $\overline{\overline{D}}(\mathbf{x}, \mathbf{y}, \mathbf{z}, \gamma) = D(\mathbf{x}, \mathbf{y}, \mathbf{z}, \gamma)$

\rightarrow In my numerical code I therefore solve :

$$\frac{\partial n}{\partial t} = -\nabla \cdot (D(\mathbf{r}, \gamma) \cdot \nabla n) + \frac{\partial}{\partial \gamma} (\dot{\gamma} n) + S(\gamma, \mathbf{r}, t)$$

MODELING THE GAMMA-RAY EMISSION

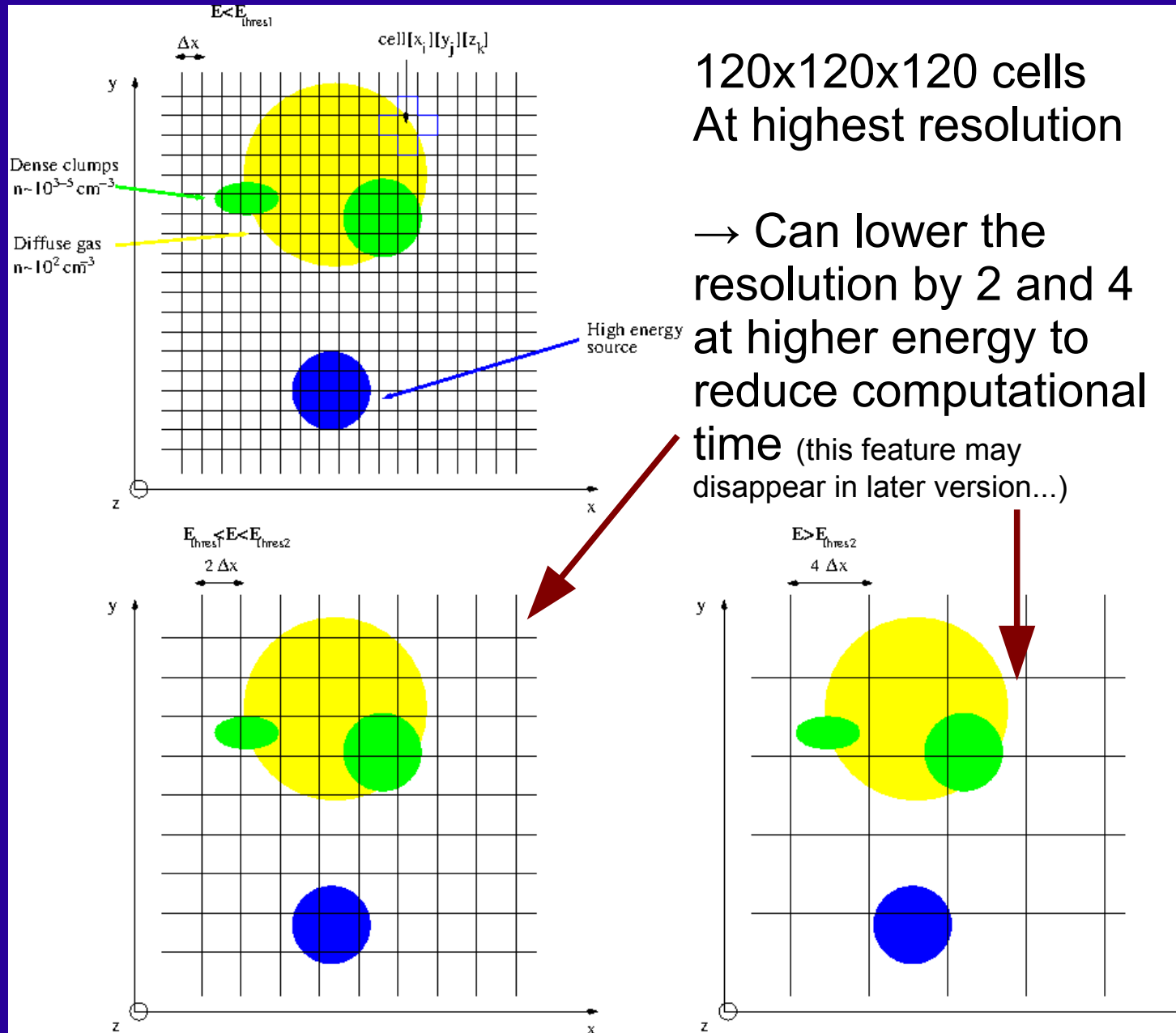
DISCLAIMER

NUMERICAL CODES COMPUTING THE GAMMA-RAY EMISSION FROM THE PROPAGATION OF CRs IN OUR GALAXY ALREADY EXIST !

- GALPROP (see Troy's talk) : Model the CR distribution propagating across our Galaxy and the background gamma-ray emission. → Very important for detections of GeV sources with Fermi (*Strong and Moskalenko 1998* for introduction paper)
- PICARD (*Kissman et al 2014*)

MY MODELING CODE IS AIMING AT STUDYING THE GAMMA-RAY EMISSION ON A MORE LOCAL LEVEL

HOW THE NUMERICAL CODE WORK



1/ Define a template 3D distribution of the **diffuse** and **dense molecular gas** in the region based on our **CO(J=1-0)** and **CS(J=1-0)** surveys

2/ Define the property of the **high energy source** :

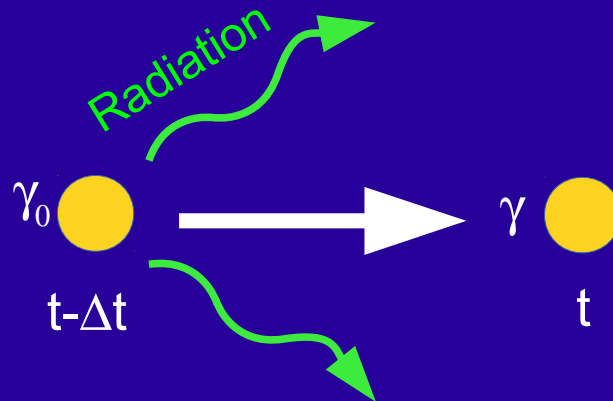
- Impulsive
- Continuous
- Power-law (cutoff)
- Broken power-law (cutoff)

HOW THE NUMERICAL CODE WORK (2)

3/ For each Δt , solve the discretized equation in each cells:

$$n \left| \begin{array}{l} \gamma \\ t \\ x, y, z \end{array} \right. = \sum_{i=x,y,z} \left[\frac{\dot{\gamma}_0}{\dot{\gamma}} D \left| \begin{array}{l} \gamma_0 \\ t - \Delta t \\ i + \Delta i/2 \end{array} \right. \left(n \left| \begin{array}{l} \gamma_0 \\ t - \Delta t \\ i + \Delta i \end{array} \right. - n \left| \begin{array}{l} \gamma_0 \\ t - \Delta t \\ i \end{array} \right. \right) \right. \\ \left. + \frac{\dot{\gamma}'_0}{\dot{\gamma}} D \left| \begin{array}{l} \gamma'_0 \\ t - \Delta t \\ i - \Delta i/2 \end{array} \right. \left(n \left| \begin{array}{l} \gamma'_0 \\ t - \Delta t \\ i - \Delta i \end{array} \right. - n \left| \begin{array}{l} \gamma'_0 \\ t - \Delta t \\ i \end{array} \right. \right) \right]$$

$\gamma_0, \dot{\gamma}_0 \rightarrow$ Lorentz factor
and cooling rate at
time $t - \Delta t$



$\gamma, \dot{\gamma} \rightarrow$ Lorentz factor
and cooling rate at
time t

HOW THE NUMERICAL CODE WORK (3)

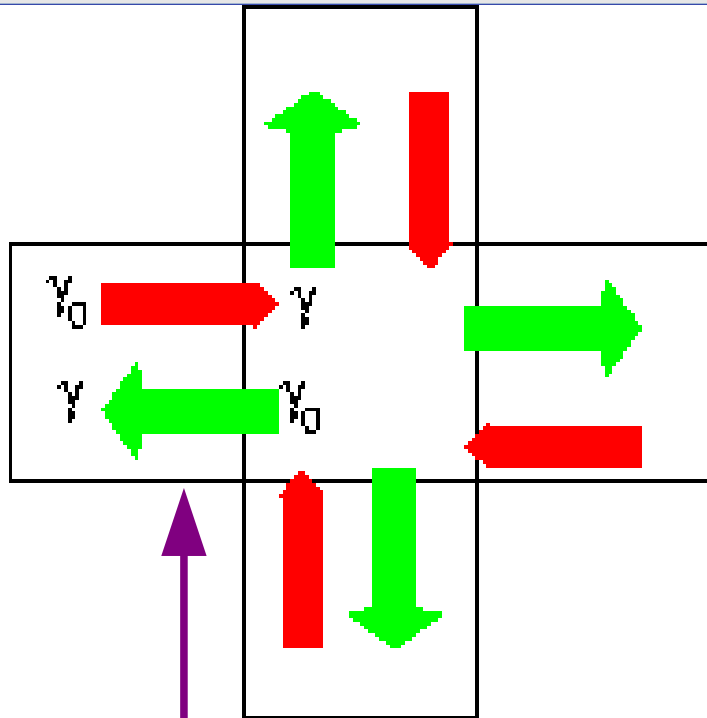
3/ For each Δt , solve the discretized equation in each cells:

$$n \left| \begin{array}{c} \gamma \\ t \\ x, y, z \end{array} \right. = \sum_{i=x,y,z} \left[\frac{\dot{\gamma}_0}{\dot{\gamma}} D \left| \begin{array}{c} \gamma_0 \\ t - \Delta t \\ i + \Delta i/2 \end{array} \right. \left(n \left| \begin{array}{c} \gamma_0 \\ t - \Delta t \\ i + \Delta i \end{array} \right. - n \left| \begin{array}{c} \gamma_0 \\ t - \Delta t \\ i \end{array} \right. \right) \right. \\ \left. + \frac{\dot{\gamma}'_0}{\dot{\gamma}} D \left| \begin{array}{c} \gamma'_0 \\ t - \Delta t \\ i - \Delta i/2 \end{array} \right. \left(n \left| \begin{array}{c} \gamma'_0 \\ t - \Delta t \\ i - \Delta i \end{array} \right. - n \left| \begin{array}{c} \gamma'_0 \\ t - \Delta t \\ i \end{array} \right. \right) \right]$$

$D \equiv (\Delta t / \Delta x^2) D(\gamma) \rightarrow$ UNITLESS DIFFUSION COEFFICIENT

\rightarrow Fraction of the density transferred from one cell to another

HOW THE NUMERICAL CODE WORK (3)



Assumed Diffusion coefficient *Gabici et al (2006)*

$$D(\gamma) = 3 \times 10^{27} \chi (\gamma mc^2 / 1 \text{ GeV})^{1/2} (B / 3 \mu\text{G})^{-1/2}$$

$\chi \equiv$ suppression factor $\sim 0.01-0.1$

see *Protheroe et al (2008), Gabici et al (2010)*

Crutcher (2010) relation B vs n_H in dense clouds

$$B = \begin{cases} 10 \left(\frac{n_H}{300 \text{ cm}^{-3}} \right)^{0.65} \mu\text{G} & \text{for } n_H \geq 300 \text{ cm}^{-3} \\ 10 \mu\text{G} & \text{for } n_H < 300 \text{ cm}^{-3} \end{cases}$$

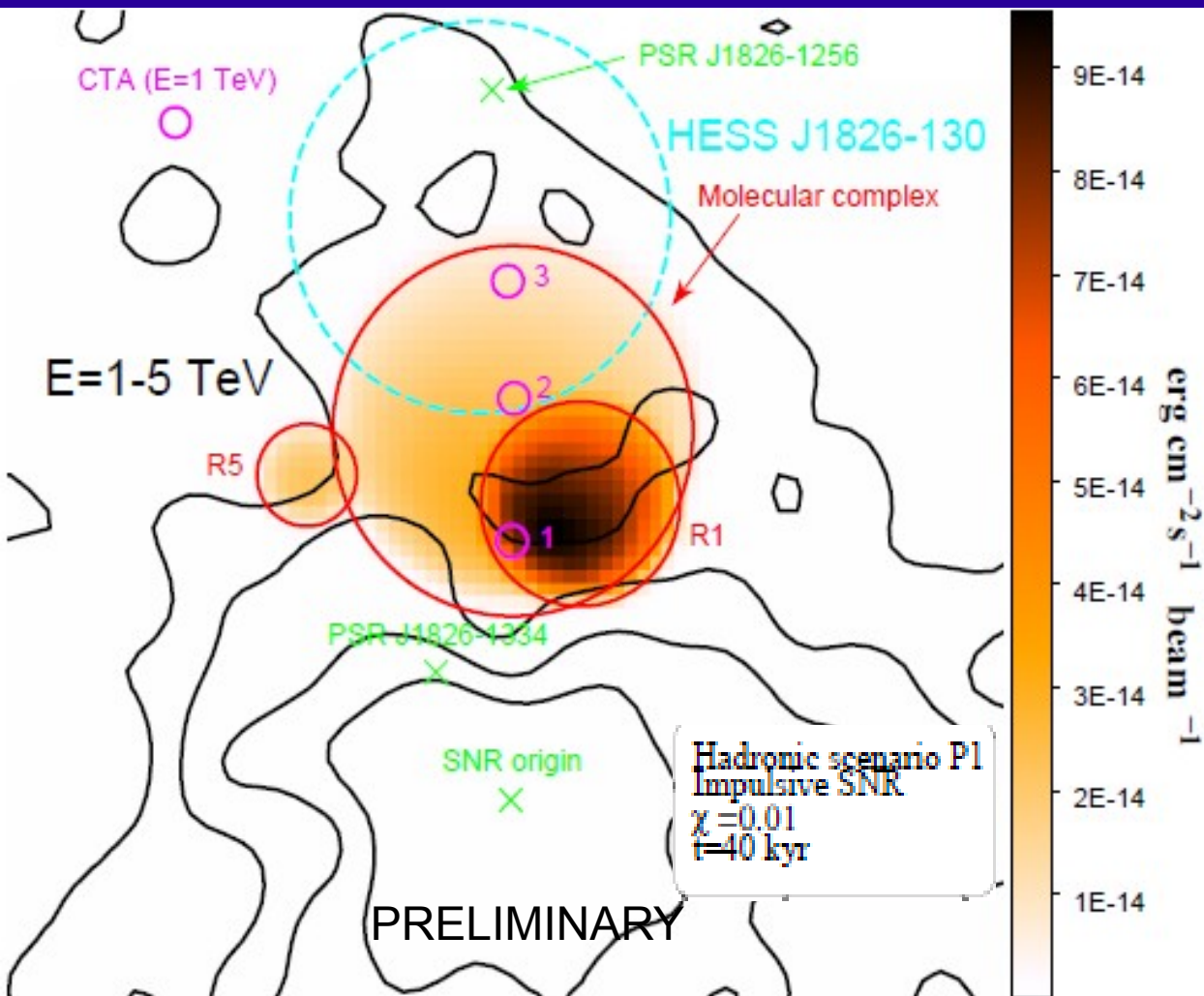
Particle density transfer between cells (left and central grid) :

$$\leftarrow n(\text{cell}[x_i][y_j][z_k], \gamma_0) \frac{\dot{\gamma}_a}{\dot{\gamma}} \frac{D(\text{cell}[x_i][y_j][z_k]) + D(\text{cell}[x_{i-1}][y_j][z_k])}{2} \frac{\Delta t}{\Delta x^2}$$

$$\rightarrow n(\text{cell}[x_{i-1}][y_j][z_k], \gamma_0) \frac{\dot{\gamma}_a}{\dot{\gamma}} \frac{D(\text{cell}[x_i][y_j][z_k]) + D(\text{cell}[x_{i-1}][y_j][z_k])}{2} \frac{\Delta t}{\Delta x^2}$$

RESULTS DISPLAY

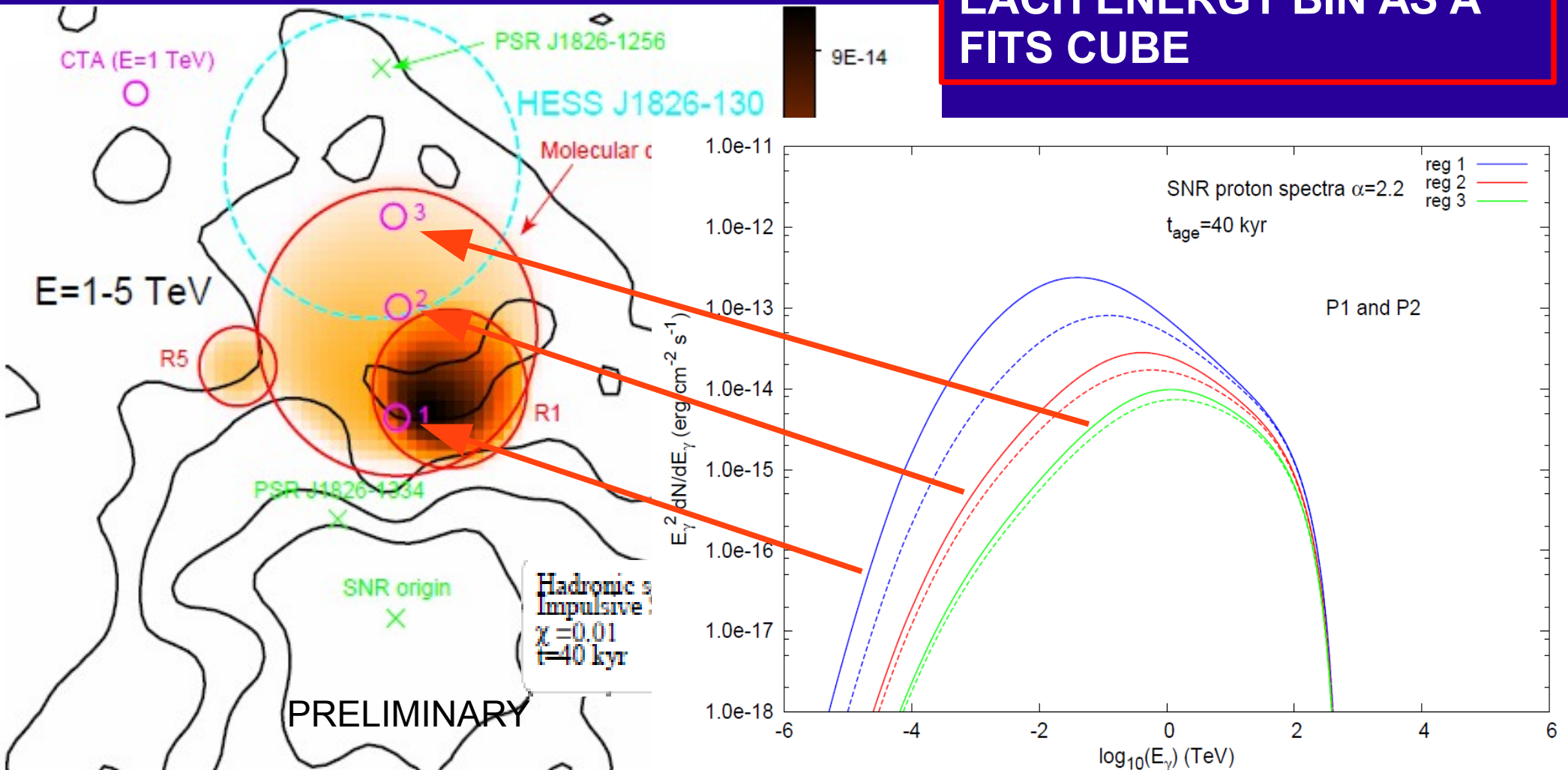
→ OUTPUTS THE GAMMA-RAY INTENSITY AT EACH POSITION AND EACH ENERGY BIN AS A FITS CUBE



→ Hadronic scenario :
Gamma-rays overlapping with
The molecular clouds at 4 kpc

RESULTS DISPLAY

→ **OUTPUTS THE GAMMA-RAY INTENSITY AT EACH POSITION AND EACH ENERGY BIN AS A FITS CUBE**

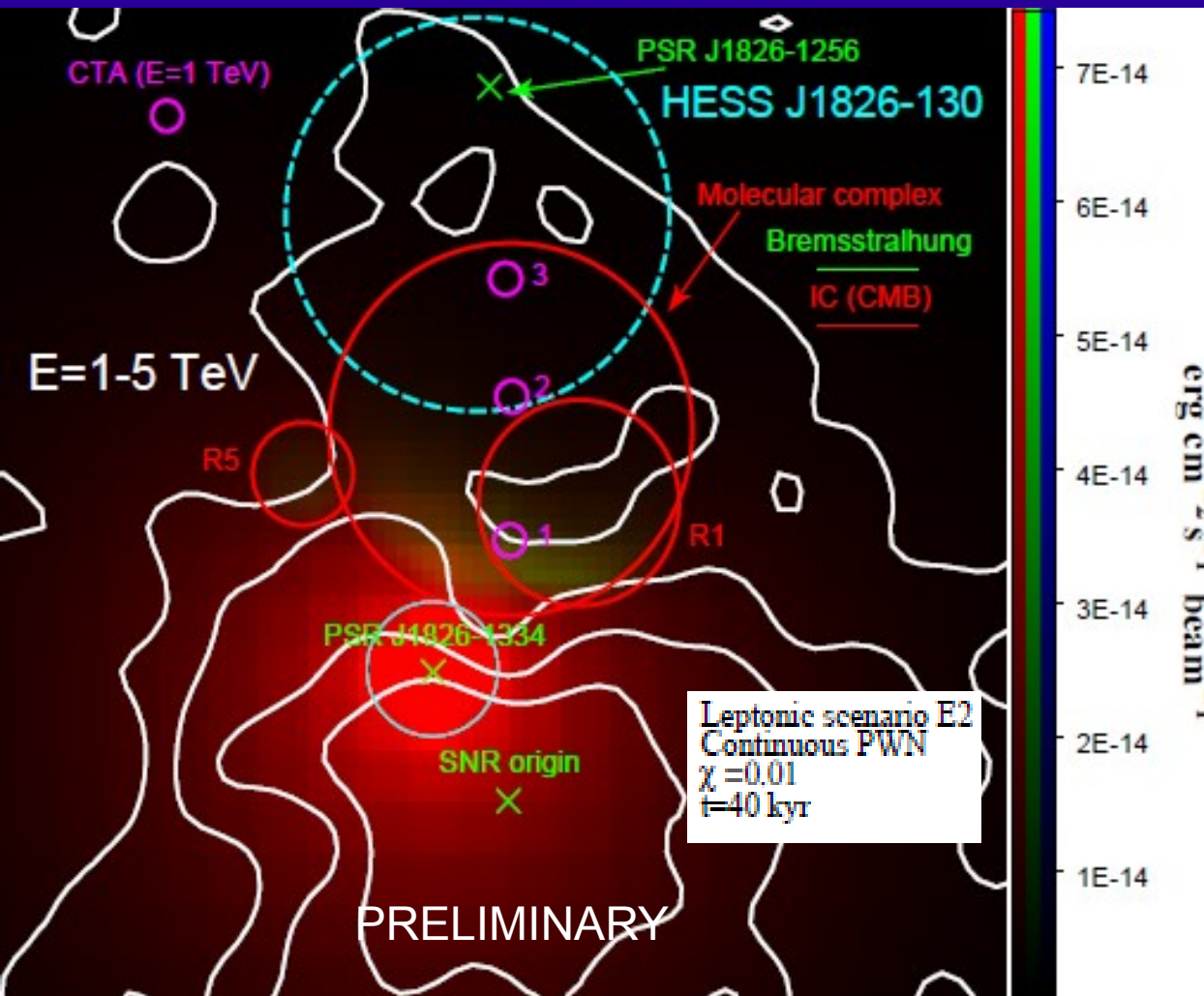


→ Hadronic scenario :
Gamma-rays overlapping with
The molecular clouds at 4 kpc

→ **Hardening** of the gamma-ray SED
expected as we move away from the
SNR

RESULTS DISPLAY

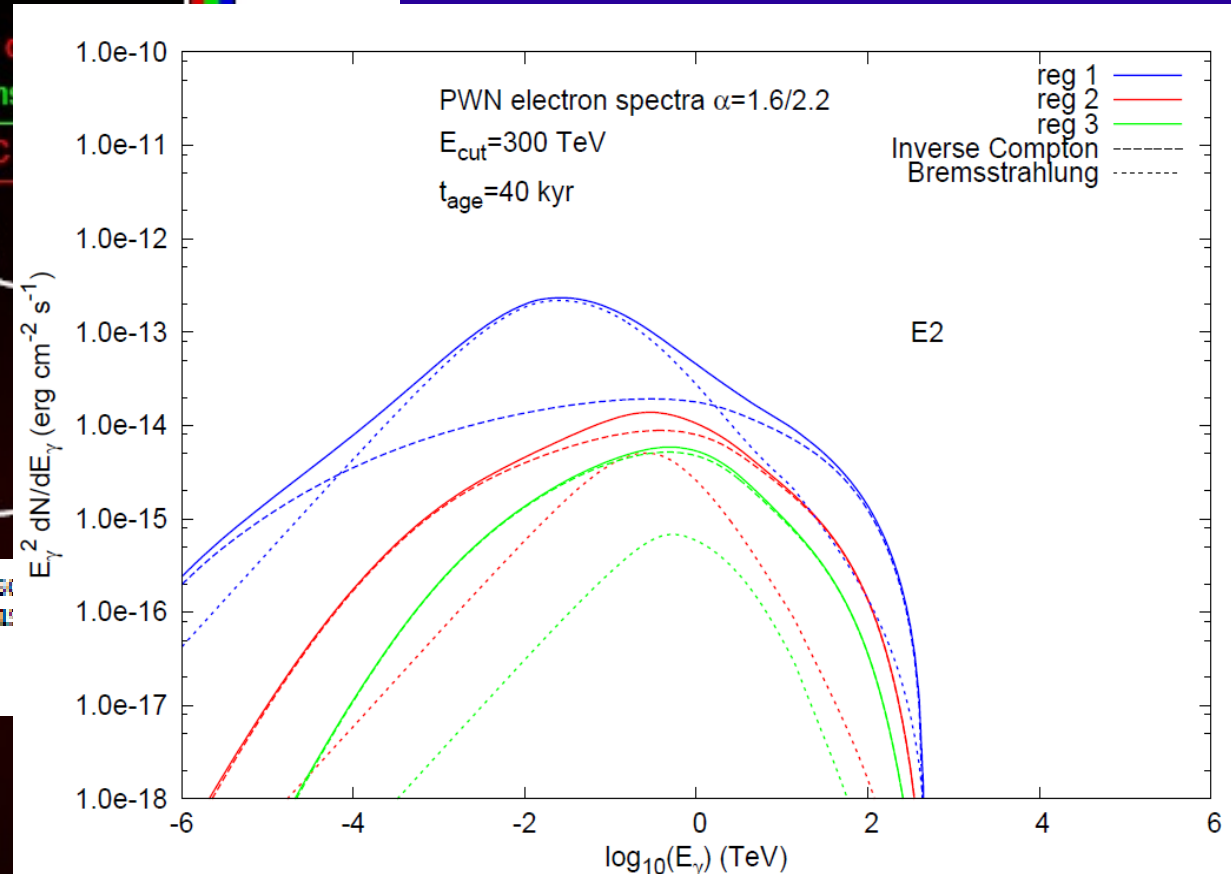
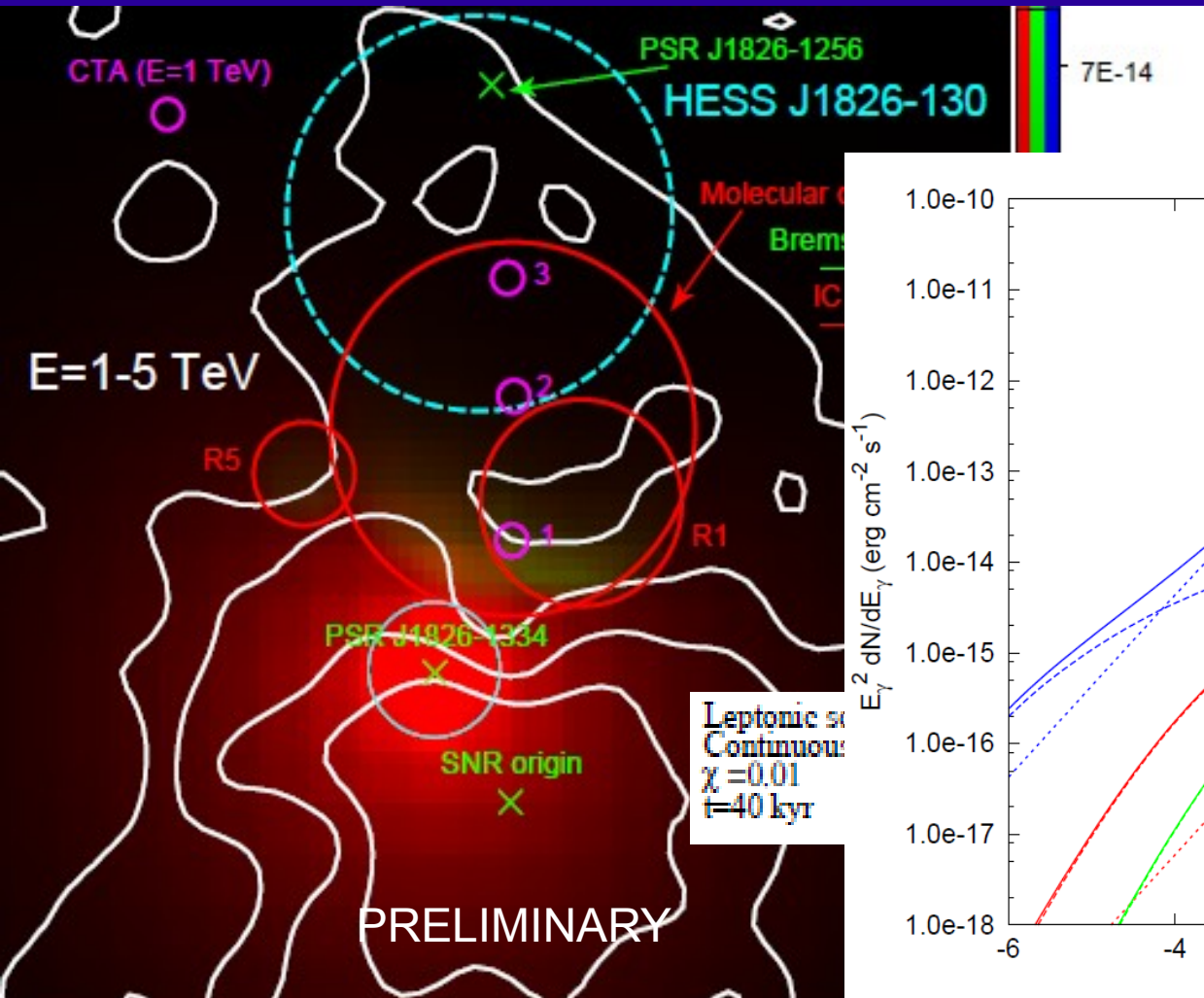
→ OUTPUTS THE GAMMA-RAY INTENSITY AT EACH POSITION AND EACH ENERGY BIN AS A FITS CUBE



→ Leptonic scenario : TeV gamma-ray emission not overlapping with molecular cloud +Bremsstrahlung may be significant

RESULTS DISPLAY

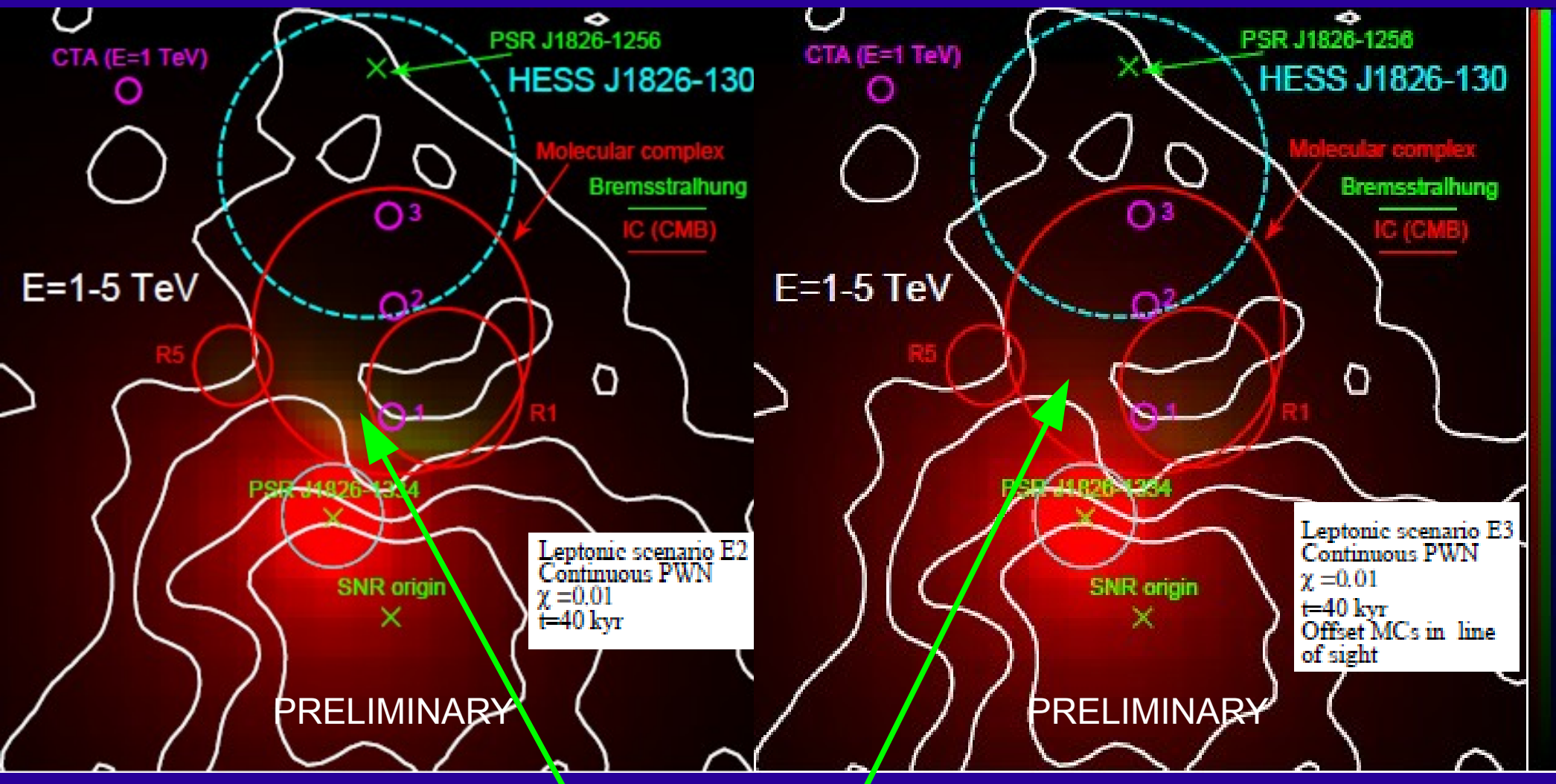
→ **OUTPUTS THE GAMMA-RAY INTENSITY AT EACH POSITION AND EACH ENERGY BIN AS A FITS CUBE**



→ Leptonic scenario : TeV gamma-ray emission not overlapping with molecular cloud +Bremsstrahlung may be significant

→ **Softening** of the TeV gamma-ray SED expected as we move away from the PWN

RESULTS DISPLAY



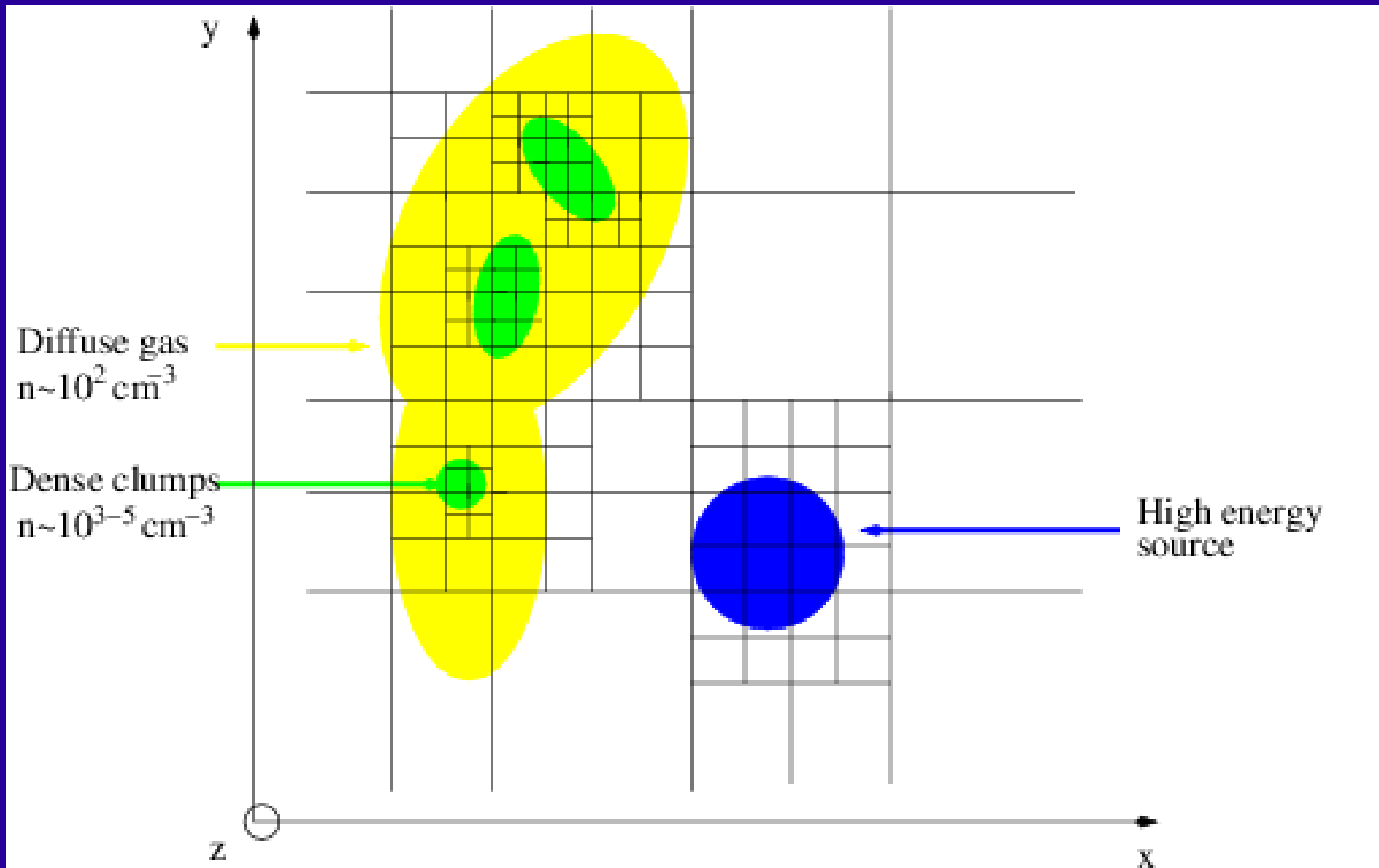
→ Leptonic gamma-ray morphology somewhat sensitive to the position of molecular clouds => **NEED TO MODEL X-RAYS EMISSION !!**

UPCOMING UPGRADES AND FUTURE WORK (1)

- IMPLEMENT MODELLING OF THE X-RAY EMISSION → **USEFUL TO OBTAIN FURTHER INFORMATION ABOUT THE MOLECULAR CLOUDS – TeV SOURCE ASSOCIATION**
- A MORE IN-DEPTH STUDIES OF THE SYSTEMATIC ERRORS FROM THE NUMERICAL COMPUTATIONS → **NECESSARY BEFORE PLANNING ANY PUBLICATIONS WITH THIS CODE**
- IMPLEMENT ARC AND FILAMENT STRUCTURE TO BETTER MATCH THE MORPHOLOGY OF THE GAS OBSERVED WITH THE MOPRA/NANTEN SURVEYS
- CONSTRAINT THE COLUMN DENSITY PIXEL BY PIXEL → **TO AVOID OVERESTIMATING THE HADRONIC TeV EMISSION IN THE LINE OF SIGHT**
- MAKE THE CODE MORE COMPUTATIONALLY EFFICIENT → **(test various dynamics gridding algorithm e.g OCTREE)**

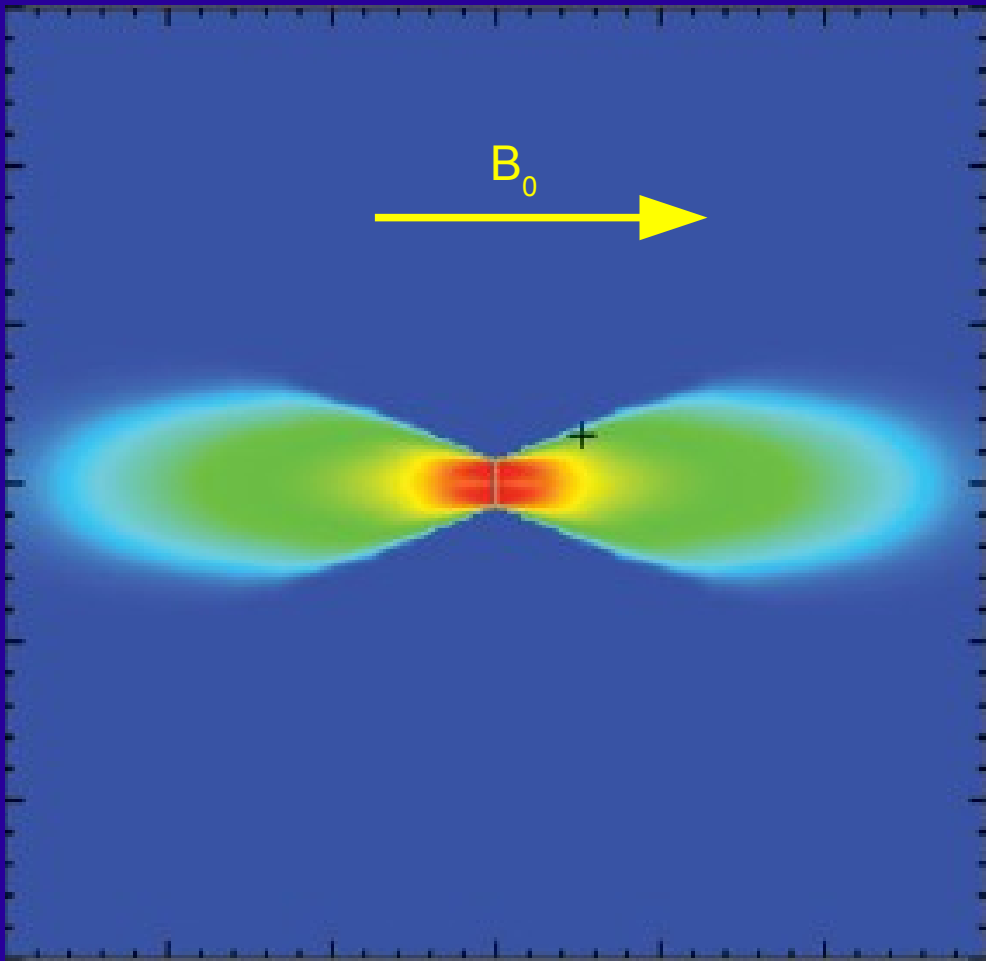
UPCOMING UPGRADES AND FUTURE WORK (2)

- MAKE THE CODE MORE COMPUTATIONALLY EFFICIENT → (test various dynamics gridding algorithm e.g OCTREE)



GETTING OVERAMBITIOUS ?

- ACCOUNT FOR POSSIBLE ANISOTROPY DIFFUSION ALONG PRIMARY B FIELD LINES (?)



CR overdensity map showing their anisotropic diffusion due to $\delta B/B_0 < 1$
(Gabici et al 2013)

THANKS !

Executive Producer

Gavin Rowell

Code Designer

Fabien Voisin

HPC Programmer

Fabien Voisin

Test designer

Fabien Voisin

Tester

Andrew Curzons

Fabien Voisin

EXPERTISE NEEDED IN :

- CODE DESIGNING
- CODE TESTING
- MODELLING X-RAY EMISSION
- ANISOTROPIC CR DIFFUSION...